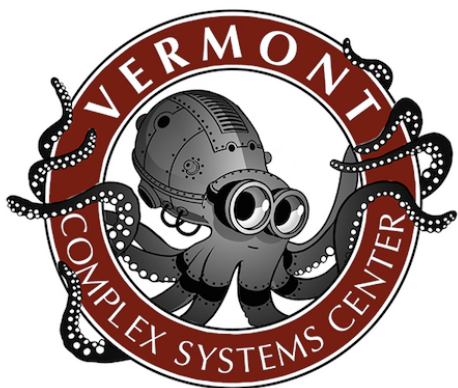
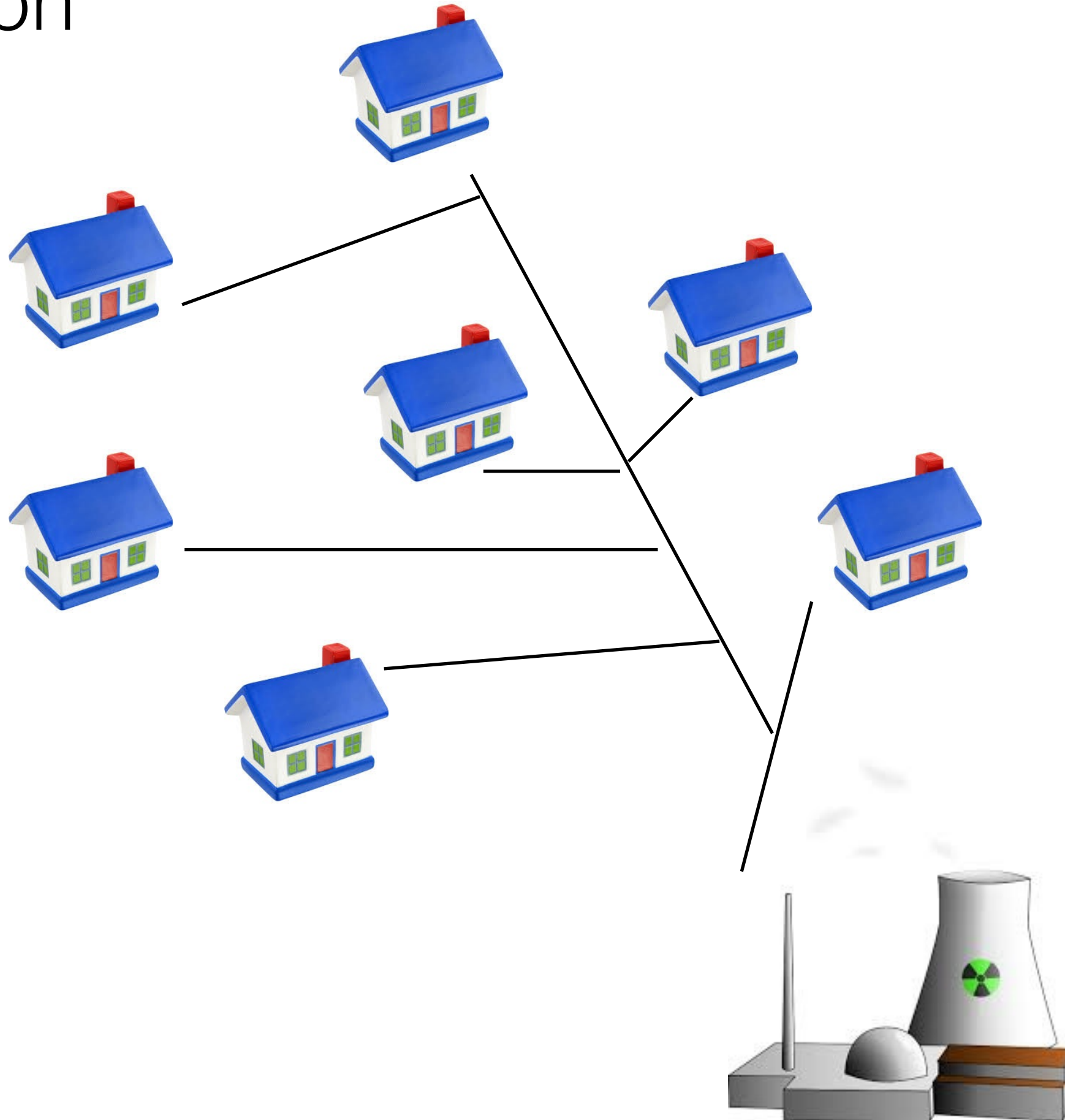


