# The Life Cycle of Firms and the Productivity Advantages of Large Cities

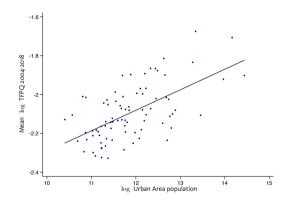
Tomás Budí-Ors

CEMFI, visting Yale

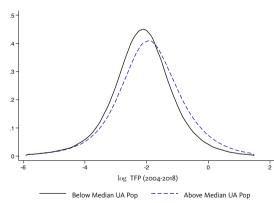
Yale Macro Breakfast
April 2023

#### Motivation

#### Firms are, on average, more productive in larger cities



(a) Relationship between Urban Area population and firm TFPQ in Spain



(b) Distribution of  $\log$ TFPQ across Spanish Urban Areas

#### Motivation

#### Firms are, on average, more productive in larger cities

- Different mechanisms
  - 1. Agglomeration (Rosenthal and Strange 2004, Combes et al 2012, Behrens et al 2014, Gaubert 2018)
  - 2. Sorting (Behrens et al 2014, Gaubert 2018)
  - 3. Selection (Melitz and Ottaviano 2008, Combes et al 2012, Behrens et al 2014)
- So far, the importance of 1.–3. for the urban productivity premium disciplined with static models
  - ightarrow This paper: a dynamic perspective
  - Goals:
    - (a) Quantify 1.–3. using theory and data on firm growth and firm dynamics across the city-size distribution
    - (b) Revisit the implications of place-based policies for aggregate productivity

# What I am doing

- Facts on firms' life-cycle growth, firm entry and firm exit across the city-size distribution in Spain
  - Firm growth over the life-cycle is higher in larger cities
  - No relevant differences in entry and exit rates across cities of different size
  - Firm reallocation is negligible ( $\sim$ 0.01% of firms per year reallocate)
- Canonical model of firm dynamics (Hopenhayn 1992) augmented with
  - + Agglomeration externality
  - + Ex-ante (productivity type) and ex-post (productivity shocks) firm heterogeneity
  - → captures the mechanisms that generate the urban productivity premium
- Model-based identification strategy to quantify the extent of sorting vs agglom vs selection in the UPP
  - → Today: comparative statics exercise to discuss the identification of some key parameters

#### Related Literature

- Productivity advantages of large cities and firm sorting, selection, and agglomeration Rosenthal and Strange (2004), Combes, Duranton, Gobillon, Puga, and Roux (2012) Behrens, Duranton, and Robert-Nicoud (2014), Gaubert (2018), Ziv (2019)
  - → A new identification strategy based on data and theory of firm dynamics
- Firm dynamics across regions
  Brinkman, Coen-Pirani, and Siegel (2016), Walsh (2019), Brandt, Kambourov, and Storesletten (2019), Klenow and Li (2022)
  - → A different question: revising why firms located in large cities are more productive
- 3 Firm growth over the life cycle Haltiwanger, Jarmin, and Miranda (2013), Hsieh and Klenow (2014), Arkolakis (2016), Sterk, Sedláçek, Pugsley (2021)
  - → A look at its geographical dimension

#### **Facts**

Facts

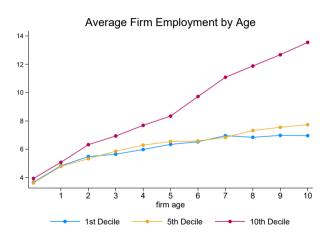
#### Data

- Balance sheet information of non-financial Spanish firms, collected by the Bank of Spain
  - Annual frequency 2004-2018
  - Around 1.2 million firms, each one observed an average of 5 years
  - Information on firm sector, employment, capital, wage bill and location of headquarters
  - Drawbacks:
    - Data at the firm level rather than at the establishment-level
    - Imperfect to study firm exit, as firms stop showing up in the sample but continue operating
- Geography: 83 Urban Areas (UA) defined by Ministry of Transports and Mobility



