Variable Selection and Regression Analysis of Smoking Cessation Outcomes Using Regularization: A Reanalysis of the BASC-Varenicline Trial Data

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Abstract

Background: Individuals with past or present major depressive disorder (MDD) experience unique barriers to smoking cessation. While varenicline has been shown to be more effective than traditional nicotine replacement therapy in achieving abstinence for individuals with and without MDD, its lower effectiveness for those with MDD suggests that MDD-responsive treatment strategies are necessary. A recent determined that varenicline improved abstinence, but BASC did not, either with or without varenicline. In light of this surprising result, we use data from this study to examine baseline variables as potential predictors of end-of-treatment abstinence and moderators of behavioral treatment's effect thereon.

Methods: We examine data from a randomized, placebo-controlled 2x2 factorial design study of 300 smokers with past or present MDD, who received either placebo or varenicline and standard treatment (ST) or behavioral activation for smoking cessation (BA). Missing data was imputed through multiple imputation. A cross-validated Lasso was applied at the optimally chosen value of λ for coefficient estimates. Subsequently a bootstrap procedure is carried out to estimate confidence intervals and assess significance of the coefficients.

Results: The participant's Fagerstrom Test for Cigarette Dependence score, complementary reinforcers (i.e., pleasurable events associated with smoking), and the log of the participant's Nicotine Metabolite Ratio were all baseline predictors of abstinence controlling for treatment type. The model demonstrated good discriminative ability (validation AUC=TODO: XXX). Our moderator analysis demonstrated that no variables could be identified as potential moderators of the therapy based treatment (BA or ST).

Conclusion: Lasso regression with bootstrap confidence interval estimates identified meaningful predictors of abstinence. *TODO: INSERT SENTENCE ABOUT IDENTIFIED PREDICTORS*. We were unable to identify treatment effect moderators. Limitations include the relatively small sample size, which led to convergence issues and challenges handling class imbalance in the outcome which suggests these findings should be validated in larger studies. Future research might benefit from more sophisticated regularization approaches and larger, more diverse samples to better understand treatment effect heterogeneity in this population.

Introduction

More than 30% of individuals with major depressive disorder (MDD) are daily smokers (Han et al. 2022; Smith et al. 2020; Weinberger et al. 2020). These individuals experience certain characteristic barriers to smoking cessation. Compared to smokers without MDD, they tend to be more likely to smoke heavily, to experience greater dependence on smoking, and to consider smoking to be more rewarding than other activities; it may thus be unsurprising that smokers with MDD experience more severe withdrawal symptoms (Breslau, Kilbey, and Andreski 1992; Spring, Pingitore, and McChargue 2003; Weinberger, Desai, and McKee 2010; Lyons et al. 2008). Smoking relapse is also associated with lower experience of reward and cognition, both of which tend to be impaired among those diagnosed with MDD (Leventhal et al. 2009; Cook et al. 2010; Patterson et al. 2009). Even past MDD adversely affects smoking cessation treatment outcomes (Hitsman, Papandonatos, et al. 2013).

Perhaps because of these challenges, individuals with MDD have typically been excluded from smoking treatment clinical trials (Hitsman et al. 2003; Hitsman, Papandonatos, et al. 2013; Talukder et al. 2023). Only six trials have explored smoking cessation in individuals with MDD (Evins et al. 2008; Anthenelli et al. 2013; Thorsteinsson et al. 2001; Hall et al. 2006; Minami et al. 2022; Hitsman et al. 2023), two of which had sample sizes of fewer than 50 participants (Thorsteinsson et al. 2001; Minami et al. 2022).

Additional research evaluating approaches to smoking cessation in this population is necessary. One such approach is treatment with varenicline, a pharmaceutical intervention shown to lessen cravings, withdrawal, withdrawal-related cognitive impairment, and reward from smoking (Patterson et al. 2009; Hitsman, Hogarth, et al. 2013; Perkins et al. 2010; Sofuoglu et al. 2009; West et al. 2008; McClure et al. 2012; Cinciripini et al. 2013). While cessation with varenicline was higher in smokers without any mental health disorders (Anthenelli et al. 2016), one trial of varenicline for individuals with MDD found greater abstinence versus placebo at 52 weeks (28.5% vs. 17.5%) (Anthenelli et al. 2013). However, individuals with mental health disorders, including MDD, are more likely to be prescribed nicotine replacement therapy, a comparatively less effective therapy, than varenicline (Anthenelli et al. 2016; Taylor et al. 2020). This hesitance to prescribing varenicline may stem from a prior boxed warning that, as of 2016, has been removed based on studies evincing the safety of varenicline for individuals with and without mental health disorders (Anthenelli et al. 2016).

The data in our study is derived from a recent randomized, placebo-controlled trial which examined whether the effectiveness of varenicline for smoking cessation in adults with current or past MDD is enhanced by behavioral activation for smoking cessation (BASC) (Hitsman et al. 2023). Behavioral activation (BA) increases reward experience and decreases avoidance-based coping (35-37 Cuijpers, Van Straten, and Warmerdam 2007; Dimidjian et al. 2011; Hopko et al. 2003; MacPherson et al. 2010). A prior pilot study indicated that individuals with elevated depression symptoms, but not MDD, had better cessation results at 26 weeks with BA and nicotine replacement therapy compared to those with standard behavioral treatment (ST) and nicotine replacement therapy (14.3% vs. 0%) (MacPherson et al. 2010).

The Hitsman study from which we draw our data uses a 2x2 factorial design, with 300 participants with past or present MDD treated, over 12 weeks, with BASC or ST alongside placebo or varenciline. Although the Hitsman study found that BASC did not outperform ST with respect to abstinence at 27 weeks, with or without varenicline, it did find that varenicline improved short- and longer-term abstinence compared to placebo (Hitsman et al. 2023). The dual goals of our analysis of the Hitsman et al. (2023) data will be to assess whether and how baseline variables (1) moderate behavioral treatment's effect on end-of-treatment (EOT) abstinence and (2) predict EOT abstinence, controlling for pharmaceutical and behavioral treatments.

