PROBLEM:

Prx = 15 dBm , B = 18 MHz T = - 165 dBm/Hz

- (a) At least 95% of the users are in Rooms: 1, 2, and 3

 [SRE MATLAB] The SNR that can be avarianteed to at least 95% of the users is the SNR of Room 3 (i.e. the bouest one) which is 14, 4473 dB
- (b) Rayleigh fading Expression for the CDF of the SNR including variation in both location and fading $F_{\Gamma}(\chi) = P(\Gamma \leq \chi) = \int_{-\infty}^{\chi} f_{\Gamma}(\chi) d\chi = 1 e^{-\chi/\bar{\chi}} / P(\Gamma > \chi) = e^{-\chi/\bar{\chi}}$

In this case,

$$F_{T_{RL}}(\vec{y}) = P(T_{a_{L}} \leq \vec{y}) = \sum_{i=1}^{4} P(T \leq \vec{y} \mid Rovin_{i} = \lambda) P(Rovin_{i} = \lambda)$$

$$= o_{16} \left(1 - e^{-\frac{3}{2}} \right) + o_{13} \left(1 - e^{-\frac{3}{2}} \right) + o_{106} \left(1 - e^{-\frac{3}{2}} \right) + o_{104} \left(1 - e^{-\frac{3}{2}} \right) \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx = a_{L} \int_{a_{L}}^{a_{L}} \left(1 - e^{-\frac{3}{2}} \right) dx =$$

- han this voice C f age after SNR than this $h(f, o) = P_1 C^{-2\pi_j} f^{2_1} + \sqrt{p_1} C^{-2\pi_j} f^{2_2} \Rightarrow |h|^{\frac{1}{2}} = f_1 + f_2$ Hence, $SNR_{alg} = \frac{p_1 + p_2}{WN_0}$
- (b) Engodic Capacity \Rightarrow $C_E = E[log(1+y)]$ $\leq log(1+E[y]) = log(1+SNRANg) \Rightarrow$ $C_E \leq log(1+SNRANg)$ (c) AWEN Capacity limear scale (p) $\frac{P_4}{WN_0} = 8dB \xrightarrow{limear} 6,31 / \frac{P_2}{WN_0} = 5dB \xrightarrow{D} 3,16$ $SNRANG \approx 9,76 dB / CE \leq log(1+9,4624) \approx 3,387$

00-01045

$$L(r) = \log \frac{\rho(r|c=1)}{\rho(r|c=0)}$$

$$\int -A\sqrt{\frac{E_{x}}{2}} if c=0$$

$$p(r|c=0) = \frac{A}{\sqrt{\pi N_{0}}} e^{-\frac{(r+r)\sqrt{2}}{2}}$$

$$L(r) = \log \frac{\rho(r \mid C = \Delta)}{\rho(r \mid C = 0)} = \frac{-(r - A\sqrt{\frac{E_X}{2}})^2 + (r + A\sqrt{\frac{E_X}{2}})^2}{N_0}$$

$$= \frac{r^2 + 2rA\sqrt{\frac{E_X}{2}} - (A\sqrt{\frac{E_X}{2}})^2 + r^2 + 2rA\sqrt{\frac{E_X}{2}} + (A\sqrt{\frac{E_X}{2}})^2}{N_0}$$

$$= \frac{4rA\sqrt{E_X}}{N_0} = \frac{2\sqrt{2}rA\sqrt{E_X}}{N_0} = \frac{2rA\sqrt{2E_X}}{N_0}$$

(b) Bimony Simmetric Chammed

$$r = c + w \pmod{2}$$

$$\omega = \begin{cases} 1 \text{ with probability } p \\ 0 \text{ with probability } 1 - p \end{cases}$$

$$L(r) = \log \frac{p(r|c=\Delta)}{p(r|c=0)} \Rightarrow L(1) = \log \frac{\Lambda - p}{p} / L(0) = \log \frac{p}{1 - p}$$

$$p(r|c=0)$$
Which can be written as: $L(r) = (2r-1) \log \frac{1 - p}{p}$, for $r = 0, 1$

(C) Non-coherent channel

$$V = \begin{cases} h + m & \text{when } C = 1 \\ m & \text{when } C = 0 \end{cases}$$

$$h \sim CN(0, Es), m \sim CN(0, N_0)$$

$$L(r) = \log \frac{\rho(r|c=\Delta)}{\rho(r|c=0)} \qquad \rho(r|c=0) = \frac{1}{11N_0} e^{-\frac{1}{11N_0}} r = m \sim cN(0, N_0)$$

$$P(r(C=\Delta) = \frac{1}{\pi(N_0 + E_S)} e^{-1r)^2/(N_0 + E_S)}, \quad r = h + m \sim CN(e, E_S + N_0)$$
assuming h and m are independent

$$L(r) = \log \frac{\frac{1}{M(N_0 + E_S)}}{\frac{1}{MN_0}} = \frac{\log \frac{N_0}{E_{S+N_0}} + \frac{-|r|^2}{(N_0 + E_S)}}{\frac{1}{MN_0}} = \log \frac{N_0}{E_{S+N_0}} + \frac{1}{N_0} = \log \frac{N_0}{E_{S+N_0}} + \frac{1}{N_0} = \log \frac{N_0}{E_{S+N_0}}$$