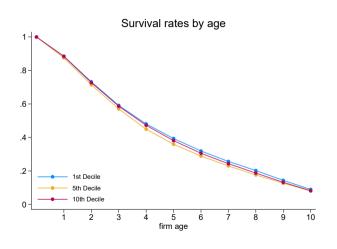
- Notion of local labor market (68% of population, 73% of firms in full sample)
  - Final sample with 5 million firm-year observations, 915 thousand firms
- Compute UA size as the number of people within 10km of the average person in UA (De La Roca, Puga 2017)

# 1. Firm growth over the life cycle is higher in large cities



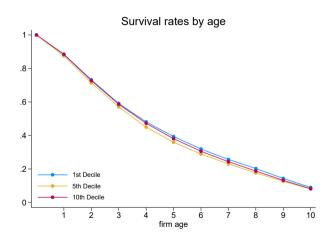
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  - Holds within sector SEE
  - Also in terms of VA per worker

### 1. Firm growth over the life cycle is higher in large cities



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  - Also in terms of VA per worker
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  - No relevant differences in exit rates by age across cities

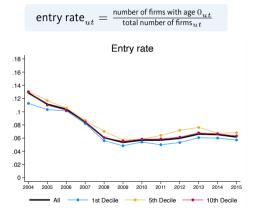
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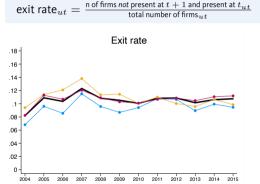


- Firms grow much more as they age in large cities
  - Holds within sector SEE
  - Also in terms of VA per worker
- Not explained by survival bias
  - No relevant differences in exit rates by age across cities
- Mainly driven by a small group of high-growth firms
- Not associated to some of the common drivers of misallocation
  - (e.g. different labor regulation, tax regime or contract law)

### 2. Entry and exit rates are similar for cities of different size

• Compute the entry and exit rates in Urban Area (UA) u in year t as





- Entrants are more productive in large cities, yet not larger in terms of employment or capital
- Exiters are more productive and larger in big cities

#### From the Facts to the Model

- In larger cities
  - 1. Firms grow more over the life-cycle, both in terms of employment and value added
  - 2. The entry and the exit rates are not different than in smaller cities
  - 3. Firms are larger and more productive

- A model relating the facts to the mechanisms of the urban productivity premium
  - Firm dynamics as in Hopenhayn (1992)  $\rightarrow$  endogenous exit (selection)
  - Agglomeration externality: city size (population) increases firm TFP, more so for high productivity firms
    - → Induces sorting of ex-ante more productive firms into large cities

### Model

#### Environment

- A city economy: agents operate in a single-city world of exogenous size L or a world of isolated city-islands
- Representative household: continuum of identical members (of size L)
  - Static problem, no savings
- Production
  - Heterogeneous firms in both ex-ante profiles and ex-post shocks that determine efficiency z
  - Production requires only labor  $\ell$ , hired every period, and shows decreasing returns

$$y=\varphi(z,L)\ell^{\gamma}\quad\text{with}\quad\gamma<1$$

- ightarrow firm TFP  $arphi(z, \underline{L})$  affected by city size  $\underline{L}$
- Firm dynamics: endogenous entry and exit
  - Endogenous exit due to fixed cost of operation  $c_f$
  - Free entry condition as entry is costly  $c_e$

#### Incumbent firms

#### Production and exit

ullet Static production problem o solve for labor demand, ouput and profits (final good is the numeraire)

$$\ell(z, \underline{L}, w) = \frac{\gamma}{w} \frac{\varphi(z, \underline{L})^{\frac{1}{1-\gamma}}}{c(w)}, \qquad y(z, \underline{L}, w) = \frac{\varphi(z, \underline{L})^{\frac{1}{1-\gamma}}}{c(w)}, \qquad \pi(z, \underline{L}, w) = (1-\gamma) \frac{\varphi(z, \underline{L})^{\frac{1}{1-\gamma}}}{c(w)}$$

where 
$$c\left(w\right) = \left(\frac{w}{\gamma}\right)^{\frac{\gamma}{1-\gamma}}$$