# Robustness of spatial micronetworks

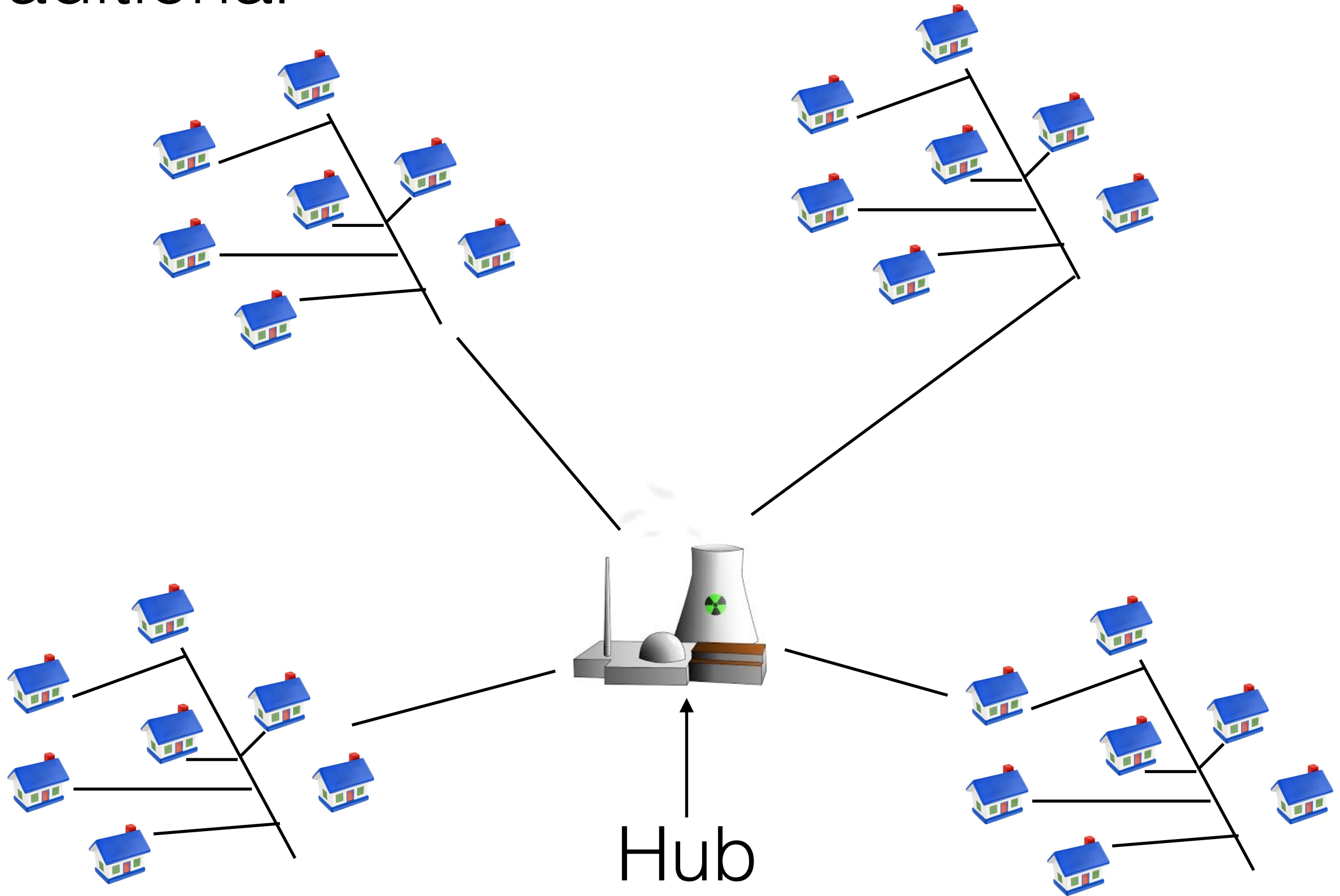
Thomas McAndrew  
University of Vermont



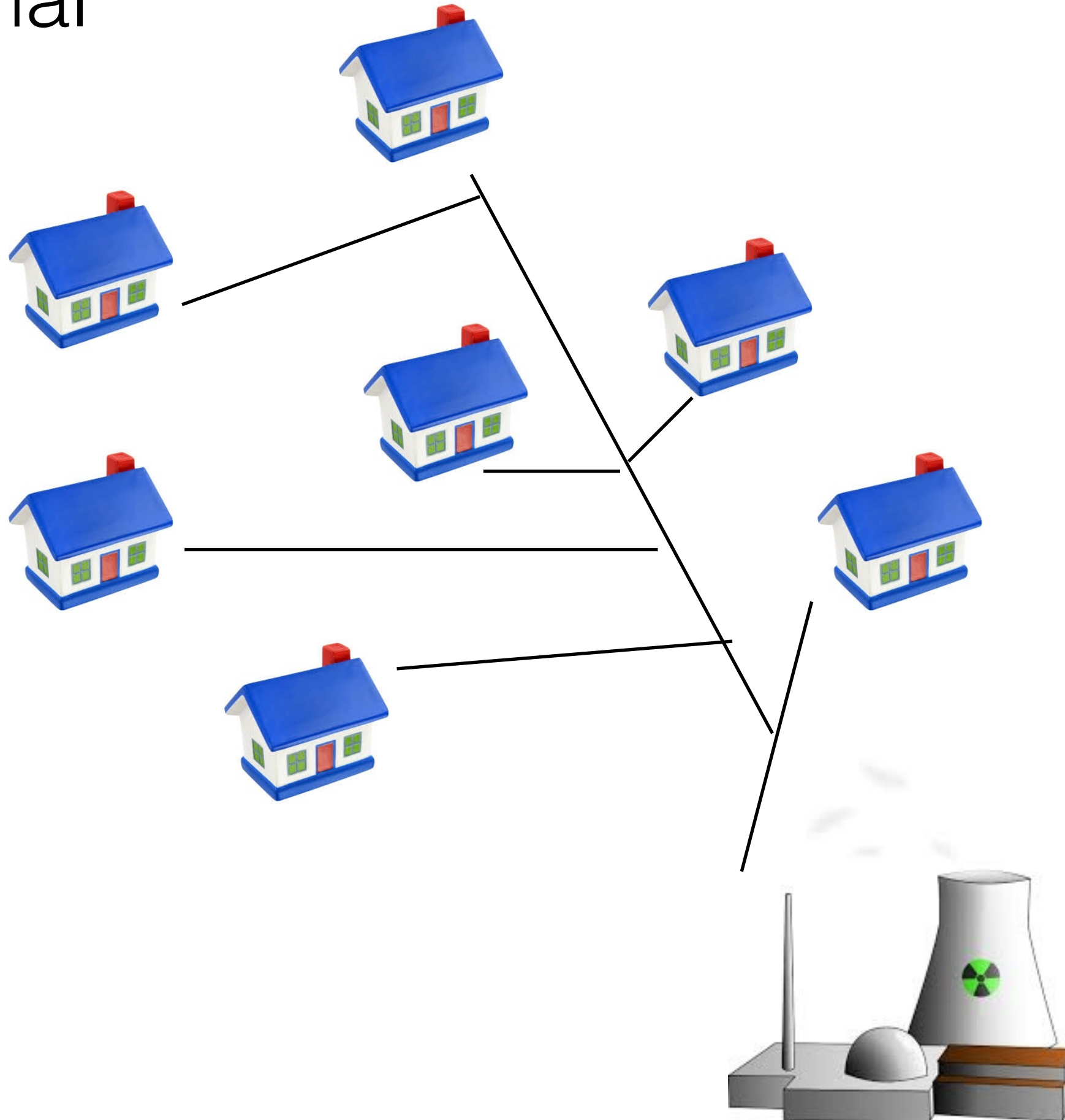
# Motivation



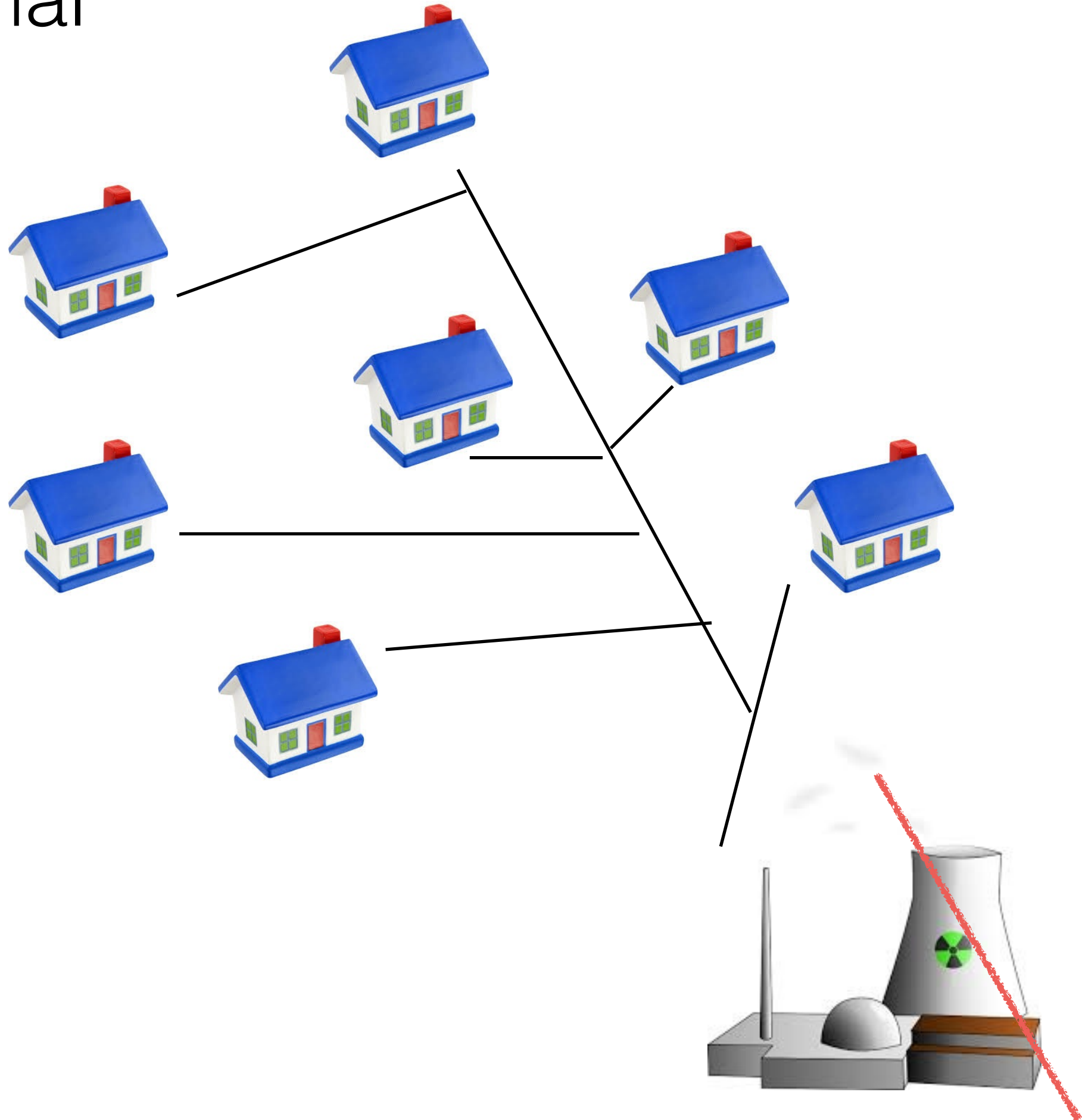
# Traditional



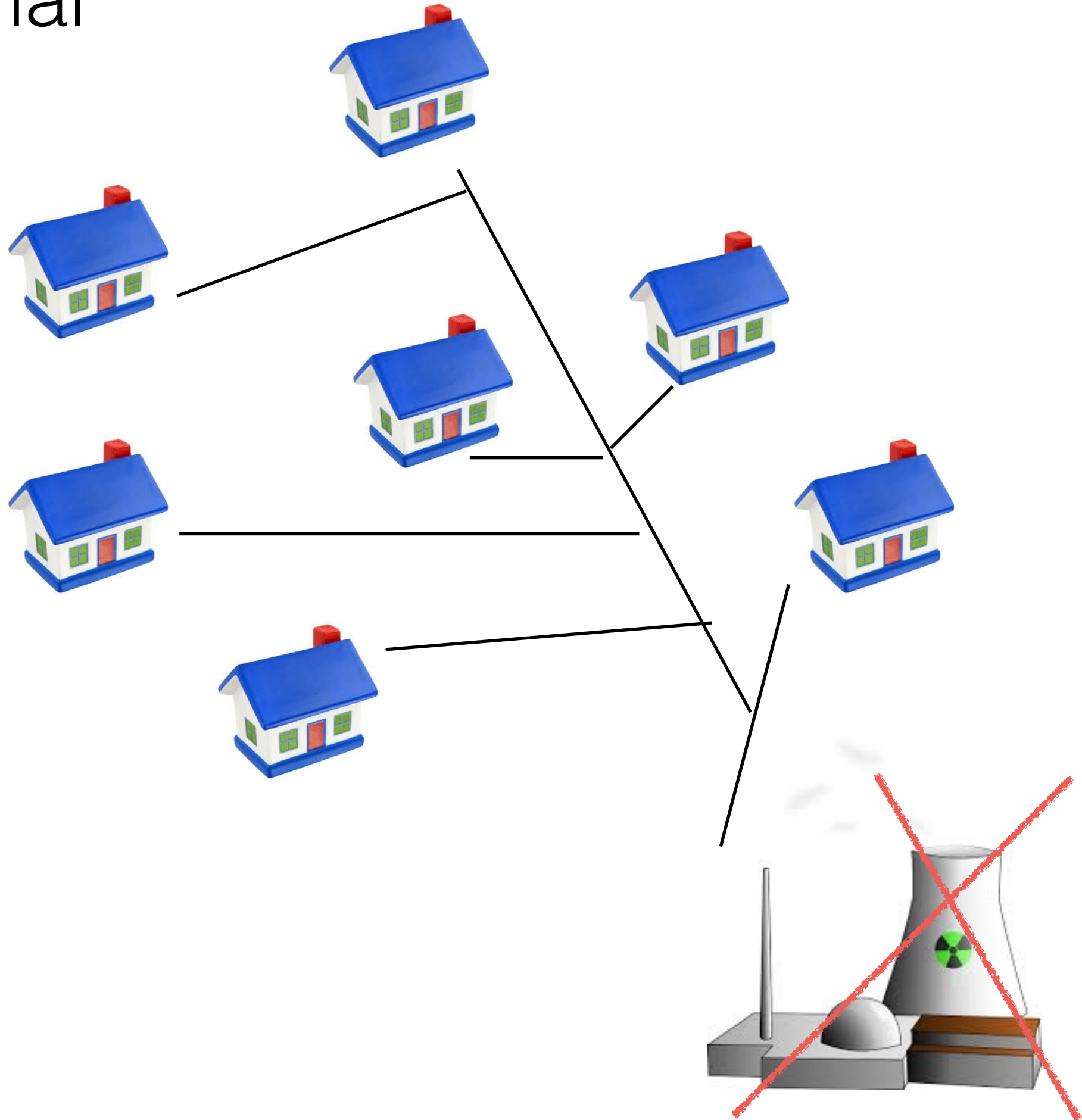
# Traditional



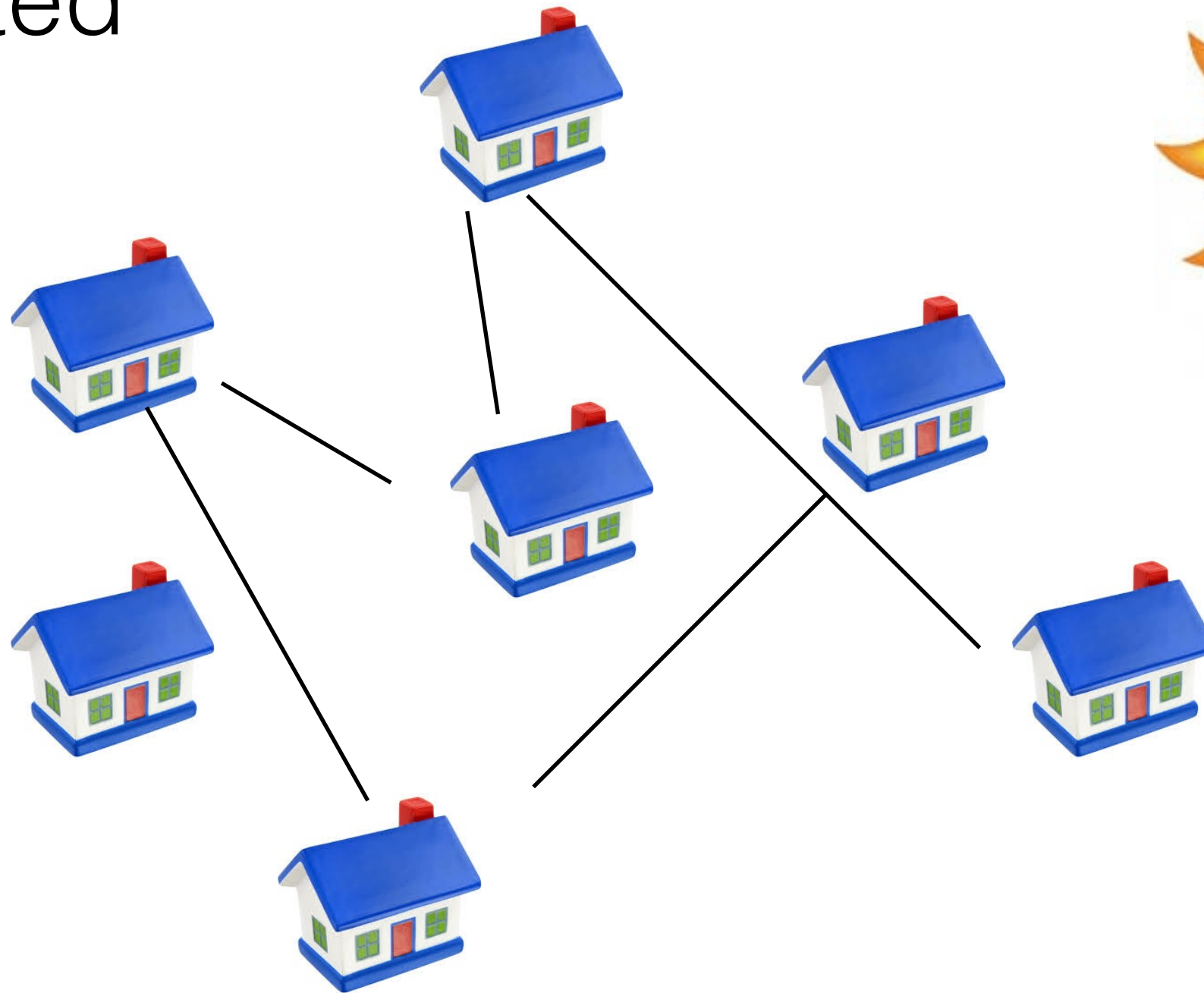
