
Master Thesis

- Implementation of stereo vision engine -

Project Report
Group 1072

Aalborg University
Electronics and IT

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Electronics and IT
Aalborg University
<http://www.aau.dk>

AALBORG UNIVERSITY

STUDENT REPORT

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Stereo vision implementation??

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Here is the abstract

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Contents

Preface	ix
1 Introduction	1
1.1 Stereo vision introduction	1
1.2 Motivation	2
1.3 Problem Introduction	2
1.4 Delimitation	2
1.5 Report Structure and Design Process	2
2 Application Analysis	5
2.1 The Basic Principal of Stereo Vision	5
2.2 Epipolar Geometry	8
2.3 Color space and gray scale	9
2.4 Resolution and disparity precision	10
2.5 Occlusions	11
2.5.1 Neighbor's Disparity Assignment : NDA	12
2.5.2 Diffusion in Intensity Space : DIS	12
2.5.3 Weighted Least Squares : WLS	13
2.5.4 Segmentation-based Least Squares : SLS	14
2.6 Mini-conclusion	15
3 Requirements	17
3.1 Requirement specification	17
3.2 Test specification	17
4 Algorithm design	19
4.1 Efficient Edge Preserving Stereo Matching:	19
4.2 Fast Cost-Volume Matching:	20
4.2.1 Guided image filter	20
4.3 Simulation and comparison	21
4.4 Choosing an algorithm	21

5	Platform Analysis	23
6	Design methodology	25
7	Architecture design	29
7.1	Parallelism Analysis	29
7.2	Allocation and Scheduling	30
7.2.1	RC scheduling	31
7.2.2	TC schedule	33
7.3	Finite State Machine with Data Path design	33
7.3.1	FSMD example	33
7.4	VHDL + Simulation	36
8	Acceptance test	39
9	Conclusion	41
	Bibliography	43
A	Allocation test	45
A.1	General procedure	45
A.2	Adder	46
A.3	Subtract	46
A.4	Adder/Subtract	46
A.5	Multiplier - LUT	46
A.6	Multiplier - DSP48	47
A.7	Divider	47
B	Extra Figures	49

■ find på et bedre navn til denne sektion	15
■ Få lavet en tabel som indeholder kravene	17
■ Regner med at lave en test hvor jeg med min egen python simulering trækker dataen ud lige før hvor dataen skal bruges i det jeg har fået lavet et hardware design af. så vil jeg samligne med middlebury test sets	17
■ skriv hvordan jeg vil teste de forskellige krav	17
■ beskrive middlebury test sets her? Nej beskriv dem i appendix	17
■ ROUGH SKETCH not done yet	19
■ simulation af de 2 algorithmmer og samlign resultaterne.	21
■ Nok en anden titel til denne sektion. Skriv hvilken algorithmme jeg går videre med	21
■ beskriv Zynq platformen. kom ind på hvad den indeholder	23
■ bedre navn og cite ds190 product specification og måske trm?	23
■ FPGA constraints ==> $C = f(A, T, P, N)$, Lav en tabel	23
■ læs om system design methodologies i gajski's Embedded Systems De- sign - Modeling, Synthesis and Verification og beskriv Platform Method- ology	25
■ NOT DONE! rough sketch. De nedenstående trin er hvad jeg skal igen- nem: Para. Anal., Alloc., Optimizaiton, FSMMD og VHDL + simulering	29
■ lav om til operation og husk mult	31
■ find et bedre ord	33
■ tjek op på synkront dataflow diagram og state diagram	33
■ tænk i register! transfer! level og ikke i FSMMD	33
■ udfør accept test udfra test specifikationen (brug data fra python simuler- ing og giv det til VHDL implementationen)	39

Preface

Here is the preface. You should put your signatures at the end of the preface.

Aalborg University, September 23, 2016

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Chapter 1

Introduction

In this chapter, the project is introduced and motivated. Furthermore, a brief description is presented for stereo vision and the use for it at HSA systems. Lastly, this chapter also describes a delimitation of the project and report.

1.1 Stereo vision introduction

In 280 A.D the greek mathematician Euclid noticed that the perception of depth is caused by each eye receiving a dissimilar image of the same object. Throughout history different people have been working on this this concept. In 1933 Sir Charles Wheatstone began mimic and forced the perception of depth by developing the stereoscope. The stereoscope use images taken by two cameras placed next to each other and the stereoscope then isolated the images so each eye only see one image. This mimics the depth perception and the viewer would be able to see depth in the images. [7]

Beginning around 1970 computer vision began appearing and a big part of this area is stereo vision, the measurement of depth mimicing the human vision using two cameras [6]. The ability to measure depths enables a computer to distinguish between objects and hence better interact and react on the world.

HSA systems wish to follow packages going through their system. A strategically placed stereo vision camera will enable them to know how many and where these packages are in the system. In case of errors and the like the printer system is the able to notice when the conveyor belt is empty and ready to reset.

In future uses HSA system would like the stereo vision system to have very precise depth measurements of 2 mm.

1.2 Motivation

The area of stereo vision have be researched thoroughly and precise algorithms have been found but most algorithms are very heavy computational wise. HSA system wish for a stereo vision system which can run real-time (10 fps) and have a high precision of 2 mm.

1.3 Problem Introduction

HSA systems wish to follow packages going through their system. A strategically placed stereo vision camera will enable them to know how many and where these objects are in the system. The primary objectives of this is to:

- Analyze obstacles within stereo vision
- Analyze different stereo algorithms
- Design and optimize an architecture for executing stereo vision

1.4 Delimitation

This project is mainly concerned with the design and implementation of a hardware design for a FPGA. This project will not focus on developing a new stereo vision algorithm. Obstacles and issue with stereo algorithms will be analyzed but simpler solution will be used for most obstacles.

1.5 Report Structure and Design Process

The A³ model is a basic design model used internally at AAU and is illustrated on figure 1.1 on the facing page. The model consist of tree design domains which it will explore and it will help structure this report. These domains are Application, Algorithm and Architecture.

The search for a solution starts in the application domain where the problem and application are being explored. Chapter 2 on page 5: Application Analysis will explore the Application domain and the resulting specification for the application are presented in chapter 3 on page 17. In this project not a lot of applications are explored since the problem and the wanted application have been given by HSA system.

When moving to a new domain it can result in landing in different areas of the domain as seen on figure 1.1 on the next page. The solid arrows goes from a single

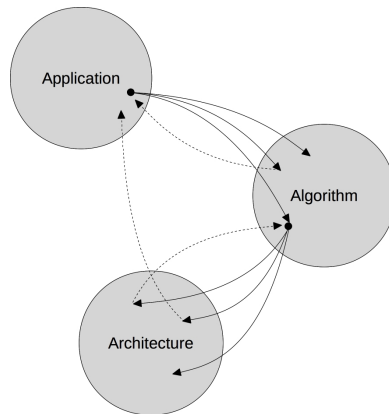


Figure 1.1: A³ model

point in the preceding domain and spreads out to different points in the current domain and these different points can, in the case of the algorithm domain, represent different algorithms. Chapter 4 on page 19 will explore the algorithm domain.

Chapter 6 on page 25 will described a methodology to go from a algorithm in the algorithm domain to some hardware architecture in the architecture domain.

Notice the dashed arrows in figure 1.1. These arrows shows that when you are exploring some domains new information might be given which require you to go back to a former domain and change the found specification etc. and then start moving to a new domain from new.

Chapter 8 on page 39 will test whether the found solution comply with the requirements in 3 on page 17 and chapter 9 on page 41 will conclude the project and its findings.

Chapter 2

Application Analysis

This chapter will explore the application domain from the A^3 model. First the basic principles of stereo vision will be described and then other aspects such as color versus grayscale etc. are analyzed. The results from this chapter will be used in the next chapter 3 on page 17.

2.1 The Basic Principal of Stereo Vision

A standard stereo vision setup consist of two similar cameras placed horizontally at a specified distance from each other. This distance is called the baseline. Figure 2.1 shows an example of this setup.

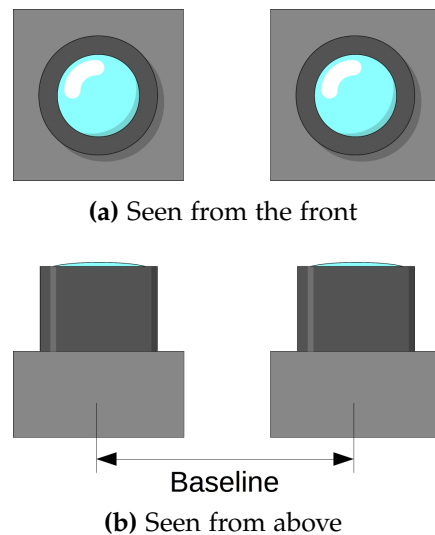


Figure 2.1: Illustration of a standard stereo setup

Figure 2.2 shows how a scene is seen by the camera, is inverted in the optical center and projected onto the image sensor in the camera. The original image plane is located at the position of the image sensor but it is inverted compared to scene captured. To simplified comparisons to the real world an image plane can be placed opposite of the optical center at the same distance from the center and this image plane will not be inverted.