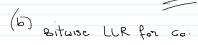
PROBLEM 6

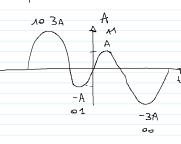
$$Y = X + M$$
 $M \sim \left(0, \frac{N_0}{2}\right)$ $X = \begin{cases} -3A & \text{if } C_0, C_1 = 00 \\ -A & \text{if } C_0, C_1 = 01 \end{cases}$
 $A = \begin{cases} C_0, C_1 = A_1 \\ A & \text{if } C_0, C_1 = A_2 \end{cases}$
 $3A = \begin{cases} C_0, C_1 = A_2 \\ C_0, C_1 = A_2 \end{cases}$

(a)
$$\int_{0}^{average} symbol energy$$

$$E|X|^{2} = \underbrace{\frac{9A^{2} + A^{2} + A^{2} + 9A^{4}}{4}}_{A} = 5A^{2}$$

$$5A^{2} = \underbrace{Es}_{2} \Rightarrow A = \underbrace{Es}_{Ao}$$





$$L_{o}(r) = \log \underbrace{P(r|C_{o}=1)}_{P(r|C_{o}=0)} \qquad P(r|C_{o}) = \underbrace{\frac{\Lambda}{2} \left[P(r|C_{o},C_{A}=0) \right]}_{P(r|C_{o},C_{A}=0)}$$

$$N(3A,N_{o}/2) \qquad N(A,N_{o}/2)$$

$$N(3A,N_{o}/2) \qquad N(A,N_{o}/2)$$

$$P(r|C_{o},C_{A}=0,0) + P(r|C_{o},C_{A}=0,1)$$

$$N(-3A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2) \qquad N(-A,N_{o}/2)$$

$$N(-A,N_{o}/2) \qquad N(-A,N_{o}/2) \qquad N(-A,N_{o$$

$$L_{1}(r) = \log \left[\frac{\rho(r|c_{0},c_{1}=e,\Lambda) + \rho(r|c_{0},c_{1}=\Lambda,\Lambda)}{\rho(r|c_{0},c_{1}=0,0) + \rho(r|c_{0},c_{1}=\Lambda,0)} \right]$$

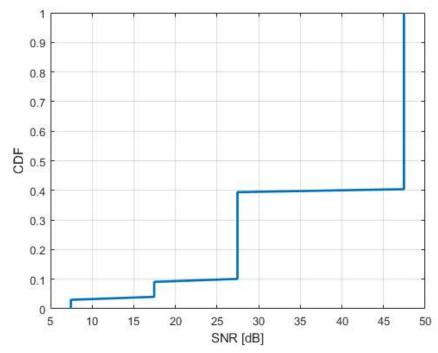
$$= \log \left[\frac{c - (r+A)^{2}/N_{0} - (r-A)^{2}/N_{0}}{e - (r+3A)^{2}/N_{0} + e^{-(r-3A)^{2}/N_{0}}} \right]$$

Wireless Communications EL-GY 6023

Homework 4 - Tommy Azzino (ta1731)

Problem 3

```
path_losses = [60, 80, 90, 100];
Ptx = 15; % dBm
B = 18e6;
N0 = -165;
N0_{lin} = db2pow(N0-30);
Ptx_lin = db2pow(Ptx-30);
Prx = Ptx - path_losses;
Prx_lin = db2pow(Prx-30);
SNRs_dB = pow2db(Prx_lin/(N0_lin*B));
user_distribution = [0.6, 0.3, 0.06, 0.04];
snr_cdf = [];
for i=1:length(SNRs_dB)
    snr\_cdf = [snr\_cdf, repelem(SNRs\_dB(i), user\_distribution(i)*100)];
end
figure;
plot(sort(snr_cdf), linspace(0,1,length(snr_cdf)), "LineWidth",2);
grid on;
xlabel("SNR [dB]"); ylabel("CDF");
```



```
disp(SNRs_dB(3));
```

17.4473

(a)

As we can see from the plot above, we have that 95 % of the users will experience an SNR value of at least 17.4473 dB.

(c)

```
npoints = 10000;
snrs = linspace(-10,60,npoints);
F = zeros(npoints,1);
```

```
for i=1:npoints
    F(i) = dot((1-exp(-db2pow(snrs(i))./db2pow(SNRs_dB))), user_distribution);
end
snr_t = interp1(F,snrs,0.05);
fprintf(1, 'SNR that can be guaranteed to at least 95 perc of the users with fading [dB] = %f\n', snr_t);
```

SNR that can be guaranteed to at least 95 perc of the users with fading [dB] = 10.208600