In order to accomplish these dual goals, we use regularized linear models. Regularization, also known as shrinkage, reduces variance by fitting a model with all p predictors, with the estimated coefficients shrunken towards zero relative to the least square estimates (Hastie, Tibshirani, and Friedman (2009); pp. 204). We use this technique here because our goal can be understood as a variable selection problem. The Lasso method of regularization, which comepls some of the coefficients to be exactly equal to zero, can also be used for variable selection [Hastie, Tibshirani, and Friedman (2009); pp. 204, 219]. Best subset regression seeks the optimal subset of predictors by evaluating all possible combinations, thereby ensuring selection of the model with the lowest prediction error, although at a computational cost that increases exponentially with the number of predictors (Hazimeh and Mazumder 2020; Hastie, Tibshirani, and Wainwright 2015).

In contrast, L0+L2 regularization combines the sparsity-promoting L0 penalty, which counts the number of non-zero coefficients, with the L2 penalty that shrinks coefficients towards zero without zeroing them,

effectively balancing variable selection with the need to manage multicollinearity and enhance model accuracy (Hazimeh and Mazumder 2020; Hastie, Tibshirani, and Wainwright 2015; Paul 2024). The relaxed lasso, a modification of the Lasso method, initially applies the Lasso to determine a subset of variables by shrinking some coefficients to zero, then refits these selected variables with a reduced or absent Lasso penalty, potentially reducing bias while retaining the variable selection advantage of the original Lasso approach (Meinshausen 2007). L0+L2 and relaxed Lasso are considered the best trade-offs between variable selection and goodness of fit [Paul (2024); hazimeh2020fast]. Best subset, L0+L2, and relaxed Lasso are more computationally difficult than standard Lasso.

Another important extension of the Lasso regularization technique are those techniques which allow for specification of groups, order, or structure within the covariates such that penalties are applied with respect to the structure rather than individual covariates independently. These techniques include hierarchical Lasso (Bien, Taylor, and Tibshirani 2013), group Lasso [Meier, Van De Geer, and Bühlmann (2008); simon2012standardization], and sparse-group Lasso (Simon et al. 2013). This structural approach is particularly valuable when dealing with features that have natural groupings or hierarchical relationships, such as we examining complex interaction terms. As with he extensions of Lasso mentioned above, these techniques are less computationally efficient than standard Lasso. For this reason we opt to focus on application of the standard Lasso and leave extensions to modified Lasso regressions to future work.

Methods

Variables

First, we note that all covariates, other than abstinence (abst), are baseline variables. The following variables are binary: pharmacotherapy (Var); psychotherapy (BA); sex (sex_ps); indicators of whether the participant identifies as non-Hispanic white, Black, and/or Hispanic (NHW, Black, and Hisp); whether the individual smokes within five minutes of waking up (ftcd.5.mins); other lifetime DSM-5 diagnosis (otherdiag); whether the participant takes antidepressant medication (antidepmed); current or past MDD (mde_curr); and exclusive use of methylated cigarettes (Only.Menthol). The numeric variables are age (age_ps); cigarettes per day (cpd_ps); and Nicotine Metabolism Ratio (NMR). All remaining variables are ordinal. However, we treat income (inc) and education (edu) as ordinal, but (as we discuss below) treat the following variables as numeric: FTCD score (ftcd_score); bdi_score_pq1; cigarette reward value (crv_total_pg1); substitute reinforcer score (hedonsum_n_pq1); complementary reinforcer score (hedonsum_y_pq1); anhedonia (shaps_score_pg1); and readiness to quit smoking (readiness).

The ftcd_score is the participant's score on the Fagerstrom Test for Cigarette Dependence, a six-item survey intended to evaluate the quantity of cigarette consumption, dependence, and compulsion to smoke; answers are scored and summed to yield a total score of 0-10, with higher scores indicating a greater physical dependence on nicotine (Fagerström 2011). The bdi_score_pq1 is the participant's score on the Beck Depression Inventory, or BDI-II, a 21-item survey scored from 0 to 63 measuring the severity of depression, with higher scores indicating greater severity (Beck, Steer, and Brown 1996).

The crv_total_pq1 score measures the participant's score on a questionnaire measuring preference for smoking over other traditionally rewarding activities, measured on a scale of 0 to 15, where 1 point is added for each time the participant chooses smoking (Spring, Pingitore, and McChargue 2003). Substitute and complimentary reinforcer scores (hedonsum_n_pq1 and hedonsum_y_pg1) come from a participant's score of the cross-product of frequency (measured from 0 to 2) and level of enjoyableness (0 to 2) for a 45-item version of the Pleasant Events Schedule (MacPhillamy and Lewinsohn 1982); based

on the participant's report of whether an event is or is not associated with smoking, it is designated a complementary or substitute reinforcer, the cross products of which are summed.

Anhedonia (shaps_score_pq1) is assessed with the 14-item Snaith-Hamilton Pleasure Scale (SHAPS), where 14 statements are ranked on a 4-point Likert scale, with higher scores indicating greater enjoyment of typically rewarding experiences (Snaith et al. 1995). Nicotine metabolism ratio, otherwise known as nicotine metabolite ratio (NMR), is calculated as the ratio of 3'hydroxycotinine (3HC) to cotinine; NMR is a biomarker where higher NMR is associated with faster metabolism of nicotine (Siegel et al. 2020).

Exploratory Data Analysis

The original paper uses a 2x2 factorial design. However, we choose to keep the treatment variables separate because the sample size is very small and further reducing the sample size to the four groups at issue would significantly limit the Lasso's ability to fit the data. That the 2x2 factorial design is not necessary to answer the research question validates our choice.

In addition to summary statistics available in Table 1 and the correlation matrix, we also inspect univariate histograms (omitted for space) for all variables. This reveals one non-normal variable, NMR, for which we consider transformations as noted below. Bivariate relationships are explored in Figure 1. Additionally we examine the distribution and association of all variables between levels of abst, BA, and Var (tables omitted for space).

