

$$y_i = \alpha + \beta x_i + \varepsilon_i$$

$$H_0: \beta = 0 \rightarrow \text{didn't work}$$

$$H_1: \beta \neq 0 \rightarrow \text{did work}$$

$$H_0: \beta = 0$$

$$H_1: \beta > 0$$

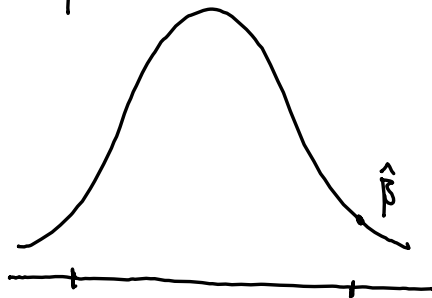
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(i) what do the hypotheses
really mean

$\hat{\beta} \approx 0$ then want to conclude H_0 is prob. true
if not \rightarrow false

$$\hat{\beta} = \frac{\hat{\text{cov}}(x_i, y_i)}{\hat{\text{var}}(x_i)}$$

$\hat{\beta}$ has a distribution



$$y_i = \alpha + \beta x_i + \varepsilon_i \quad \varepsilon_i \sim N(0, \sigma^2)$$

~~Assume~~

$$\hat{\beta} \sim N(\beta, v)$$

$$\frac{\sigma^2}{\sum (x_i - \bar{x})^2} = v$$

• Assume $\beta = 0$

• work out $P(\hat{\beta} > \text{what we see})$

• if low \Rightarrow reject that $\beta = 0$

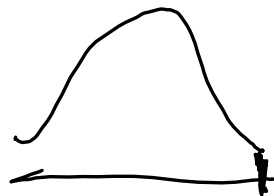
$$\hat{v} = \frac{s^2}{\sum (x_i - \bar{x})^2}$$

Under H_0

$$\hat{\beta} \sim N(0, v) \Rightarrow \frac{\hat{\beta}}{\sqrt{v}} \sim N(0, 1)$$

[if $\beta = 0$]

$$Z = \frac{\hat{\beta}}{\sqrt{\hat{v}}} = \frac{\hat{\beta}}{\text{se}(\hat{\beta})} \sim N(0, 1)$$

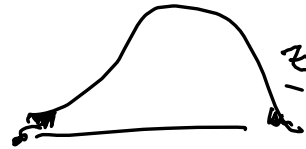
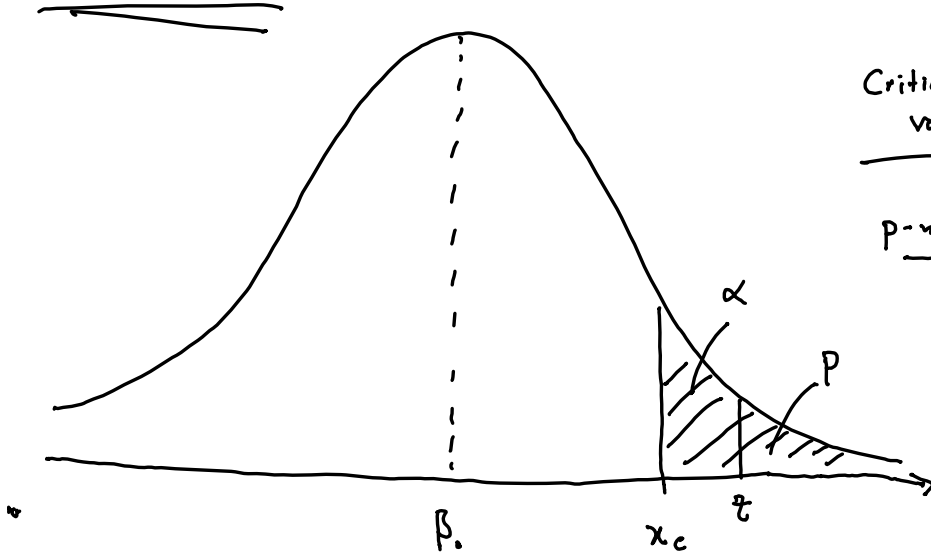