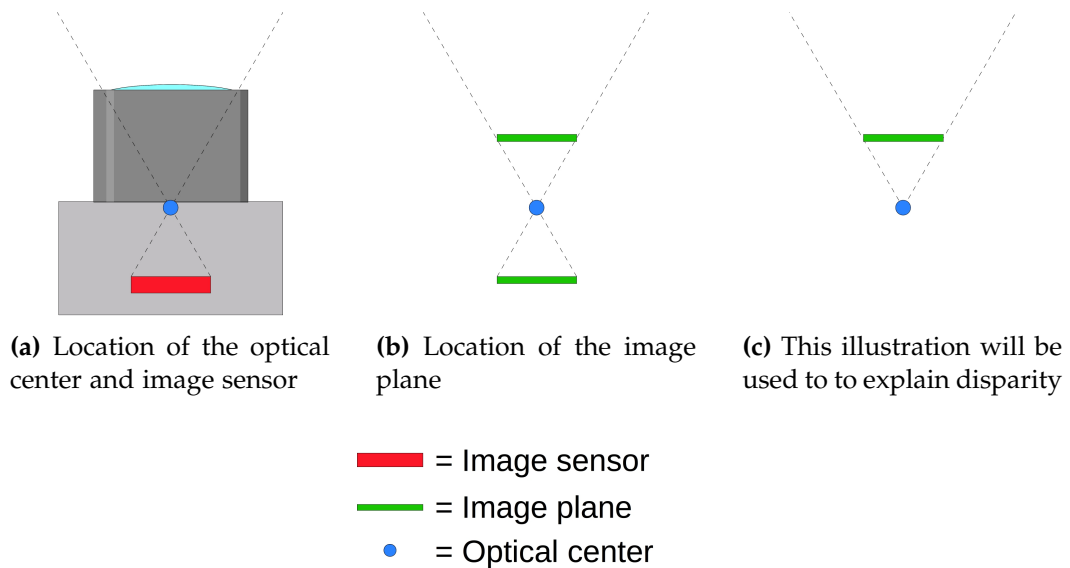


Figure 2.2: Illustration of going from camera to image plane

Figure 2.3a shows that a single camera is not able to differentiate between two points at the same angle from the optical center but a different distance. Figure 2.3b shows that adding the second camera shows that you then are able to differentiate between the two points.

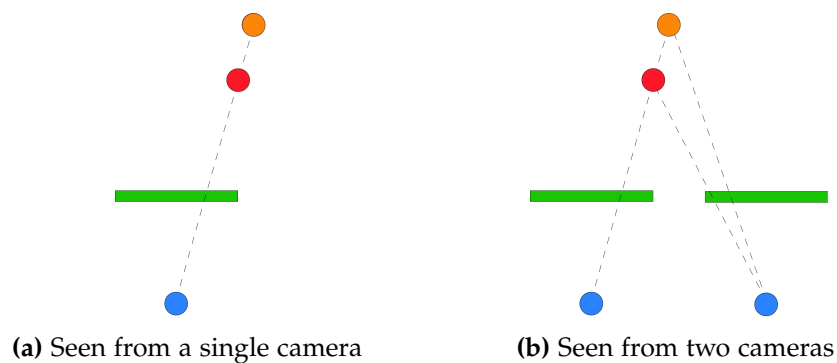


Figure 2.3: Example of two points in a scene at different depths

Figure 2.4 on the next page shows how the depth to a point can be calculated from

the difference in x-positions on the image plane (the disparity). Figure 2.4a and 2.4b shows how the disparity change depending on the distance to the point. Figure 2.4c shows the point in the scene (p), where line of sight cross the image planes (i_1 and i_2) and the optical centers (c_1 and c_2). From these points two similarly angled triangles can be created. One between p , i_1 and i_2 and the other triangle between p , c_1 and c_2 . For similarly angled triangles the ratio between the height and the bottom width is the same for each triangles and hence the following equation can be formed:

$$\frac{b}{z} = \frac{L}{z - f} = \frac{b - (x_1 - x_2)}{z - f} \quad (2.1)$$

$x_1 - x_2$ is also called the disparity, d , and equation 2.1 can be simplified:

$$z = \frac{b \cdot f}{d} \quad (2.2)$$

In equation 2.2 b and f is known hence only the disparity is needed to find z . So to find the distance to a point you should find the location of the point in the two images and calculate the displacement.

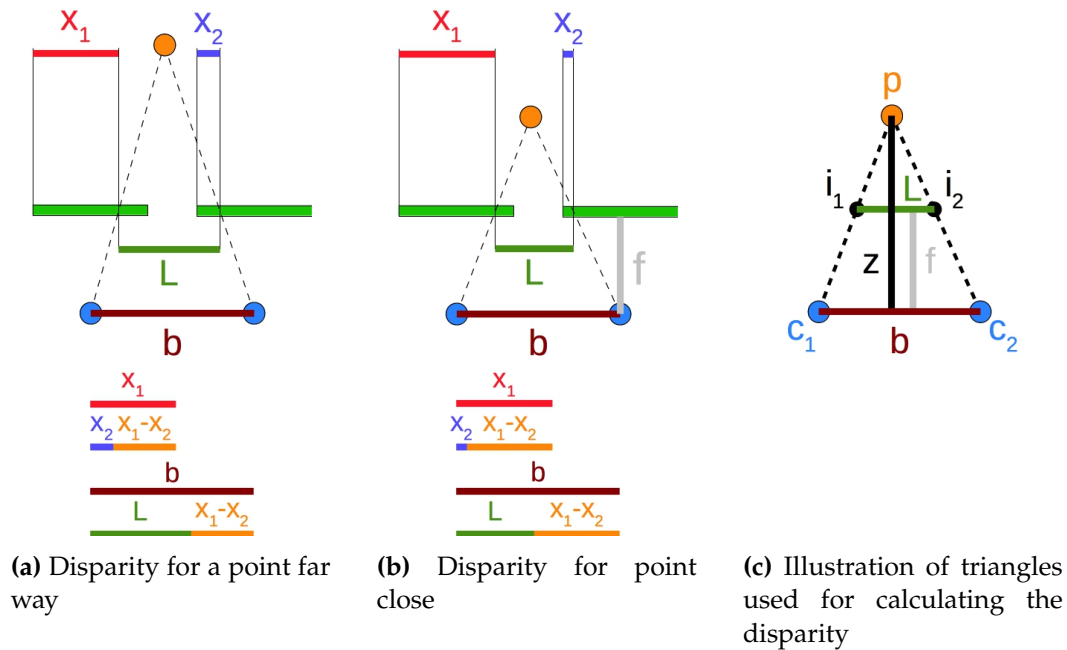


Figure 2.4: Illustration of how to calculate depth from disparity

This explains the basic of stereo vision. The rest of this chapter will venture into other areals of stereo and describe the difficulties and solutions for each area.

2.2 Epipolar Geometry

Section 2.1 assumes that the stereo image planes are ideal, align exactly and being parallel with the baseline but in a real scenario the cameras will have small imperfections and variations which will make the image planes not align perfectly.

Figure 2.5 shows a pair of stereo images. As seen when searching for a corresponding point in the second camera (e.g. the top of the bottle) then a 2D search area is needed. To simplify the search epipolar geometry can be used.

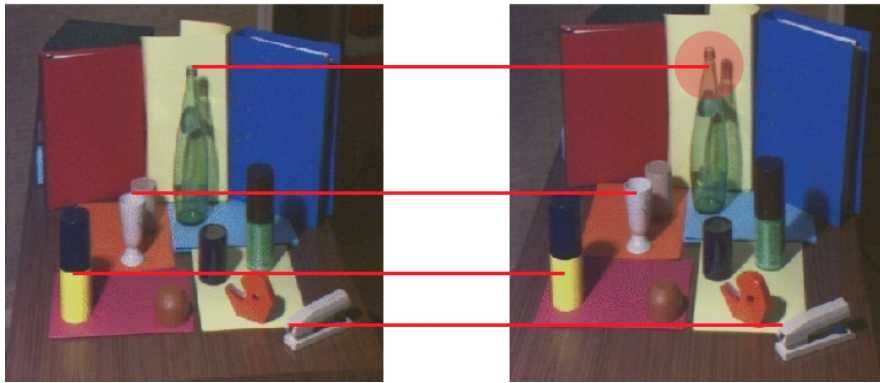


Figure 2.5: Non-rectified stereo pair [4]

Epipolar geometry occurs when a scene is seen from two different views. Figure 2.6 on the facing page illustrates epipolar geometry. An epipole is the projection, on one camera's image plane, of the optical center of the other camera and is illustrated on figure 2.6 on the next page as e_1 and e_2 . The red line going through p_1 (the projection of point P on the image plane) and e_1 is called an epipolar line and a corresponding epipolar line can be found in the other image plane going through p_2 and e_2 . When searching for the corresponding point in the other image the search can be simplified from a 2D search to a 1D search along the epipolar. To simplify the search further the image can be rectified.

