PTX = 15 dBm , B=18 MHZ T = -165 dBm/Hz

- At least 95% of the users one in Rooms: 1,2, and 3 [ SEE MATURE] The SNR that can be guaranteed to at least 95% of the usons is the SNR of Room 3 (i.e. the lowestone) which is 17, 4473 dB
- (b) Rayleigh fading Expression for the CDF of the SNR including variation in both location and fading

$$F_{\Gamma}(\chi) = P(\Gamma \leq \chi) = \int_{-\infty}^{\gamma} f_{\Gamma}(\chi) d\chi = \Lambda - e^{-\chi/\bar{\chi}} / P(\Gamma > \chi) = e^{-\chi/\bar{\chi}}$$

In this case,

$$F_{\eta_{RL}}(\vec{y}) = P(\Gamma_{a_{L}} \leq y) = \sum_{i=1}^{4} P(\Gamma \leq y \mid Room = \lambda) P(Room = \lambda)$$

$$= o_{16} \left( \lambda - e^{-y/\bar{y}_{2}} \right) + o_{13} \left( 1 - e^{-y/\bar{y}_{2}} \right) + o_{106} \left( 1 - e^{-y/\bar{y}_{3}} \right) + o_{104} \left( 1 - e^{-y/\bar{y}_{4}} \right), \text{ where } \bar{y}_{i} = avg SNR \text{ in } Room i.$$

- (c) SNR quaranteed to at least 95% of the people with slow fading  $0.05 = F_{RL}(8) = P(P_{RL} SS) = \sum_{n=1}^{\infty} SEE THTLAB to at least 95% of the uses$ value use want to find \_\_\_\_ The SNR value use can quarantee vis ~ 10,2086 dB 5% of users will have less value / 95% vill have than this value / 95% vill have expeater SNR than this
- h(1,0) = 1P1 e-21, ft + 1P2 e-21, ft = 11+P2

(P)

In this case, 
$$C = \frac{1}{2} \left[ log \left( 1 + \frac{l_1}{NoW} \right) + log \left( 1 + \frac{l_2}{NoW} \right) \right]$$

$$\frac{P_1}{W N_0} = 8 dB \qquad \frac{\text{Linear}}{D} 6,31 \qquad \frac{P_2}{W N_0} = 5 dB \qquad \frac{\text{Linear}}{D} 3,16$$

$$L(r) = \log \frac{\rho(r|C=1)}{\rho(r|C=0)}$$

(a) Real-valued bimoory channel with fading

$$V = A_X + W$$
,  $\omega \sim N(0, \frac{N_0}{2})$ ,  $x = \begin{cases} \sqrt{E_X/2} & \text{if } c=0 \\ -\sqrt{E_X/2} & \text{if } c=0 \end{cases}$ 

$$Ax = \begin{cases} A\sqrt{E_{X}} & \text{if } c=0 \end{cases} \qquad \omega \sim N/0, \frac{N_{0}}{2}$$

$$P(r|c=1) = \frac{1}{1\pi N_{0}} e^{-\frac{r}{N_{0}}} \frac{\left(r - A\sqrt{E_{X}}\right)^{2}}{\sqrt{\pi N_{0}}} e^{-\frac{r}{N_{0}}} e^$$

$$L(r) = \log \frac{\rho(r \mid C = \Delta)}{\rho(r \mid C = 0)} = \frac{-(r - A\sqrt{\frac{E_{x}}{2}})^{2} + (r + A\sqrt{\frac{E_{x}}{2}})^{2}}{N_{0}}$$

$$= \frac{-r^{2} + 2rA\sqrt{\frac{E_{x}}{2}} - (A\sqrt{\frac{E_{x}}{2}})^{2} + r^{2} + 2rA\sqrt{\frac{E_{x}}{2}} + (A\sqrt{\frac{E_{x}}{2}})^{2}}{N_{0}}$$

$$= \frac{4rA\sqrt{E_{x}}}{N_{0}} = \frac{2\sqrt{2}rA\sqrt{E_{x}}}{N_{0}} = \frac{2rA\sqrt{2}E_{x}}{N_{0}}$$

(b) Bimary Simmetric Chammed

$$r = c + w \pmod{2} \qquad \omega = \begin{cases} 1 \text{ with probability p} \\ 0 \text{ with probability } 1 - p \end{cases}$$

$$r \text{ can be } 0,1 \qquad \Rightarrow (1) = \log_{10} \frac{p(r|c=1)}{p} \qquad \Rightarrow (1) = \log_{10} \frac{1-p}{p} \qquad \text{which can be consisten as: } L(r) = (2r-1)\log_{10} \frac{1-p}{p}, \text{ for } r=0,1$$