When dividing the sample for each variable by abst we see that there is a significant difference between those who abstain and those who do no in the Var. This is because of the noted effectiveness of the treatment Var. We also observe marginal significance in the variable ftcd_score with abstainers having lower baseline scores. This could be a confounder, but makes logical sense as higher ftcd_score indicates greater dependency which would make it more difficult to abstain. There are no other significant differences in variables between groups of abst. Finally, when dividing the sample for each variable by BA we see that there are no significant differences in variables between groups of BA. Lastly, when dividing the sample for each variable by Var we see one significant difference in abst, essentially a mirror image of the difference discussed prior.

We note that certain survey variables, specifically ftcd_score, crv_total_pq1, readiness, shaps_score_pq1, hedonsum_y_pq1, and hedonsum_n_pq1 are ordinal but will be treated here as either numeric integers or continuous for the purpose of the modeling. This presents a limitation in that we are treating ordinal variables as evenly spaced. Doing so is more or less justifiable for different variables. For example, we are more justified in treating hedonsum_y_pq1 and hedonsum_n_pq1 as continuous, given that each score is made up of the product of two ordinal scales; by using the cross-product, the study authors have made some assumptions about relative scale that obfuscates the ordinal nature of the original.

Nevertheless, treating these variables as ordinal is untenable here, as it would make individual cell sizes incredibly small and lead to parameter proliferation in modeling. Another potential solution would be grouping ordinal variables into discernible levels, as with inc, discussed below, but this would take an in-depth understanding of the meaning and spacing for each score that we do not have at present. Said another way, grouping the variables without fully understanding how relative distance between ordinal levels is expressed would lead to our making similar assumptions about the spacing between levels as we make in treating the variables as continuous. We note this is consistent with the handling of survey score variables in Table 1 of the original paper.

To ameliorate the potential loss of accurate fit from treating ordinal variables as numeric, we use polynomial fit for each variable, allowing non-linearities between the log odds ratio for these variables and

the outcome. The default contrast handling for ordinal covariates in R is a polynomial contrast. Applying the polynomial score transformation approximates this relationship, without incurring the cost of a parameter for all but one level of the variable. We note that this polynomial relationship is important to the predictive power of the model. Further, these polynomial terms allow us to model and interpret predictions for the outcome across the full scale of ordinal covariates even when that relationship is non-linear. Future work could examine fitting a model without these polynomial terms, which would trade interpretability for parsimony.

Table 1: Summary of Variables

Characteristic	Overall n = 300	BASC + placebo n = 68	$\begin{array}{c} \mathrm{BASC} + \\ \mathrm{varenicline} \ \mathrm{n} = \\ 83 \end{array}$	ST + placebo n = 68	ST + varenicline $n = $ 81	
age_ps	50.0 (12.6)	50.7 (13.5)	50.3 (13.2)	50.3 (10.8)	48.7 (12.7)	
sex_ps						
Male	$135.0 \ (45.0\%)$	30.0 (44.1%)	$39.0 \ (47.0\%)$	29.0~(42.6%)	37.0 (45.7%)	
Female	165.0~(55.0%)	38.0~(55.9%)	44.0~(53.0%)	39.0~(57.4%)	44.0 (54.3%)	
NHW	$105.0 \ (35.0\%)$	24.0 (35.3%)	34.0~(41.0%)	22.0 (32.4%)	25.0 (30.9%)	
Black	157.0 (52.3%)	37.0 (54.4%)	37.0 (44.6%)	40.0 (58.8%)	43.0 (53.1%)	
Hisp	18.0 (6.0%)	5.0 (7.4%)	4.0 (4.8%)	4.0 (5.9%)	5.0 (6.2%)	
inc	,	,	,	,	,	
Less than \$20,000	110.0 (37.0%)	25.0 (37.3%)	30.0 (36.6%)	26.0 (38.2%)	29.0 (36.3%)	
\$20,000-35,000	68.0 (22.9%)	16.0 (23.9%)	17.0 (20.7%)	14.0 (20.6%)	21.0 (26.3%)	
\$35,001-50,000	46.0 (15.5%)	8.0 (11.9%)	13.0 (15.9%)	14.0 (20.6%)	11.0 (13.8%)	
\$50,001-75,000	38.0 (12.8%)	12.0 (17.9%)	12.0 (14.6%)	8.0 (11.8%)	6.0 (7.5%)	
More than \$75,000	35.0 (11.8%)	6.0 (9.0%)	10.0 (12.2%)	6.0 (8.8%)	13.0 (16.3%)	
edu	(, , ,	(11)	()	((, , , ,	
Grade School	1.0~(0.3%)	1.0~(1.5%)	0.0~(0.0%)	0.0~(0.0%)	0.0~(0.0%)	
Some High School	16.0 (5.3%)	3.0 (4.4%)	7.0 (8.4%)	2.0 (2.9%)	4.0 (4.9%)	
High School Graduate/GED	76.0 (25.3%)	23.0 (33.8%)	15.0 (18.1%)	11.0 (16.2%)	27.0 (33.3%)	
Some College/Technical School	116.0 (38.7%)	22.0 (32.4%)	32.0 (38.6%)	38.0 (55.9%)	24.0 (29.6%)	
College Graduate	91.0 (30.3%)	19.0 (27.9%)	29.0 (34.9%)	17.0 (25.0%)	26.0 (32.1%)	
ftcd_score	5.2 (2.1)	5.3 (2.0)	5.1 (2.3)	5.4 (2.1)	5.2 (2.1)	
ftcd.5.mins	138.0 (46.0%)	32.0 (47.1%)	33.0 (39.8%)	35.0 (51.5%)	38.0 (46.9%)	
readiness	6.8 (1.2)	6.8 (1.4)	6.7 (1.2)	7.0 (1.3)	6.7 (1.1)	
cpd_ps	15.1 (7.9)	15.6 (9.1)	15.5 (8.5)	15.0(7.2)	14.4 (6.6)	
crv_total_pq1	7.2(3.7)	7.4 (3.8)	7.2(3.9)	7.0 (3.7)	7.1(3.5)	
$hedonsum_n_pq1$	22.6 (19.6)	23.2(20.3)	22.9 (19.0)	20.8 (20.1)	$23.4\ (19.5)$	
hedonsum_y_pq1	25.4 (19.4)	27.7 (21.5)	22.4 (17.0)	27.4 (19.9)	25.0 (19.4)	
otherdiag	133.0 (44.3%)	35.0 (51.5%)	30.0 (36.1%)	28.0 (41.2%)	40.0 (49.4%)	
antidepmed	82.0 (27.3%)	28.0 (41.2%)	24.0 (28.9%)	15.0 (22.1%)	15.0 (18.5%)	
mde_curr						
Past	153.0~(51.0%)	36.0~(52.9%)	43.0~(51.8%)	37.0~(54.4%)	37.0~(45.7%)	
Current	147.0 (49.0%)	32.0 (47.1%)	40.0 (48.2%)	31.0 (45.6%)	44.0 (54.3%)	
NMR	0.4 (0.2)	0.3(0.2)	0.4(0.2)	0.4 (0.3)	0.4(0.2)	
Only.Menthol	178.0 (59.7%)	40.0 (58.8%)	48.0 (58.5%)	43.0 (64.2%)	47.0 (58.0%)	