# Traditional



# Traditional

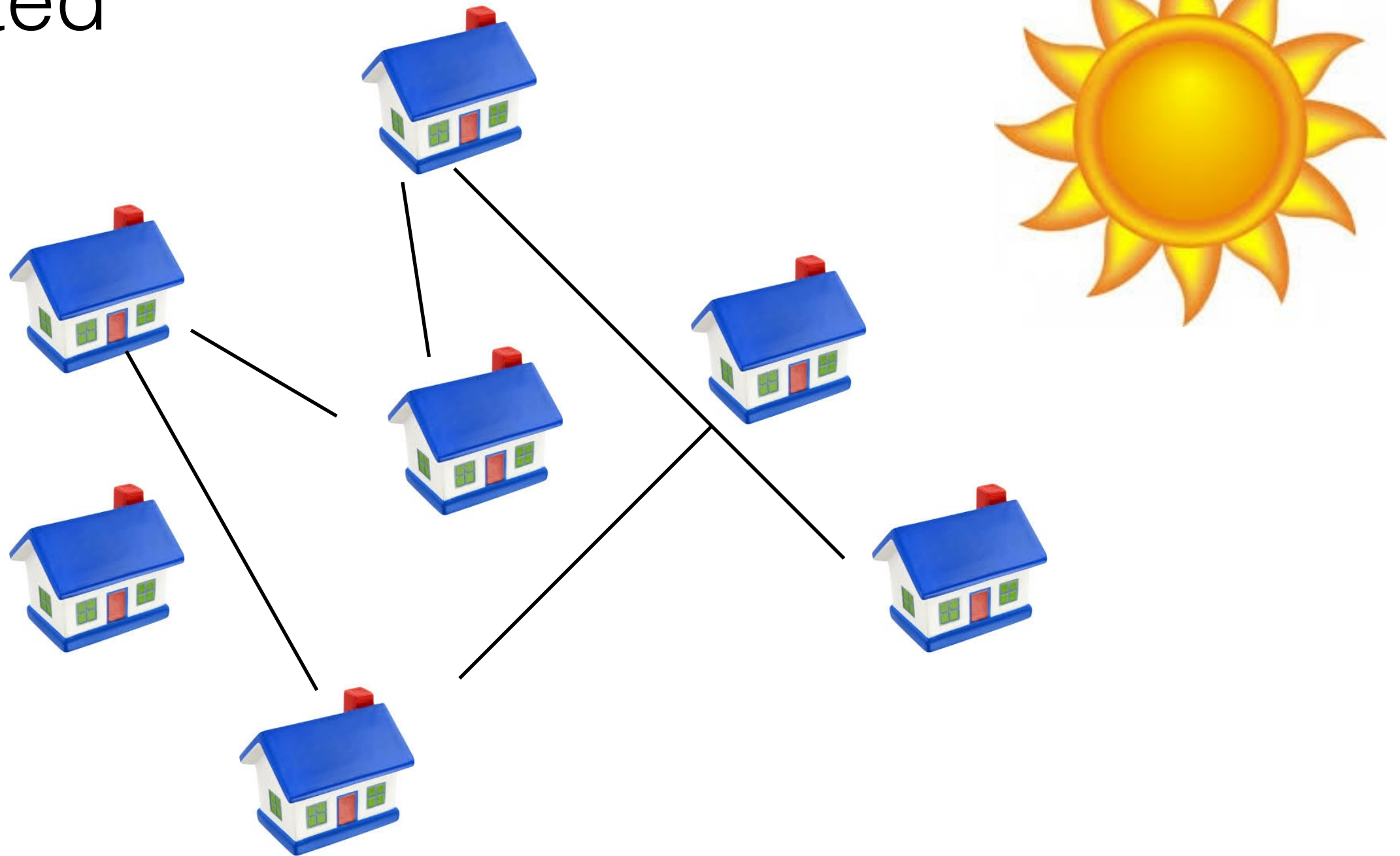


# Distributed





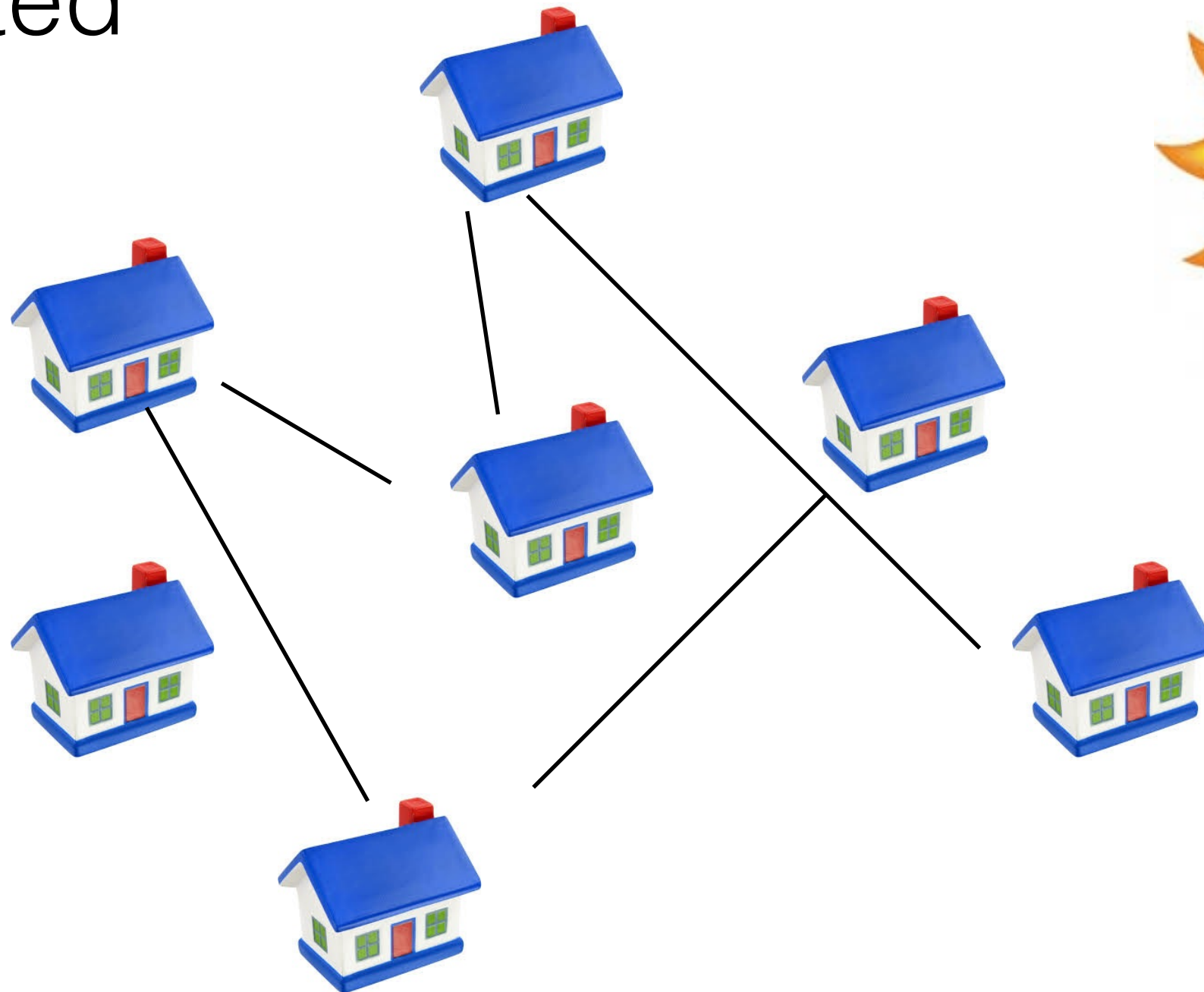
# Distributed



## Share Electric Bill

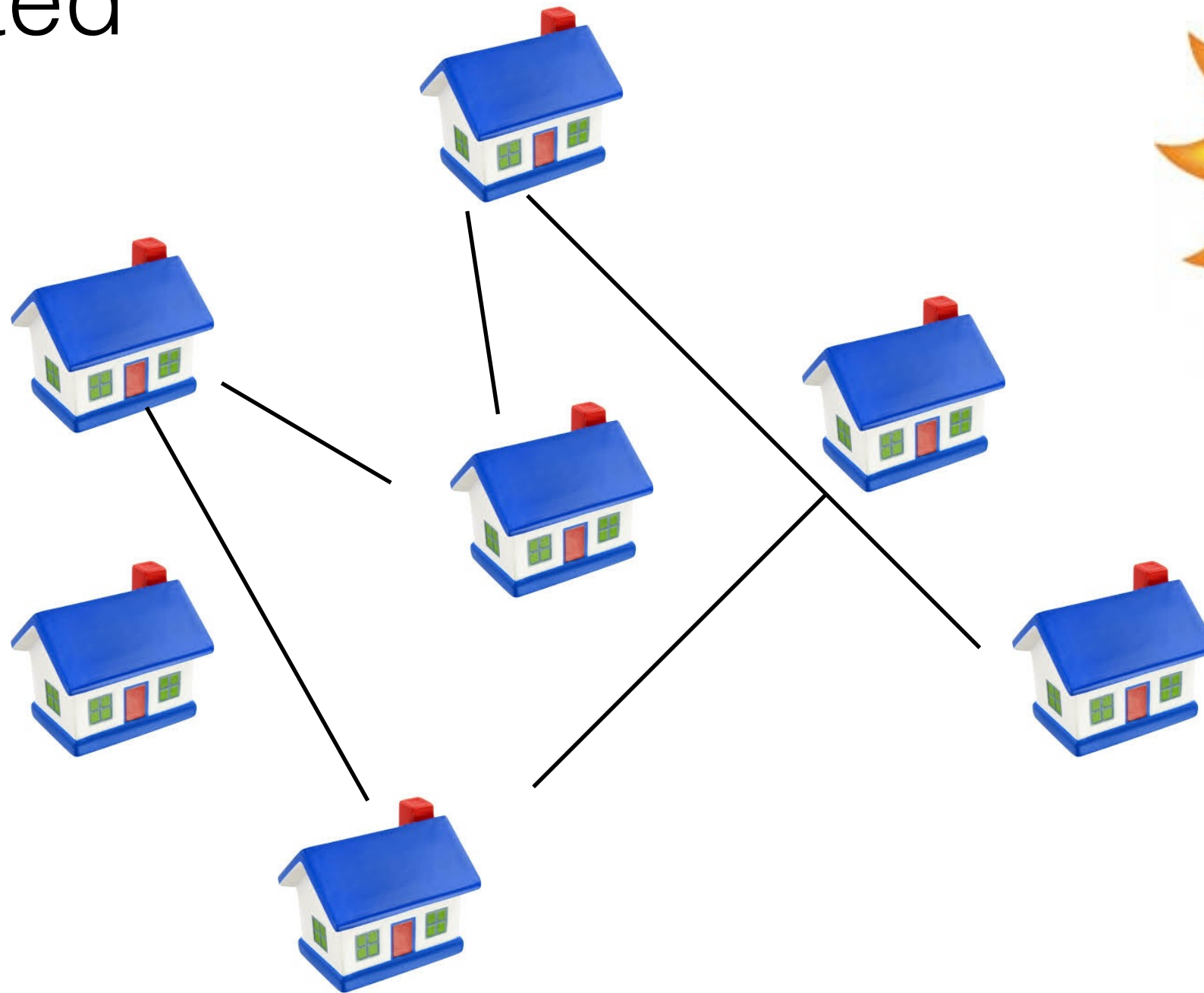


# Distributed



Share Electric Bill  
Connectedness

# Distributed



Share Electric Bill  
Connectedness  
Lower Carbon Footprint