- Realized firm efficiency z is a function of an exogenous Markovian state vector  $\mathbf{s}$  (to be discussed later)
- ullet Before  $z(\mathbf{s})$  is realized, a firm may exit and avoid paying the fixed cost of operation  $c_f$
- $\rightarrow$  The value of a firm with state vector s in a city of size L at time t

$$V\left(\mathbf{s}, L, w_{t}\right) = \max \left\{ \mathbb{E}\left[\pi(\mathbf{s}', L, w_{t}) - c_{f} + \beta V\left(\mathbf{s}', L, w_{t+1}\right) \mid \mathbf{s}\right], 0 \right\}$$

where s' is the value of the state realized after the continuation decision

# Entry, Aggregation, and Market clearing

#### Firm entry

- ullet After paying entry cost  $c_e$ , entrants observe their initial level of  ${f s}$ 
  - ightarrow Depending on  $V(\mathbf{s},L,w_t)$  decide to operate and pay  $c_f$  or exit immediately and never produce
- Free entry condition (all potential entrants are indifferent between entry or not)

$$\int_{\mathbf{s}} V\left(\mathbf{s}, L, w_{t}\right) d\hat{G}\left(\mathbf{s}\right) \leq c_{e} \quad \text{ with equality if the mass of entrants } m_{t} > 0$$

#### Aggregation

• The distribution of incumbent firms  $\mu_t$  follows the law of motion

$$\mu_{t+1}(\mathbf{s}') = \int_{\mathbf{s}} \underbrace{(1 - x(\mathbf{s}))}_{\text{exit policy}} G(\mathbf{s}' \mid \mathbf{s}) d\mu_t + m_{t+1} \int_{\mathbf{s}} (1 - x(\mathbf{s})) d\hat{G}(\mathbf{s})$$

#### Market clearing: labor

$$L = (1 - x(\mathbf{s})) \left[ \int_{\mathbf{s}} \ell(\mathbf{s}, L, w) d\mu_t + m_{t+1} \int_{\mathbf{s}} \ell(\mathbf{s}, L, w_t) d\hat{G}(\mathbf{s}) \right]$$

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#### Market clearing: goods

$$C = (1 - x(\mathbf{s})) \left[ \int_{\mathbf{s}} (y(\mathbf{s}, L, w) - c_f) d\mu_t + m_{t+1} \int_{\mathbf{s}} (y(\mathbf{s}, L, w) - c_f) d\hat{G}(\mathbf{s}) \right] - c_e m_{t+1}$$

### Productivity externality: agglomeration economies

• So far, no stance on how city size affects firm TFP (model in general form with  $\varphi(z,L)$ )

- Evidence that more productive firms are disproportionately more productive in larger cities
   Combes et al 2012
  - $\rightarrow$  Complementarity between L and z
  - Follow Gaubert (2018) and assume  $\varphi(z,L) = \exp\left(\alpha \log L + \log z \left(1 + \log L\right)^{\eta}\right)^{1-\gamma}$ 
    - ightarrow log-supermodularity of profits i.e.  $\frac{\partial^2 \log \pi(z,L,w)}{\partial \log L \partial \log z} > 0$ , most productive firms are better-off in large cities
    - ightarrow lpha is the traditional agglomeration elasticity, while  $\eta$  controls the extent of complementarity between z and L