Note:

Mean (SD); n (%)

Other notable decisions include omission of Hisp due to insufficient sample size (18 individuals), which is a limitation of our analysis. We considered taking the three race and ethnicity variables NHW, Black, and Hisp and producing a single race plus ethnicity variable with mutually exclusive groups for non-Hispanic white, non-Hispanic Black, Hispanic, and Other. However because there are only 18 individuals noted as Hisp (and only two of those individuals are Black), this hypothetical combined race plus ethnicity variable would've suffered from the same cell size issue as other factors with many levels.

We further note that based on our correlation matrix there is a very high correlation (well over 85%) between NHW and Black. This issue combined with the issue noted previously lead us to also drop the NHW variable. We also note that use of only menthol cigarettes is highly correlated with both NHW, Black, inc, and edu. This is a concern, but as menthol cigarette use may be a unique trait and we are conducting regularized regression, we elect to leave this variable in the model and allow the penalty to aid our choice.

TODO: We conclude by grouping levels of edu and inc to limit parameter proliferation and allow for estimation and model convergence, given that Table 1 shows that there is insufficient sample within each level when not grouped. And, to take the log of the one true continuous variable, NMR, to encourage normality. Regarding the last decision, we do not assume normality, but note that normalizing transformations can encourage convergence and simplify the loss landscape.

Finally, we note that there is a minor class imbalance issue ($\sim 2.1:10$). The outcome is somewhat rare, and this could lead to model fitting issues. Correcting for this class imbalance is a potential area for improvement and a limitation.

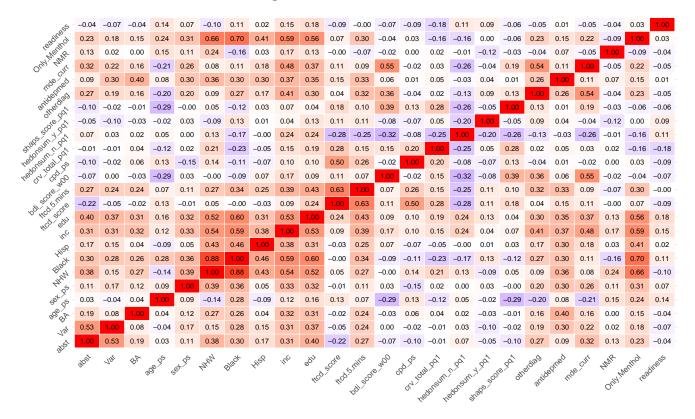


Figure 1: Correlation Matrix

Missingness

We examined the amount of missing data by variable and by sample. The most missing data in any single record is two missing variables. There are seven variables missing data. The most missing data exists in NMR with 21 missing values (7%). There are 241 complete cases, which would reduce our sample by 59 records. This strongly suggests the need for imputation. After inspecting the data, we ran Little's test for MCAR. The null hypothesis for this test is that the data are not MCAR. The p-value was over 0.05, so we cannot reject the null hypothesis. We conclude that there is evidence that these data are

missing completely at random. Missing data in covariates will be imputed during the bootstrap process to preserve the already limited sample available.

Modeling

We use a Lasso model to answer both questions at issue. To evaluate baseline variables that predict abst, we construct a Lasso model that includes all main effects and polynomial terms for score variables. To evaluate baseline moderators of the effect of BA on abst, we also use a Lasso model, but the model that we use this time includes all main effects and polynomial terms of scores, as well as interactions of those terms with BA. We note that there is still the assumption that there is a linear relationship between the log odds of predictors and the outcome, but not an assumption of linearity between the predictors and the outcome itself.

We choose a Lasso model due to its constraints on potential values of the coefficients, introducing desirable bias to the model when performed correctly, which prevent overfitting. We choose not to use L0, L0+L2, or relaxed Lasso: while all three are computationally more difficult and would have more convergence issues than Lasso, the former two also have a harsher penalty (Hazimeh and Mazumder 2020; Hastie, Tibshirani, and Wainwright 2015; Meinshausen 2007).

First, we perform an 80/20 validation training split, where each split has the same proportion of positive outcomes (where abst=1). We proceed with the bootstrap of the training data: first, through a bootstrap re-sample of the data, then imputing missing data, and by estimating our Lasso on the imputed bootstrap data as many times as necessary. Coefficients are pooled and confidence intervals are estimated. Bootstrap is used to stabilize estimates due to volatility caused by low sample size and to estimate confidence intervals for coefficients.

After the estimates are derived from the bootstrap procedure, we evaluate the model's performance using the validation data. We tested the model's performance using the pooled estimates on validation data in order to assess calibration and discrimination. For the former, we use calibration plots comparing the model's abstinence predictions to the study's actual results. For the latter, we use AUC and ROC to test whether the model could correctly identify participants who were or were not abstinent.

