### Linear Regression

### The input variable is denoted by x, also called as the input feature

## The output variable is denoted as y, also called the target variable

### Training Set

Living Area of the House in sq. ft. (X)	Price of the House in dollars (Y)
1000	50000
400	25000
350	24000
2000	90000

#### Training Example

$$(x^{(2)}, y^{(2)}) = (400, 2500)$$

### A Training Set is a list of Training Examples

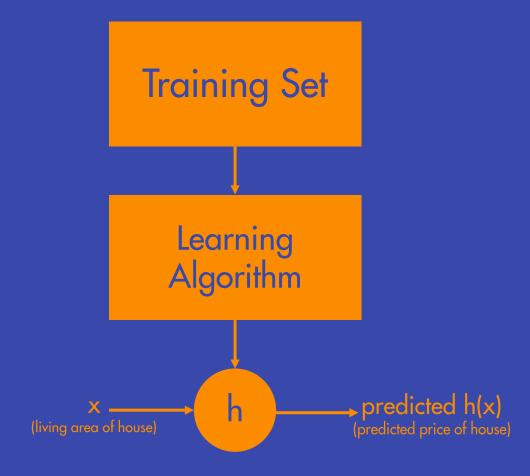
### Hypothesis

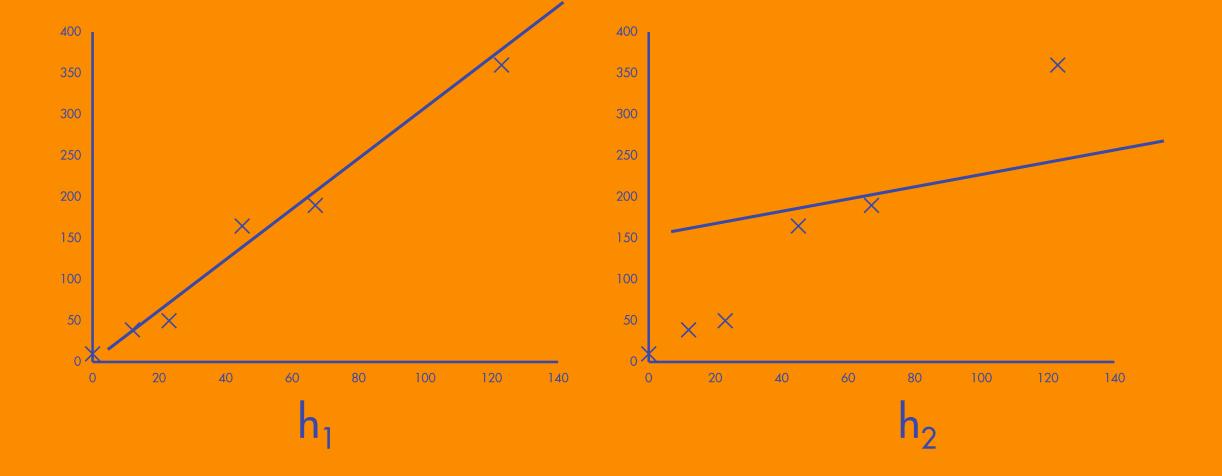
h is a function that maps the feature x into a predicted output h(x).

