

Beamer presentation template

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Agenda

Introduction

System representation

System analysis

Control design

Overlay curvy arrows

\mathcal{A} is a linear completely positive
and trace preserving map

“Stochastic” map

ρ are density operators:
 $\rho \in \mathbb{C}^{n \times n}$, $\rho = \rho^\dagger \geq 0$ and $\text{tr}[\rho] = 1$

Quantum probability distributions

$$\begin{cases} \rho(t+1) = \mathcal{A} [\rho(t)] \\ p(t) = \mathcal{C} [\rho(t)] \end{cases}$$

Overlay curvy arrows

\mathcal{A} is a linear completely positive and trace preserving map

“Stochastic” map

p are probability vectors:
 $p \in \mathbb{R}^m$ $p_i \geq 0$ and $\sum_i p_i = 1$

Classical probability distribution

ρ are density operators:

$\rho \in \mathbb{C}^{n \times n}$, $\rho = \rho^\dagger \geq 0$ and $\text{tr}[\rho] = 1$

Quantum probability distributions

$$\begin{cases} \rho(t+1) = \mathcal{A} [\rho(t)] \\ p(t) = \mathcal{C} [\rho(t)] \end{cases}$$

\mathcal{C} is a linear map that gives the probabilities of the outcome of a measurement
Output map

This model includes hidden markov model but **does not include** the effects of conditioning.

Sample frame title

In this slide, some important text will be **highlighted** because it's important.
Please, don't abuse it.

Remark

Sample text

Important theorem

Sample text in alert box

Examples 1

Sample text in green box. The title of the block is "Examples".

Optimal reduction



Remark

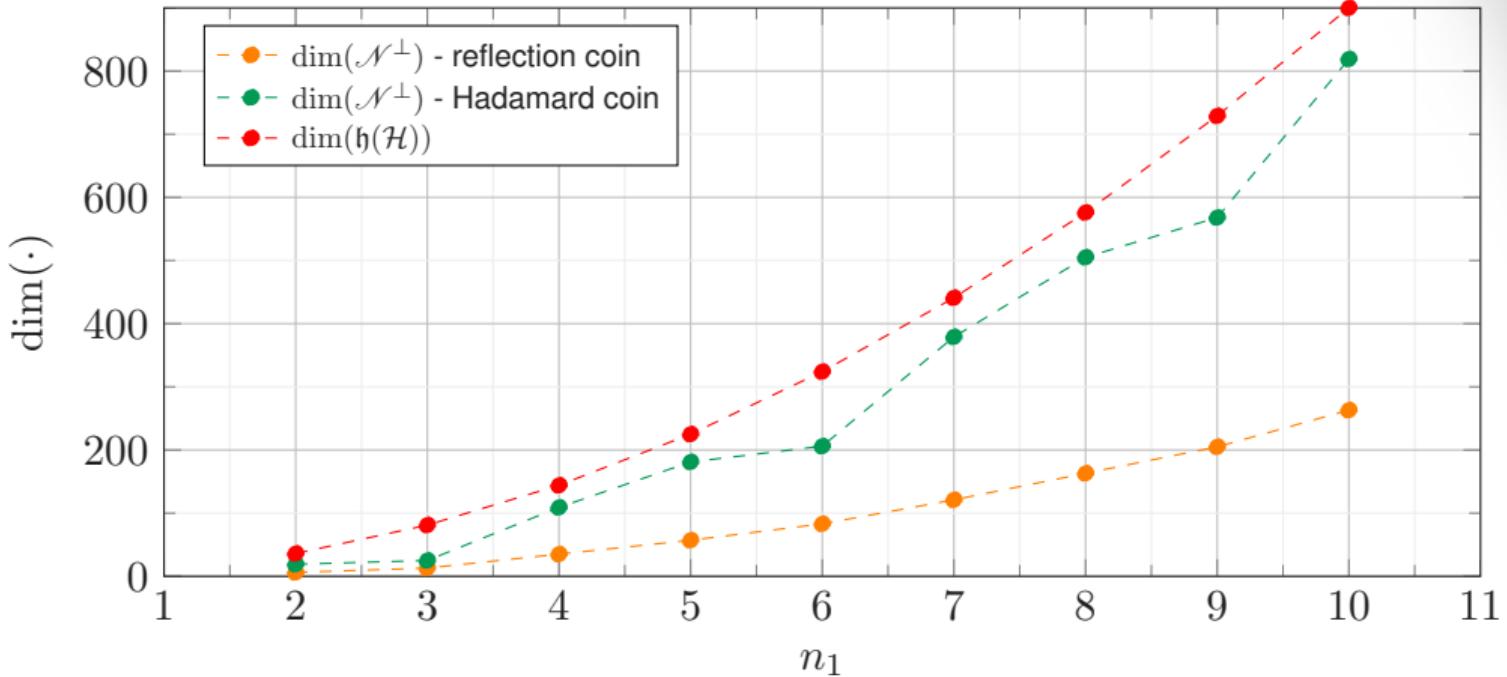
A first draft on the related “Model reduction for Hidden Markov Models” can be found on [arXiv : 2208.05968](https://arxiv.org/abs/2208.05968)