Rectification will transform the stereo images to remove lens distortion and make them into standard form. The standard form is helpful since all epipolar lines then will be horizontal and this simplifies the search for corresponding points to search along the x-axis. Figure 2.7 on the facing page shows the stereo image pair from figure 2.5 but rectified. As seen, now the corresponding points can be found by following the horizontal lines or the x-axis.

The issue with rectification is that it is difficult to get a perfect match with the

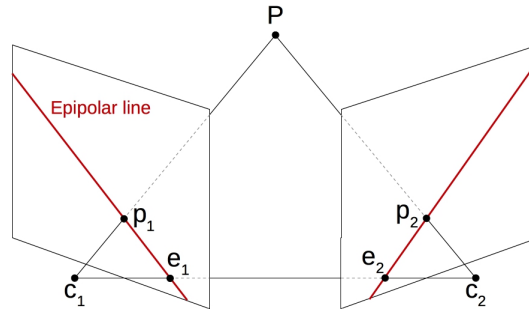


Figure 2.6: Illustration of epipolar geometry

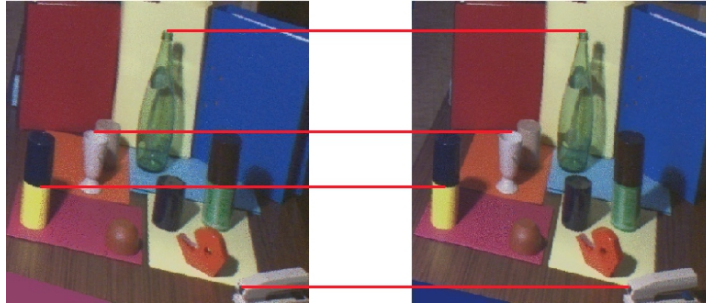


Figure 2.7: Rectified stereo pair [4]

stereo setup since the every camera and its objective will be unique and require and all new manual adjustment. HSA system theorizes that a system can be developed which instead of rectifying the image it will find the epipolar lines and feed this information to the stereo cameras.

In this project stereo image pairs from Middlebury Vision Test sets [5] will be used which are rectified hence the rectification of image will not be researched further in this project.

2.3 Color space and gray scale

Colors can be represented in many different ways digitally using color spaces. Two of the most common color spaces are grayscale and RGB. Some articles have researched what impact different color spaces can have on the result from a stereo algorithm.

For this project the impact of color spaces haven't been studied but instead the findings in [1] are used. This article studies the impact of color spaces on stereo matching by investigating 9 color spaces and 3 different methods. Table 2.1 on the following page shows parts of the results from [1]. In this table the *Measure* column

Measure	Type	Correct [%]	Time
Ncc	G	52.3	52
	C	55.2	141
D ₁	G	49.5	63
	C	51.6	140
PRATT	G	29.1	86
	C	45.2	225
ISC	G	44.9	126
	C	52.6	245
SMPD ₂	G	49.9	569
	C	56.5	2109

Table 2.1: Part of table containing results from [1]

is the algorithm used, *Type* specifies whether it is grayscale (G) or color (C) with the best color space used, the *Correct* column is the percentage of correct matches and *Time* is the execution time. The article conclude that using color always results in better matching but from table 2.1 it is notice that using grayscale lowers the execution time a lot (down to 27-51 % of color execution time) and in most cases not resulting much worse matching results.

Since the project mostly focus on a fast stereo matching algorithm and minding the results from table 2.1 it is decided to use gray scale in case Normalized Cross Correlation is used or to check whether gray scale gives much worse result of another algorithm.

2.4 Resolution and disparity precision

The depth resolution depends on different things in the stereo camera setup. The camera resolution, the focal length, the baseline etc. Looking at a equation 2.2 the constraints for a camera setup can be calculated. HSA system would requires that the system have a 2 mm depth resolution between 0.5 m and 1.5 m and the camera used will be a *Imaging Source DMK 72BUC02*. The range field (horopter) is what part of the system the

$$z = \frac{b \cdot f}{d} \quad (2.3)$$

2.5 Occlusions

Occlusions occurs when a object closer to the camera setup blocks some of object or a whole object behind it. Figure 2.8 illustrates two cylinders seen by a stereo camera setup where occlusion occurs. Figure 2.8a shows that the right camera can't see all of the blue cylinder because the red cylinder blocks the view while the left camera can see the whole of both cylinder. When searching for corresponding points in the occluded area issues occurs. Following the arrow on figure 2.8b it is seen that the edge of the blue cylinder can't be found and it will result in calculating a wrong disparity value.

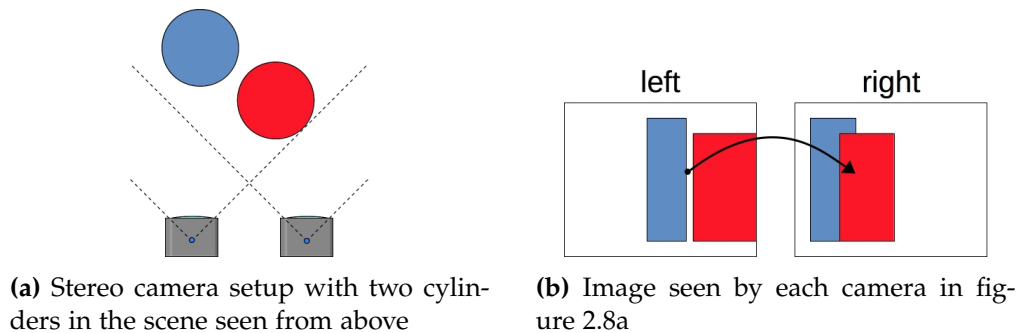


Figure 2.8: Illustration of occlusions

There exist different types of occlusions: partial occlusions, self occlusions, border occlusions and total occlusions. Partial occlusions is when an object is only partial obstructed as seen on figure ?? on page ?. Self occlusion occurs on round surfaces such as faces, and balls and as seen on figure 2.9a on the following page the surfaces marked with red can be seen by one camera but not the other camera. Border occlusions occurs when an object or part of an object is outside the view of one camera but not the other camera as seen with the blue object on figure 2.9b on the next page. Total occlusion is when an object is completely blocked by an object in the view of one camera but not in the other camera and an example of this is seen with the red object on figure 2.9b on the following page.

Occluded points can be found by running stereo matching again but switching which camera is used as reference and then compare the disparity values found for each direction. When occluded areas are found these can be filled using different methods. For this project new methods haven't been developed or studied but instead the findings from [3] is used which will be described in section 2.5.1 to 2.5.4 on pages 12–14. All these methods assume that the stereo matching is using the left image as reference i.e. the points in the left image are searched for in the right image.

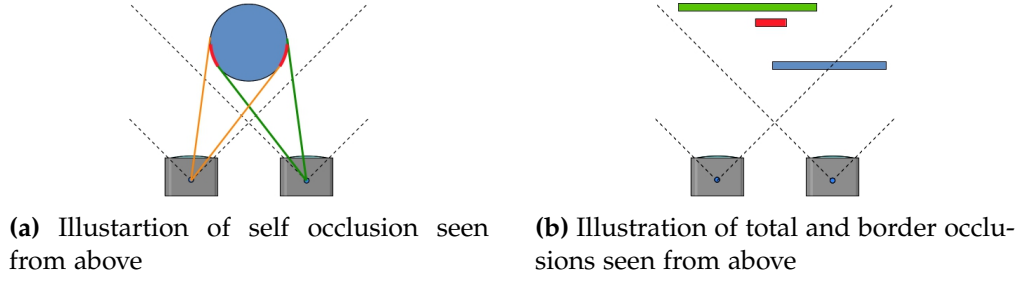


Figure 2.9: Illustration of different types of occlusions

2.5.1 Neighbor's Disparity Assignment : NDA

This is one of the simpler method to fill occlusions. It functions by selecting an occluded point, p_L , then find then nearest non-occluded point, q_L , to the left when filling non-border occlusion. With border occlusion the nearest point to the right is found instead. This method assumes that this non-occluded point is part of same surface as the occluded point (this can be seen on figure 2.8 on the previous page) and the disparity value from q_L can be assigned to p_L . This method have some issues. In cases of total occlusions (see figure 2.9b) wrong disparity values will be given to the total occluded object since it isn't a part of the nearest surface with non-occluded points to the left. In cases with self occlusions the occluded area should have disparity values close to the disparity values of the non-occluded points to the right (This will be the area of the surface which is in view of both cameras) but using NDA will give the occluded area disparity values corresponding to the background.

2.5.2 Diffusion in Intensity Space : DIS

This method is inspired by diffusion. Diffusion is the movement of molecules or atoms from a high concentration region to a low concentration region.