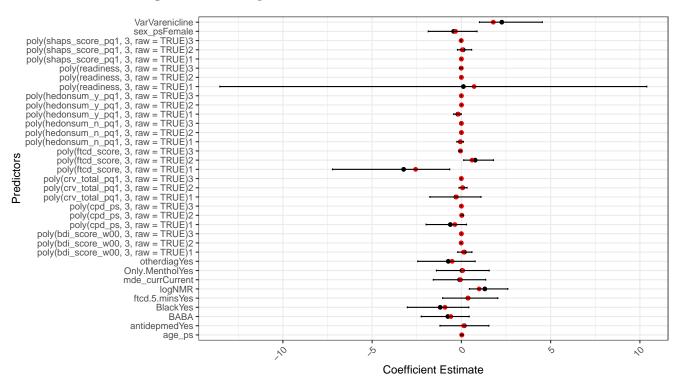
TODO For the main effects model, enforcement of additional sparsity beyond the Lasso's inherent variable selection was unnecessary, as the number of parameters relative to sample size did not suggest overfitting. However, the moderator model, which included interaction terms with BA treatment, presented a higher risk of overfitting due to the substantially increased number of parameters. Therefore, we implemented additional sparsity criteria for the moderator model: coefficients were retained in the final model only if they were consistently selected (non-zero) across a high proportion of bootstrap iterations (threshold = 0.90). This approach helps prevent overfitting by ensuring that selected moderators demonstrate robust relationships with the outcome across multiple bootstrap samples, rather than capturing spurious associations that might arise from the increased model complexity introduced by interaction terms.

Results

Baseline Variables Predict Abstinence

Results are presented for bootstrapped Lasso regression on outcome abstinence, including main effects of baseline covariates and controlling for other treatments. Only coefficients with confidence intervals not containing zero are presented in the table of results (noted as significant).

Figure 2: Bootstrap Confidence Intervals for Lasso Coefficients



There are four significant baseline predictors of abstinence: ftcd_score, Var, hedonsum_y_pq1, and logNMR. Varenicline treatment showed a strong positive association with abstinence TODO (OR = 10.84, 95% CI: 1.22-4.11), with participants receiving varenicline having nearly 11 times higher odds of achieving abstinence compared to those receiving placebo, consistent with prior literature on varenicline's efficacy. Additionally, nicotine metabolism rate demonstrated a positive relationship with abstinence outcomes, with each unit increase in log(NMR) associated with 4.28 times higher odds of abstinence TODO (95% CI: 0.63-2.09). That logNMR predicts abstinence is also understandable. As noted above, NMR indicates faster or slower metabolism of nicotine. Among other potential explanations for this variable's predictive value, individuals with faster nicotine metabolism tend to experience more intense withdrawal symptoms (Liakoni et al. 2019), as well as greater physical dependence and reward (Sofuoglu et al. 2012), presumably making abstinence more difficult. This finding regarding NMR is particularly noteworthy as it appears to diverge from some previous research suggesting faster metabolizers typically experience greater difficulty achieving cessation, though the relationship between metabolism and cessation outcomes is known to be complex and may be treatment-dependent.

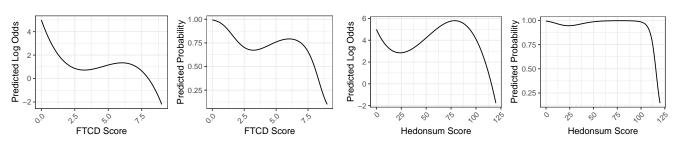
Table 2: Lasso Regression Coefficient Estimates

Predictor	Estimate (Primary)	Estimate (Mean)	Estimate (Median)	Odds Ratio	Lower 2.5%	Upper 97.5%	Proportion Non-Zero	Sig.
VarVarenicline	1.786	2.389	2.264	5.965	1.015	4.535	1.000	Yes
$poly(ftcd_score, 3, raw = TRUE)1$	-2.564	-3.424	-3.235	0.077	-7.220	-0.655	0.999	Yes
$poly(ftcd_score, 3, raw = TRUE)2$	0.600	0.822	0.772	1.822	0.132	1.795	0.998	Yes
$poly(ftcd_score, 3, raw = TRUE)3$	-0.043	-0.060	-0.056	0.958	-0.134	-0.010	0.999	Yes
poly(hedonsum_y_pq1, 3, raw = TRUE)1	-0.166	-0.205	-0.201	0.847	-0.431	-0.008	0.999	Yes
$\log NMR$	0.996	1.367	1.314	2.706	0.449	2.598	1.000	Yes

The polynomial variables are difficult to interpret in the same efficient manner as the continuous logNMR or binary Var, therefore we produce plots to enhance our understanding. The FTCD score (ftcd_score) and complementary reinforcer score (hedonsum_y_pq1) both demonstrated significant non-linear relationships with abstinence. As visualized in Figure 3, the relationship between FTCD score and abstinence probability follows a complex cubic pattern, with the highest probability of abstinence occurring at low levels of dependence and decreasing non-linearly as the score increases. Similarly, hedonsum_y_pq1 exhibited a non-linear relationship with abstinence (Figure 4), where the probability of abstinence decreased more steeply at higher levels of complementary reinforcement. These relationships between FTCD score or complementary reinforcement score and the outcome are produced while holding all other variables at zero (for numeric variables) or their reference level (for categorical variables).

As discussed in greater detail above, a higher score for complementary reinforcers denotes greater frequency of and/or more enjoyment of activities associated by the participant with smoking. It makes intuitive sense that, as our results suggest, participants whose more frequent and/or more enjoyable pleasurable events with smoking would have a harder time quitting. For one thing, engaging in those frequent, pleasurable, and smoking-associated activities would likely lead them to wish to smoke. Moreover, they might have fewer opportunities to engage in pleasurable activities not associated with smoking, undermining their ability to find alternative sources of reward. These findings suggest that both nicotine dependence and the degree to which participants associate pleasurable activities with smoking have complex, rather than straightforward linear, relationships with abstention.