Let's see some
results

Analysis of the coined quantum walks



Imported code from file

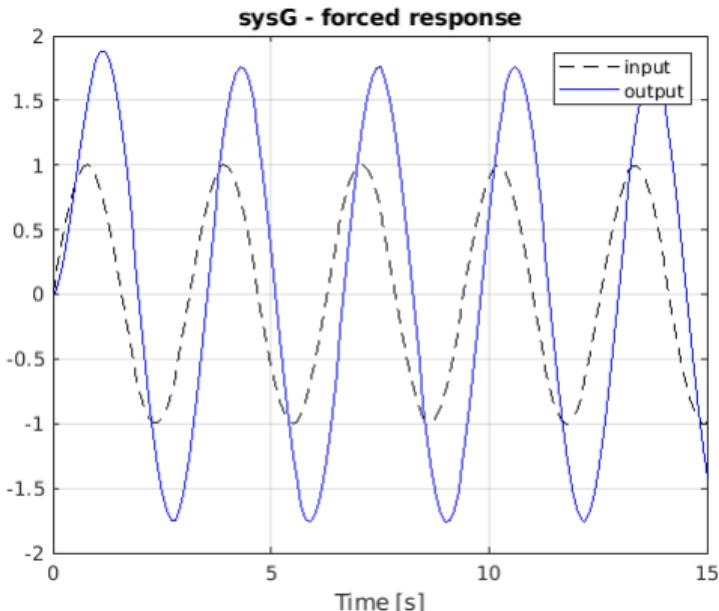
$$\begin{aligned}G(s) &= \frac{5s + 50}{s^2 + 101s + 100} \\&= 5 \frac{s + 10}{(s + 1)(s + 100)}\end{aligned}$$

$$\begin{cases} \dot{x}(t) = Ax(t) + Bu(t) \\ y(t) = Cx(t) + Du(t) \end{cases}$$

$$A = \begin{bmatrix} 0 & 1 \\ -100 & -101 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix},$$
$$C = \begin{bmatrix} 50 & 5 \end{bmatrix}, \quad D = [0]$$

```
1 % Transfer function form
2 num = 5 * [1, 10];
3 den = [1, 101, 100];
4 sysG = tf(num,den)
5
6 % Zeros, Poles and Gain form
7 z = -10;
8 p = [-1, -100];
9 k = 5;
10 sysG = zpk(z,p,k)
11
12 % State space form
13 A = [0, 1; -100, -101];
14 B = [0; 1];
15 C = 5 * [10, 1];
16 D = 0;
17 sysG = ss(A, B, C, D)
```

Inline code (Clearly needs some work)



Display forced response

```
1 t = 0:0.1:15;
2 u = sin(2*t);
3 x0 = 0;
4 y = lsim(sysG, u, t,
5 x0);
6
7 figure;
8 plot(t, u, 'k--');
9 hold on;
10 plot(t, y, 'b');
11 legend('input',
12 'output');
13 grid on;
```

Columns



Encapsulated form:

The CST stores and uses the model-related data via LTI objects (objects in the sense of object-oriented programming).

From the encapsulated form it is possible to access the non-encapsulated data via dot-notation

Non-encapsulated form:

poles and zeros, state/input/output matrices etc. etc.

Conclusions and outlook

Classical control tools can be used to study quantum walks and find the minimal linear model capable of reproducing the output probability distribution.

Grover's algorithm uses surprisingly few resources.

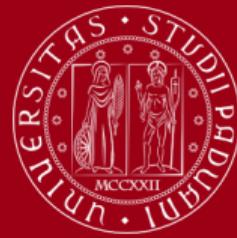
Future directions:

- Robustness to initialization errors.
- More general output functions.
- **Completely positive and trace preserving constraint.**

Thank you for your attention!



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