### Productivity process

- Urban productivity premium may reflect the sorting of ex-ante more productive firms (Gaubert, 2018)
- ightarrow Allow for productivity process in which firms are ex-ante heterogeneous (Sterk, Sedláçek, Pugsley, 2021)
  - try to identify mean of ex-ante component across cities

ex-ante het ex-post het 
$$u_{i,a}=\rho_u u_{i,a-1}+\theta_i, \qquad \qquad u_{i,-1}\sim iid(0,\sigma_u^2), \qquad \theta_i\sim iid(\mu_\theta,\sigma_\theta^2), \quad \mid \rho_u\mid \leq 1$$

$$v_{i,a} = \rho_v v_{i,a-1} + \zeta_{i,a},$$
  

$$\varepsilon_{i,a} \sim iid(0, \sigma_z^2)$$

 $\log z_{i,a} = \underbrace{u_{i,a}} + \underbrace{v_{i,a} + \varepsilon_{i,a}}_{}$ 

$$v_{i,-1} = 0,$$
  $\zeta_{i,a} \sim iid(0, \sigma_{\varepsilon}^2), \quad |\rho_v| \leq 1$ 

(where  $z_{i,a}$  is the efficiency of firm i at age a)

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$$\log z_{i,a} = \underbrace{u_{i,a}}_{\text{ex-ante het}} + \underbrace{v_{i,a} + \varepsilon_{i,a}}_{\text{ex-post het}} \qquad \text{(where $z_{i,a}$ is the efficiency of firm $i$ at age $a$)}$$
 
$$u_{i,a} = \rho_u u_{i,a-1} + \underbrace{\theta_i}_{\text{productivity}} \qquad \underbrace{u_{i,-1}}_{\text{initial}} \sim iid(0,\sigma_u^2), \qquad \theta_i \sim iid(\mu_\theta,\sigma_\theta^2), \mid \rho_u \mid \leq 1$$

condition

(where  $z_{i,a}$  is the efficiency of firm i at age a)

- $\rightarrow$  Heterogeneity in long-run productivity level determined by  $\frac{\theta_i}{1-\alpha}$
- $\rightarrow$  Heterogeneity in convergence to long-run level determined by  $u_{i,-1}$

$$v_{i,a} = \rho_v v_{i,a-1} + \zeta_{i,a},$$
  $v_{i,-1} = 0,$   $\zeta_{i,a} \sim iid(0, \sigma_{\varepsilon}^2),$   $|\rho_v| \leq 1$   
 $\varepsilon_{i,a} \sim iid(0, \sigma_{\varepsilon}^2)$ 

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$$\begin{aligned} u_{i,a} &= \rho_u u_{i,a-1} + \theta_i, & u_{i,-1} \sim iid(0,\sigma_u^2), & \theta_i \sim iid(\mu_\theta,\sigma_\theta^2), & |\rho_u| \leq 1 \\ v_{i,a} &= \underbrace{\rho_v v_{i,a-1} + \zeta_{i,a}}_{\text{standard AR(I) process}}, & v_{i,-1} &= 0, & \zeta_{i,a} \sim iid(0,\sigma_\varepsilon^2), & |\rho_v| \leq 1 \end{aligned}$$

$$\underbrace{\varepsilon_{i,a}}_{\text{noise shock}} \sim iid(0,\sigma_z^2)$$

#### Identification I

• Problem: higher ex-ante firm productivity  $\mu_{\theta}$  or city size L have the same implication for empl *levels* 

$$\log \ell_{i,a} = \log \gamma - \log w - \log c(w) + \alpha \log L + (1 + \log L)^{\eta} \log z_{i,a}$$

Employment growth (in Steady State) can be informative

$$\log \ell_{i,a+1} - \log \ell_{i,a} = (1 + \log L)^{\eta} (\log z_{i,a+1} - \log z_{i,a})$$

- Differences in employment growth between
  - old firms in same city ightarrow only from ex-post shocks (as ex-ante type is differenced away and L is common)
  - young firms in same city  $\rightarrow$  from differences in ex-ante profiles and ex-post shocks
  - old firms in different cities  $\rightarrow$  from differences in L and ex-post shocks
  - young firms in different cities ightarrow from differences in L, ex-ante profiles and ex-post shocks
- → Comparing employment growth of old vs young firms in same vs different cities is informative about the importance of sorting vs agglomeration for the city productivity premium

