Master Thesis

- Implementation of stereo vision engine -

Project Report

Group 1072

Aalborg University
Electronics and IT

Here you can write something about which tools and software you have used for typesetting the document, running simulations and creating figures. If you do not know what to write, either leave this page blank or have a look at the colophon in some of your books.??

AALBORG UNIVERSITY

STUDENT REPORT

Title:
Stereo vision implementation??

Theme:
Master Thesis??

Project Period:
Spring Semester 2016

Project Group:
1072

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Copies: 4

Page Numbers: 37

Date of Completion:
August 16, 2016

Abstract:

Here is the abstract

Contents

Todo list

Preface

Here is the preface. You should put your signatures at the end of the preface.

Aalborg University, August 16, 2016

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Chapter 1

Introduction

In this chapter, the project is introduced and motivated. Furthermore, a brief description is presented for stereo vision and the use for it at HSA systems . Lastly, this chapter also describes a delimitation of the project and report.

Måske anden formulering

1.1 Stereo vision introduction

In 280 A.D the greek mathematician Euclid described the perception [3]
Human has the incredible ability of depth perception. This is due to our two eyes which are separated a bit from each other. Since the eyes are separated they each receive different images. These images are combined in the brain and enable us to perceive depth. This is shown on figure 1.1.
This concept can be used in computer system and enable a system to perceive depth and hence distinguish between different objects.
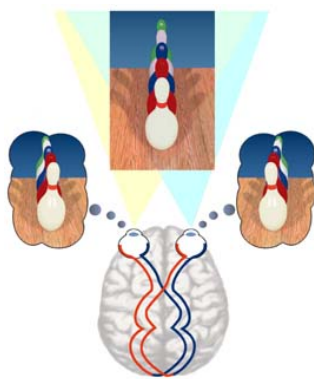
Figure 1.1: Example of human stereo vision [2]

1

Use of stereo vision:
Giving the ability of distinguishing between objects to a computer system gives the
system the ability to perform more task. These task includes counting number of
people entering pass through a secure door, enables a robot arm to interact with
different objects.

HSA systems wish to keep an eye on packages going through their system. A
strategically placed stereo vision camera will enable them to know how many and
where these objects are in the system.

1.2   Motivation

Stereo vision algorithms usually are very heavy computational wise. A high reso-
lution real-time stereo vision can be hard to acquire.

1.3   Problem Introduction

HSA systems wish to keep an eye on packages going through their system. A
strategically placed stereo vision camera will enable them to know how many and
where these objects are in the system. The primary objectives of this is to:

- Analyze obstacles within stereo vision

- Analyze different stereo algorithms

- Design and optimize an architecture for executing stereo vision

1.4   Delimitation

This project is mainly concerned with the design and implementation of a hard-
ware design for a FPGA. This project will not focus on developing a new stereo
vision algorithm. Obstacles and issue with stereo algorithms will not be

1.5   Report Structure and Design Process

The A3 methodology is a way to handle a system design. Figure 1 shows a dia-
gram of the A3 method. As seen it consist of 3 spaces: Application, Algorithm,
and Architecture. The report will follow this structure where chapter 2: Applica-
tion Analysis will explore the Application space and chapter 3: Requirements will
contain a specification for moving into the Algorithm space. Chapter 4: Algorithm
Analysis will explore the algorithm space with the requirements as constraints.
The chapter will conclude in the choice of an algorithm to be implemented on the
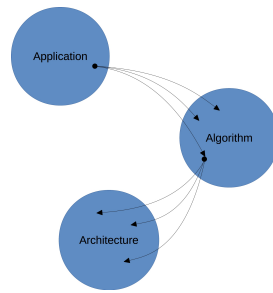
Figure 1.2: A3 model

hardware. Chapter 6: Design methodology will describe different methods which can be used to move from the algorithm space to the architecture space. Chapter 7: Architecture Design will explore the architecture space based on the chosen algorithm. The chapter will result in a implementation of the design on the hardware platform.

Chapter 2

Application Analysis

This chapter starts by describes the basic principles of stereo vision then different

aspects such as color versus gray scale etc are analyzed.

2.1 basic principal of stereo vision

A stereo vision setup normally consists of two cameras placed horizontally at a specified distance from each other (the baseline). An example of this is on figure 2.1

(a) Seen from the front

Baseline

(b) Seen from above
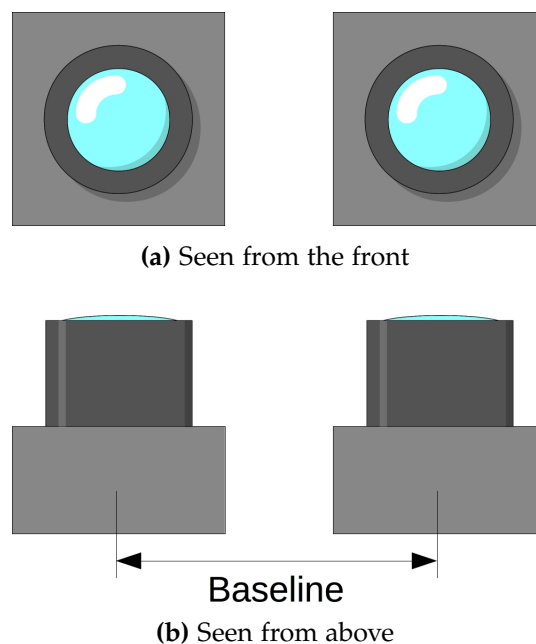
Figure 2.1: Illustration of stereo setup

Figure 2.2 shows how a scene is seen by the camera, is inverted in the optical center and projected onto the image sensor in the camera. The original image plane is located at the position of the image sensor but it is inverted compared to scene captured. To simplified comparisons to the real world an image plane can be placed opposite of the optical center at the same distance from the center and this image plane will not be inverted.

