



Data Structures

Lesson 2

Topics

- STL Data Structures
- Non-STL Data Structures

Static Array

```
int array1[10];  
int array2[10] = {0,1,2,3,4,5,6,7,8,9}  
int array3[10] = {1} // [1,0,0,0,0,0,0,0,0,0]  
int array4[10] = {0} // [0,0,0,0,0,0,0,0,0,0]  
  
cin >> array1[0]; //Get an integer  
int* array5 = new int[*array1] //Dynamic array allocation  
  
for(i = 0; i <= 10; ++i){ //Get an entire array  
    cin >> array2[i];  
}  
  
Int array6[2][3] = {{1,2,3},{4,5,6}}
```

Vector

- Dynamic array – basic operations are $O(1)$ amortized
- Can be used as list, queue, stack
- Common functions:
 - []
 - push_back()
 - pop_back()
 - insert()
 - erase()
 - size()
 - empty()
 - clear() //Use between test cases
 - resize() //Use between test cases

Vector

```
vector<int> arr1(5, 0); // [0,0,0,0,0]
arr1[0] = 1; // [1,0,0,0,0]
arr1.push_back(3); // [1,0,0,0,0,3]
vector<int> arr2 = arr1; //copy
arr1.pop_back(3); // [1,0,0,0,0]
auto it = arr1.begin();
it++; it++;
arr1.insert(it,arr2.begin(),arr2.end()) // [1,0,1,0,0,0,0,3,0,0,0]
arr1.erase(arr1.begin()) // [0,1,0,0,0,0,3,0,0,0]
```

Set

- Based on Balanced Binary Search Tree (Balanced-BST)
 - Basic operations - $O(\log n)$
 - Objects must support “<” operator
- Common Functions:
 - insert()
 - search()
 - erase()
 - size()
 - empty()
 - min/max – Not functions, see code
 - lower_bound()/upper_bound()

Set

```
set<int> set1 = {3,14,15,92,65,35,89,79,32,38};  
int min = *set1.begin(); // 3  
int max = *set1.rbegin(); // 92  
cout << *set1.lower_bound(15); // 15  
cout << *set1.lower_bound(16); // 32
```

map

- Similar to set, but supports key-value operations

```
map<int, char> map1 = {{1, 'a'}, {3, 'c'}, {2, 'b'}};  
for(auto it: map1){ cout << it.first << it.second; } //abc  
map1[3] = 'C';  
cout << map1[3]; // C  
map1[4] = 'd';  
map1[5] = 'e';  
auto itlow = map1.lower_bound(2); //inclusive  
auto itupp = map1.upper_bound(4); //exclusive  
cout << itlow->second; // b  
cout << itupp->second; // e  
map1.erase(itlow, itupp);  
for(auto it: map1){ cout << it.first << it.second; } //ae
```


multiset/multimap

- multiset/multimap – allows key repetition
- Also Balanced-BST
- No [] operator

Set and Map variations

- `unordered_set/unordered_map`
- Based on Hash Table
 - Basic operations – $O(1)$ (on average)
 - Objects must support “`()`” operator (implementing a hash function)
 - And “`==`” operator.
- Not recommended for complex data types in competitive programming

unordered_set/unordered_map

- Based on Hash Table
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 - And “==” operator.
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unordered_set/unordered_map

```
unordered_map<string, int> ht;
ht["key"] = 5;
cout << ht["key"]; // 5
if (ht.find("key") != ht.end())
    cout << "key found";
else
    cout << "key not found";
cout << "second=" << ht["second"];
// Implicitly create an item (val=0) for non-existent keys.
ht["third"]++;
// Increase by 1 if the key already exists in the hash table. If not,
insert the key and set the value as 1.
for (auto& p : ht) //Order unknown
{ cout << "key=" << p.first << " " << "val=" << p.second << endl; }
```

priority_queue

- Min/Max heap
- Common functions:
 - top()
 - pop()
 - push()
 - empty

priority_queue

```
vector<int> arr = { 5,3,6,3,2,1,1 };
priority_queue<int> max_heap(arr.begin(),arr.end()); //  $O(n)$ 
while (!max_heap.empty()) { // 6,5,3,3,2,1,1
    cout << max_heap.top();
    max_heap.pop(); // no return val
}
priority_queue<int, vector<int>, greater<int> > min_heap;
min_heap.push(6);min_heap.push(8);
min_heap.push(1);min_heap.push(2); //  $O(\log n)$ 
while (!min_heap.empty()) // 1,2,6,8
{
    cout << min_heap.top() << endl;
    min_heap.pop();
}
```

Break & Competition

bitset

- An efficient Boolean array with logic operations
- Common functions:
 - reset()
 - set()
 - test()
 - count()
 - any()
 - all()
 - none()
 - $\&$, $|$, \wedge , \sim operators (And, Or, Xor, Not)
 - \gg , \ll (Bit shift)

bitset

```
bitset<8> bset1; // [0,0,0,0,0,0,0,0]
bset1.set(); // [1,1,1,1,1,1,1,1]
bset1.reset(3); bset1.reset(5); // [1,1,1,0,1,0,1,1]
bset1.flip(6); // [1,1,1,0,1,0,0,1]
cout << bset1.none(); // false
cout << bset1.any(); // true
cout << bset1.all(); // false
bitset<8> bset2; // [0,0,0,0,0,0,0,0]
bset2.set(0); // [1,0,0,0,0,0,0,0]
bset2 = (bset2 >> 3) | (bset2 >> 5) // [0,0,0,1,0,1,0,0]
cout << (bset1 & bset2).none(); // true
cout << (bset1 | bset2).all(); // true
cout << ((~bset1) ^ bset2).any(); // false
```

bitmask

- If the number of flags is small we can use integers instead of bitset
- Advantage: Much faster
- Disadvantage: No built in interface

```
int b1 = 10; // 00001010
int b2 = 18; // 00010010
int b3 = b1 & b2; // 00000010
int b4 = b1 | (b3<<4); // 00101010
for(int i = 0; i < 8; ++i){
    if(b4 & 1<<i) cout << "true";
    else          cout << "false";
} // false,true,false,true,false,true,false,false
```