After detecting occluded regions with cross-checking during stereo matching, the diffusion energy for the region is approximated. This method is depended on the stereo matching algorithm because it use the energy from the last iteration to determine initial diffusion energy for the area. But a change to the method can be made to make it independent from the stereo matching. The initial energy will be 0. Then the diffusion energy for non-border occlusion is found by:

$$E(p_L) = \min_{l_{p_L} = \{0, \dots, l_{max}\}} \left(\frac{1}{2|q_L \in \mathcal{N}(p_L) \wedge l_{q_L} = l_{p_L}|} \sum_{q_L \in \mathcal{N}(p_L) \wedge l_{q_L} = l_{p_L}} (|\bar{I}(p_L) - \bar{I}(q_L)| + E(q_L)) \right) \quad (2.4)$$

And the diffusion energy for border occlusions are found by by:

$$E(p_L) = \min_{l_{p_L} = \{0, \dots, l_{p_{Lf}} - 2\}} \left(\frac{1}{2|q_L \in \mathcal{N}(p_L) \wedge l_{q_L} = l_{p_L}|} \sum_{q_L \in \mathcal{N}(p_L) \wedge l_{q_L} = l_{p_L}} (|\bar{I}(p_L) - \bar{I}(q_L)| + E(q_L)) \right) \quad (2.5)$$

The diffusion energy will be calculated for each occluded point and for each point the disparity which corresponds the minimum $E(p_L)$ is set as the disparity l_{p_L} for the occluded point.

2.5.3 Weighted Least Squares : WLS

In this approach, WLS, all the non-occluded and filled occluded neighbors in a neighborhood around the occluded point is considered valid points and is used as control points in interpolation.

Since the neighborhood contains both foreground points and background points and the occluded point is expected to be a part of the background then the background points should have more influence than foreground points. It is assumed that the color intensity between objects is significantly different and this property can be used to distinguish between foreground points and background points.

Each error term in the aggregated residual should be weighted so the foreground don't have much influence. With this the aggregated residual is defined as:

$$\Delta = \sum_{q_L \in \mathcal{N}(p_L)} w_{q_L} (\hat{l}_{p_L}(p_L) - l_{p_L}(q_L))^2 \quad (2.6)$$

where $w_{q_L} = e^{-\mu_L |\bar{I}(p_L) - \bar{I}(q_L)|}$ (the weight) is the likelihood of p_L with q_L under the assumption of an exponential distribution model of $|\bar{I}(p_L) - \bar{I}(q_L)|$. $\bar{I}(p_L)$ is the mean intensity of p_L and μ_L is the decay rate. $\hat{l}_{p_L}(p_L)$ is the estimated disparity of p_L (will be estimated during interpolation) and $l_{p_L}(q_L)$ is the disparity of q_L .

How to estimate $\bar{I}(p_L)$ and μ_L :

$\bar{I}(p_L)$ is the mean intensity of p_L which can be obtained using mean shift algorithm in a window around p_L . To estimate this value the initialize the algorithm with $\bar{I}(p_L)$ equal to the intensity of p_L then the mean shift algorithm repeatedly picks those neighbors inside the window that satisfy $|\bar{I}(p_L) - \bar{I}(q_L)| \geq 3\mu^{-1}$ and the assign the average of intensities of the selected neighbors to $\bar{I}(p_L)$ until $\bar{I}(p_L)$ converges to a fixed average. $|\bar{I}(p_L) - \bar{I}(q_L)|$ has decay rate μ_L which is related to the decay rate μ of the variable $|I(p_L) - I(q_L)|$ by $\mu_L^2 = \mu$.

A matrix containing all the coordinates:

$$F = \begin{bmatrix} x_1 & y_1 & 1 \\ \vdots & \ddots & \vdots \\ x_n & y_n & 1 \end{bmatrix} \quad (2.7)$$

Vector with the corresponding labels for the coordinates in F :

$$L = [l_1 \cdots l_N] \quad (2.8)$$

Linear model:

$$l_{p_L} = a + bx(p_L) + cy(p_L) \quad (2.9)$$

Where $(x(p_L), y(p_L))$ is the coordinates of p_L and a, b and c are the model parameters.

The weights for the control points can be express in a vector as:

$$w = [w_{q_{L1}} \ w_{q_{L2}} \ \cdots \ w_{q_{LN}}]' \quad (2.10)$$

Then we compute two new matrices, F_w and L_w :

$$F_w = \text{diag}(w)F \quad (2.11)$$

$$L_w = \text{diag}(w)L \quad (2.12)$$

The model parameter vector:

$$P = [a \ b \ c]' \quad (2.13)$$

By combining the equations above then the following equation is given:

$$P = (F_w^T F_w)^{-1} F_w^T L_w \quad (2.14)$$

With these equation the disparity of the occluded point can be estimated:

$$\hat{l}_{p_L} = [1 \ x(p_L) \ y(p_L)]P \quad (2.15)$$

2.5.4 Segmentation-based Least Squares : SLS

Biggest difference between WLS and SLS is that SLS only uses non-occluded points as control points. The control points is a subset of the non-occluded neighboring points. The control points are segmented from the neighborhood by applying different constraints: visibility constraint, disparity gradient constraint and color similarity cues.

Sequence of operations:

- Select an occluded point
- Select control points from the neighborhood around the occluded point
- Interpolate the disparity of the occluded point from the segmented control points

$\mathcal{N}(p_L)$ is a set of non-occluded, neighboring points which will be use for control points in the interpolation. For points to be added to \mathcal{N} then it needs to fulfill some constraints.

Disparity gradient constraint: In most cases the horizontal closest non-occluded point to the right, p_{Lf} , will be part of the foreground and the occluded should be a part of the background. In this cases every non-occluded point with a lower disparity than p_{Lf} will be added to \mathcal{N} hence the condition for added the point, q_L , will be $l_{q_L} < l_{p_{Lf}}$. If the foreground object is narrow then all the non-occluded neighboring points might be from the background and have the same disparity. Due to this a second condition have to be added to the constraint. The horizontal closest non-occluded point to the left will be called p_{Lb} and a second condition is created: $|l_{p_{Lb}} - l_{q_L}| \leq 1$. When these conditions are combined the constraint can be defined as:

$$|l_{p_{Lb}} - l_{q_L}| \leq 1 \vee l_{q_L} < l_{p_{Lf}} \quad (2.16)$$

surface constraint: It is assumed that $\mathcal{N}(p_L)$ will contain points from maximum 2 different surfaces (due to the small neighborhood). Some cases might contain a third surface but this is expected to occur very seldom and therefore it is disregarded. The point with the lowest disparity, l_{min} , is assumed to belong to one of the surfaces and the point with the highest disparity, l_{max} , is assumed to belong to the other surfaces. If $l_{max} - l_{min} \leq 1$ then it is assumed the all the points in \mathcal{N} belongs to a single surfaces otherwise the points have to be segmented into 2 groups. The first group will contain all points which satisfies $|l - max - l_{q_L}| \leq 1$ and the other group will contain all the points which satisfies $|l - min - l_{q_L}| \leq 1$.

Color constraint: The average truncated color distance from the occluded point, p_L , to each of the two groups to determine which group the point belongs to. The average truncated color distance is found by:

$$D(p_L, \mathcal{N}_i(p_L)) = \frac{1}{|\mathcal{N}_i(p_L)|} \sum_{q_L \in \mathcal{N}_i(p_L)} \psi(p_L, q_L) \quad (2.17)$$

2.6 Mini-conclusion

To conclude this chapter the findings for each area in stereo vision will be examined and it will be specified which solution will be used from this point.

find på et bedre navn til denne sektion

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Chapter 3

Requirements

3.1 Requirement specification

Få lavet en tabel som indeholder kravene

No.	Parameter	Value	Unit	Additional Information	Source
1	Something something	0 to 48	Mhz	• Something	1
2	Something something	0 to 48	Mhz	• Something	1
General requirements					
• Something something something					

3.2 Test specification

Regner med at lave en test hvor jeg med min egen python simulering trækker dataen ud lige før hvor dataen skal bruges i det jeg har fået lavet et hardware design af. så vil jeg samligne med middlebury test sets

skriv hvordan jeg vil teste de forskellige krav

beskrive middlebury test sets her? Nej beskriv dem i appendix

Chapter 4

Algorithm design

ROUGH SKETCH not
done yet

In this chapter the two stereo vision algorithms, Efficient Edge Preserving Stereo Matching (EPPSM) and Fast Cost-Volume Matching (FCV), is described. Lastly, a simulation of each algorithm is created and the results of these simulations are compared and from this, an algorithm is chosen.