(a) Location of the optical center and image sensor

(b) Location of the image plane

(c) This illustration will be used to to explain disparity

= Image sensor
= Image plane
= Optical center
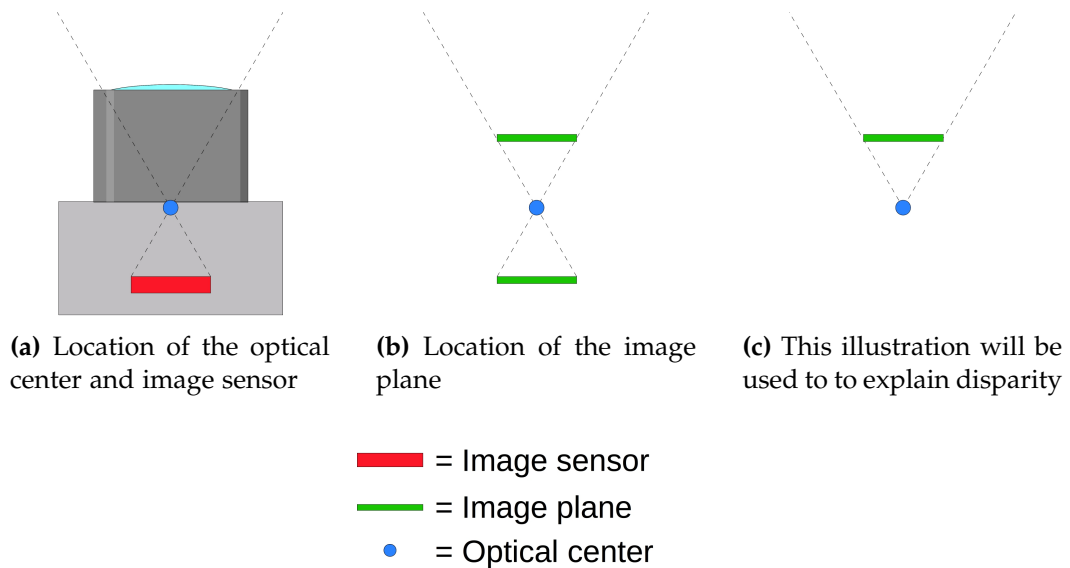
Figure 2.2: Illustration of going from camera to image plane

Figure 2.3a shows that a single camera is not able to differentiate between two points at the same angle from the optical center but a different distance. Figure 2.3b shows that adding the second camera shows that you then are able to differentiate between the two points.

(a) Seen from a single camera

(b) Seen from two cameras
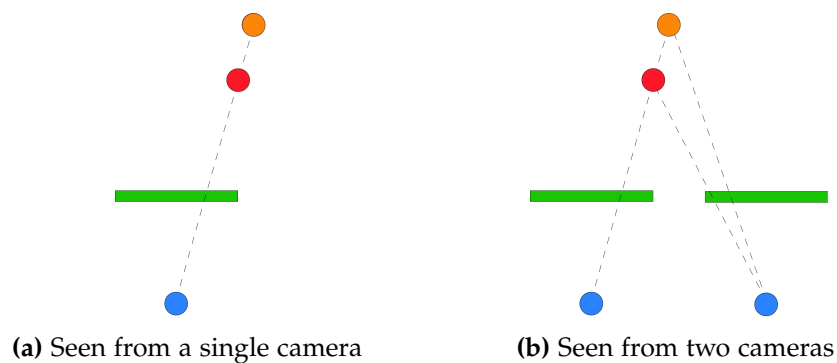
Figure 2.3: Example pf two points in a scene at different depths

Figure 2.4 shows how the depth to a point can be calculated from the difference in

x-positions on the image plane (the disparity). Figure 2.4a and 2.4b shows how the disparity change depending on the distance to the point. Two similar triangles can be created. One between the point, and the two optical centers. The other triangle is created between the point in the scene and the points where the dashed lines cross the image plane. Figure 2.4c shows these two triangles and their heights. The small triangle have a height of z and the bottom (the brown line) is equal to the baseline (purple line) minus the disparity and the large triangle have a height of $f + z$ and the bottom width is equal to the baseline. The ratio between the height and the bottom width is the same in the two triangles and hence the following equation can be formed:

$$\frac{z + f}{b} = \frac{z}{b - d} \tag{2.1}$$

$$z = \frac{b \cdot f}{d} \tag{2.2}$$
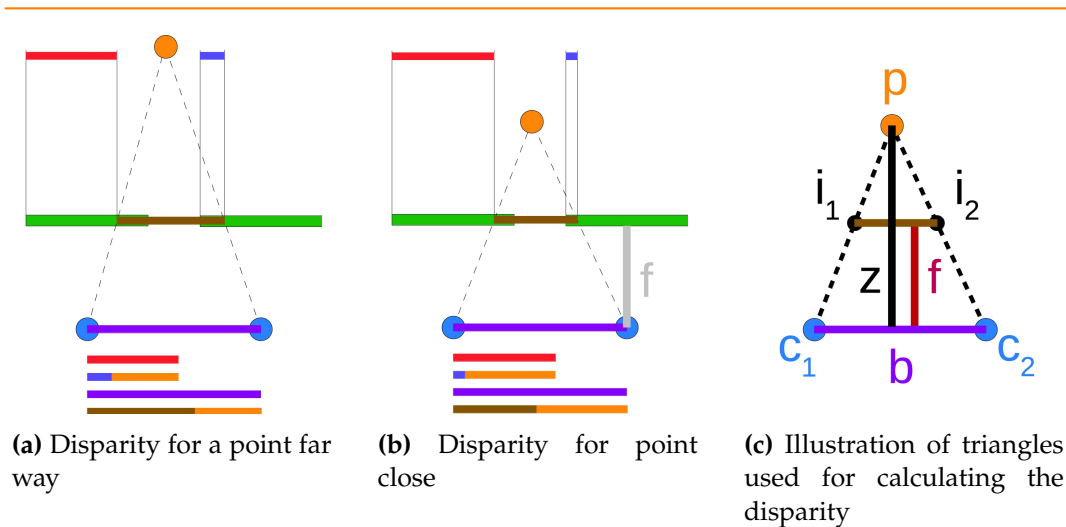
ret denne formel til på et tidspunkt. 2.2 er korrekt. Ændre den anden + måske figuren (z går vist fra baseline og ikke bare fra image plane)

(a) Disparity for a point far way

(b) Disparity for point close

(c) Illustration of triangles used for calculating the disparity

Figure 2.4: Illustration of how to calculate depth from disparity

This explains the basic of stereo vision. The rest of this chapter will venture into other areals of stereo and describe the difficulties and solutions for each area.