(C) Non-coherent channel

$$V = \begin{cases} h \perp m & \text{when } C = \Delta \\ M & \text{when } C = 0 \end{cases}$$

$$h \sim CN(o, Es), m \sim CN(o, No)$$

$$L(r) = \log \frac{\rho(r|c=\Delta)}{\rho(r|c=0)} \qquad \rho(r|c=0) = \frac{1}{\sqrt{2\pi N_0}} e^{-\frac{1}{2} \frac{1}{N_0}} e^{-\frac{1}{2} \frac{1}{N_0}} e^{-\frac{1}{2} \frac{1}{N_0}}$$

$$P(r(c=1) = \frac{1}{\sqrt{2\pi(N_0 + E_s)}} e^{-|r|^2/2(N_0 + E_s)})$$

$$r = R_1 m \sim CN(e, E_s + N_0)$$
assuming R and m are independent

$$L(r) = \log \frac{\frac{1}{\sqrt{\frac{1}{2\pi(N_{0}+E_{S})}}} e^{-\frac{|r|^{2}/2(N_{0}+E_{S})}{2}}}{\frac{1}{\sqrt{\frac{1}{2\pi}N_{0}}} e^{-\frac{|r|^{2}/2(N_{0}+E_{S})}{2}}} = \frac{1}{2}\log \frac{N_{0}}{E_{S}+N_{0}} + \frac{-|r|^{2}}{2(N_{0}+E_{S})} + \frac{1}{2N_{0}} = \frac{1}{2}\log \frac{N_{0}}{E_{S}+N_{0}} + \frac{|r|^{2}}{2(N_{0}+E_{S})}$$

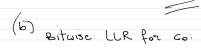
PROBLEM 6

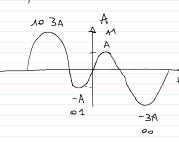
$$Y = X + M$$
  $M \sim \left(0, \frac{N_0}{2}\right)$   $X = \begin{cases} -3A & \text{if } C_{0}, C_{1} = 00 \\ -A & \text{if } C_{0}, C_{1} = 0.1 \end{cases}$   
 $A = \begin{cases} C_{0}, C_{1} = 1.1 \\ 3A & \text{if } C_{0}, C_{1} = 1.0 \end{cases}$ 

(a) 
$$\int_{0}^{avonage} symbol envry$$

$$E|X|^{2} = \underbrace{\frac{9A^{2} + A^{2} + A^{2} + 9A^{4}}{4}}_{A} = 5A^{2}$$

$$5A^{2} = \underbrace{Es}_{2} = A = \underbrace{\underbrace{Es}_{Ao}}_{Ao}$$





$$L_{o}(r) = \log \underbrace{\frac{\rho(r|C_{o}=\Delta)}{\rho(r|C_{o}=\Delta)}} \qquad \rho(r|C_{o}) = \frac{\Lambda}{2} \left[ \frac{\rho(r|C_{o},C_{\Delta}=\Delta) + \rho(r|C_{o},C_{\Delta}=\Delta)}{\rho(r|C_{o},C_{\Delta}=\Delta)} \right]$$

$$N(3A,N_{o}/2) \qquad N(A,N_{o}/2)$$

$$N(3A,N_{o}/2) \qquad N(A,N_{o}/2)$$

$$P(r|C_{o},C_{\Delta}=A,\Delta) + \rho(r|C_{o},C_{\Delta}=A,\Delta)$$

$$P(r|C_{o},C_{\Delta}=A,\Delta) + \rho(r|C_{o},C_{\Delta}=A,\Delta)$$

$$N(-3A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_$$

$$L_{1}(r) = \log \left[ \frac{P(r|C_{0},C_{1} = e,1) + P(r|C_{0},C_{1} = 1,1)}{P(r|C_{0},C_{1} = 0,0) + P(r|C_{0},C_{1} = 1,0)} \right]$$

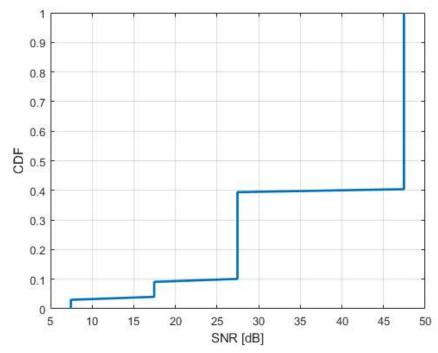
$$= \log \left[ \frac{C - (r+A)^{2}/N_{0} - (r-A)^{2}/N_{0}}{e - (r+3A)^{2}/N_{0} + e^{-(r-3A)^{2}/N_{0}}} \right]$$

## Wireless Communications EL-GY 6023

Homework 4 - Tommy Azzino (ta1731)

Problem 3

```
path_losses = [60, 80, 90, 100];
Ptx = 15; % dBm
B = 18e6;
N0 = -165;
N0_{lin} = db2pow(N0-30);
Ptx_lin = db2pow(Ptx-30);
Prx = Ptx - path_losses;
Prx_lin = db2pow(Prx-30);
SNRs_dB = pow2db(Prx_lin/(N0_lin*B));
user_distribution = [0.6, 0.3, 0.06, 0.04];
snr_cdf = [];
for i=1:length(SNRs_dB)
    snr\_cdf = [snr\_cdf, repelem(SNRs\_dB(i), user\_distribution(i)*100)];
end
figure;
plot(sort(snr_cdf), linspace(0,1,length(snr_cdf)), "LineWidth",2);
grid on;
xlabel("SNR [dB]"); ylabel("CDF");
```



```
disp(SNRs_dB(3));
```

17.4473

(a)

As we can see from the plot above, we have that 95 % of the users will experience an SNR value of at least 17.4473 dB.

(c)

```
npoints = 10000;
snrs = linspace(-10,60,npoints);
F = zeros(npoints,1);
```

```
for i=1:npoints
    F(i) = dot((1-exp(-db2pow(snrs(i))./db2pow(SNRs_dB))), user_distribution);
end
snr_t = interp1(F,snrs,0.05);
fprintf(1, 'SNR that can be guaranteed to at least 95 perc of the users with fading [dB] = %f\n', snr_t);
```

SNR that can be guaranteed to at least 95 perc of the users with fading [dB] = 10.208600