# Model - construction

$$d_{\text{eff}}(i, j) = \sqrt{N} \lambda d_{ij} + (1 - \lambda)$$

$$\begin{array}{ccc} 0 & \lambda & 1 \\ \hline \text{Non-Spatial} & & \text{Spatial} \end{array}$$

# Model - construction

$$d_{\text{eff}}(i, j) = \sqrt{N} \lambda d_{ij} + (1 - \lambda)$$

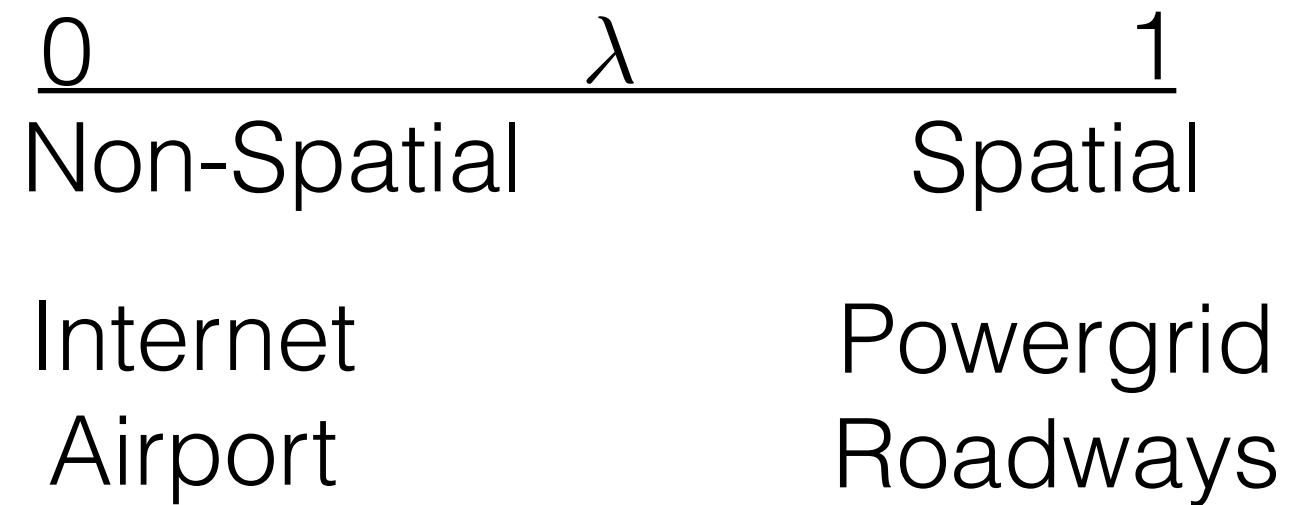
$\frac{0}{\text{Non-Spatial}} \quad \lambda \quad \frac{1}{\text{Spatial}}$

