Problem 1. (*PicoBot: Empty Room Coverage*) Write a PicoBot program empty_room.pb with rules that instruct the bot to cover the entirety of an empty rectangular room. Your program should work regardless of how big the room is and regardless of where the bot starts.

```
$ python picobot.py -e env1.txt < empty_room.pb
...
Coverage reached!</pre>
```

Problem 2. (Squared Distance) Write an HMMM program squared_distance.hmmm that takes four numbers x_1, y_1, x_2, y_2 representing the coordinates of two points on a plane and prints the approximate squared Euclidean distance between the two, calculated as $(x_1 - x_2)^2 + (y_1 - y_2)^2$.

```
$ python hmmmSimulator.py -f squared_distance.b -n
3
2
-1
5
25
```

Problem 3. (Sum of Ints) Write an HMMM program sum_of_ints.hmm that takes a nonnegative integer n as input and prints the sum $1 + 2 + 3 + \cdots + (n-1) + n$.

```
$ python hmmmSimulator.py -f sum_of_ints.b -n
100
5050
```

Problem 4. (*Primality Testing*) Write an HMMM program primality.hmmm that takes an integer n > 2 as input and prints 1 if n is prime, and 0 otherwise. Hint: a number n is prime if it is not divisible by any number $i \in [2, \sqrt{n}]$.

```
$ python hmmmSimulator.py -f primality.b -n
31
1
$ python hmmmSimulator.py -f primality.b -n
35
0
```

Problem 5. (Euclid's Algorithm, Iterative Approach) Write an HMMM program $gcd_iter.hmmm$ that takes two nonnegative integers x and y as input and prints their greatest common divisor, calculated iteratively using Euclid's Algorithm: if y divides x, the gcd of x and y is y; otherwise, the gcd of x and y is the same as the gcd of y and $x \mod y$, ie, in the next iteration y takes the place of x and y takes the place of y.

```
$ python hmmnSimulator.py -f gcd_iter.b -n
54
24
6
$ python hmmnSimulator.py -f gcd_iter.b -n
22
45
```

Problem 6. (Euclid's Algorithm, Recursive Approach) Write an HMMM program gcd_rec.hmmm that takes two nonnegative integers x and y as input and prints their greatest common divisor (gcd), calculated recursively using Euclid's Algorithm:

$$\gcd(x,y) = \begin{cases} \gcd(y,x \bmod y) & \text{if } y \neq 0, \text{ and} \\ x & \text{if } y = 0. \end{cases}$$

```
$ python hmmmSimulator.py -f gcd_rec.b -n
54
24
6
$ python hmmmSimulator.py -f gcd_rec.b -n
22
45
```

Files to Submit

- 1. empty_room.pb
- $2. \ {\tt squared_distance.hmmm}$
- 3. sum_of_ints.hmmm
- $4. \ {\tt primality.hmmm}$
- $5.\ \mathtt{gcd_iter.hmmm}$
- $6.\ \mathtt{gcd_rec.hmmm}$
- 7. report.txt

Before you submit:

• Make sure your programs meet the input and output specifications by running the following command on the terminal:

```
$ python run_tests.py [cproblems>]
```

where the optional argument cproblems lists the numbers of the problems you want to test; all the problems are tested if no argument is given.

• Make sure your report doesn't exceed 400 lines, doesn't contain spelling mistakes, and doesn't contain lines that exceed 80 characters.