4.1 Efficient Edge Preserving Stereo Matching:

This algorithm works in three steps. The first step is calculating a cost for each pixel and disparity. This cost is a combination of the sum of absolute differences and hamming distance of the census transform around each pixel.

$$C_d^{SAD}(x, y) = \sum_{i=1}^3 |I_{left}(x, y, i) - I_{right}(x + d, y, i)| \quad (4.1)$$

$$C_d^{CENSUS}(x, y) = Ham(CT_{left}(x, y), CT_{right}(x + d, y)) \quad (4.2)$$

$$C_d(x, y) = \alpha \cdot C_d^{SAD}(x, y) + (1 - \alpha) \cdot C_d^{CENSUS}(x, y) \quad (4.3)$$

where d is the disparity estimate, I_{left} is the left image, I_{right} is the right image, i is the color (rgb), $Ham(x_1, x_2)$ is the hamming distance between x_1 and x_2 , and CT_{left} and CT_{right} is the census transform around the specified pixel

then a permeability weight is calculated. Permeability is known from biomedicine and describes the ability to transfer through a membrane. The permeability weight is inspired by this and describes how well the color transfers from one pixel to another pixel.

$$\mu(x, y) = \min(e^{\frac{-\Delta R}{\sigma}}, e^{\frac{-\Delta G}{\sigma}}, e^{\frac{-\Delta B}{\sigma}}) \quad (4.4)$$

$$\mu_{tb}(x, y) = \min(e^{\frac{-(R(x, y) - R(x, y-1))}{\sigma}}, e^{\frac{-(G(x, y) - G(x, y-1))}{\sigma}}, e^{\frac{-(B(x, y) - B(x, y-1))}{\sigma}}) \quad (4.5)$$

lastly, the cost is aggregated resulting in a combined cost for each pixel at each disparity. The cost from equation ?? is first aggregated horizontally using permeability weights from equation ?. Then the result from horizontal aggregation is aggregated vertically also using the permeability weight.

$$C_d^{lr}(x, y) = C_d(x, y) + \mu_{lr}(x, y) \cdot C_d(x - 1, y) \quad (4.6)$$

$$C_d^{lr}(x, y) = C_d(x, y) + \sum_{i=1}^{x-1} \left(C_d(x - i, y) \cdot \prod_{j=i}^x \mu_{lr}(x - j, y) \right) \quad (4.7)$$

With a cost at each pixel at each disparity estimate, the disparity map can be generated by minimization along the disparity estimates.

4.2 Fast Cost-Volume Matching:

This algorithm starts by calculating a cost for each pixel at each disparity estimate. This cost consists of the sum of absolute differences and differences in the gradient.

$$C_d^{SAD}(x, y) = \sum_{i=1}^3 |I_{left}(x, y, i) - I_{right}(x + d, y, i)| \quad (4.8)$$

$$C_d^{Grad}(x, y) = \nabla_x I_{left}^g(x, y) - \nabla_x I_{right}^g(x, y) \quad (4.9)$$

$$C_d(x, y) = \alpha \cdot C_d^{SAD}(x, y) + (1 - \alpha) \cdot C_d^{Grad}(x, y) \quad (4.10)$$

These cost values are then filtered using a Guided Image Filter. The guided image filter is a filter uses a reference image to generate the weights. The guided image filter is described further in section 4.2.1

$$C'_d(x, y) = \sum_j W_{i,j}(I) C_d(x, y) \quad (4.11)$$

The correct disparity for each pixel can then be found by minimizing along the disparity estimates as seen in equation 4.12.

$$f(x, y) = \arg \min_{d \in [0, d_{max}]} C'_d(x, y) \quad (4.12)$$

4.2.1 Guided image filter

The guided image filter uses a image as a reference for weighting the input. The output from the filter is seen in equation

$$q_i = \sum_j W_{i,j}(I) p_j \quad (4.13)$$

$$q_i = a_k I_i + b_k, \forall i \in \omega_k \quad (4.14)$$

where:

$$a_k = \frac{\frac{1}{|\omega|} \sum_{i \in \omega_k} I_i p_i - \mu_k \bar{p}_k}{\sigma_k^2 + \epsilon} \quad (4.15)$$

$$b_k = \bar{p}_k - a_k \mu_k \quad (4.16)$$

algorithm

Input:

filtering input image: p

guidance image: I

radius: r

epsilon: ϵ

Output:

filtering output: q

Steps:

1. $\mu_I = f_{mean}(I)$
 $\mu_p = f_{mean}(p)$
 $\rho_{II} = f_{mean}(I \cdot I)$
 $\rho_{Ip} = f_{mean}(I \cdot p)$
2. $\sigma_I = \rho_{II} - \mu_I \cdot \mu_I$
 $cov_{Ip} = \rho_{Ip} - \mu_I \cdot \mu_p$
3. $a = cov_{Ip} / (\sigma_I + epsilon)$
 $b = \mu_p - a \cdot \mu_I$
4. $\mu_a = f_{mean}(a)$
 $\mu_b = f_{mean}(b)$
5. $q = \mu_a \cdot I + \mu_b$

4.3 Simulation and comparison

simulation af de 2 algoritmer og samlign resultaterne.

4.4 Choosing an algorithm

Nok en anden titel til denne sektion. Skriv hvilken algoritme jeg går videre med

Chapter 5

Platform Analysis

5.1

- beskriv Zynq platformen. kom ind på hvad den indeholder
- bedre navn og cite ds190 product specification og måske trm?
- FPGA constraints ==> C = f(A, T, P, N), Lav en tabel

Part	Quantity
Programmable logic cells	85,000
Look-Up Tables	53,200
Flip-flops	106,400
Extensible Block Ram	560 kB
Programmable DSP slices	220

Table 5.1: Parts on zynq 7020

Chapter 6

Design methodology

In [2] the Gajski-Kuhn Y-chart is described and it is illustrated on figure 6.1a. This chart can help describe a way to design a system. It moves between the three domains: Behaviour, Structure and Physical.

læs om system design methodologies i gajski's Embedded Systems Design - Modeling, Synthesis and Verification og beskriv Platform Methodology

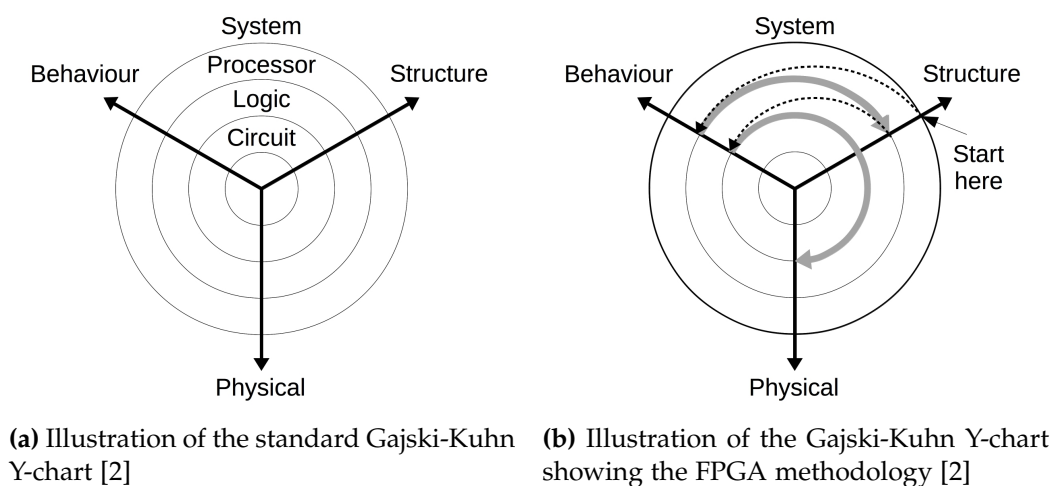


Figure 6.1: Illustrations of Gajski-Kuhn Y-chart

noter til mig selv

processor synthesis:

side 32 i gajski pdf

- (a) allocation of components and connections
- (b) cycle-accurate scheduling
- (c) Binding of variables, operations and transfers
- (d) Synthesis of controller

(e) Model refinement

(a-c) kan udføres sammen eller i hvilken som helst rækkefølge men de er afhængige af hinanden. Hvis de udføres samtidigt bliver synthesisen kompleks og utilregnelig. en strategi er at udføre det i følgende rækkefølge: a c b

Alle trinene ovenover kan udføres automatisk eller manuelt. Hvis det hele bliver udført automatisk kaldes det processor-level synthesis eller high-level synthesis (HLS). Hvis a-d bliver udført manuelt og e automatisk kaldes det model refinement.

System-level behavioral model / system synthesis: side 35

- (a) Profiling and estimation.
- (b) Component and connection allocation
- (c) Process and channel binding
- (d) Process scheduling
- (e) IF component insertion
- (f) Model refinement

1.3 System Design methodology: side 39

model algebra side 42

algebra:<objects, operations>

$$a * (b + c) = a * b + a * c$$

dette gør det muligt for system designere at optimere designet vha. arithmetic algebra regler. Udtrykket til venstre for = kræver en multiplier og en adder hvorimod udtrykket på højre side kræver 2 multipliers og en adder.

modelalgebra : <objects, compositions>

1.4 System-level models: side 44

applications designers, system designers og implementations designers.

2 system design methodologies side 56

Dette kapitel beskriver forskellige system design methodologies.

Bottom-up: start i bunden (circuit level) kød fra behavior til physical og lav et library. brug dette library til næste level.

Top-down: Start i øverste level (system level) kød fra behavior over til structure. gå et level ned og gentag. ved nederste level gå fra behavior til physical.