2.2 Rectification of stereo pairs

The examples in section 2.1 uses ideal images to explain how stereo vision functions but in the real world the disparity is the difference along the epipolar lines which will have a different slope of each line and image. Different things can be done to simplify the search along epipolar lines. One thing is to rectify the stereo

image pair. This will make all the epipolar lines horizontal and hence you only need to search along the x-axis.

The issue with rectification is that it is difficult to get a perfect match with the stereo setup since the every camera and its objective will be unique and require and all new manual adjustment. HSA system theorizes that a system can be developed which instead of rectifying the image it will find the epipolar lines and feed this information to the stereo camera. In this project stereo image pairs from Middlebury Vision Test set [**da**] will be used which are rectified hence the rectification of image will not be researched further in this project.

2.3   Color space and gray scale

> skriv noget om forskellige farve rum og grayscale og deres inflydelse på stereo algorithmen

The article **Color correlation-based matching** takes the subject of difference in result when using color and which color space is used and grayscale when performing stereo matching. It performs different methods / algorithms using 9 different colorspace including grayscale. The result from the article is that color gives a better result with a few percentage of more correct estimations but the run time is much higher (ranging from 1.9 to 3.7 higher run time than grayscale on the teddy test set). From this it is decided to not use color in case of Normalized Cross Correlation

2.4   Resolution and disparity precision

> skriv noget om disparitets opløsning i forhold til billede opløsning osv.

2.5   Occlusion filling

> skriv noget om metoder til at udfylde occlusions områder

This section will describe methods for filling the occluded areas. All these methods comes from the article: *Occlusion filling in stereo: Theory and experiments* by *Shafik Hyq, Andreas Koschan* and *Mongi Abidi*. All these methods assume that the stereo matching is going from left image to right image i.e. templates are taken from the left image matched onto the right image.

2.5.1   Neighbor's Disparity Assignment : NDA

This is the simplest method to fill occlusions. It functions by selecting an occluded point, p_L, then find then nearest non-occluded point, q_L, to the left when filling non-border occlusion. With border occlusion the nearest point to the right is found instead. It is assumed that this non-occluded point is part of same surface as the occluded point (this can be seen on figure **??**) and the disparity value from q_L can

be assigned to p_L. This method have some issues. In cases of total occlusions (see figure **??**) then a wrong disparity value is given to the total occluded object since it isn't a part of the nearest surface with non-occluded points to the left. In cases with self occlusions the occluded area should have disparity values close to the disparity values of the non-occluded points to the right (This will be the area of the surface which is in view of both cameras) but using NDA will give the occluded area disparity values corresponding to the background.

2.5.2   Diffusion in Intensity Space : DIS

This method is inspired by diffusion. Diffusion is the movement of molecules or atoms from a high concentration region to a low concentration region.
After detecting occluded regions with cross-checking during template matching, the diffusion energy for the region is approximated. This method is depended on the stereo matching algorithm because it use the energy from the last iteration to determine initial diffusion energy for the area.
A change to the method can be made to make it independent from the stereo matching. The initial energy will be 0. Then the diffusion energy for non-border occlusion is found by:

$$E(p_L) = \min_{l_{p_L}=\{0,...,l_{max}\}} \left(\frac{1}{2|q_L \in \mathcal{N}(p_L) \wedge l_{q_L}=l_{p_L}|} \sum_{q_L \in \mathcal{N}(p_L) \wedge l_{q_L}=l_{p_L}} (|\bar{I}(p_L) - \bar{I}(q_L)| + E(q_L)) \right)$$
(2.3)

And the diffusion energy for border occlusions are found by by:

$$E(p_L) = \min_{l_{p_L}=\{0,...,l_{P_{Lf}}-2\}} \left(\frac{1}{2|q_L \in \mathcal{N}(p_L) \wedge l_{q_L}=l_{p_L}|} \sum_{q_L \in \mathcal{N}(p_L) \wedge l_{q_L}=l_{p_L}} (|\bar{I}(p_L) - \bar{I}(q_L)| + E(q_L)) \right)$$
(2.4)

The diffusion energy will be calculated for each occluded point and for each point the disparity which corresponds the minimum $E(p_L)$ is set as the disparity l_{p_L} for the occluded point.

2.5.3   Weighted Least Squares : WLS

In this approach, WLS, all the non-occluded and filled occluded neighbors in a neighborhood around the occluded point is considered valid points and is used as control points in interpolation.
Since the neighborhood contains both foreground points and background points and the occluded point is expected to be a part of the background then the background points should have more influence than foreground points. It is assumed that the color intensity between objects is significantly different and this property

can be used to distinguish between foreground points and background points. Each error term in the aggregated residual should be weighted so the foreground don't have much influence. With this the aggregated residual is defined as:

$$\Delta = \sum_{q_L \in \mathcal{N}(p_L)} w_{q_L}(\hat{l}_{p_L}(p_L) - l_{p_L}(q_L))^2 \tag{2.5}$$

where $w_{q_L} = e^{-\mu_L|\bar{I}(p_L)-I(q_L)|}$ (the weight) is the likelihood of p_L with q_L under the assumption of an exponential distribution model of $|\bar{I}(p_L) - I(q_L)|$. $\bar{I}(p_L)$ is the mean intensity of p_L and μ_L is the decay rate. $\hat{l}_{p_L}(p_L)$ is the estimated disparity of p_L (will be estimated during interpolation) and $l_{p_L}(q_L)$ is the disparity of q_L.
How to estimate $\bar{I}(p_L)$ and μ_L:
$\bar{I}(p_L)$ is the mean intensity of p_L which can be obtained using mean shift algorithm in a window around p_L. To estimate this value the initialize the algorithm with $\bar{I}(p_L)$ equal to the intensity of p_L then the mean shift algorithm repeatedly picks those neighbors inside the window that satisfy $|\bar{I}(p_L) - I(q_L)| \geq 3\mu^{-1}$ and the assign the average of intensities of the selected neighbors to $\bar{I}(p_L)$ until $\bar{I}(p_L)$ converges to a fixed average. $|\bar{I}(p_L) - I(q_L)|$ has decay rate μ_L which is related to the decay rate μ of the variable $|I(p_L) - I(q_L)|$ by $\mu_L^2 = \mu$.
A matrix containing all the coordinates:

$$F = \begin{bmatrix} x_1 & y_1 & 1 \\ \vdots & \ddots & \vdots \\ x_n & y_n & 1 \end{bmatrix} \tag{2.6}$$