$$h(x) = \theta_0 + \theta_1 x$$

## The algorithm is trying to learn the best h for the training set.

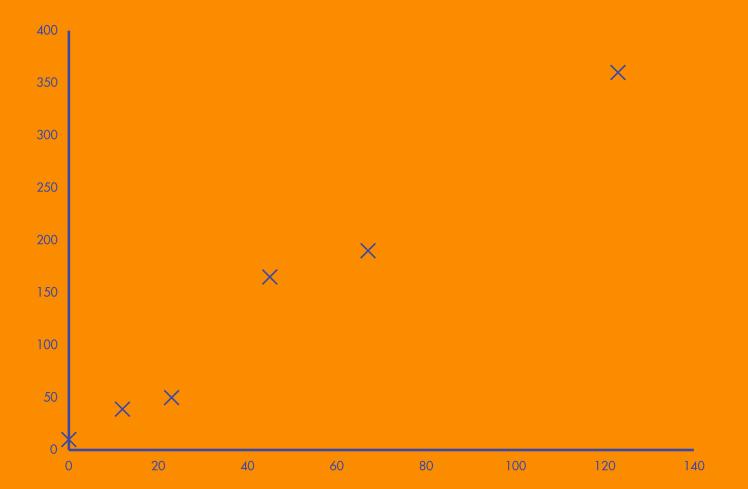
### Model Representation



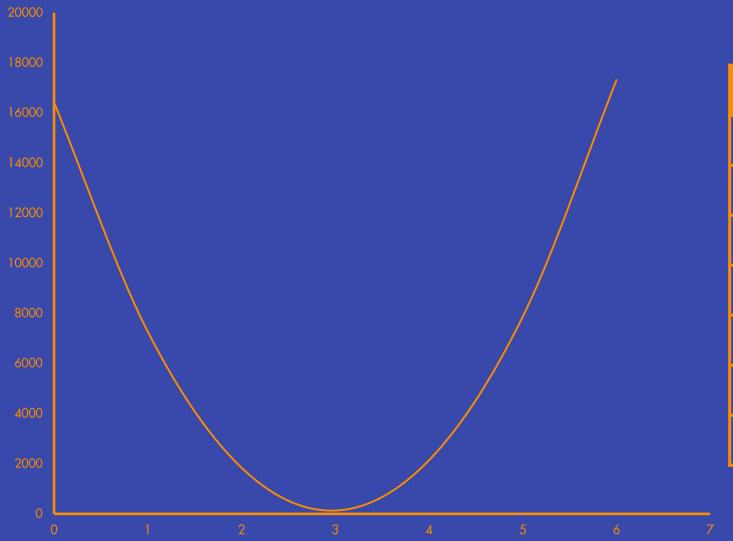


$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^{m} (h(x^{(i)}) - y^{(i)})^2$$

# The smaller the value of $J(\theta_0, \theta_1)$ , the better the fit of the hypothesis to the training set



×	у
12	39
23	50
45	165
0	10
123	360
67	190



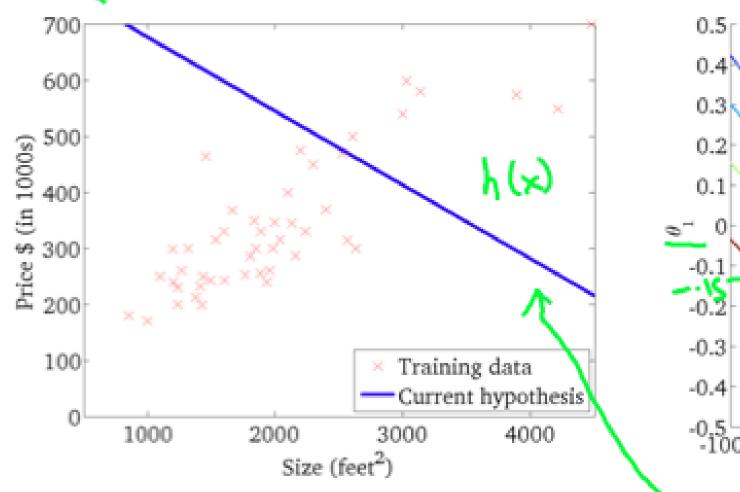
$\boldsymbol{\theta_i}$	$J(\theta_1)$	
0	16420.5	
1	7271.3	
2	1841.5	
3	131	
4	2139.8	
5	7868	
6	17315	

