

1. Consider the prime  $p = 9929$  and the primitive element 2.
  - a) Show the steps of the Diffie-Hellman between Alice and Bob for  $a = 1983$  and  $b = 2014$ .
  - b) What is the value of the agreed secret key?
2. Consider the RSA public and private key pairs:  $(e, n) = (17, 902801)$  and  $(d, n, p, q, \phi) = (423953, 902801, 911, 991, 900900)$ .
  - Given  $M_1 = 500000$ , compute  $C_1 = M_1^e \pmod{n}$ .
  - Given  $C_2 = 707631$ , compute  $M_2 = C_2^d \pmod{n}$ .
3. RSA with three primes would also work:  $n = pqr$ ,  $\phi(n) = (p-1)(q-1)(r-1)$ ,  $\gcd(e, \phi(n)) = 1$ , and  $d = e^{-1} \pmod{\phi(n)}$ .
  - a) Setup an example RSA public/private key pair using primes 29, 31, 37, and  $e = 17$ .
  - b) Encrypt  $m = 10000$  and then decrypt the ciphertext.
  - c) Explain why RSA with three primes algorithm is not preferred.