Vector with the corresponding labels for the coordinates in F:

$$L = [l_1 \ \cdots \ l_N] \tag{2.7}$$

Linear model:

$$l_{p_L} = a + bx(p_L) + cy(p_L) \tag{2.8}$$

Where $(x(p_L), y(p_L))$ is the coordinates of p_L and a, b and c are the model parameters.
The weights for the control points can be express in a vector as:

$$w = [w_{q_{L1}} \ w_{q_{L2}} \ \cdots \ w_{q_{LN}}]' \tag{2.9}$$

Then we compute two new matrices, F_w and L_w:

$$F_w = diag(w)F \tag{2.10}$$
$$L_w = diga(w)L \tag{2.11}$$

The model parameter vector:

$$P = [a \ b \ c]' \tag{2.12}$$

By combining the equations above then the following equation is given:

$$P = (F_w^T F_w)^{-1} F_w^T L_w \tag{2.13}$$

With these equation the disparity of the occluded point can be estimated:

$$\hat{l}_{p_L} = [1 \ x(p_L) \ y(p_L)] P \tag{2.14}$$

2.5.4 Segmentation-based Least Squares : SLS

Biggest difference between WLS and SLS is that SLS only uses non-occluded points as control points. The control points is a subset of the non-occluded neighboring points. The control points are segmented from the neighborhood by applying different constraints: visibility constraint, disparity gradient constraint and color similarity cues.
Sequence of operations:

- Select an occluded point

- Select control points from the neighborhood around the occluded point

- Interpolate the disparity of the occluded point from the segmented control points

$\mathcal{N}(p_L)$ is a set of non-occluded, neighboring points which will be use for control points in the interpolation. For points to be added to $\mathcal{N}$ then it needs to fulfill some constraints.
Disparity gradient constraint: In most cases the horizontal closest non-occluded point to the right, p_{Lf}, will be part of the foreground and the occluded should be a part of the background. In this cases every non-occluded point with a lower disparity than p_{Lf} will be added to $\mathcal{N}$ hence the condition for added the point, q_L, will be $l_{q_L} < l_{p_{Lf}}$. If the foreground object is narrow then all the non-occluded neighboring points might be from the background and have the same disparity. Due to this a second condition have to be added to the constraint. The horizontal closest non-occluded point to the left will be called p_{Lb} and a second condition is created: $|l_{p_{Lb}} - l_{q_L}| \leq 1$. When these conditions are combined the constraint can be defined as:

$$|l_{p_{Lb}} - l_{q_L}| \leq 1 \vee l_{q_L} < l_{p_{Lf}} \tag{2.15}$$

surface constraint: It is assumed that $\mathcal{N}(p_L)$ will contain points from maximum 2 different surfaces (due to the small neighborhood). Some cases might contain a third surface but this is expected to occur very seldom and therefore it is disregarded. The point with the lowest disparity, l_{min}, is assumed to belong to one of the surfaces and the point with the highest disparity, l_{max}, is assumed to belong to the other surfaces. If $l_{max} - l_{min} \leq 1$ then it is assumed the all the points in

$\mathcal{N}$ belongs to a single surfaces otherwise the points have to be segmented into 2 groups. The first group will contain all points which satisfies $|l - max - l_{q_L}| \leq 1$ and the other group will contain all the points which satisfies $|l - min - l_{q_L}| \leq 1$. **Color constraint:** The average truncated color distance from the occluded point, p_L, to each of the two groups to determine which group the point belongs to. The average truncated color distance is found by:

$$D(p_L, \mathcal{N}_i(p_L)) = \frac{1}{|\mathcal{N}_i(p_L)|} \sum_{q_L \in \mathcal{N}(p_L)} \psi(p_L, q_L) \qquad (2.16)$$

2.6   Mini-conclusion

find på et bedre navn til denne sektion

To conclude this chapter the findings for each area in stereo vision will be examined and it will be specified which solution will be used from this point.

•

Chapter 3

Requirements

3.1 Requirement specification

No.	Parameter	Value	Unit	Additional Information	Source
1	Something something	0 to 48	Mhz	• Something	1
2	Something something	0 to 48	Mhz	• Something	1

General requirements
• Something something something

3.2 Test specification

Chapter 4

Algorithm design

In this chapter the two stereo vision algorithms, Efficient Edge Preserving Stereo Matching (EEPSM) and Fast Cost-Volume Matching (FCV), is described. Lastly, a simulation of each algorithm is created and the results of these simulations are compared and from this, an algorithm is chosen.

