# Perturbed Universes and Inflationary Models

MSci. Thesis

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# 1 Acknowledgments

blah blah

## 2 Abstract

The aim of this project is to investigate inflationary models and discover new models that give near scale invariance in accordance with Cosmic Microwave Background data.

#### 3 Introduction

- 3.1 Cosmic Microwave Background (CMB)
- 3.2 Cosmological Problems
- 4 Theory
- 4.1 Friedmann Equations
- 4.2 Inflation
- 4.3 Mukhanov Sasaki Equation
- 4.4 Power Spectrum
- 4.5 Spectral Index
- 5 Matching Conditions
- 5.1 Jacobi Elliptic
- 5.2 Constant w

#### 6 Hamiltonian Jacobi

#### 6.1 Outline

The evolution of scalar fields is described by the Klein [1] Gordon Equation

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0 \tag{1}$$

$$H^{2} = \frac{8\pi}{3m_{pl}^{2}} \left[ \frac{1}{2}\dot{\phi}^{2} + V(\phi) \right]$$
 (2)

- 6.2 Intermediate Inflation
- **6.3**  $n_s = 1$
- **6.4**  $n_s \neq 1$
- 6.5 Proof of Slow roll
- 6.6 Equation of State
- 6.7 Potential
- 7 Conclusion

### References

[1] Herbert Goldstein. Classical mechanics. Addison-Wesley, Reading, Mass. ; Wokingham, 2nd ed. edition, 1980. ID:  $44 \text{IMP}_A LM A_D S 2141267570001591$ .