Solution R-4.13

| Θ(1) | 2 ¹⁰ | | | |
|--------------------|-----------------------|----------------|----------------|--|
| Θ(n) | $2^{\log n} = n$ | 4n | 3n + 100 log n | |
| Θ(n log n) | n log n | 4 n log n + 2n | | |
| Θ(n ²) | n ² + 10 n | | | |
| Θ(n ³) | n³ | | | |
| Θ(2 ⁿ) | 2 ⁿ | | | |

Solution R-4.16

The Ex1 method runs in O(n) time.

Solution R-4.17

The Ex2 method runs in O(n) time.

Solution R-4.18

The Ex3 method runs in $O(n^2)$ time.

Solution R-4.19

The Ex4 method runs in O(n) time.

Solution R-4.20

The Ex5 method runs in $O(n^3)$ time.

Solution R-4.22

| | 1 sec | 1 hour | 1 month (30 days) | 1 century |
|----------------|------------------------|----------------------------|------------------------------------|--------------------------|
| log n | ≈ 10 ³⁰⁰⁰⁰⁰ | ≈ 10 ¹⁰⁰⁰⁰⁰⁰⁰⁰⁰ | ≈10 ^{0.8×10¹²} | ≈10 ¹⁰¹⁵ |
| n | 10 ⁶ | 3.6×10 ⁹ | ≈ 2.6 ×10 ¹² | ≈ 3.12 ×10 ¹⁵ |
| nlog n | ≈ 10 ⁵ | ≈ 10 ⁹ | ≈ 10 ¹¹ | ≈ 10 ¹⁴ |
| n ² | 1000 | 6×10 ⁴ | ≈ 1.6 ×10 ⁶ | ≈ 5.6 ×10 ⁷ |
| n ³ | 100 | ≈ 1500 | ≈ 14000 | ≈ 1 500000 |
| 2 ⁿ | 19 | 31 | 41 | 51 |

Solution C-4.9

$$\sum_{i=1}^{n} i^{2} \le \sum_{i=1}^{n} n^{2} = n \times n^{2} = n^{3} = O(n^{3})$$