4.1 Efficient Edge Preserving Stereo Matching:

This algorithm works in three steps. The first step is calculating a cost for each pixel and disparity. This cost is a combination of the sum of absolute differences and hamming distance of the census transform around each pixel.

$$C_d^{SAD}(x,y) = \sum_{i=1}^{3} |I_{left}(x,y,i) - I_{right}(x+d,y,i)| \tag{4.1}$$

$$C_d^{CENSUS}(x,y) = Ham(CT_{left}(x,y), CT_{right}(x+d,y)) \tag{4.2}$$

$$C_d(x,y) = \alpha \cdot C_d^{SAD}(x,y) + (1-\alpha) \cdot C_d^{CENSUS}(x,y) \tag{4.3}$$

where d is the disparity estimate, I_{left} is the left image, I_{right} is the right image, i is the color (rgb), $Ham(x_1, x_2)$ is the hamming distance between x_1 and x_2, and CT_{left} and CT_{right} is the census transform around the specified pixel
then a permeability weight is calculated. Permeability is known from biomedicine and describes the ability to transfer through a membrane. The permeability weight is inspired by this and describes how well the color transfers from one pixel to another pixel.

$$\mu(x,y) = \min(e^{\frac{-\Delta R}{\sigma}}, e^{\frac{-\Delta G}{\sigma}}, e^{\frac{-\Delta B}{\sigma}}) \tag{4.4}$$

$$\mu_{tb}(x,y) = \min(e^{\frac{-(R(x,y)-R(x,y-1))}{\sigma}}, e^{\frac{-(G(x,y)-G(x,y-1))}{\sigma}}, e^{\frac{-(B(x,y)-B(x,y-1))}{\sigma}}) \tag{4.5}$$

lastly, the cost is aggregated resulting in a combined cost for each pixel at each disparity. The cost from equation ?? is first aggregated horizontally using permeability weights from equation ??. Then the result from horizontal aggregation is aggregated vertically also using the permeability weight.

$$C_d^{lr}(x,y) = C_d(x,y) + \mu_{lr}(x,y) \cdot C_d(x-1,y) \tag{4.6}$$

$$C_d^{lr}(x,y) = C_d(x,y) + \sum_{i=1}^{x-1} \left(C_d(x-i,y) \cdot \Pi_{j=i}^{i} \mu_{lr}(x-1,y) \right) \tag{4.7}$$

With a cost at each pixel at each disparity estimate, the disparity map can be generated by minimization along the disparity estimates.

4.2   Fast Cost-Volume Matching:

This algorithm starts by calculating a cost for each pixel at each disparity estimate. This cost consists of the sum of absolute differences and differences in the gradient.

$$C_d^{SAD}(x,y) = \sum_{i=1}^{3} |I_{left}(x,y,i) - I_{right}(x+d,y,i)| \tag{4.8}$$

$$C_d^{Grad}(x,y) = \nabla_x I_{left}^g(x,y) - \nabla_x I_{right}^g(x,y) \tag{4.9}$$

$$C_d(x,y) = \alpha \cdot C_d^{SAD}(x,y) + (1-\alpha) \cdot C_d^{Grad}(x,y) \tag{4.10}$$

These cost values are then filtered using a Guided Image Filter. The guided image filter is a filter uses a reference image to generate the weights. The guided image filter is described further in section 4.2.1

$$C_d'(x,y) = \sum_j W_i, j(I) C_d(x,y) \tag{4.11}$$

The correct disparity for each pixel can then be found by minimizing along the disparity estimates as seen in equation 4.12.

$$f(x,y) = \arg \min_{d \in [0,d_{max}]} C_d'(x,y) \tag{4.12}$$

4.2.1   Guided image filter

The guided image filter uses a image as a reference for weighting the input. The output from the filter is seen in equation

$$q_i = \sum_j W_{i,j}(I)p_j \tag{4.13}$$

$$q_i = a_k I_i + b_k \quad , \forall i \in \omega_k \tag{4.14}$$

where:

$$a_k = \frac{\frac{1}{|\omega|}\sum_{i \in \omega_k} I_i p_i - \mu_k \bar{p}_k}{\sigma_k^2 + \epsilon} \tag{4.15}$$

$$b_k = \bar{p}_k - a_k \mu_k \tag{4.16}$$

algorithm

Input:
filtering input image: p
guidance image: I
radius: r
epsilon: ϵ
Output:
filtering output: q
Steps:

1. $\mu_I = f_{mean}(I)$
   $\mu_p = f_{mean}(p)$
   $\rho_{II} = f_{mean}(I \cdot I)$
   $\rho_{Ip} = f_{mean}(I \cdot p)$

2. $\sigma_I = \rho_{II} - \mu_I \cdot \mu_I$
   $cov_{Ip} = \rho_{Ip} - \mu_I \cdot \mu_p$

3. $a = cov_{Ip}/(\sigma_I + epsilon)$
   $b = \mu_p - a \cdot \mu_I$

4. $\mu_a = f_{mean}(a)$
   $\mu_b = f_{mean}(b)$

5. $q = \mu_a \cdot I + \mu_b$

4.3   Simulation and comparison

simulation af de 2 algo-
rithmer og samlign resul-
taterne.

4.4   Choosing an algorithm

Nok en anden titel til
denne sektion. Skriv
hvilken algorithme jeg
går videre med

Chapter 5

Platform Analysis

5.1

beskriv Zynq platformen. kom ind på hvad den indeholder

bedre navn og cite ds190 product specification og måske trm?

FPGA contraints ==> C = f(A, T, P, N), Lav en tabel

Part	Quantity
Programmable logic cells	85,000
Look-Up Tables	53,200
Flip-flops	106,400
Extensible Block Ram	560 kB
Programmable DSP slices	220

Table 5.1: Parts on zynq 7020

Chapter 6

Design methodology

In [1] the Gajski-Kuhn Y-chart is described and it is illustrated on figure 6.1a. This chart can help describe a way to design a system. It moves between the three domains: Behaviour, Structure and Physical.