Platform methodology: side 61

FPGA methodology: side 64

er based på FPGA substrat som består af multitudine af 4-bits ROM celler (Look-up Tables (LUTs)) og disse LUTs kan implementere enhver 4-variable boolsk funktion. I denne design methodology vil hver RTL komponent i biblioteket være opbygget af disse 4-variable funktioner. Og derefter bliver processor delene synthesiseret af

disse RTL componenter.

sagt på en anden måde: denne metodologi bruger en top-down approach på både system og processor levels hvor standard og custom Processing Elements og Communication Elements er opbygget af LUTs. Et system design starter ved at man mapper en applikation ned på en given platform og derefter syntheser brugerdefineret komponenter ned til RTL komponenter som er defineret in form af LUTs. Standard processor komponenter i processor biblioteket er allerede defineret i form af LUTs. Når alle vores komponenter er defineret vha LUTs så simplificere vi designet ned til LUTs og BRAM og derefter kan vi udføre placering og routing med værktøjer FPGA producenten har udviklet.

Denne form for top-down metode har de samme svagheder som andre top-down metoder som er at det kan være svært at optimere hele designet ved at simplificere designet ned til basiske LUT celler. Derudover ved udvikler heller ikke om hvordan FPGA producentens værktøj placerer og forbinder LUTs og BRAMs.

Chapter 7

Architecture design

This chapter will describe the design process for the hardware architecture. In section ?? a parallelism analysis is performed. Section ?? will describe the allocation and scheduling of the hardware elements.

NOT DONE! rough sketch. De nedenstående trin er hvad jeg skal igennem: Para. Anal., Alloc., Optimizaiton, FSM D og VHDL + simulering

7.1 Parallelism Analysis

The inherent parallelism of the system has been analyzed to find out which improvements can be made. Figure xx shows a diagram of the whole system and on the following pages, data flow graphs (DFG) for each subsystem can be found.

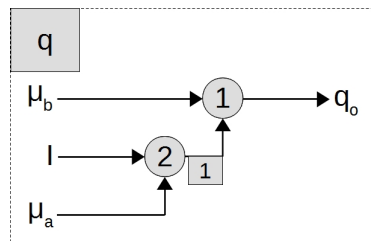


Figure 7.1: Synchronous data flow graph of the q block in the guided image filter

To find the parallelism in the system precedence graphs (PG) have to be created. Since the subsystems are simple the precedence graphs can be created looking at the system from end to start and for each operator find out which signal is needed and have to be calculated before. Another method is to create a synchronous data flow graph (SDFG) and from the SDFG a matrix, $\underline{\Gamma}$, can be created. This matrix expresses the relationship between the in- and outputs from each node in the SDFG and is called the *topology* matrix. An example of an SDFG is illustrated on in figure

7.1. In this example the topology matrix is then:

$$\underline{\underline{\Gamma}} = \begin{matrix} & \text{nodes} \\ \text{arcs} & \begin{bmatrix} -1 & 1 \end{bmatrix} \end{matrix} \quad (7.1)$$

If $\text{rank}(\underline{\underline{\Gamma}}) \leq s - 1$ where s is the number of nodes then a positive integer vector \underline{q} can be found such that $\underline{\underline{\Gamma}} \cdot \underline{q} = \underline{0}$. Then resulting \underline{q} is:

$$\underline{q} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad (7.2)$$

This \underline{q} vector expresses how many times each node have to be executed within one sample period.

With $\underline{\underline{\Gamma}}$ and \underline{q} a periodic admissible sequential sequence (PASS) can be found. This tells a sequential sequence in which the nodes can be executed and with it, a periodic admissible parallel sequence (PAPS) can be generated. To find the PASS generate a randomly ordered list of all the nodes, L . For each

7.2 Allocation and Scheduling

To develop a Finite State Machine (FSM) we need to know which hardware is allocated and when each operation is scheduled. This enables us to define some states for the FSM.

From section 7.1 on the previous page some precedence graphs are found and theses graphs shows how many FUs can run in parallel. We need to know how much hardware is needed for each FU. To calculated some simple system have been generate in Vivado 2016.2 and then synthesized. Then utilization of the hardware can be found. Appendix A on page 45 describes in detail the procedure and table ?? shows the result.

	LUT	FF	BRAM	DSP48
Adder	15	15	-	-
Adder/Subtractor	≈ 16	15	-	-
Subtract	15	15	-	-
Multiplier - LUT	352	36	-	-
Multiplier - DSP48	-	-	-	1
Divider	≈ 177	82	0.5	7

Table 7.1: Number of logic elements used in average for each FU

To create the FSM specification we need to introduce time into the precedence graphs to establish some states. To achieve this scheduling is used. There exists different methods for scheduling and some of these are:

- Resource Constrained (RC)
- Time Constrained (TC)

7.2.1 RC scheduling

For both methods the first step is create as soon as possible (ASAP) and as late as possible (ALAP) schedules. Then for the RC scheduling a ready list is created. This list contains a list of operations which are ready for scheduling and sorted by mobility. The mobility, $M(op)$, expresses the difference between the states in which the operation, op , have been scheduled in ASAP and ALAP schedules, e.i. $S_{ALAP}(op) - S_{ASAP}(op)$.

lav om til operation og
husk mult

Figure 7.2 shows an example of an ASAP and an ALAP schedule. As seen on the figure node 1-10, 13, 17, 20 and 22-23 are part of the critical path and therefore mobility is 0 for each of the nodes. Nodes 11-12,14-15,18 and 21 all have a mobility of 2 and nodes 16 and 19 have a mobility of 3.

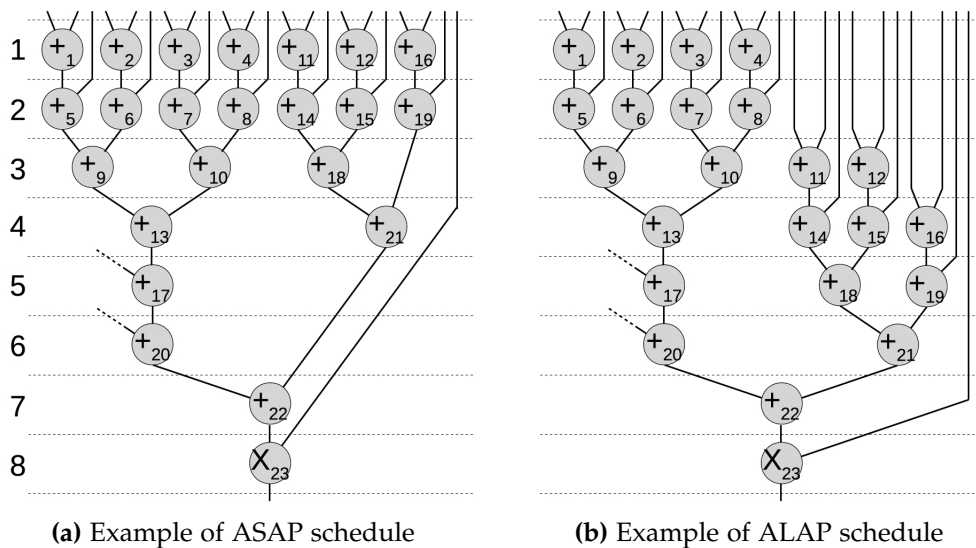


Figure 7.2: Illustration of ASAP and ALAP schedules. The illustration shows a part of the mean filter shown on figure ?? on page ??

With mobility found for each node/operation then a ready list can be generated. Add every ready node and then sort them by mobility. In the start the list would look like this: 1. node 1 ($M(+_1) = 0$), 2. node 2 ($M(+_2) = 0$), 3. node 3

($M(+_3) = 0$), 4. node 4 ($M(+_4) = 0$), 5. node 11 ($M(+_{11}) = 2$), 6. node 12 ($M(+_{12}) = 2$) and 7. node 16 ($M(+_{16}) = 3$).

Lets say the system have 3 ALU's available then node 1-3 can be scheduled to state 1 since they are higher on the ready list and there is no free ALU for the remaining nodes. The scheduled nodes are removed and the ready list is updated with newly available nodes. The list is still sorted by mobility and will now look like this: 1. node 4 ($M(+_4) = 0$), 2. node 5 ($M(+_5) = 0$), 3. node 6 ($M(+_6) = 0$), 4. node 7 ($M(+_7) = 0$), 5. node 11 ($M(+_{11}) = 2$), 6. node 12 ($M(+_{12}) = 2$) and 7. node 16 ($M(+_{16}) = 3$).

Then nodes 4-6 are scheduled into state 2 since they have lower mobility than the rest of the ready list. The list is updated again and will look like this: 1. node 7 ($M(+_7) = 0$), 2. node 8 ($M(+_8) = 0$), 3. node 9 ($M(+_9) = 0$), 4. node 11 ($M(+_{11}) = 2$), 5. node 12 ($M(+_{12}) = 2$) and 6. node 16 ($M(+_{16}) = 3$).

Nodes 7-9 are scheduled into state 3 and the list is updated again: 1. node 10 ($M(+_{10}) = 0$), 2. node 11 ($M(+_{11}) = 2$), 3. node 12 ($M(+_{12}) = 2$) and 4. node 16 ($M(+_{16}) = 3$).