Internet  
Airport

# Model - construction

$$d_{\text{eff}}(i, j) = \sqrt{N} \lambda d_{ij} + (1 - \lambda)$$



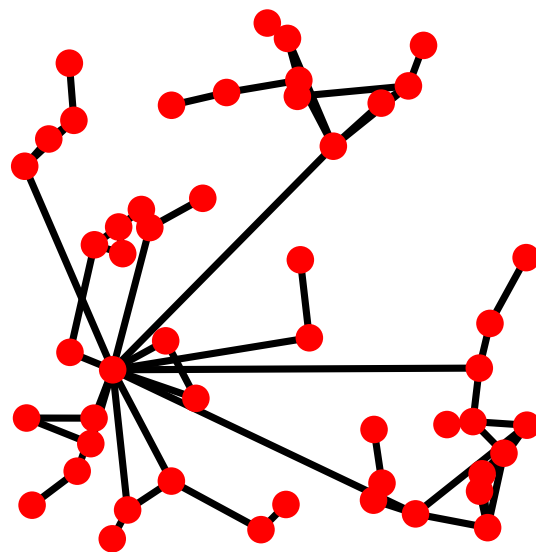
# Model - construction

$$d_{\text{eff}}(i, j) = \sqrt{N} \lambda d_{ij} + (1 - \lambda)$$

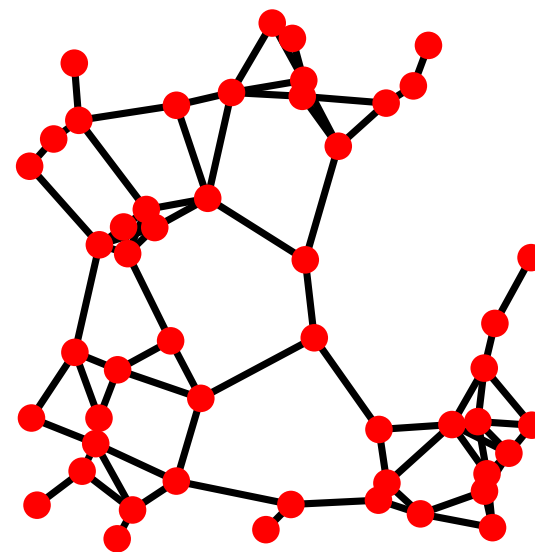
 

0	$\lambda$	1
Non-Spatial		Spatial
Internet		Powergrid
Airport		Roadways

$\lambda = 0$



$\lambda = 1$



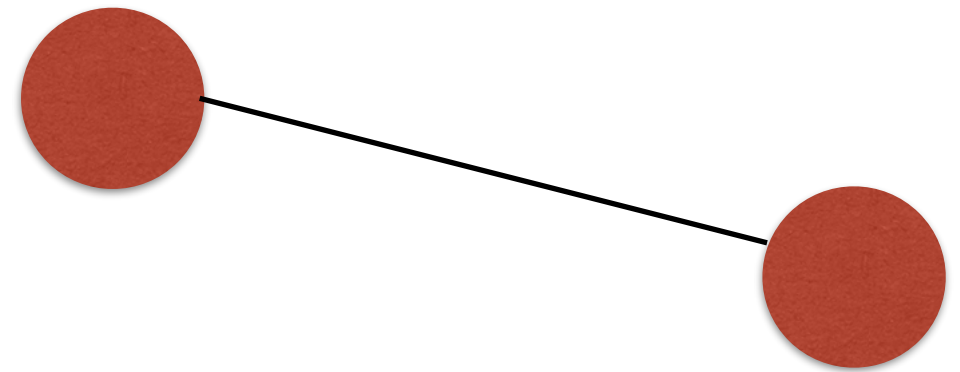




# Model -destruction

# Model -destruction

Look at each link

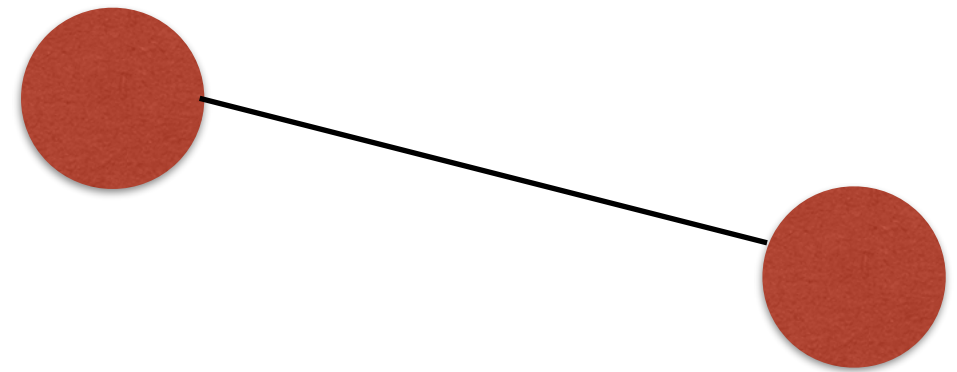


# Model -destruction

Flip a Coin



Look at each link

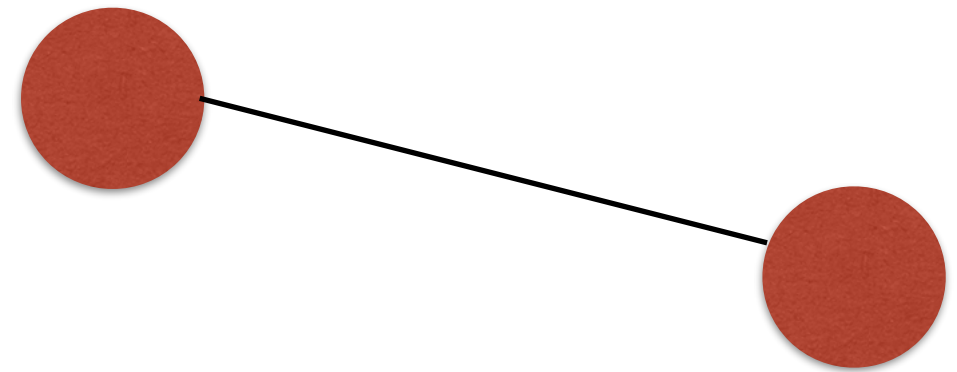


# Model -destruction

Flip a Coin



Look at each link



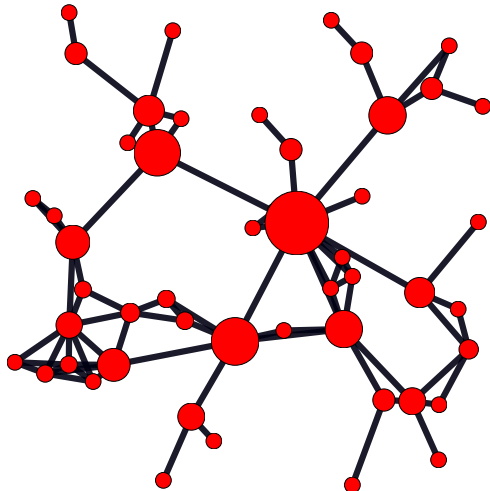
**Longer** edges are **more likely** to fail