(a) Illustration of the standard Gajski-Kuhn Y-chart [1]

(b) Illustration of the Gajski-Kuhn Y-chart showing the FPGA methodology [1]
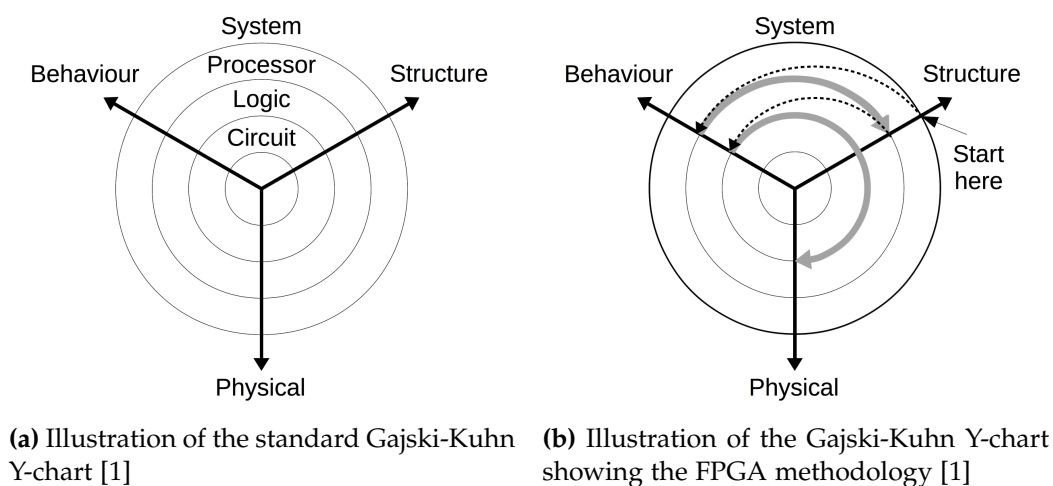
Figure 6.1: Illustrations of Gajski-Kuhn Y-chart

noter til mig selv

processor synthesis:
side 32 i gajski pdf
(a) allocation of components and connections
(b) cycle-accurate scheduling
(c) Binding of variables, operations and transfers
(d) Synthesis of controller

(e) Model refinement
(a-c) kan udføres sammen eller i hvilken som helst rækkefølge men de er afhængige
af hinanden. Hvis de udføres samtidigt bliver synthesen kompleks og utilregnlig.
en strategi er at udføre det i følgende rækkefølge: a c b
Alle trinene ovenover kan udføres automatisk eller manuelt. Hvis det hele bliver
udført automatisk kaldes det processor-level synthesis eller high-level synthesis
(HLS). Hvis a-d blvier udført manuelt og e automatisk kaldes det model refine-
ment.

System-level behavioral model / system synthesis: side 35
(a) Profiling and estimation.
(b) Component and connection allocation
(c) Process and channel binding
(d) Process scheduling
(e) IF component insertion
(f) Model refinement

1.3 System Design methodology: side 39
model algebra side 42
algebra:<objects, operations>
$a * (b + c) = a * b + a * c$
dette gør det muligt for system designere at optimere designet vha. arithmetic
algebra regler. Udtrykket til venstre for = kræver en multiplier og en adder hvo-
rimod udtrykket på højre side kræver 2 multipliers og en adder.
modelalgebra : <objects, compositions>

1.4 System-level models: side 44
applications designers, system designers og implementations designers.

2 system design methodologies side 56
Dette kapitel beskriver forskellige system design methodologies.
Bottom-up: start i bunden (circuit level) kør fra behavior til physical og lav et li-
brary. brug dette library til næste level.
Top-down: Start i øverste level (system level) kør fra behavior over til structure. gå
et level ned og gentag. ved nederste level gå fra behavior til physical.
Platform methodology: side 61
FPGA methodology: side 64
er based på FPGA substrat som består af multitude af 4-bits ROM celler (Look-up
Tables (LUTs)) og disse LUTs kan implementere enhver 4-variable boolsk funktion.
I denne design methodologi vil hver RTL kompement in biblioteket være opbygget
af disse 4-variable funktioner. Og derefter bliver processor delene synthesizeret af

disse RTL componenter.

sagt på en anden måde: denne methodologi bruger en top-down approach på både system og processor levels hvor standard og custom Processing Elements og Communication Elements er opbygget af LUTs. Et system design starter ved at man mapper en applikation ned på en given platform og derefter syntheser brugerdefineret kompenenter ned til RTL komponenter som er defineret in form af LUTs. Standard processor komponenter i processor biblioteket er allerede defineret i form af LUTs. Når alle vores komponenter er defineret vha LUTs så simplificere vi designet ned til LUTs og BRAM og derefter kan vi udføre placering og routing med værktøjer FPGA producentet har udviklet.

Denne form for top-down metode har de samme svagheder som andre top-down metoder som er at det kan være svært at optimere hele designet ved at simplificere designet ned til basiske LUT celler. Derudover ved udvikler heller ikke om hvordan FPGA producentens værktøj placerere og forbinder LUTs og BRAMs.

Chapter 7

Architecture design

This chapter will describe the design process for the hardware architecture. In section **??** a parallelism analysis is performed. Section **??** will describe the allocation and scheduling of the hardware elements.

NOT DONE! rough sketch. De nedenstående trin er hvad jeg skal igennem: Para. Anal., Alloc., Optimizaiton, FSMD og VHDL + simulering

7.1 Parallelism Analysis

The inherent parallelism of the system has been analyzed to find out which improvements can be made. Figure xx shows a diagram of the whole system and on the following pages, data flow graphs (DFG) for each subsystem can be found.
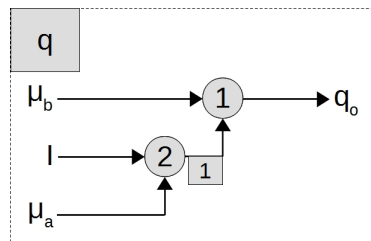
Figure 7.1: Synchronous data flow graph of the q block in the guided image filter

To find the parallelism in the system precedence graphs (PG) have to be created. Since the subsystems are simple the precedence graphs can be created looking at the system from end to start and for each operator find out which signal is needed and have to be calculated before. Another method is to create a synchronous data flow graph (SDFG) and from the SDFG a matrix, $\underline{\Gamma}$, can be created. This matrice expresses the relationship between the in- and outputs from each node in the SDFG and is called the *topology* matrix. An example of an SDFG is illustrated on in figure

7.1. In this example the topology matrix is then:

$$\underline{\underline{\Gamma}} = \begin{array}{c} \text{nodes} \\ \text{arcs} \end{array} \begin{bmatrix} -1 & 1 \end{bmatrix} \tag{7.1}$$

If $rank(\underline{\underline{\Gamma}}) \leq s - 1$ where s is the number of nodes then a positive integer vector $\underline{q}$ can be found such that $\underline{\underline{\Gamma}} \cdot \underline{q} = \underline{0}$. Then resulting $\underline{q}$ is:

$$\underline{q} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \tag{7.2}$$

This $\underline{q}$ vector expresses how many times each node have to be executed.