#### Identification II

Identification argument holds conditional on exit rates being the same across space

$$\Delta \log \ell_{i,a} = (1 + \log L)^{\eta} \Delta \log z_{i,a}$$

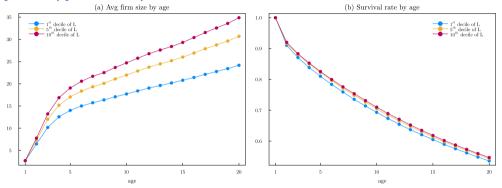
- $\rightarrow \Delta \log \ell_{i,a}$  for old firms in the same city depends on ex-post shocks but *also* on endogenous exit (selection), which in turn depends on ex-ante heterogeneity
- One way of dealing with this is assuming that exit is exogenous, but unappealing to study possibly stronger selection in citites
- An alternative is to allow entry costs to vary by city size  $c_e(L) = c_0 L^{\chi}$ 
  - With higher  $c_e$ , the free entry condition is satisfied at a lower w, affecting incumbents productivity and as a result exit rates
  - Empirically, it could be justified as a reduced-form counterpart of the higher price of land in large cities

### Comparative statics

- Borrow productivity process calibrated by Sterk, Sedláçek, Pugsley (2021) for US firms
- Set structural parameters arbitrarily/to standard values
- ullet Solve model for different values of city size L and compare outcomes
  - 1) Same productivity process in all cities
  - 2) Ex-ante better firms in large cities
  - 3) Ex-ante better firms and higher entry costs in large cities
- Show identification strategy at work

# Employment levels and Survival rates by age

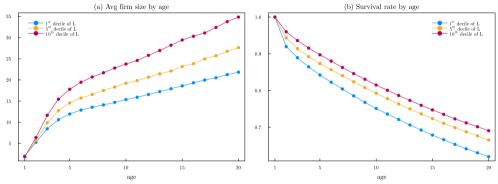
#### 1. Same productivity process in all city-sizes



- Firms are more productive in cities due to the agglomeration externality, and so larger
  - This is partly compensated by higher wages in large L, specially for young firms
- Firms grow following good productivity shocks, which are amplified by city size  $\Delta \log \ell_{i,a} = (1 + \log L)^{\eta} \Delta \log z_{i,a}$
- ullet Survival rates similar across L sizes because higher productivity in large cities is compensated by higher w

# Employment levels and Survival rates by age

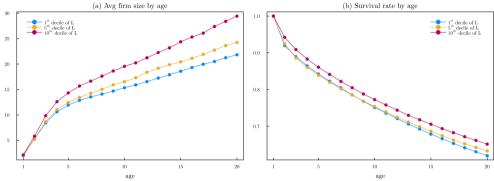
#### 2. Ex-ante better firms in large cities (higher $\mu_{\theta}$ )



- Firms in large cities are now exogenously more productive
  - For given  $c_e$ , equilibrium w increases to satisfy the free-entry condition (making operation more costly)
  - → Extra selection on entry in large cities (i.e. entrants must be ex-ante very productive)
  - → Highly-productive firms cope better with shocks and exit less

# Employment levels and Survival rates by age

3. Ex-ante better firms in large cities (higher  $\mu_{ heta}$ ) and higher entry costs  $c_e$ 

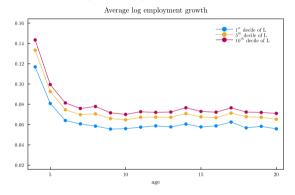


- Entrants in large cities are also exogenously more productive, however
  - As  $c_e$  also increases, the w that satisfies the free-entry condition is not that high
  - $\rightarrow$  Selection of ex-ante types on entry not that demanding
  - → Exit rates increase, as less *ex-ante* highly-productive incumbents