Union-Find

- **Goal:** Given a collection of items $\{1, \dots, n\}$, construct an efficient data structure which supports the following operations:
 - **Find(i):** Determine which subset a particular element is in. By comparing the result of two Find operations, one can determine whether two elements are in the same subset.
 - **Union(i, j):** Join two subsets into a single subset.
- Union-Find is a part of the [Kruskal MST algorithm](#).

Union-Find

- Naïve implementation – Graph of items
 - Union(i, j) adds an edge i and j , Find(i) determines subset ID using DFS.
 - Worst case time complexity for $O(n^2)$
- Better solution - Disjoint-set forests
 - Union(i, j), Find(i) in $O(\log^* n)$ amortized – almost constant!
- Implementation:
 - Inverted trees for the disjoint-set forests are represented using parent arrays.
 - Refer to [DS1](#) or [Wikipedia](#) and the attached .cpp file for more info.

Do Union(0, 1)

```
  1  2  3
  /
0
```

Do Union(1, 2)

```
  1  3
 /  \
0    2
```

Do Union(2, 3)

```
  1
 / | \
0  2  3
```

Union-Find

```
struct unionfind
{
    vector<int> rank;
    vector<int> parent;
    unionfind(int size) {
        rank=vector<int>(size,0);
        parent=vector<int>(size);
        for(int i=0;i<size;i++)
            parent[i]=i;
    }
    int find(int x){
        int tmp=x;
        while(x!=parent[x]) x=parent[x];
        while(tmp!=x) {
            int remember=parent[tmp];
            parent[tmp]=x;
            tmp=remember; }
    }
```

```
        return x;
    }
    void Union(int p, int q){
        p = find(p);
        q = find(q);
        if(q==p)
        {
            return;
        }
        if(rank[p] < rank[q]) parent[p]
= q;
        else parent[q] = p;
        if(rank[p] == rank[q])
rank[p]++;
    }
};
```

Segment tree

- **Problem:** Given an array of numbers (a_1, \dots, a_n) , construct an efficient data structure which supports the following operations:
 - **Add** (i, x) : Add x to the i -th cell ($a_i \leftarrow a_i + x$)
 - **Max** (i, j) : Return $\max\{a_i, \dots, a_j\}$
- Naïve approach - Use an array.
 - Add (i, x) in $O(1)$, Max (i, j) complexity is $O(n)$.
 - Worst case complexity for m queries is $O(mn)$.
- Better: Use a segment tree!
 - Add (i, x) , Max (i, j) are computed in $O(\log n)$.
 - Worst case complexity for m queries is $O(m \log n)$.

Segment Tree

1: [0, 16)															
2: [0, 8)								3: [8, 16)							
4: [0, 4)				5: [4, 8)				6: [8, 12)				7: [12, 16)			
8: [0, 2)		9: [2, 4)		10: [4, 6)		11: [6, 8)		12: [8, 10)		13: [10, 12)		14: [12, 14)		15: [14, 16)	
16: 0	17: 1	18: 2	19: 3	20: 4	21: 5	22: 6	23: 7	24: 8	25: 9	26: 10	27: 11	28: 12	29: 13	30: 14	31: 15

- Can be easily adapted to compute the sum/xor/max/min of all elements in a given segment.
- Implementation:
 - Example is included in the attached .cpp file.
 - Refer to [Wikipedia](#) for more info.
 - The following blog post contains a brief introduction and examples: <http://codeforces.com/blog/entry/18051>

Segment Tree

```
const int N = 1e5; // limit for array size
int n; // array size
int t[2 * N];

void build() { // build the tree
    for (int i = n - 1; i > 0; --i) t[i] = t[i<<1] + t[i<<1|1];
}

void modify(int p, int value) { // set value at position p
    for (t[p += n] = value; p > 1; p >>= 1) t[p>>1] = t[p] + t[p^1];
}

int query(int l, int r) { // sum on interval [l, r)
    int res = 0;
    for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
        if (l&1) res += t[l++];
        if (r&1) res += t[--r];
    }
    return res;
}
```


Fenwick tree (BIT)

- Similar to a Segment Tree, but even quicker to implement.
- Only supports the **Sum**(0, j) sums (i.e prefix sums).
- For more info-
 - <https://www.hackerearth.com/practice/data-structures/advanced-data-structures/fenwick-binary-indexed-trees/tutorial/>
 - <https://www.topcoder.com/community/data-science/data-science-tutorials/binary-indexed-trees/>

Fenwick tree (BIT)

```
int BIT[1000] = {0}, a[1000], n;
```

```
void update(int x, int val)
```

```
{
```

```
    for(; x <= n; x += x&-x)
```

```
        BIT[x] += val;
```

```
}
```

```
int query(int x)
```

```
{
```

```
    int sum = 0;
```

```
    for(; x > 0; x -= x&-x)
```

```
        sum += BIT[x];
```

```
    return sum;
```

```
}
```