7.2   Allocation and Scheduling
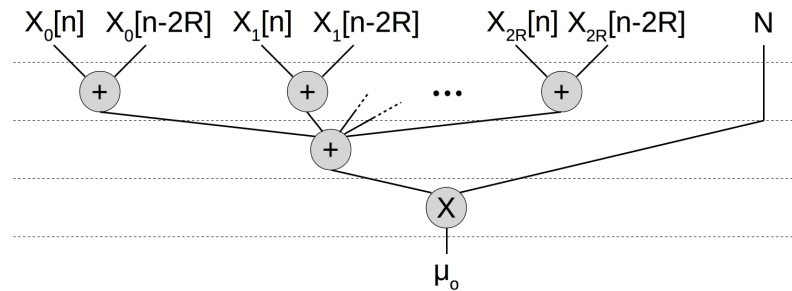
Figure 7.2: Precedence graph mean filter
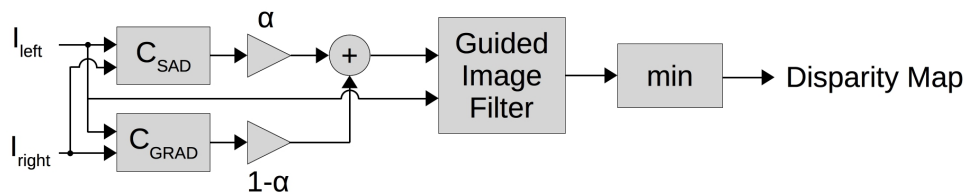
Figure 7.3: The complete system

noter til mig selv

lav dfg -> pg -> architecture. dette er steppet mellem algoritme og arkitektur domænerne i A3 modellen. Se første side i mm7 i reconf. kursuset.
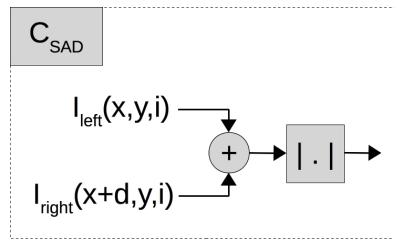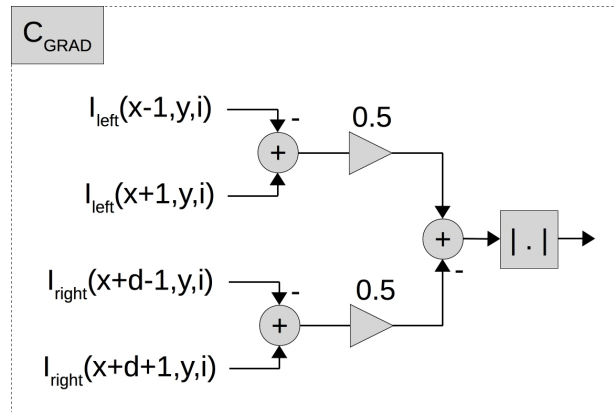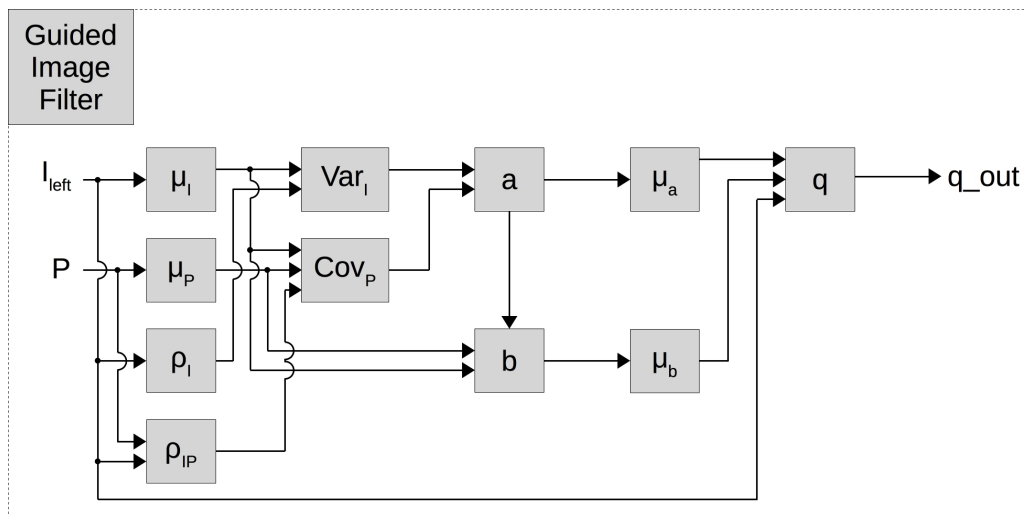
Figure 7.4: C_{SAD}