### Employment growth: identification of sorting parameter

#### 1. Same productivity process in all city-sizes

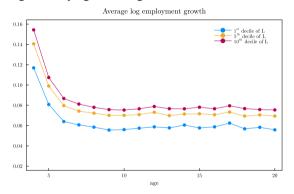
• Plot mean employment growth by age since age = 4



- Gap in employment growth in  $\log$  terms explained by city size and different exit profiles, not by differences in  $\mu_{ heta}$ 
  - $\rightarrow$  the elasticity of this gap to city-size identifies  $\eta$

### Employment growth: identification of sorting parameter

- 2. Ex-ante better firms in large cities (higher  $\mu_{\theta}$ )
  - Plot mean employment growth by age since age =4

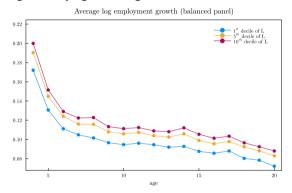


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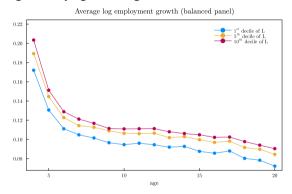
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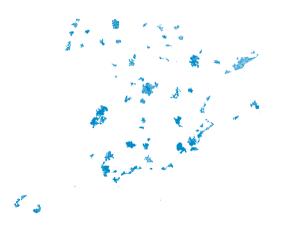
### Final remarks and Next steps

- Firm growth over the life cycle is higher in large cities, allowing firms to become larger
  - → This can be the result of agglomeration economies or differences in firms productivity across cities
- Using the predictions for firm growth of a standard firm dynamics model with agglomeration externalities, I propose a way to disentangle productivity differences from city-size advantages
- Next steps
  - Empirical implementation
     GMM with moment conditions arising from the model
  - Model extension
    - Model at this point unsuited for interesting place-based policy counterfactuals
       Entry subsidy does not change fundamental productivity of firms entering in each location
    - Firms may know their ex-ante productivity and then choose where to operate

# Appendix

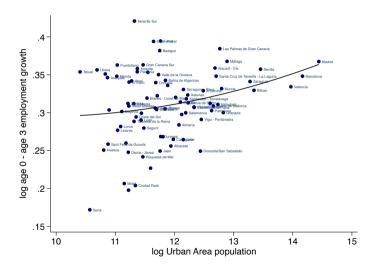
#### Urban Areas in Spain

 Spain has 85 Urban Areas defined by the Ministry of Transports and Mobility Smallest is Teruel with 32,500 people in 2004; largest is Madrid with 5,472,387 people in 2004



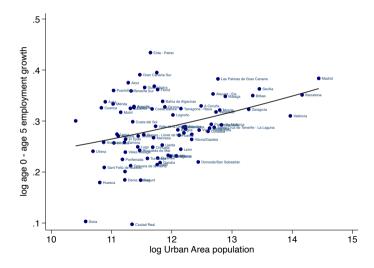


### 1'. Firm growth across the city-size distribution



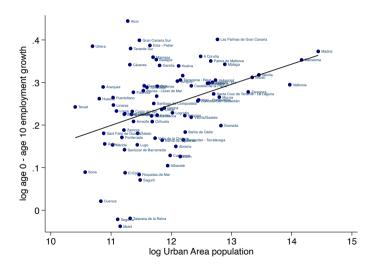


### 1'. Firm growth across the city-size distribution





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Allow local population to have a different effect along the firm life cycle

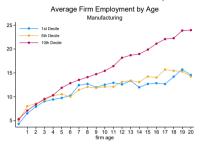
$$\log \text{firm growth}_{iust} = \alpha_{st} + \sum_{a}^{A} \gamma_a \mathbf{1}_{\{\mathsf{Age}_{iust} = a\}} + \sum_{a}^{A} \beta_a \log \text{population}_{ut} \times \mathbf{1}_{\{\mathsf{Age}_{iust} = a\}} + \epsilon_{iust}$$