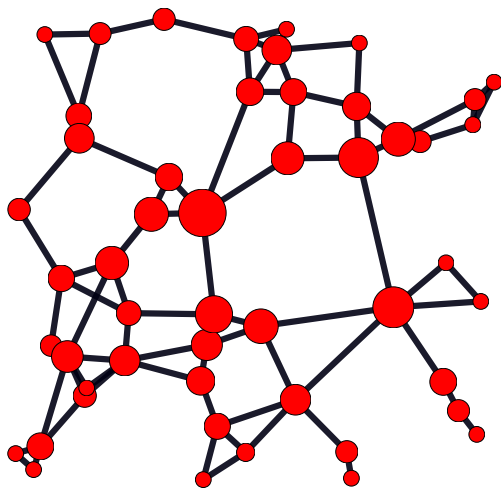
# Size of Node = Importance

$\alpha = 0.0$

$\lambda = 0$

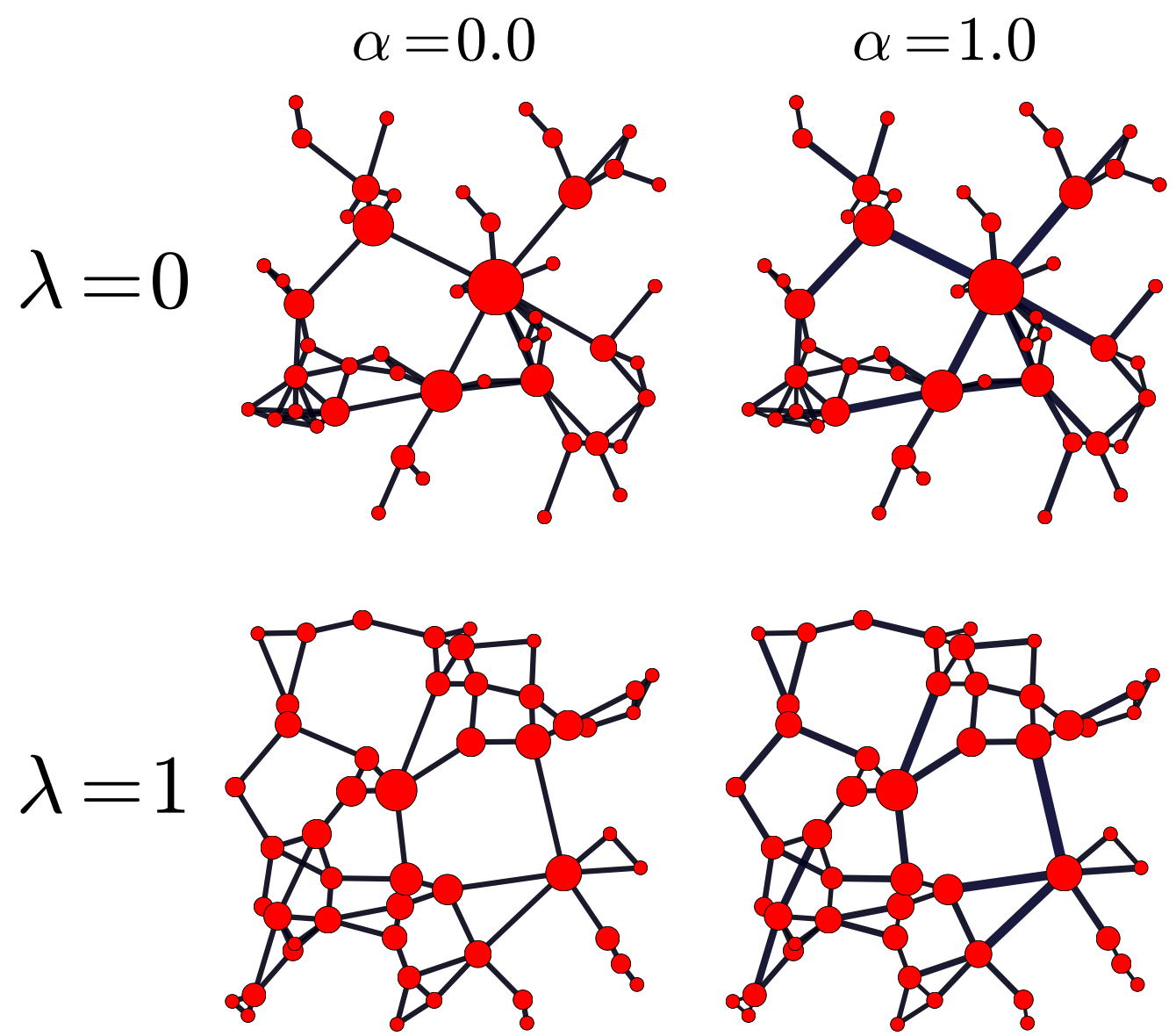


$\lambda = 1$



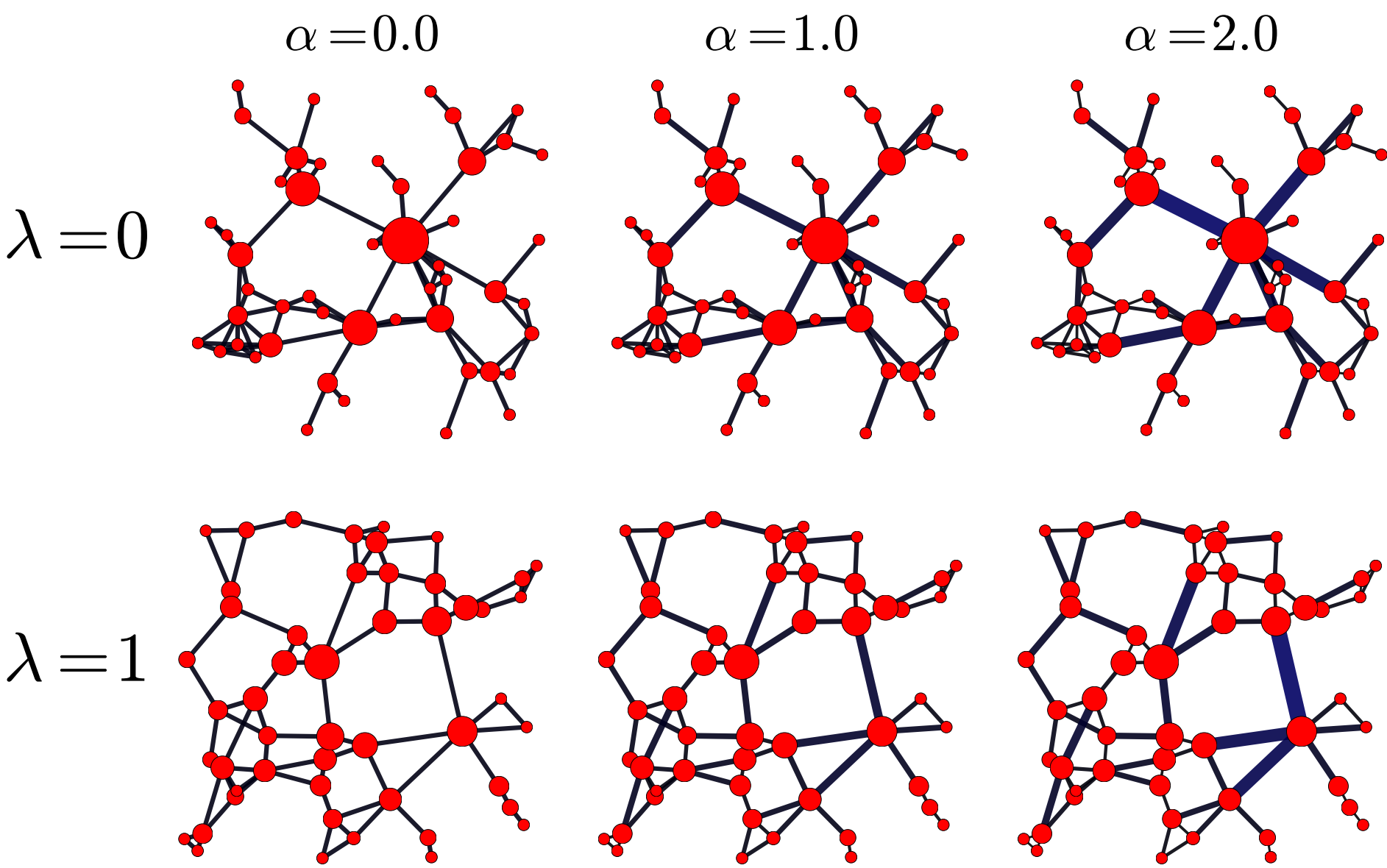


# Size of Node = Importance



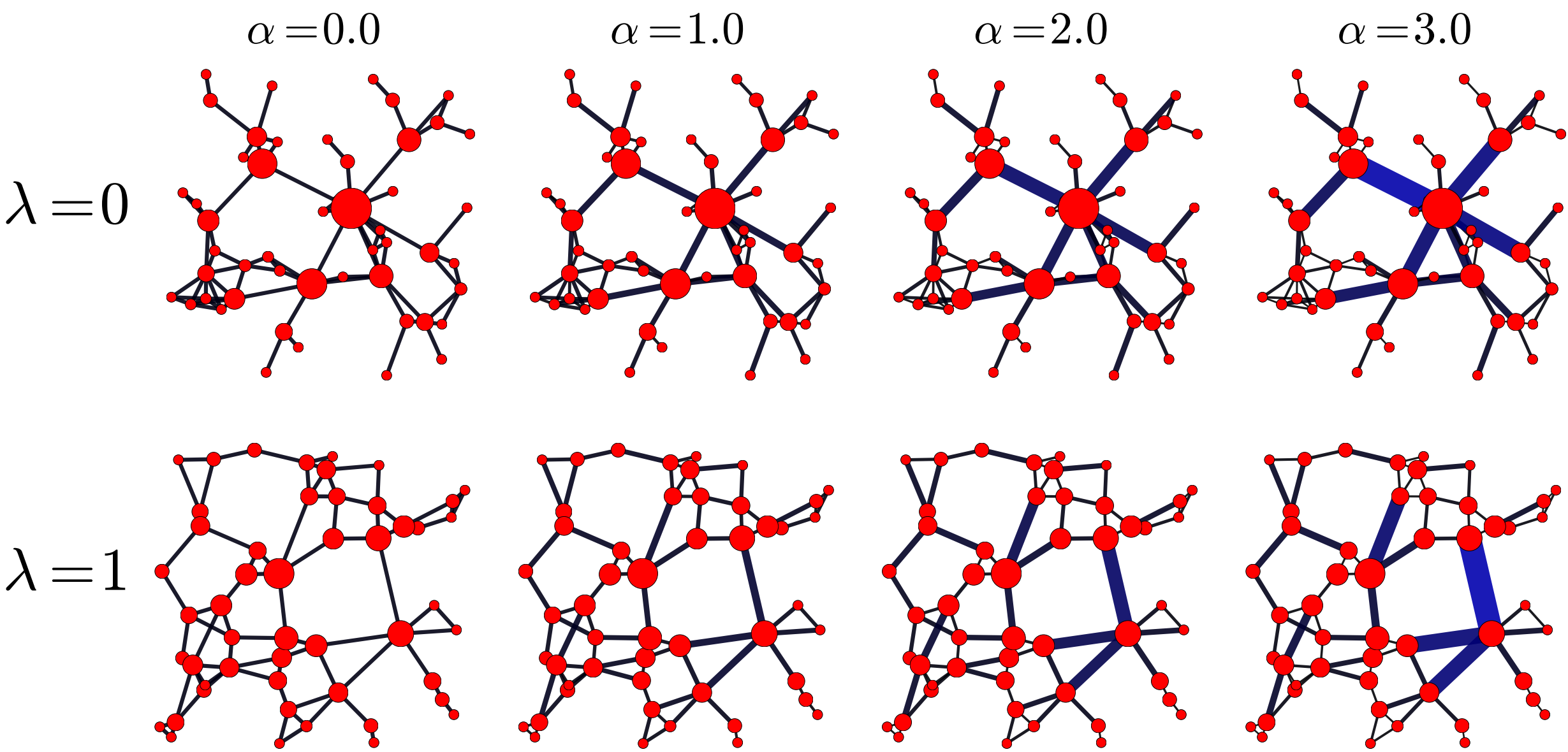
Link thickness = number of times failed