Figure 7.5: C_{GRAD} ikke sikker

Figure 7.6: Guided image filter

DSP ALG -> Precedence Graph -> Control data flow graph -> scheduling/allocation
-> FSMD specification -> assignment -> architecture
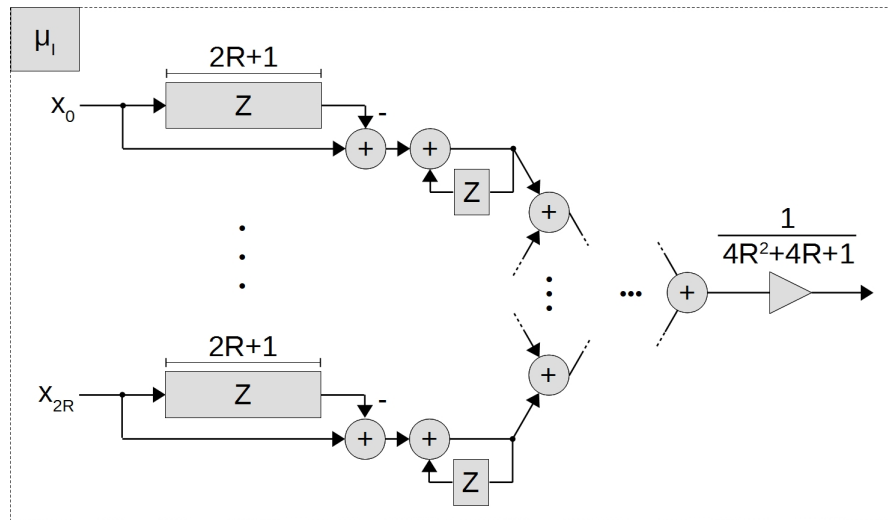mm7 side (3) Force Directed Scheduling
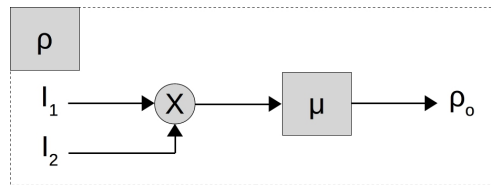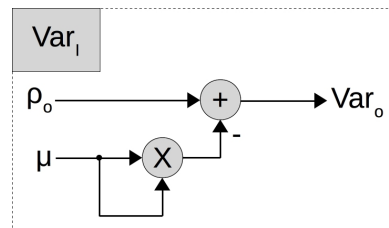
Figure 7.7: Mean filter

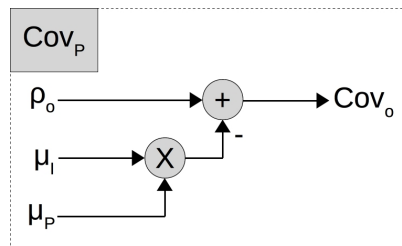**Figure 7.8:** Correlation

Figure 7.9: Variance
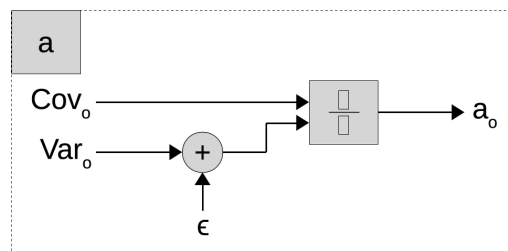

Figure 7.10: Covariance
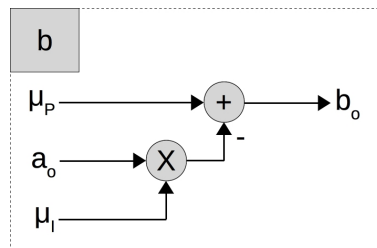
Figure 7.11: A box
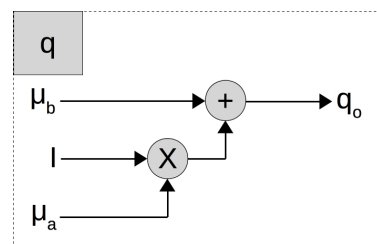

Figure 7.12: B box

Figure 7.13: Q box

Wanhammer [4] side 244 i pdf / 229 i bogen:
Precedence graphs. De beskriver in hvilken rækkefølge forskellige events (a,b,c) sker. order of occurrences of events
Latency: dette er tiden tager at genere et output fra man har modtaget input.
Throughput: dette er tiden mellem outputs
Interleaving: increase throughput af sekventielle algoritmer.

Fra wiki: https://en.wikipedia.org/wiki/Analysis_of_parallel_algorithms
tag det med en gran salt. er nok hovedsagligt til General Purpose Processors (GPP)
p processors, T_p time computation

- *work*: total number of operations on the processors. Is equal to T_1.

- *span*: the critical path. Length of longest series of data dependent operations. Is equal to T_∞

- *cost*: is pT_p and describes the total time spent by all p on both waiting and computing.

Laws:

- *Work law*: $pT_p \geq T_1$. the cost is at least equal to the work

- *Span law*: $T_p \geq T_\infty$. a finite number of processors, p, can't outperform an infinite number of processors

With these definitions and laws the following measures of performance can be given:

- *Speedup*: is the gain in speed when comparing parallel execution to sequential execution: $S_p = T_1/T_2$

- *Efficiency*: is the speedup per processor: S_p/p

- *Parallelism*: is the ratio T_1/T_∞ and it describes the maximum speedup on any number of processors. By *span law* the *parallelism* bounds the speedup: if $p > T_1/T_\infty$ then $T_1/T_p \leq T_1/T_\infty < p$

- *Slackness*: is $T_1/(pT_\infty)$. a slackness than one implies (by span law) that perfect linear speedup is impossible on p processors.

Execution on a limited number of processors
Parallelitets analyse bliver normalt udført under den antagelse at man har et ube-grænset antal processor tilgængeligt. Dette er selvfølgelig ikke realistisk men ikke et problem da hvilken som helst beregning som kan laves på N processorer kan også blive udført på p processorer hvor $p < N$ ved at lade hver processor udføre flere "enheders" arbejde.
Brent's law:
$$T_p \leq T_N + \frac{T_1 - T_N}{p}$$
$$T_p = O\left(T_N + \frac{T_1}{p}\right)$$
$\frac{T_1}{p} \leq T_p < \frac{T_1}{p} + T_\infty$ det viser at *span* og *work* giver nogle fornuftige grænser for computation time.

7.3 Allocating / Scheduling

7.4 Optimization

7.5 FSMD design

7.6 VHDL + Simulation

Box filter / Mean function

As seen from the guided image filter algorithm the mean function $f_{mean}(x)$ is used multiple q

memory requirement:

$3 \cdot 8$ bits per pixel (rgb image). test image is 741×497 so for the test image $8.838.648$ bits ≈ 9 megabit ≈ 1.1 megabyte.

this section should contain the design for my boxfilter or mean function

VHDL/Simulation

skriv om VHDL kode og simulation af filteret

Implementation/Test

skriv om implementation på FPGA'en og gerne verificere det virker

Chapter 8

Acceptance test

udfør accept test udfra test specifikationen (brug data fra python simulering og giv det til VHDL implementationen)

Chapter 9

Conclusion

This chapter will contain the conclusion

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