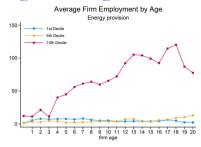
	$\log$ firm growth
Age=1 $ imes$ log population	0.0009
Age=2 $\times$ $\log$ population	0.0107***
Age=3 $ imes \log$ population	0.0083***
Age=4 $ imes \log$ population	0.0050***
Age=5 $ imes \log$ population	0.0057***
Age=6 $ imes \log$ population	0.0045***
Age=7 $ imes \log$ population	0.0046***
Age=8 $ imes \log$ population	0.0012
Age=9 $ imes \log$ population	0.0023***

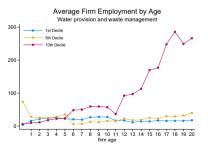
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0.0019**
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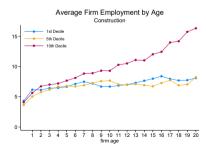
→ Firms grow more in large cities over their life-cycle (controlling by sector and age)



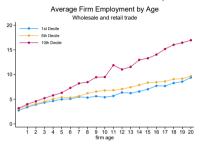


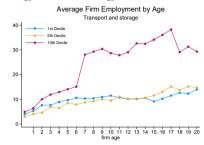


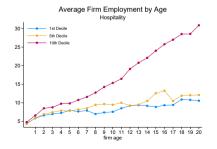


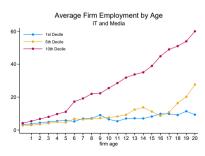






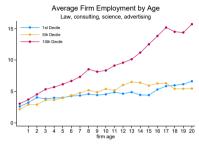


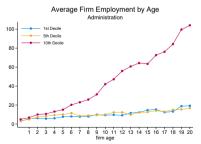


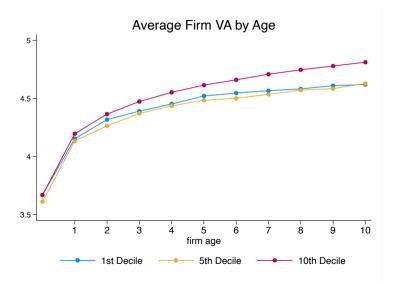


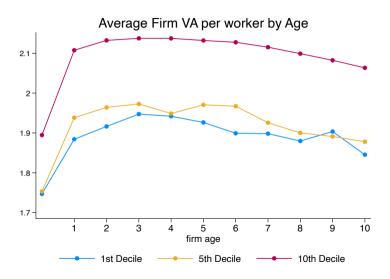


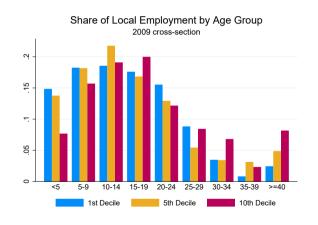




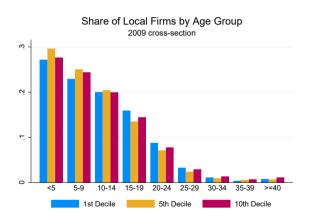




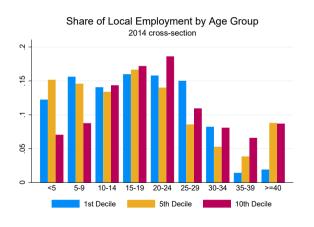




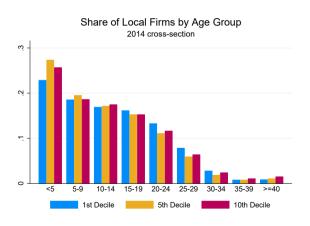
- → The share of local employment accounted for by old firms is larger in big cities
- → The firm age distribution is similar across the city-size distribution



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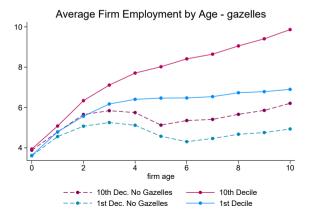
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#### 1'. Higher firm growth in large cities is driven by small group of high-growth firms