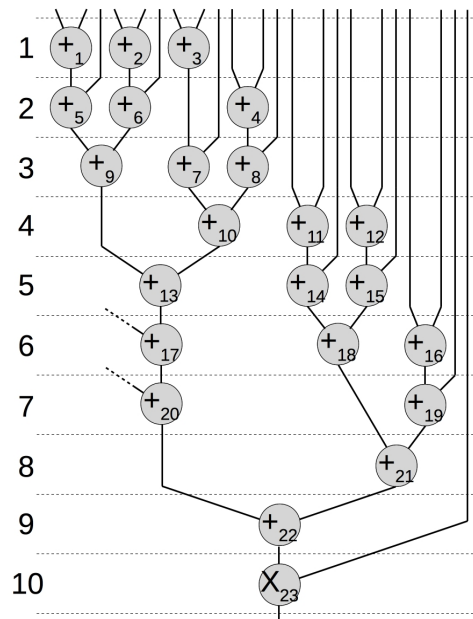


Figure 7.3: RC schedule

This is repeated until all nodes have been scheduled and the result is seen in figure 7.3. This schedule uses 2 states more than the ASAP and ALAP but it

reduces the cost since it uses 1 less ALU than the ALAP schedule and 5 less than the ASAP schedule.

This information is described in [2].

7.2.2 TC schedule

The RC schedule improves the cost of the implementation while the TC intends to improve the performance of the implementation. First a maximum number of states is decided and then ASAP and ALAP schedules are generated and mobility ranges are found. Then some probabilities are assigned to each operation. These probabilities express the probability for the specified operation to be scheduled in each state in its mobility range e.g. operation 11 in 7.2 on page 31 have $1/3$ probability for being scheduled in each of state 1-3 if maximum number of states is kept at 8. Figure 7.4 shows the probabilities for each operation in figure 7.2 on page 31. Fortsæt med at skrive senere

find et bedre ord

		ALU	MULT
1	$+_1$ $+_2$ $+_3$ $+_4$	$1 \times 4^{+1/3} \times 2^{+1/4} = 4^{11/12}$	0
2	$+_5$ $+_6$ $+_7$ $+_8$	$1 \times 4^{+1/3} \times 4^{+1/4} \times 2 = 5^{10/12}$	0
3	$+_9$ $+_{10}$	$1 \times 2^{+1/3} \times 5^{+1/4} \times 2 = 4^{2/12}$	0
4	$+_{13}$	$1^{+1/3} \times 4^{+1/4} \times 2 = 2^{10/12}$	0
5	$+_{17}$	$1^{+1/3} \times 2^{+1/4} \times 1 = 1^{11/12}$	0
6	$+_{20}$	$1^{+1/3} = 1^{1/3}$	0
7	$+_{22}$	1	0
8	\times_{23}	0	1

Figure 7.4: Probabilities for each operation in figure 7.2 on page 31

7.3 Finite State Machine with Data Path design

7.3.1 FSMD example

This section will contain an example of a FSMD design example but only of a small part of the system to show how to design a FSMD but also to show that it is a really extensive process. For this example the *b* block (see figure 7.17 on page 38) from the guided image filter (see figure 7.11 on page 37) and it is shown here on figure 7.5a on the following page.

tjek op på synkront dataflow diagram og state diagram

tænk i register! transfer! level og ikke i FSMD

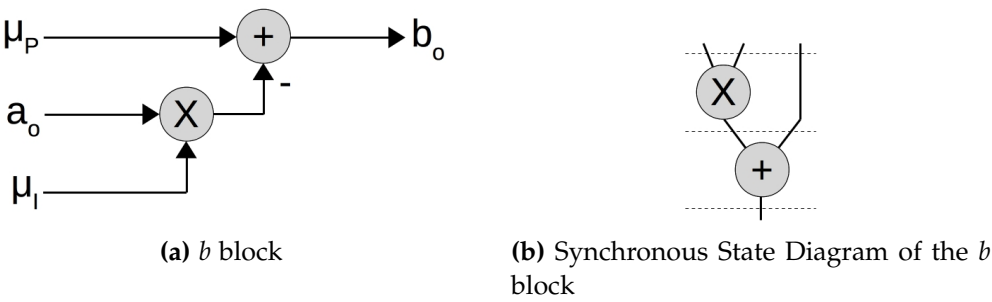


Figure 7.5: *b* block FSMDF stuff

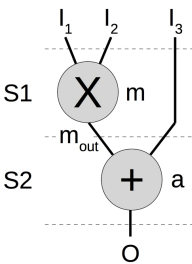


Figure 7.6: Synchronous State Diagram with every connection, functional units, in- and outputs named

	S ₁	S ₂
I ₁	✓	
I ₂	✓	
I ₃		✓
m _{out}		✓
O		✓

Table 7.2: Life-time analysis

```
-- test
...
begin
  process (clk) -- Sequential process
  begin
    if rising_edge(clk) then
      state <= next_state;
    end if;
  end process;

  process (state, reset, cars, short, long) -- Combinational process
```

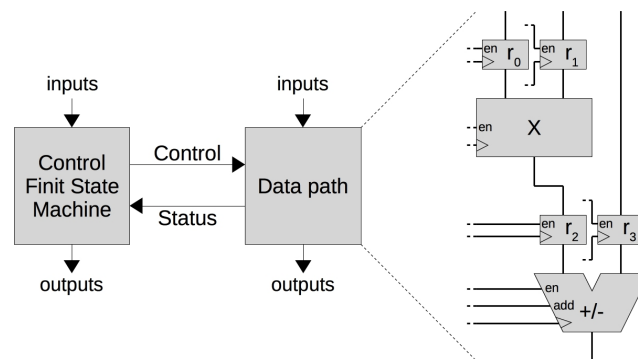


Figure 7.7: Finite State Machine with Data path and the design of the data path is shown.

```
begin
  if reset = '1' then
    next_state <= S1;
  else
    case state is
      when S1 =>
        m_out = I_1 * I_2;
      when S2 =>
        r_2 <= m_out;
        0 <= r_2 - I_3;
    end case;
  end if;
end process;
```

noter til mig selv

Controller <-signaler-> Data path

Controller:

Data path: indeholder register, FU, connections, network osv.

skal jeg lave et eksempel med en lille del af mit system? så kan man se hvor voldsomt det kan blive og se processen. Derefter kan jeg vise hvad jeg kommer frem til

noter fra møde med peter:

- lifetime analysis
- synchronous diagram

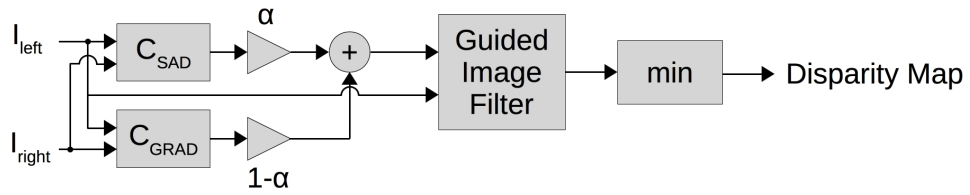
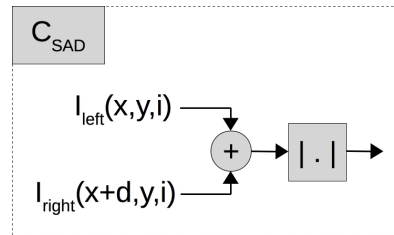
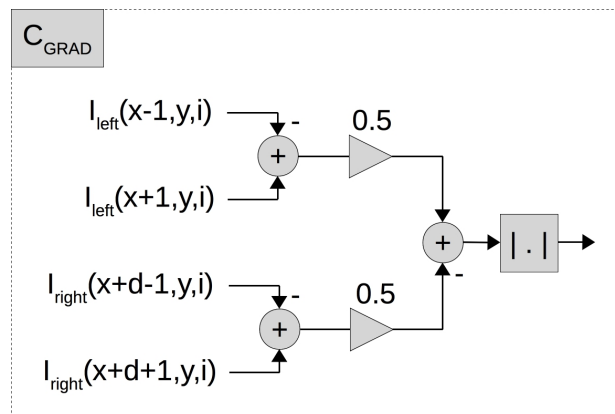