Figure 3: Relationship between FTCD Score and Figure 4: Relationship between Hedonsum Score Estimates and Estimates



Diagnostics

Figure 5: Lasso ROC / AUC Plot

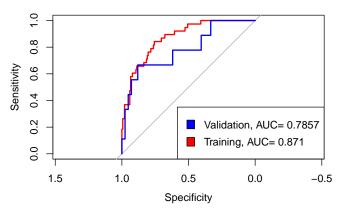
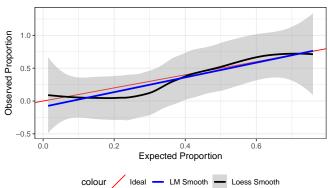


Figure 6: Lasso Calibration Plot: Validation Data



The model's discriminative ability was assessed using ROC curves and calibration plots (Figures 4 and 5). The Lasso model demonstrated good discriminative performance with an AUC of $TODO\ XXX$ on

the validation set, though some overfitting is suggested by the higher training AUC of *TODO XXX*. The calibration plot reveals generally good agreement between predicted and observed probabilities at lower ranges, but shows increasing uncertainty at higher probability ranges, as evidenced by the widening confidence bands around the Loess curve. This pattern is not unexpected given the class imbalance in our data. The overall calibration suggests the model provides reasonably reliable probability estimates, especially in the more commonly observed lower probability ranges.

Baseline Variables as Moderators of BA

Results are presented for bootstrapped Lasso regression on the outcome abstinence, with main effects included and unpenalized. Interactions of baseline covariates with BA are included and penalized, allowing the Lasso to select the interaction terms of consequence. Only coefficients with confidence intervals not containing zero are presented in the table of results (noted as significant).

Our moderator analysis revealed that anhedonia shaps_score_pq1 significantly moderated the effect of BA treatment on abstinence outcomes TODO (Table 3). This relationship was markedly non-linear, as visualized in TODO Figure 6. The diverging curves for standard treatment versus BA demonstrate that the effect of BA on abstinence varies substantially based on baseline anhedonia levels. For participants with higher SHAPS scores (indicating higher anhedonia), BA and standard treatment showed similar effectiveness. However, as baseline anhedonia decreased, BA demonstrated increasingly superior outcomes compared to standard treatment, suggesting that BA may be particularly beneficial for individuals experiencing lower levels of anhedonia. This finding is somewhat paradoxical given BA's proposed mechanism of action in increasing reward experience and decreasing avoidance-based coping. We might expect those with higher anhedonia to do better with BA, but we observe the opposite.

The model also confirmed the robust effect of varenicline (OR = 816.00, 95% CI: 3.22-15.39), though the wide confidence interval suggests considerable uncertainty in the effect size estimate.

Table 3: Lasso Regression Coefficient Estimates

Predictor	Estimate (Primary)	Estimate (Mean)	Estimate (Median)	Odds Ratio	Lower 2.5%	Upper 97.5%	Proportion Non-Zero	Sig.
VarVarenicline	2.317	8.989	6.939	10.148	2.442	27.204	1	Yes

Diagnostics

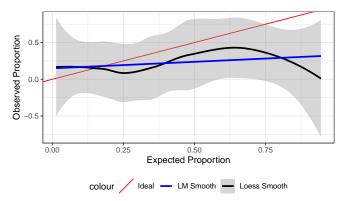
Figure 7: Lasso ROC / AUC Plot

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Figure 8: Lasso Calibration Plot: Validation Data



TODO The diagnostic plots for the moderator analysis (Figures 7 and 8) suggest more modest model performance compared to our main effects model. The ROC curves show fair discriminative ability with an AUC of 0.59 on the validation set and 0.67 on the training set. This decreased performance relative to our previous model likely reflects the increased complexity introduced by interaction terms and the inherent difficulty in predicting treatment effect heterogeneity especially in small samples. The calibration plot reveals substantial deviation from the ideal diagonal, with the model showing a tendency toward overoptimistic predictions in the mid-range probabilities and under-prediction at higher probabilities. The wide confidence bands around the Loess curve indicate considerable uncertainty in these predictions. These diagnostics suggest that while the model successfully identified a meaningful treatment-moderator interaction with anhedonia, its overall predictive accuracy is limited and its probability estimates should be interpreted with caution.

Conclusion

In this reanalysis of the BASC-Varenicline trial data, we identified several important predictors of smoking cessation success among individuals with current or past MDD. Our primary analysis confirmed varenicline's strong positive effect on abstinence and revealed complex non-linear relationships between cessation success and baseline characteristics including nicotine dependence (FTCD score) and complementary reinforcement. Notably, higher nicotine metabolism rates were associated with improved cessation outcomes, a finding that warrants further investigation given its divergence from some previous research.

Several limitations of our analysis warrant discussion. First, our analytical approach was constrained by sample size limitations, which led to the exclusion of Hispanic ethnicity data due to insufficient representation (n=18) and necessitated the grouping of educational and income categories to ensure model convergence. Second, the class imbalance in our outcome (21.33% abstinent) posed challenges for model fitting and likely contributed to the decreased accuracy of predictions at higher probability ranges, particularly in our moderator analysis. Third, convergence issues stemming from our relatively small sample size and numerous dichotomous variables limited our ability to employ more sophisticated regularization approaches. Finally, despite doing 6,000 bootstrap iterations, if given more time larger bootstrap runs would be welcome. Future analyses with larger samples might benefit from exploring alternative methods such as L0 best subset selection, L0+L2 regularization, relaxed Lasso, group Lasso, or hierarchical Lasso, which could potentially offer improved variable selection and prediction accuracy.

Despite these limitations, our findings suggest that baseline characteristics, particularly anhedonia levels, could inform the personalization of smoking cessation treatments for individuals with current or past MDD. The identified moderating effect of anhedonia on BA treatment efficacy may be valuable for clinical decision-making, though the modest predictive performance of our moderator model suggests that additional research is needed to validate and refine these findings.