- Assume H_0 is true
- Under H_0 some test statistic has known distribution

Under H_0 $Z = \frac{\hat{\beta}}{se(\hat{\beta})} \sim N(0, 1)$

- ~~and~~ calculate Z

- if Z is in tails \Rightarrow reject H_0



Critical value:

reject if $Z > x_c$

p-value:

$$z > x_c$$

\Leftrightarrow

$$p < \alpha$$

reject if $p < \alpha$

Prob ($Z > z$ under H_0)

Confidence Interval:

$$Z \in CI$$

set of numbers for which don't reject H_0

Q1

1.33

$$\log \text{Price}_i = \alpha + \beta \log \text{Area}_i + \gamma \text{AR}_i + \varepsilon_i$$

"Interpret the parameters"



price Area

↓ ↓

$$y_i = \alpha + \beta x_i + \varepsilon_i$$

$$\mathbb{E} y_i | x_i = \alpha + \beta x_i$$

$$\beta = \frac{\partial \mathbb{E}(y_i | x_i)}{\partial x_i}$$

$$\beta = \frac{\% \Delta \text{ price}}{\% \Delta \text{ area}}$$

if Area 1%^{p.p.} higher
we would expect
price 1.33 p.p. higher

"significance" of β / statistical significance

we can reject the hypothesis that $H_0: \beta = 0$
 $H_1: \beta \neq 0$ ①

② Normal errors

$$\rightarrow Z = \frac{\hat{\beta}}{\sqrt{V(\hat{\beta})}} \sim N(0,1) \text{ under } H_0: \beta = 0$$

$t_n \approx N(0,1)$ if n large

③ $T = \frac{\hat{\beta}}{se(\hat{\beta})} \sim t_{n-3}$ under H_0

④ $T = \frac{1.334}{0.091} \approx 14.66$

⑤ Pick a cutoff
($\alpha = 1\%, 5\%, 10\% \dots$)

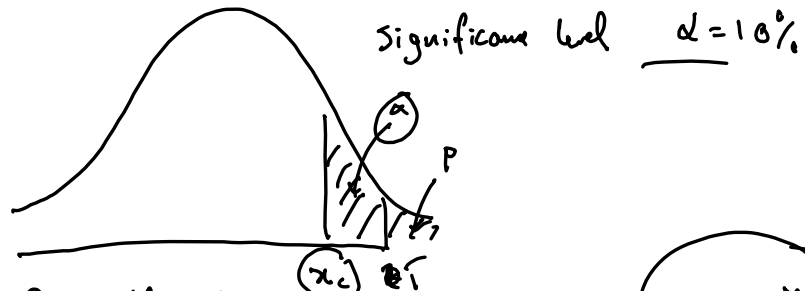
⑥ look up x_c from α

① hypothesis

② what assumptions

③ Give T.S.
and distribution
under H_0

④ calculate T.S.



① reject if $T \geq x_c$

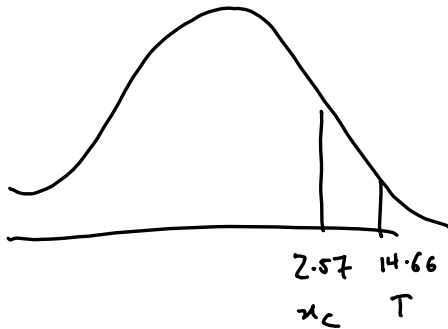
otherwise don't reject \square

$$T = 14.66$$

$$\alpha = 1\% \quad \chi_c = 2.57$$

$$H_0: \beta = 0$$

$$H_1: \beta \neq 0$$



\therefore reject H_0

$\rightarrow \underline{\beta}$ is statistically significant

$$y_i = \alpha + \overbrace{1.000060}^{\hat{\beta}} x_i + \varepsilon_i$$