# Size of Node = Importance



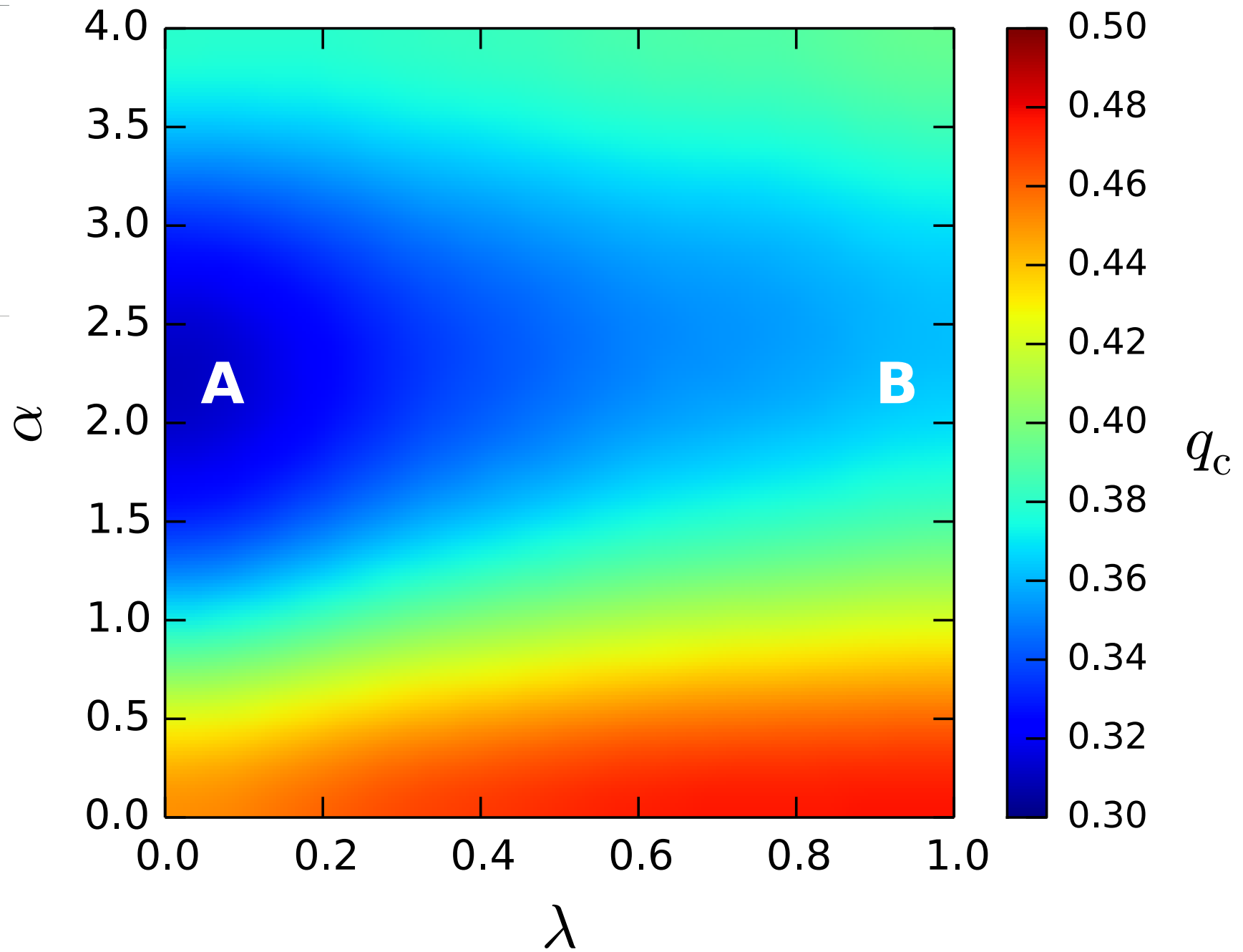
Link thickness = number of times failed

Size of Node = Importance

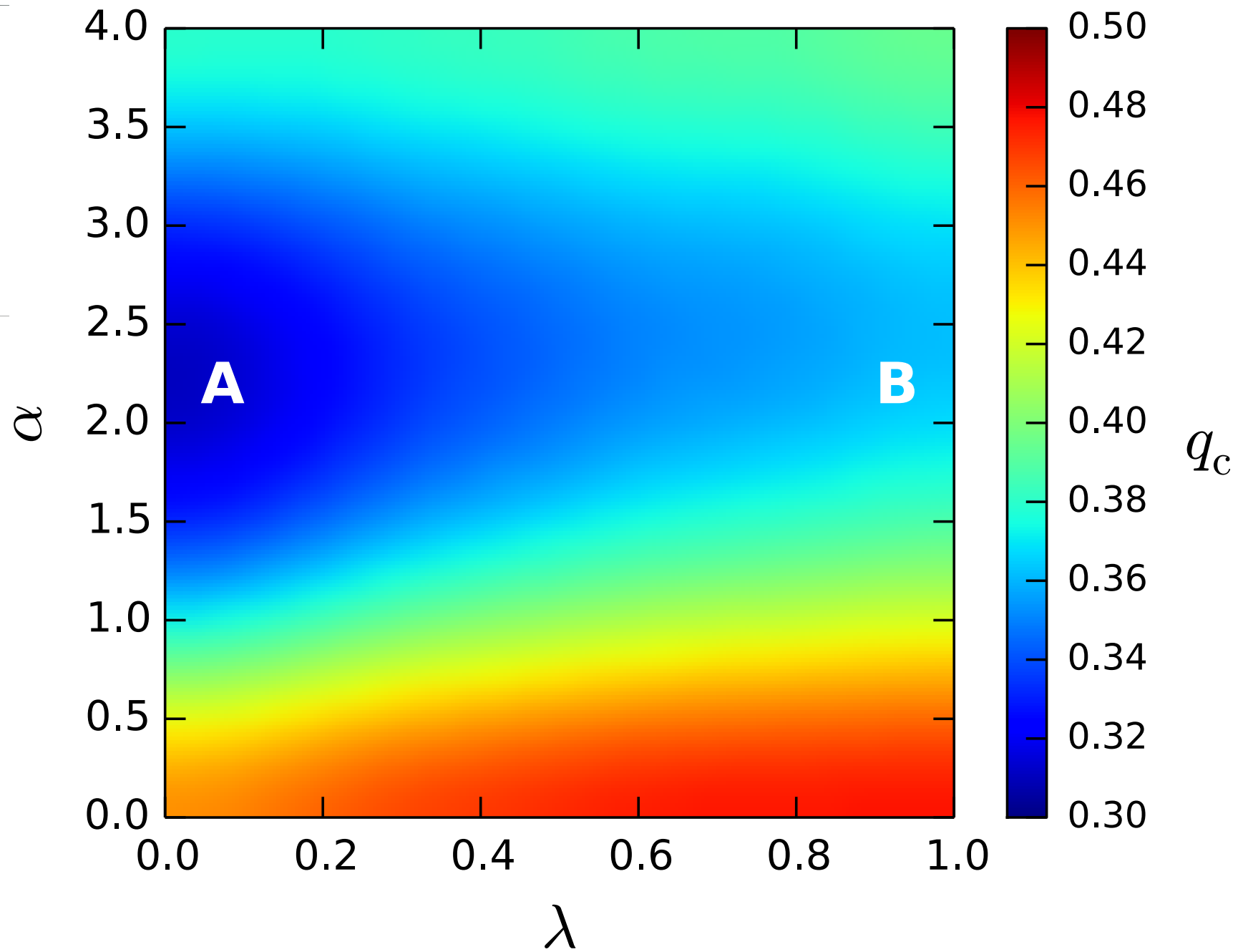


Link thickness = number of times failed

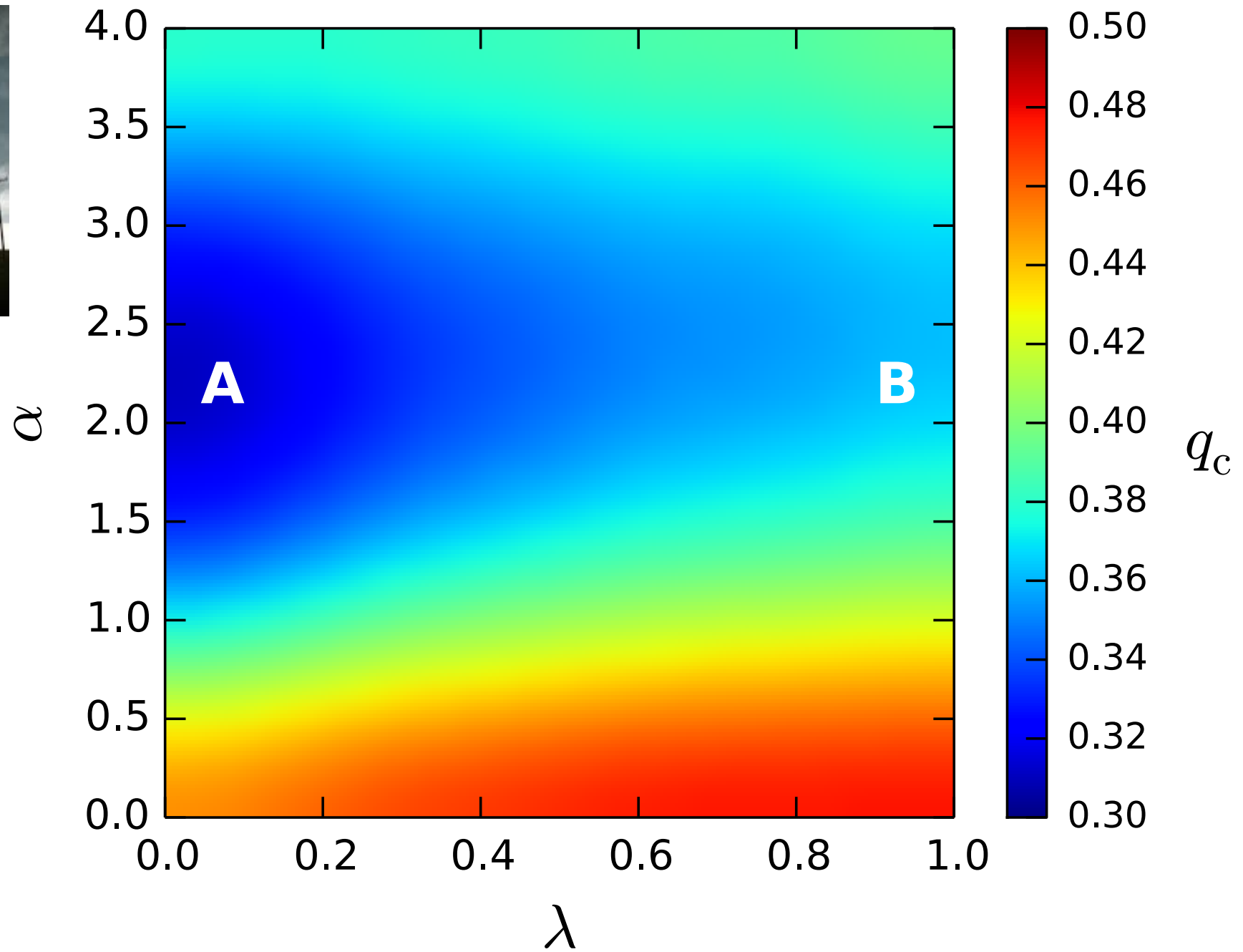