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Appendix I: Script Code

```
# --- Preamble ---
# Date of last update: Nov. 12, 2024
# R Version: 4.3.1
# Package Versions:
  tidyverse: 2.0.0
  knitr: 1.45
# kableExtra: 1.3.4
# ggplot2: 3.4.3
# naniar 1.0.0
  visdat 0.6.0
  car 3.1-2
#
#
  lme4 1.1-34
# ggpubr 0.6.0
   glmnet 4.1-8
#
# mice 3.16.0
#
  caret 6.0-94
# pROC 1.18.4
  gt 0.9.0
#
  gtsummary 1.7.2
setwd("~/GitHub/smoking_cessation_proj")
# Knitr Engine Setup
knitr::opts_chunk$set(message=F,
                     warning=F,
                     error=F,
                      echo=F,
                      fig.pos = "H" ,
                      fig.align = 'center')
# Packages
options(kableExtra.latex.load_packages = FALSE) # Required to avoid floatrow error
library(knitr)
library(kableExtra)
library(ggplot2)
library(naniar) # For mcar_test()
library(visdat) # For vis_dat()
library(tidyverse)
library(car) # For qqPlot(), vif()
library(lme4)
library(lmerTest) # Satterthwaite approximation for computing p-values on lme4
library(ggpubr)
library(glmnet)
library(mice)
library(caret)
library(pROC)
```

```
library(gtsummary)
library(gt)
source("_helpers.R")
data <- read.csv("data/project2.csv", comment.char="#")</pre>
# Convert variables
data <- data %>%
  mutate(
    abst = factor(abst, levels = c(0, 1), labels = c("No", "Yes")),
    Var = factor(Var, levels = c(0, 1),
                         labels = c("Placebo", "Varenicline")),
    BA = factor(BA, levels = c(0, 1), labels = c("Standard", "BA")),
    age_ps = as.numeric(age_ps),
    sex_ps = factor(sex_ps, levels = c(1, 2), labels = c("Male", "Female")),
    NHW = factor(NHW, levels = c(0, 1), labels = c("No", "Yes")),
    Black = factor(Black, levels = c(0, 1), labels = c("No", "Yes")),
    Hisp = factor(Hisp, levels = c(0, 1), labels = c("No", "Yes")),
    inc = factor(inc, levels = 1:5,
                 labels = c("Less than $20,000",
                            "$20,000-35,000",
                            "$35,001-50,000",
                            "$50,001-75,000",
                            "More than $75,000"), ordered = TRUE),
    edu = factor(edu, levels = 1:5,
                 labels = c("Grade School",
                            "Some High School",
                            "High School Graduate/GED",
                            "Some College/Technical School",
                            "College Graduate"), ordered = TRUE),
    ftcd_score = as.integer(ftcd_score),
    ftcd.5.mins = factor(ftcd.5.mins, levels = c(0, 1), labels = c("No", "Yes")),
    bdi_score_w00 = as.integer(bdi_score_w00),
    cpd_ps = as.integer(cpd_ps),
    crv_total_pq1 = as.integer(crv_total_pq1),
    hedonsum_n_pq1 = as.integer(hedonsum_n_pq1),
    hedonsum_y_pq1 = as.integer(hedonsum_y_pq1),
    shaps_score_pq1 = as.integer(shaps_score_pq1),
    otherdiag = factor(otherdiag, levels = c(0, 1), labels = c("No", "Yes")),
    antidepmed = factor(antidepmed, levels = c(0, 1), labels = c("No", "Yes")),
    mde_curr = factor(mde_curr, levels = c(0, 1), labels = c("Past", "Current")),
    NMR = as.numeric(NMR),
    Only.Menthol = factor(Only.Menthol, levels = c(0, 1), labels = c("No", "Yes")),
    readiness = as.integer(readiness)
```

```
)
df_tbl <- data %>%
  mutate(
    treatment_arm = case_when(
      Var == "Placebo" & BA == "Standard" ~ "ST + placebo",
      Var == "Placebo" & BA == "BA" ~ "BASC + placebo",
      Var == "Varenicline" & BA == "Standard" ~ "ST + varenicline",
      Var == "Varenicline" & BA == "BA" ~ "BASC + varenicline"
    )
  )
# gtsummary table
tbl <- df_tbl %>%
  select(
    treatment_arm,
    age_ps,
    sex_ps,
    NHW,
    Black,
    Hisp,
    inc,
    edu,
    ftcd_score,
    ftcd.5.mins,
    readiness,
    cpd_ps,
    crv_total_pq1,
    hedonsum_n_pq1,
    hedonsum_y_pq1,
    otherdiag,
    antidepmed,
    mde_curr,
    NMR,
    Only.Menthol
  ) %>%
  tbl_summary(
    by = treatment_arm,
    missing = "no",
    type = list(readiness ~ "continuous"),
    statistic = list(
      all_continuous() ~ "{mean} ({sd})",
      all_categorical() ~ "{n} ({p}%)"
    ),
    digits = list(
     all_continuous() ~ 1,
     all_categorical() ~ 1
```

```
) %>%
  add overall() %>%
  # Note: the nice header work here doesn't work because we are forced to use
  # as_kable for rendering so we can control the width
  #modify_header(label = "**Characteristic**") %>%
  modify_header(label = "Characteristic") %>%
  #modify_spanning header(all_stat_cols() ~ "**Treatment Arm**") %>%
  modify_header( # To match paper columns
    all_stat_cols() ~ paste0(
      #"**{level}**\n",
      "{level}
      "n = \{n\}"
    )
  )
tbl <- tbl %>% as_kable(
  booktabs = T,
  longtable = T,
  escape = T,
  align = c('l','c','c','c','c','c')) %>%
  column_spec(1, width="4cm", latex_valign = "m") %>%
  column_spec(2, width="2cm", latex_valign = "m") %>%
  column_spec(3, width="2cm", latex_valign = "m") %>%
  column_spec(4, width="2cm", latex_valign = "m") %>%
  column_spec(5, width="2cm", latex_valign = "m") %>%
  column_spec(6, width="2cm", latex_valign = "m") %>%
  kable_styling(