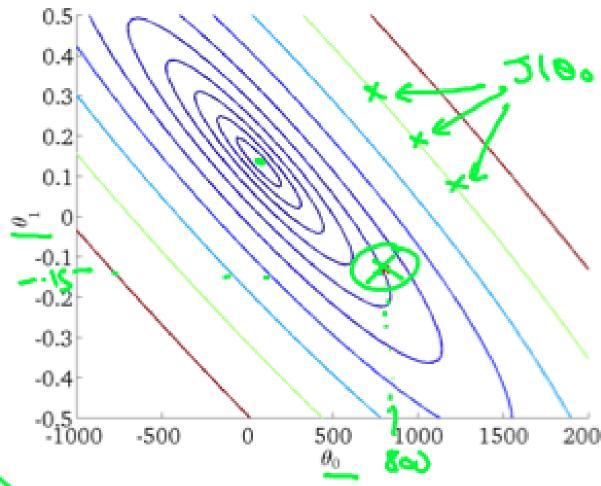
$$h_{\theta}(x)$$

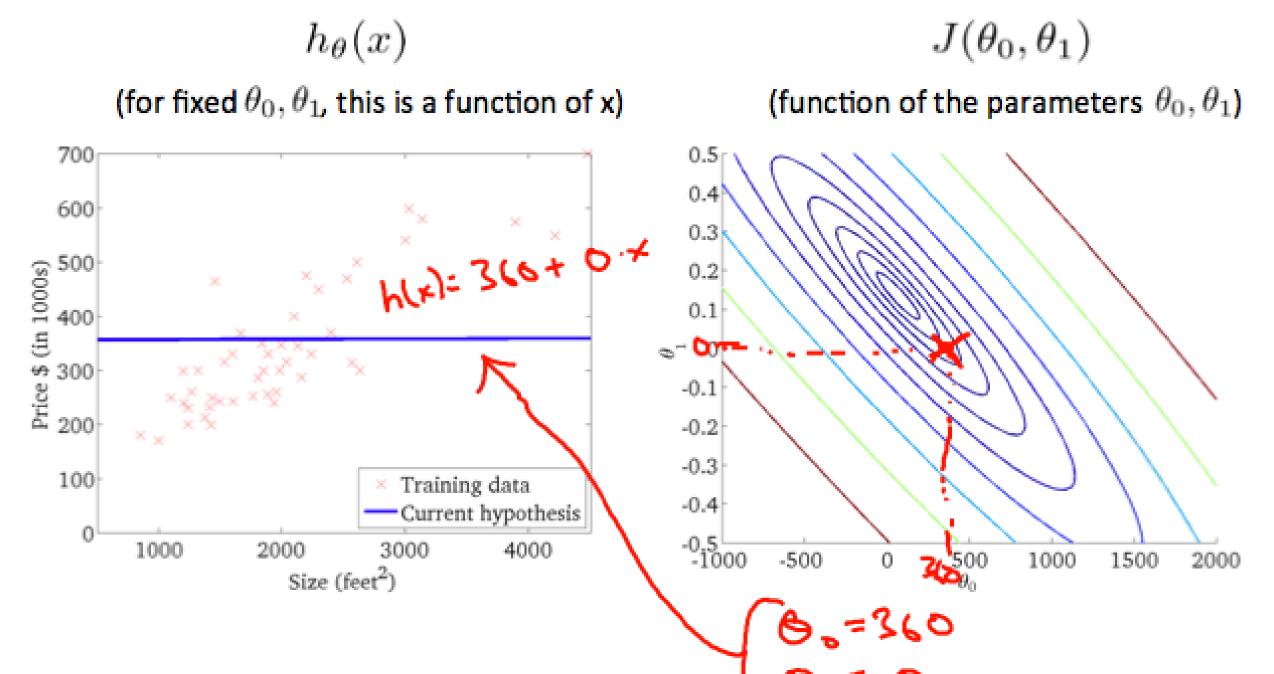
 $J(\theta_0, \theta_1)$ 

(for fixed  $\theta_0$ ,  $\theta_1$ , this is a function of x)