Figure 7.8: Data flow graph of the whole system

Figure 7.9: Data flow graph of the C_{SAD} block in figure 7.8Figure 7.10: C_{GRAD} ikke sikker

noter til mig selv

7.4 VHDL + Simulation

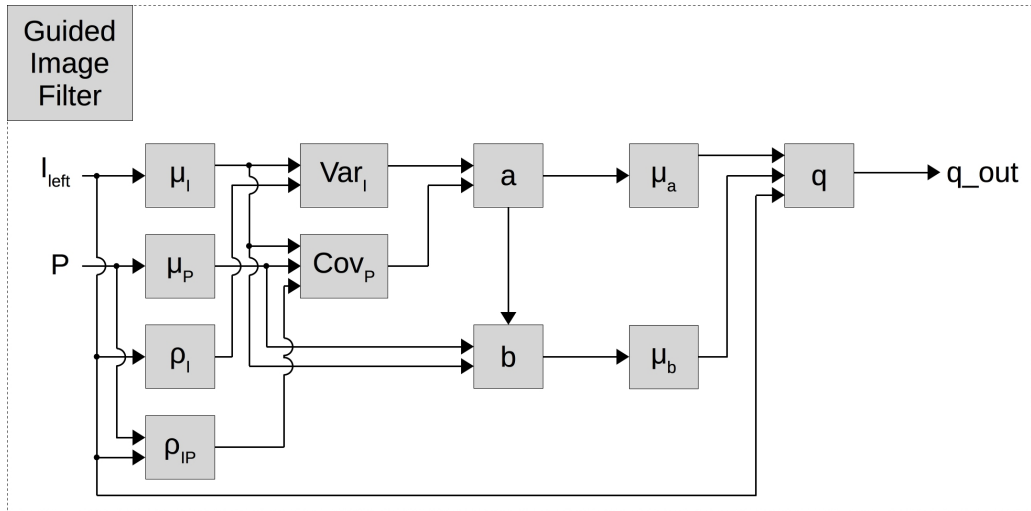


Figure 7.11: Guided image filter

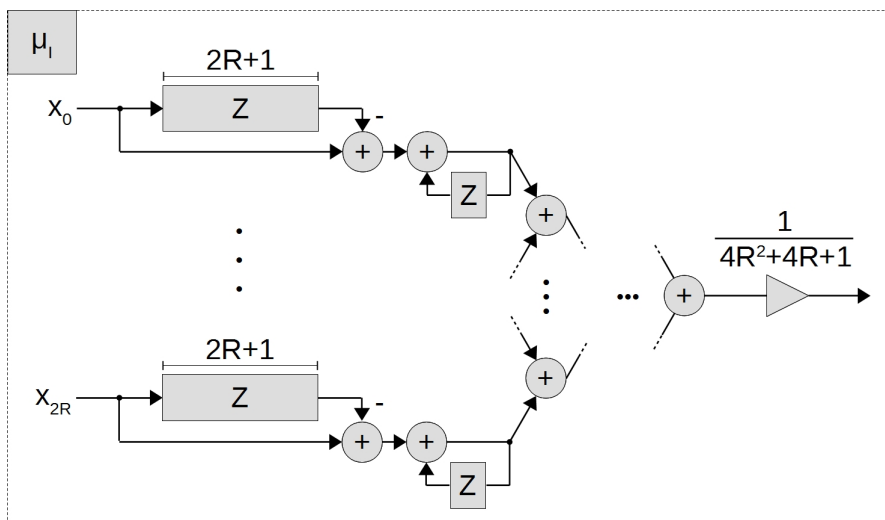


Figure 7.12: Mean filter

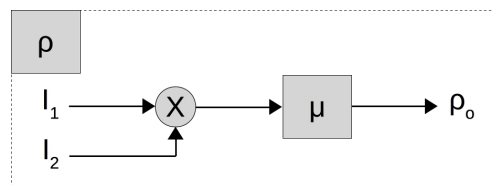


Figure 7.13: Correlation

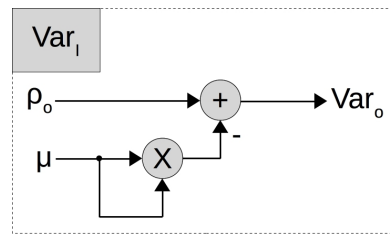


Figure 7.14: Variance

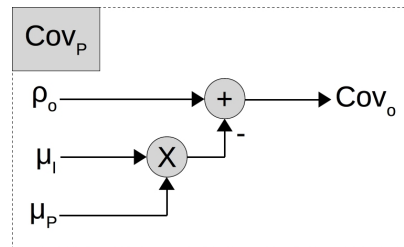


Figure 7.15: Covariance

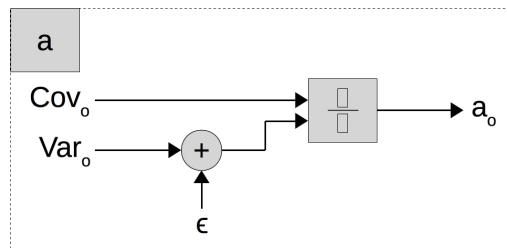


Figure 7.16: A box

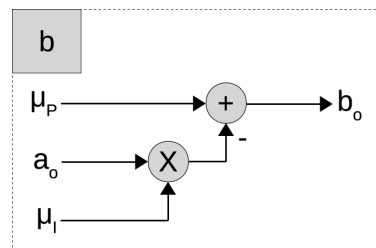


Figure 7.17: B box

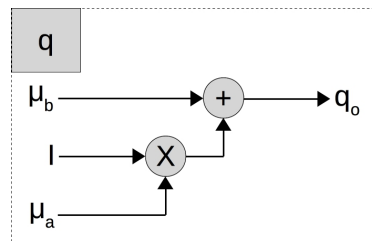


Figure 7.18: Q box

Chapter 8

Acceptance test

udfør accept test ud fra test specifikationen (brug data fra python simulering og giv det til VHDL implementationen)

Chapter 9

Conclusion

This chapter will contain the conclusion

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Appendix A

Allocation test

This appendix will explain how the average allocation of logic elements for each functional unit is found.

The result is used in table ?? on page ?? in chapter 7. The table is repeated here in table A.1

	LUT	FF	BRAM	DSP48
Adder	15	15	-	-
Adder/Subtractor	≈ 16	15	-	-
Subtract	15	15	-	-
Multiplier - LUT	352	36	-	-
Multiplier - DSP48	-	-	-	1
Divider	≈ 177	82	0.5	7

Table A.1: Number of logic elements used in average for each FU

A.1 General procedure

This section will describe the general procedure to find the utilization of logic elements for the specified FUs.

First a new project is created in Xilinx Vivado 2016.2. All the settings are set to standard except for the target which is set to ZedBoard Zynq Evaluation and Development Kit. Then a block design is created and a single IP of the wanted type is added. Then for each input and output a port is generated. The inputs are connected to the corresponding ports and between the output of the IP and the corresponding port a Xilinx Slice IP core is inserted which strips every bits except one (MSB) from the output and this IP is connected to the output and the port. This is done to not use to many I/O ports which will make . Using TCL

commands the IP block is copied 99 times and for each copy a new slice and output port is generated and connected to the copy. The inputs are all connected the original corresponding ports except for the divider FU where each copy will have its own input ports. When everything have been connected then Vivado is set to generate top-level HDL wrapper for the block design. Run synthesis and implementation and after completion check the utilization table under the project summary. Note these values, go to the block design and change one of the slices to full output width. Then run synthesis and implementation again and notices if there is a difference in LUT utilization. The LUT utilization is this value minus the LUT value from the former run + 1. These values should be divided by 100 and inserted into table A.1 on the previous page.

The following sections will describe the specific settings for each FUs.

A.2 Adder

This FU uses the Xilinx Adder/Subtractor v12.0 LogiCORE IP. The IP is set to implement using *Fabric*. The inputs are set to a width of 15 bits, mode is set to *add* and the output is set to 15 bits and latency is set to 1. All control signals are disabled.

A.3 Subtract

This FU uses the Xilinx Adder/Subtractor v12.0 LogiCORE IP. The IP is set to implement using *Fabric*. The inputs are set to a width of 15 bits, mode is set to *subtract* and the output is set to 15 bits and latency is set to 1. All control signals are disabled.

A.4 Adder/Subtract

This FU uses the Xilinx Adder/Subtractor v12.0 LogiCORE IP. The IP is set to implement using *Fabric*. The inputs are set to a width of 15 bits, mode is set to *add subtract* and the output is set to 15 bits and latency is set to 1. All control signals beside the ADD signal are disabled.

A.5 Multiplier - LUT

This FU uses the Xilinx Multiplier v12.0 LogiCORE IP. The IP is set to construct the multiplier using *LUTs* and is set to optimize for speed. The inputs are set to a width of 18 bits and the output is set to 36 bits and pipeline stages is set to 1. All control signals are disabled.

A.6 Multiplier - DSP48

This FU uses the Xilinx Multiplier v12.0 LogiCORE IP. The IP is set to construct the multiplier using *Mults* and is set to optimize for speed. The inputs are set to a width of 18 bits and the output is set to 36 bits and pipeline stages is set to 1. All control signals are disabled.

A.7 Divider

This FU uses the Xilinx Divider Generator v5.1 LogiCORE IP. The algorithm type is set to *High Radix*. The inputs are set to a width of 8 bits and the output fractional width is set to 8 bits and latency is set to 3. All control signals are disabled. With this only 5 instances of the Divider is used since each instance uses a lot of IO and to ensure the ability to run implementation without error.

Appendix B

Extra Figures

noter til mig selv

This chapter will contain extra which might fill to much in the report. Looking at you precedence graphs. Maybe make it as fold out image as we did with large diagrams in earlier reports.