# Vulnerability



# Vulnerability

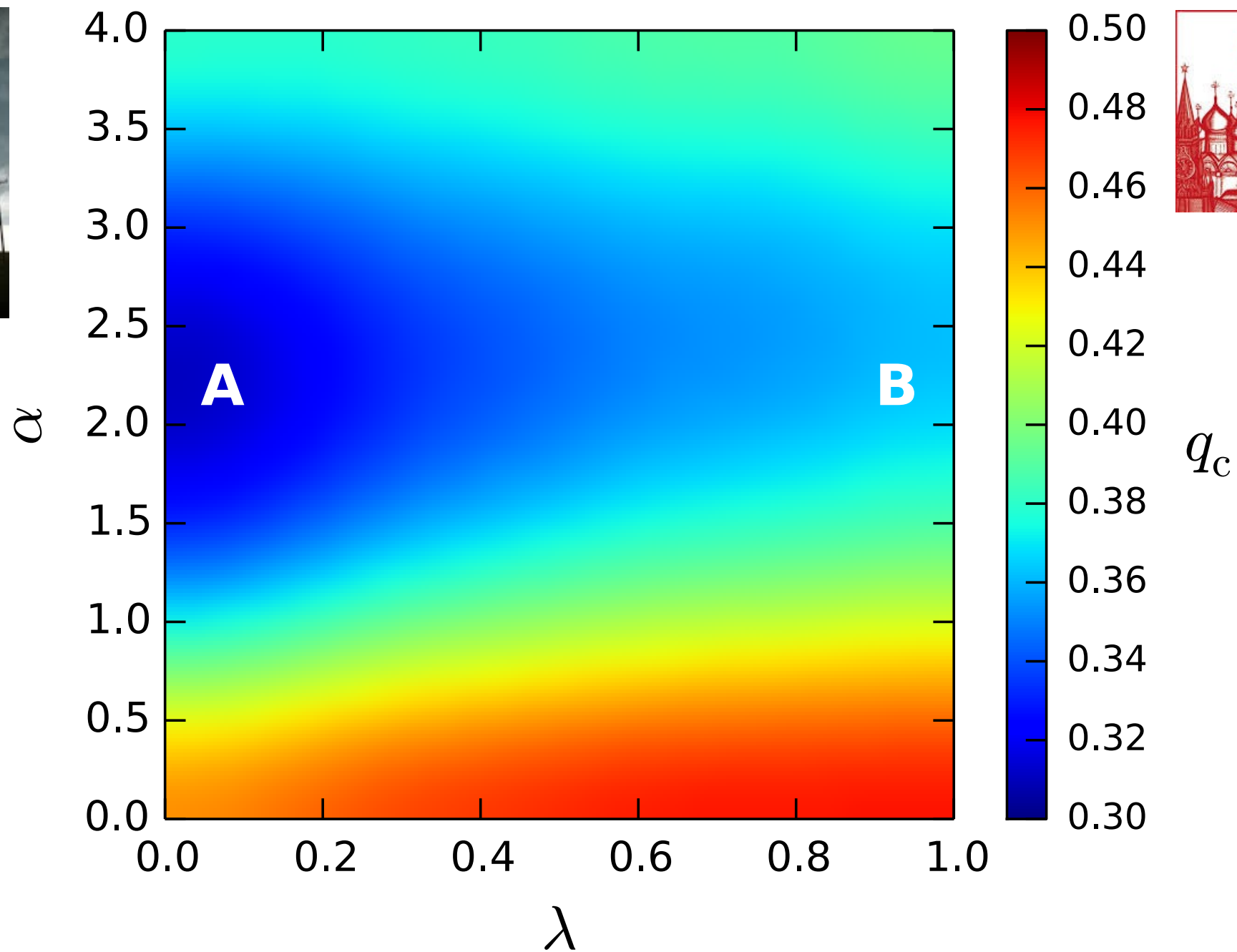


# Vulnerability

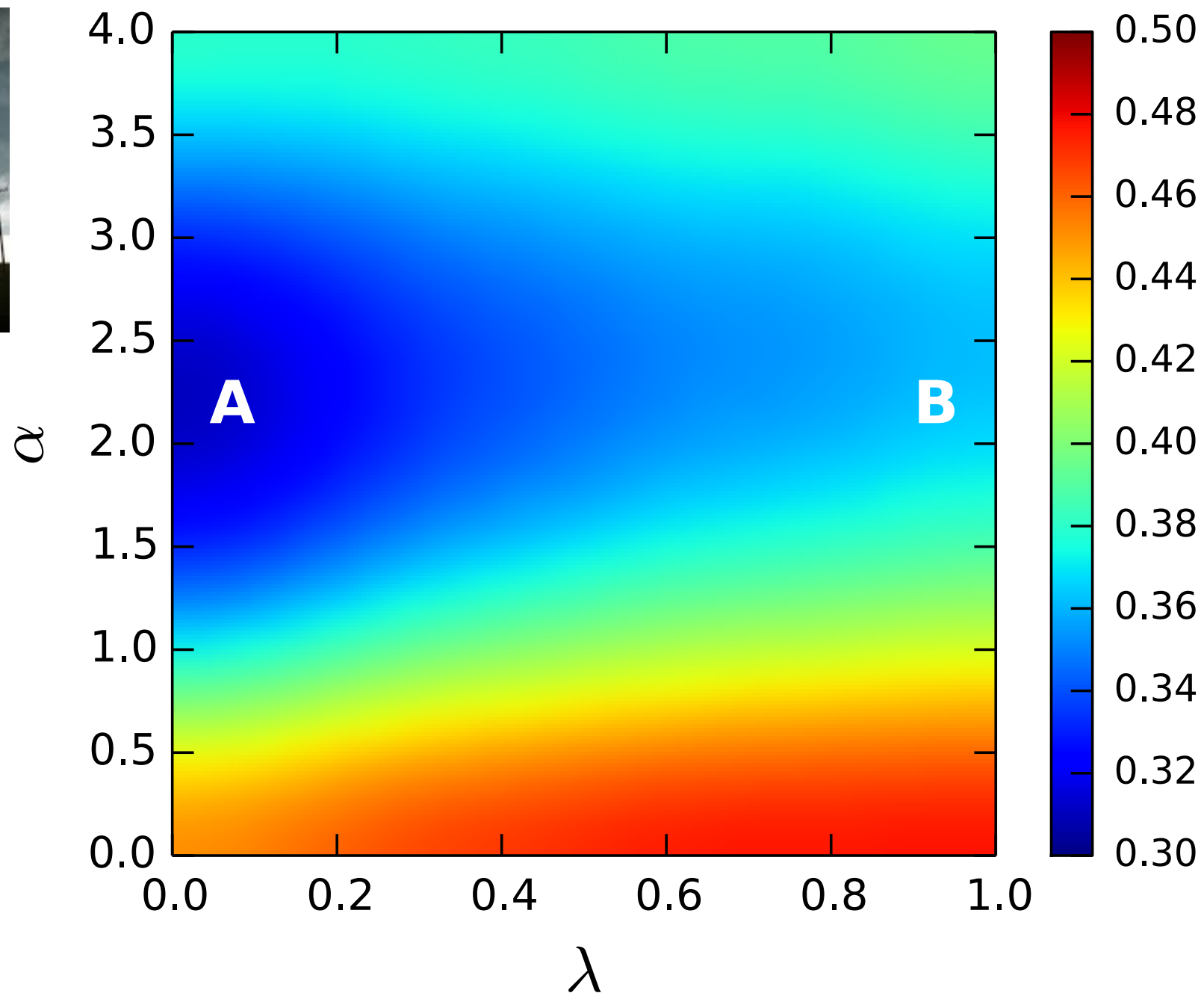




# Vulnerability



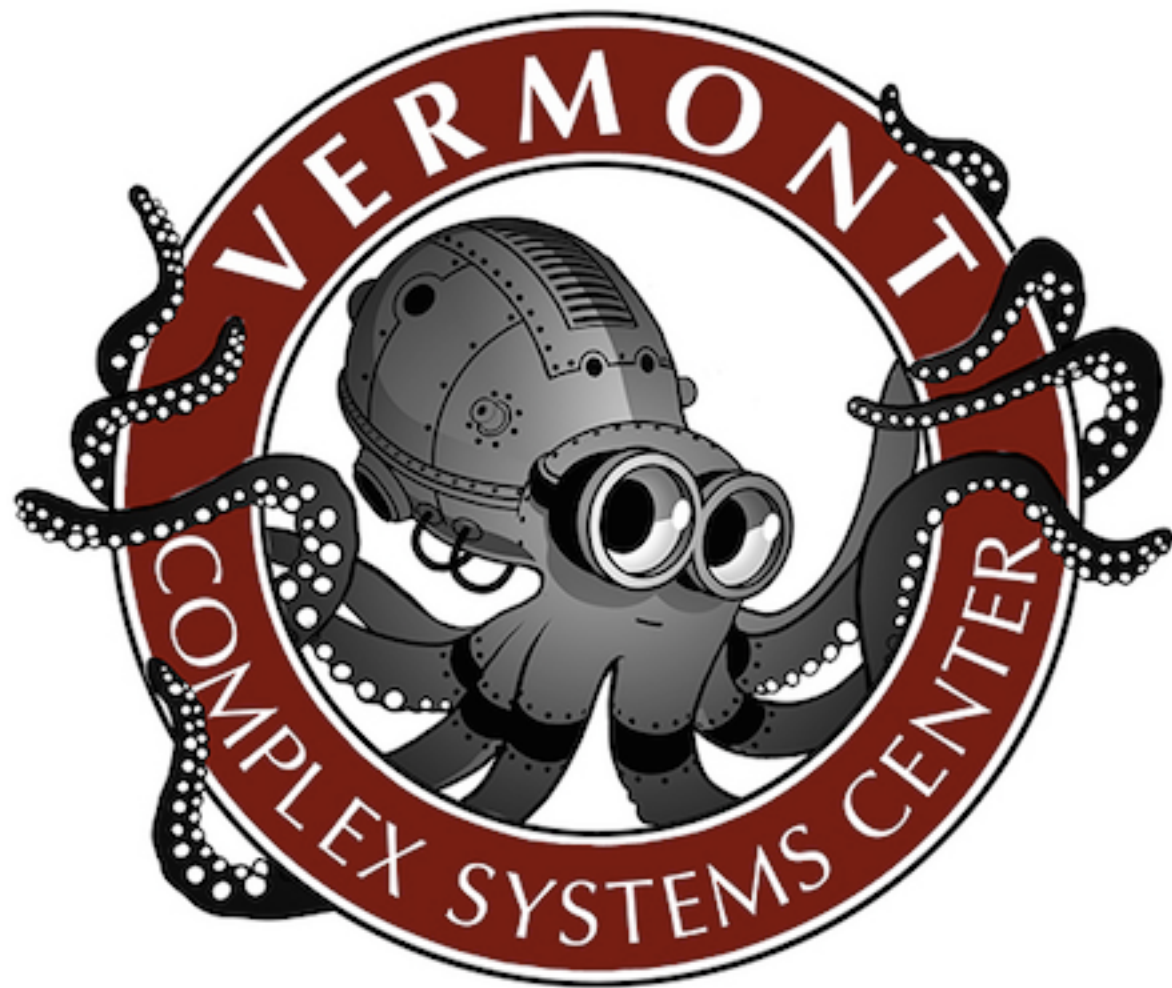
# Vulnerability



$q_c$



# Thank you



Collaborators:  
Chris Danforth  
James Bagrow



*The*  
**UNIVERSITY**  
*of* **VERMONT**