(function of the parameters  $\theta_0, \theta_1$ 





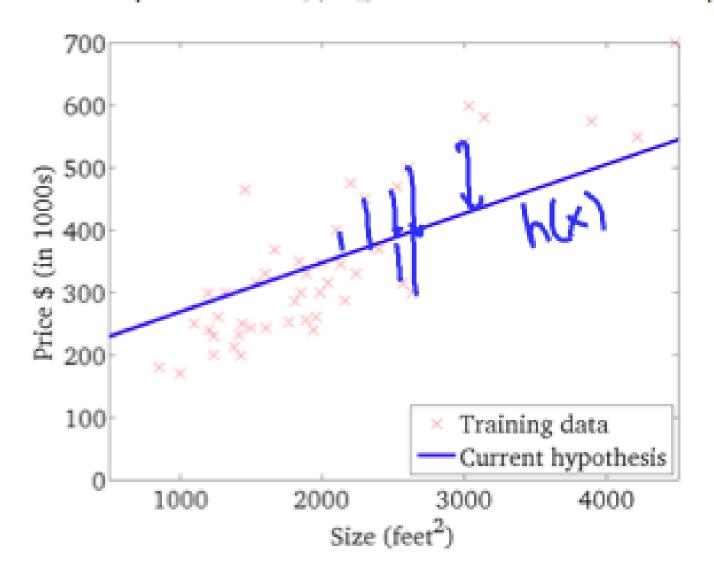


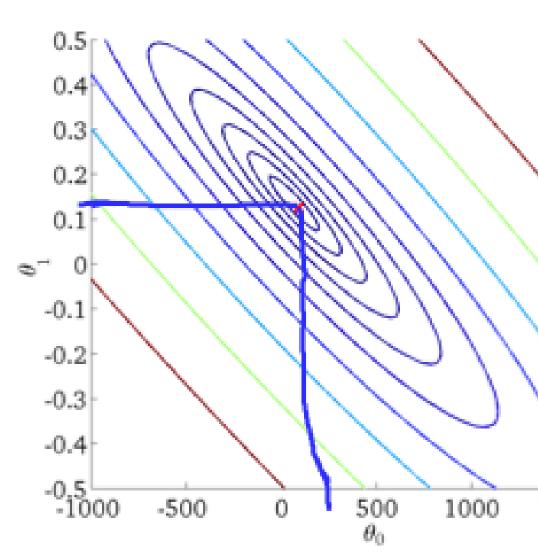
$$h_{\theta}(x)$$

 $J(\theta_0, \theta_1)$ 

(for fixed  $\theta_0$ ,  $\theta_1$ , this is a function of x)

(function of the parameter





$$J'(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^{m} ((h(x^{(i)}) - y^{(i)})x^{(i)})$$

#### Repeat until convergence:{

$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i = 1}^{m} (h(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

$$\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i = 1}^{m} (h(x^{(i)}) - y^{(i)}) x_1^{(i)}$$

x <sub>1</sub>	x <sub>2</sub>	у
12	2	39
23	-5	50
45	44	165
0	12	10
123	-12	360
67	-20	190

#### More Notations

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x_j^{(i)} = value of the feature j in the i^{th} training example x^{(i)} = the input features of the i^{th} training example m = number of training examples n = number of features
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$$h(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

$$h(x) = \begin{bmatrix} \theta_0 & \theta_1 & \dots & \theta_n \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ \vdots \\ x_n \end{bmatrix} = \theta^T x$$

$$H = X\theta = \begin{bmatrix} x_0^1 & x_1^1 & \cdots & x_n^1 \\ x_0^2 & x_1^2 & \cdots & x_n^2 \\ \vdots & \vdots & \ddots & \vdots \\ x_0^m & x_1^m & \cdots & x_n^m \end{bmatrix} \begin{bmatrix} \theta_0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix} = \begin{bmatrix} h(x_0) \\ h(x_1) \\ \vdots \\ h(x_n) \end{bmatrix}$$

$$H - y = \begin{bmatrix} h(x^{(1)}) \\ h(x^{(2)}) \\ \vdots \\ h(x^{(m)}) \end{bmatrix} - \begin{bmatrix} y^{(1)} \\ y^{(2)} \\ \vdots \\ y^{(m)} \end{bmatrix}$$

#### Repeat until convergence:{

$$\theta_{0} := \theta_{0} - \alpha \frac{1}{m} \sum_{i \neq 1}^{m} (h(x^{(i)}) - y^{(i)}) x_{0}^{(i)}$$

$$\theta_{1} := \theta_{1} - \alpha \frac{1}{m} \sum_{i=1}^{m} (h(x^{(i)}) - y^{(i)}) x_{1}^{(i)}$$

$$\vdots$$

$$\theta_{n} := \theta_{n} - \alpha \frac{1}{m} \sum_{i=1}^{m} (h(x^{(i)}) - y^{(i)}) x_{n}^{(i)}$$

Repeat until convergence (for j in [0, n]): {

$$\theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^m (h(x^{(i)}) - y^{(i)}) x_j^{(i)}$$