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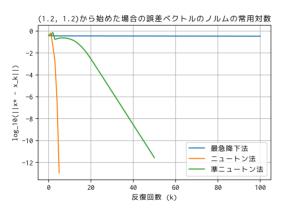
In [1]:

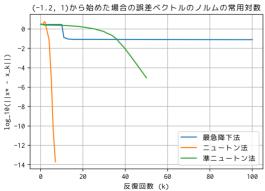
import numpy as no

```
import pandas as pd
import matplotlib.pyplot as plt
                     3 import matplotlib.p4 % matplotlib inline
In [2]:
                                return(100 * (x[1][0] - x[0][0] ** 2) ** 2 + (1 - x[0][0]) ** 2)
                           def grad_f(x):
return(np.array([[400 * x[0][0] ** 3 - 400 * x[0][0] * x[1][0] + 2 * x[0][0] - 2], [200 * (x[1][0] - x[0][0] ** 2)]]))
                           def hessian_f(x):

return(np.array([[1200 * x[0][0] ** 2 - 400 * x[1][0] + 2, -400 * x[0][0]], [-400 * x[0][0], 200]]))
                            \begin{split} & \textbf{def} \ back\_track(x, alpha, c, d, rho): \\ & \textbf{while True:} \\ & \text{if } f(x + alpha * d) <= f(x) + c * alpha * grad\_f(x).T @ d: \\ & \textbf{return} \ alpha \end{split} 
In [31:
                                     alpha *= rho
In [4]:
                           def gradient_descent(x_0, alpha = 0.5, c = 0.1, rho = 0.8, n_itr = 100):
                                 \begin{aligned} xs &= np.array([x\_0]) \\ &\text{for k in range}(n\_irt): \\ &d &= -1 * grad\_f(xs[k]) \\ &x &= np.append(xs, [xs[k] + back\_track(xs[k], alpha, c, d, rho) * d], axis = 0) \end{aligned} 
                                return xs
                           def newton_method(x_0, n_itr = 50):
                                 \begin{aligned} xs &= \text{pp.array}([x\_0]) \\ \text{for } k &\text{in } \text{range}(\texttt{m\_itr}): \\ d &= 11 * \text{rp.linalg.inv}(\text{hessian\_f}(xs[k])) @ \text{grad\_f}(xs[k]) \\ xs &= \text{pp.append}(xs, [xs[k] + d], axis = 0) \end{aligned} 
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                                return xs
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                                                                          ethod(x_0, H = np.array([[1, 0], [0, 1]]), alpha = 0.5, c = 0.1, rho = 0.8, n_itr = 50):
                                \begin{array}{ll} \textbf{lef quasi_newton\_method}(x\_0, H = np.array([[1, U], [U, 1]]), alpha = U.b, c = U. \\ xs = np.array([x\_0]) \\ for k in range(n\_itr): \\ d = -1 * H @ grad\_f(xs[k]) \\ xs = np.append(xs, [xs[k] + back\_track(xs[k], alpha, c, d, rho) * d], axis = 0) \\ - v_sft + v_1 - v_sft | v_sft| \\ \end{array} 
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                                     \begin{split} s &= xs[k+1] - xs[k] \\ y &= grad_f(xs[k+1]) - grad_f(xs[k]) \\ H &= (np.identity(2) - (s @ y.T) / (y.T @ s)) @ H @ (np.identity(2) - (y @ s.T) / (y.T @ s)) + (s @ s.T) / (s.T @ y) \\ \end{split}
                 22
                                return xs
                   1 def error(v, optimum_point = np.array([[1], [1]])):
2 return np.log10(np.linalg.norm(v - optimum_point))
In [5]:
                           def plot_errors(start, start_str):
   gradient_transition = gradient_descent(start)
   newton_transition = newton_method(start)
                                quasi_newton_transition = quasi_newton_method(start)
                               plt.plot(np.arange(len(gradient_transition)), np.apply_along_axis(error, 1, gradient_transition), flatten(), label='最急降下法') plt.plot(np.arange(len(newton_transition)), np.apply_along_axis(error, 1, newton_transition), flatten(), label='ユートン法') plt.plot(np.arange(len(quasi_newton_transition)), np.apply_along_axis(error, 1, quasi_newton_transition).flatten(), label='準ニュートン法') plt.glegend() plt.title(start_str + "から始めた場合の誤差ペクトルのノルムの常用対数") plt.xlabel('反復回数 (k)') plt.ylabel('log_10(||x* - x_k||)') plt.ylabel('log_10(||x* - x_k||)') plt.ylabel('log_10(||x* - x_k||)') plt.show()
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In [6]: 1 plot_errors(np.array([[1.2], [1.2]]), '(1.2, 1.2)') 2 plot_errors(np.array([[-1.2], [1.]]), '(-1.2, 1)')
```

/Users/uedatomohiro/.pyenv/versions/anaconda3-5.1.0/lib/python3.6/site-packages/ipykernel_launcher.py:2: RuntimeWarning: divide by zero encountered in log10





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```
| def plot_transitions(start, start_str):
    plt.scatter([1], [1], label='最適点', color='red')

    gradient_transition = gradient_descent(start)
    newton_transition = newton_method(start)
    quasi_newton_transition = quasi_newton_method(start)

    plt.plot(gradient_transition[:, 0], gradient_transition[:, 1], label='最急降下法')
    plt.plot(quasi_newton_transition[:, 0], newton_transition[:, 1], label='ユートン法')
    plt.plot(quasi_newton_transition[:, 0], quasi_newton_transition[:, 1], label='準ニュートン法')
    plt.legend()
    plt.title(start_str + "から始めた場合の誤差ベクトルのノルムの常用対数")
    plt.vlabel('仮復回数 (k)')
    plt.ylabel('log_10(|lx*-x_k|)')
    plt.grid()
    plt.show()
```

In [8]: 1 plot_transitions(np.array([[1.2], [1.2]]), '(1.2, 1.2)') plot_transitions(np.array([[-1.2], [1.]]), '(-1.2, 1)')