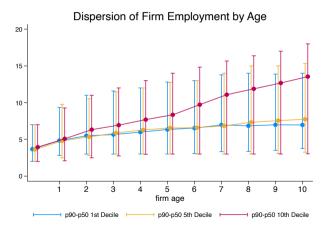
- The literature has emphasized that a small group of young firms (gazelles) account for a large share of employment growth (Haltiwanger et al. (2016), Sterk et al. (2021)) → define gazelles as firms that
  - (a) Grow at an annualized rate of 20% for their first 5 years of operation
  - (b) Reach at least 10 employees at some point during their life-cycle



- Only 4.1% of all startups in the economy
  - In smallest cities 3.9%, in largest 4.3%
  - Similar exit profiles across cities

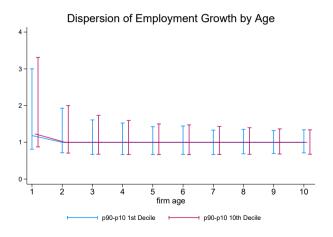
### 1'. Large firms drive the higher average life cycle growth in cities

 Compute the 90th and 50th percentile of the employment distribution at each age, for each UA size-decile



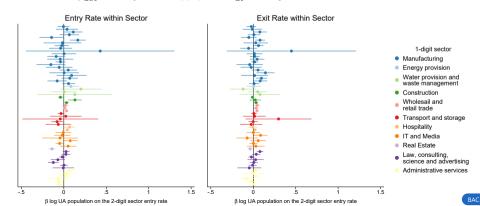
## 1'. Dispersion of firm growth is higher in large cities

 Compute the 90th and 10th percentile of the employment growth distribution at each age, for each UA size-decile



#### 2'. Entry and exit rates (at the sector level) are similar for cities of different size

- Some sectors may be characterized by higher entry and exit rates, and may be differenty present in large and small cities
  - → Define a market as UA 2-digit-sector combination and compute entry and exit rates as before
    - Keep sectors that are large enough (200 firms) and do not consider UA sectors with less than 10 firms
    - Still, several zeros, as in some markets no single firm enters or exits in some years → run Poisson regression at the sector level y<sub>ust</sub> = exp{α<sub>t</sub> + β log population<sub>ut</sub> + ε<sub>ust</sub>}



### 2'. Entrants in larger cities are more productive, yet not larger

• Regress firm K, L and TFPQ on city size, controlling by year or year-sector FE

	$\log TFPQ$	$\log TFPQ$	$\log K$	$\log K$	$\log L$	$\log L$
$\log$ population	0.0649***	0.0529***	-0.0171***	0.0094***	-0.0211***	-0.0045***
	(0.0025)	(0.0024)	(0.0036)	(0.0035)	(0.0014)	(0.0013)
Year FE 2-dig sector–year FE Observations $\mathbb{R}^2$	Yes	–	Yes	–	Yes	–
	No	Yes	No	Yes	No	Yes
	215740	215726	250059	250047	329755	329746
	0.006	0.084	0.006	0.101	0.004	0.082

Standard errors in parentheses. \* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01



## 2'. Exiters in larger cities are larger and more productive

• Regress firm K, L and TFPQ on city size, controlling by year or year-sector FE

	$\log TFPQ$	$\log TFPQ$	$\log K$	$\log K$	$\log L$	$\log L$
$\log$ population	0.0960*** (0.0017)	0.0870*** (0.0017)	0.0030 (0.0028)	0.0080*** (0.0027)	-0.0035*** (0.0012)	0.0120*** (0.0011)
Year FE	Yes	_	Yes	_	Yes	-
2-dig sector–year FE	No	Yes	No	Yes	No	Yes
Observations	510486	510475	603936	603926	723037	723030
$R^2$	0.028	0.111	0.007	0.108	0.027	0.117

Standard errors in parentheses. \* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

