

$$\frac{\pi}{2} = \left(\int_0^\infty \frac{\sin x}{\sqrt{x}} dx \right)^2 = \sum_{k=0}^\infty \frac{(2k)!}{2^{2k}(k!)^2} \frac{1}{2k+1} = \prod_{k=1}^\infty \frac{4k^2}{4k^2-1} \quad (1)$$