## TP12021

December 14, 2021

## 1 TP 1

```
[1]: import numpy as np import matplotlib.pyplot as plt

2 Exercice 1
```

question 1

```
[3]: # On définit la matrice
     A = np.array([[4,6,-2,3], [2,-1,0,1], [-7,0,1,12]],dtype= "float")
     # on l'affiche sur la sortie
     print("A= ", A)
    A = [[4. 6. -2. 3.]]
     [ 2. -1. 0. 1.]
     [-7. 0. 1. 12.]]
[4]: # on affiche une valeur
     print(A[0,3])
    3.0
    question 2
[5]: # on concatène verticalement (vstack)
     C = np.vstack((2*A[0:2,:],1/3*A[2,:]))
     print("C= ",C)
    C= [[8.
                                  -4.
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                      12.
                                                6.
     [ 4.
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                  -2.
                               0.
                                            2.
     [-2.33333333 0.
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                               0.33333333 4.
    question 3
[6]: print(np.ones([1,3]))
     B = np.vstack([np.arange(4,7,1),np.arange(5,16,5),np.ones([1,3])])
     print("B = ", B)
    [[1. 1. 1.]]
    B = [[4. 5. 6.]]
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[ 5. 10. 15.]
      [ 1. 1. 1.]]
     question 4
 [7]: C = A[0:3,0:3]
      print("C = ", C)
     C = [[4. 6. -2.]]
      [ 2. -1. 0.]
      [-7. 0. 1.]]
     question 5
[23]: # produit matriciel
      D = np.dot(B,A)
      print("D = ", D)
     D = [[-16. 19. -2. 89.]]
      [-65. 20. 5. 205.]
      [ -1. 5. -1. 16.]]
     question 6
[24]: # somme matricielle
      Y = np.sum(D,axis=1)
      print("Y = ", Y)
     Y = [90.165.19.]
         Exercice 2
     question 1
[31]: A = np.array([[4,5,6,-1],[5,10,15,2],[6,15,1,4],[-1,2,4,-2]])
      vap, vecp = np.linalg.eig(A)
      print("valeurs propres : ",vap)
      print("vecteurs propres : ", vecp)
     valeurs propres : [ 24.49531701 -11.04368827
                                                     2.31528872 -2.76691746]
     vecteurs propres : [[ 0.340821
                                        0.16909822  0.86888096  0.31669026]
      [ 0.73157879  0.50754043 -0.24619324 -0.382863 ]
      [ 0.57611269 -0.80330147 -0.10808058  0.10544909]
      [ 0.12933558  0.26175418 -0.41563609  0.86139636]]
     question 2
[32]: invvap = np.diag(1./vap)
      invA1 = np.dot(vecp,np.dot(invvap,vecp.T))
      print("invA1 = ", invA1)
      invA2 = np.linalg.inv(A)
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print("invA2 = ", invA2)
     invA1 = [[ 0.29197923 -0.04616272 -0.03231391 -0.25678015]
      [-0.04616272 -0.02827467 0.08020773 0.15522216]
      [-0.03231391  0.08020773  -0.04385459  0.00865551]
      [-0.25678015 0.15522216 0.00865551 -0.19907675]]
     invA2 = [[ 0.29197923 -0.04616272 -0.03231391 -0.25678015]]
      [-0.04616272 -0.02827467 0.08020773 0.15522216]
      [-0.03231391 0.08020773 -0.04385459 0.00865551]
      [-0.25678015  0.15522216  0.00865551  -0.19907675]]
     4 Exercice 3
     question 1
[33]: A = \text{np.array}([[1, -1, 2, 1, 2], [-1, 2, 3, -4, 1], [0, -1, 1, 0, 0]])
      rankA = np.linalg.matrix_rank(A)
      print("rankA = ", rankA)
     rankA = 3
     question 2
[34]: b = np.array([[3], [-7], [1]])
      Xs = np.linalg.solve(A[0:3,0:3],b)
      print("sol de Ax=b : ", Xs)
     sol de Ax=b : [[ 2.5]
      [-1.5]
      [-0.5]
     5 Exercice 4
[37]: A = \text{np.array}([(4, 4, 8), (1, -3, 5), (3, 7, 3)], \text{float})
      B = np.array([0, 1, -1], float).reshape(-1, 1)
      C = np.concatenate((A, B), axis=1)
      print("A = ",A)
      print("B = ",B)
      print("C = ",C)
     A = [[4. 4. 8.]]
      [ 1. -3. 5.]
      [ 3. 7. 3.]]
     B = [[0.]]
      [ 1.]
      [-1.]]
     C = [[4. 4. 8. 0.]]
      [ 1. -3. 5. 1.]
      [3. 7. 3. -1.]]
```

## 6 Exercice 5

question 1

```
[2]: A=np.array([[4,2,1,4,5,6,7],
        [1,4,-6,2,2,0,-2],
        [1,-2,3,3,-5,6,1],
        [1,-1,1,-1,2,-3,-1],
        [1,1,0,8,2,3,4]])
     b=np.array([[1],[2],[-10],[-2],[3]])
     print("A = ",A)
     print("b = ",b)
     A = [[4 \ 2 \ 1 \ 4 \ 5 \ 6 \ 7]]
      [ 1 4 -6 2 2 0 -2]
      [1-2 3 3-5 6 1]
      [ 1 -1 1 -1 2 -3 -1]
      [1 1 0 8 2 3 4]]
    b = [[ 1]]
     [ 2]
     [-10]
      [ -2]
     [ 3]]
     question 2
[3]: G = np.hstack((A,b))
     print("G = ",G)
     G = [[ 4 2 1 4]
                            5
                                6
                                        1]
      [ 1 4 -6
                  2 2
                           0 -2
                                   2]
      「 1 −2 3
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                  3 -5
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      [ 1 -1 1 -1 2 -3 -1 -2]
      Γ 1 1
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    question 3
[84]: def permL(G,i,j):
         C = np.copy(G)
         a = np.copy(C[i,:])
         C[i,:] = np.copy(C[j,:])
         C[j,:] = a
         return C
     question 4
[83]: def ajoutS(G,i,j,a):
         C = np.copy(G)
         C[i,:] = np.copy(C[i,:])+a*np.copy(C[j,:])
         return C
```

```
question 5
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[85]: def multiS(G,i,a):
           C = np.copy(G)
           C[i,:] = a*np.copy(C[i,:])
           return C
      question 6
[10]: print(permL(G,1,2))
       print(ajoutS(G,0,1,2))
       print(multiS(G,0,3))
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      question 7
[122]: def pivotGauss(G):
           C = np.copy(G)
           n = C.shape[0]
           m = C.shape[1]
           p = 0
           for j in range(m):
               if p < n:
                   k = np.argmax(abs(C[p:n,j]))
                   k = k + p
                   if C[k,j] != 0:
                       C = multiS(C,k,1/C[k,j])
                       print("reduit: ")
                       print(str(C))
                       if k != p:
                           C = permL(C,k,p)
                            print("permut:")
                           print(str(C))
                       for i in range(1,n):
```

question 8

```
[123]: print(pivotGauss(G))
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[ 1 1 0 8 2 3 4 3]]

echel:

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[ 1 1 0 8 2 3 4 3]]

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