Let y be on inverse goussian distribution, with support [0, 10) and density

$$\{(y;\xi,\lambda)=\left(\frac{\lambda}{2\pi}\right)^{1/2}y^{2}=\frac{3/2}{2}\sqrt{\lambda\xi}^{2}=\frac{-\frac{1}{2}\left(\frac{\lambda}{y}+\xi y\right)}{2}$$

$$g(y; \xi, \lambda) = \exp \left\{ -\frac{1}{2} \xi y - \frac{1}{2} \frac{\lambda}{y} \right\} + \left[\frac{1}{2} \log(\lambda) - \frac{3}{2} \log(y) - \frac{1}{2} \log(2u) \right\}$$

Set
$$\theta = -\frac{1}{2} \frac{5}{\lambda}$$
 so that $-\frac{5}{2} = \theta \lambda$ and $5\lambda = -2\theta \lambda^2$.
This gives:

$$\{(y; \theta, \lambda) = \exp \{\theta \} y - \lambda (-2\theta)^2 - \frac{1}{2} \frac{\lambda}{y} + \frac{1}{2} \log(\lambda) - \frac{3}{2} \log(y) - \frac{1}{2} \log(2\pi) \}$$

$$\begin{cases} (g; \theta, \lambda) = \exp \left\{ \frac{1}{2} \theta \right\} - \frac{1}{2} \left(\frac{1}{2} \frac{\lambda}{y} + \frac{1}{2} \log(\lambda) - \frac{3}{2} \log(y) - \frac{1}{2} \log(2i) \right\} \\ \text{Now, net } \phi = \frac{1}{\lambda}, \text{ giving } \text{ Consful here, we meed a minum (given below)} \\ \begin{cases} (g; \theta, \phi) = \exp \left\{ \frac{1}{2} \frac{\lambda}{y} + \frac{1}{2} \log(\lambda) - \frac{3}{2} \log(y) - \frac{1}{2} \log(2i) \right\} \\ \phi \end{cases}$$

Thus, we have

$$\theta = -\frac{1}{2}\frac{\$}{\lambda}$$
 commice parameter, with $\frac{\theta < 0}{\lambda}$; $\phi = \frac{1}{\lambda}$ dispersion.

$$b(\theta) = -(-2\theta)^{1/2}$$
; $a(\phi) = \phi$

$$C(\phi, y) = -\frac{1}{2\phi y} - \frac{1}{2}\log(\phi) - \frac{3}{2}\log(y) - \frac{1}{2}\log(2\tilde{u})$$

Mean Semetion

$$b'(\theta) = \frac{\delta}{\delta \theta} - (-2\theta)^{\frac{1}{2}} = \frac{1}{2(-2\theta)^{\frac{1}{2}}} \cdot \frac{2}{2} = \frac{1}{(-2\theta)^{\frac{1}{2}}} = \mu(\theta)$$

$$= \Rightarrow p^{2} = \frac{1}{-2\theta} \iff -2\theta = \frac{1}{p^{2}} \iff \theta = \frac{1}{-2p^{2}}$$

$$\Theta(p) = \frac{1}{-2p^{2}} \implies Commics link$$

Vorionce function

$$b''(\theta) = \frac{\partial}{\partial \theta} (-2\theta)^{-\frac{1}{2}} = -\frac{1}{2} (-2\theta)^{\frac{1}{2}} \cdot (-2) = \frac{1}{(-2\theta)^{\frac{1}{2}}}$$

=>
$$\vee (p) = \frac{1}{[-2\Theta(p)]^{3/2}} = \frac{1}{(-2p^2)^{3/2}} = p^3$$

$$v(y) = y^3, vor(y) = \phi y^3$$