    font_size = 8,
    latex_options = c(
    "repeat_header",
    'striped'),
    full_width = F,
    position = 'center'
  ) %>%
  footnote(general = "Mean (SD); n (%)", escape = T)
# tbl <- tbl %>%
    as_gt() %>%
    # cols_width( # Note: neither cols_width nore table.width work currently. cols_width
#
#
                  # works in gt tables but not gtsummary tables. table.width doesn't work
                  # for any LaTex/PDF Quarto docs. (12/13/24)
    #
#
       variable ~ "50pt",
#
    #
#
       var type ~ "50pt",
       var_label ~ "50pt",
#
       row type ~ "50pt",
      label ~ "50pt",
   #
#
#
       stat_0 ~ "50pt",
```

```
stat_1 ~ "50pt",
#
   # stat 2 ~ "50pt",
#
   # stat_3 ~ "50pt",
      stat_4 ~ "50pt"
#
  # "**Characteristic**` ~ "50pt" # Not an actual column, just a label
#
   # #starts_with("var") ~ "100pt"
   # #variable ~ px(100) # LaTeX doesn't like px()
    # ) %>%
# # tab_options(
       #table.font.size = "small" # Note: Doesn't currently work in PDF/LaTeX
       #table.width = "500pt" # Note: Doesn't currently work in PDF/LaTeX
# # ) %>%
#
   as_latex()
tbl
# Note: using tbl-cap rather than caption= in kbl() breaks repeated title is span page
# Table 1
summary_table(data[-1]) %>%
  kbl(#caption = "Summary of Variables", # Conflicts with Quarto referencing
      booktabs = T,
      longtable = T, # LONGTABLE
      escape = T,
      align = "c") %>%
  column_spec(1, width="2.2cm", latex_valign = "m") %>%
  column_spec(2, width="1.3cm", latex_valign = "m") %>%
  column_spec(3, width="6cm", latex_valign = "m") %>%
  column_spec(4, width="1.0cm", latex_valign = "m") %>%
  column_spec(5, width="1.0cm", latex_valign = "m") %>%
  column_spec(6, width="1.25cm", latex_valign = "m") %>%
  column_spec(7, width="1.25cm", latex_valign = "m") %>%
  kable_styling(
    font_size = 8, # Added for LONGTABLE
    latex_options = c(#'HOLD_position', # Removed for LONGTABLE
    #'scale_down', # Removed for LONGTABLE
    "repeat_header", # Added for LONGTABLE
    'striped'),
    full_width = F, # Note: TRUE does not work with LONGTABLE
    position = 'center'# Added for LONGTABLE
  ) %>%
  footnote(general = "Shapiro-Wilk test for normality;
             Grubb's test for outliers.", escape = F)
# Table 2
```

```
summary_table(data[-1], stratify_var = "abst") %>%
 kbl(
     booktabs = T,
     longtable = T, # LONGTABLE
     escape = T,
     align = "c") %>%
 column_spec(1, width="2.21cm", latex_valign = "m") %>%
 column spec(2, width="4cm", latex valign = "m") %>%
 column_spec(3, width="4cm", latex_valign = "m") %>%
 column_spec(4, width=".35cm", latex_valign = "m") %>%
 kable_styling(
   font size = 7.6, # Added for LONGTABLE
   latex_options = c(#'HOLD_position', # Removed for LONGTABLE
   #'scale_down', # Removed for LONGTABLE
    "repeat_header", # Added for LONGTABLE
    'striped'),
   full width = F, # Note: TRUE does not work with LONGTABLE
   position = 'center'# Added for LONGTABLE
 ) %>%
 footnote(general = "ns = P > 0.05,
          * = P   10.05,
          ** = P  (0.01,
          *** = P  (0.001,
          **** = P $ / \leq 0.0001
           ", escape = F) %>%
 footnote(general = "Kruskal-Wallis test for continuous variables,
          Chi-Square test for categorical variables.
          Bonferroni correction applied.", escape = F)
# Table 2
summary_table(data[-1], stratify_var = "BA") %>%
     booktabs = T,
     longtable = T, # LONGTABLE
     escape = T,
     align = "c") %>%
 column_spec(1, width="2.21cm", latex_valign = "m") %>%
 column_spec(2, width="4cm", latex_valign = "m") %>%
 column_spec(3, width="4cm", latex_valign = "m") %>%
 column_spec(4, width=".35cm", latex_valign = "m") %>%
 kable_styling(
   font_size = 7.6, # Added for LONGTABLE
   latex_options = c(#'HOLD_position', # Removed for LONGTABLE
   #'scale_down', # Removed for LONGTABLE
   "repeat_header", # Added for LONGTABLE
    'striped'),
   full width = F, # Note: TRUE does not work with LONGTABLE
   position = 'center'# Added for LONGTABLE
 ) %>%
```

```
footnote(general = "ns = P > 0.05,
           * = P   (0.05,
          ** = P  (0.01,
          *** = P   (0.001,
          **** = P  (0.0001)
           ", escape = F) %>%
  footnote(general = "Kruskal-Wallis test for continuous variables,
          Chi-Square test for categorical variables.
          Bonferroni correction applied.", escape = F)
# Table 4
summary_table(data[-1], stratify_var = "Var") %>%
  kbl(
      booktabs = T,
      longtable = T, # LONGTABLE
      escape = T,
      align = "c") %>%
  column_spec(1, width="2.21cm", latex_valign = "m") %>%
  column_spec(2, width="4cm", latex_valign = "m") %>%
  column_spec(3, width="4cm", latex_valign = "m") %>%
  column_spec(4, width=".35cm", latex_valign = "m") %>%
  kable_styling(
    font_size = 7.6, # Added for LONGTABLE
   latex_options = c(#'HOLD_position', # Removed for LONGTABLE
    #'scale_down', # Removed for LONGTABLE
    "repeat_header", # Added for LONGTABLE
    'striped'),
   full_width = F, # Note: TRUE does not work with LONGTABLE
    position = 'center'# Added for LONGTABLE
  ) %>%
  footnote(general = "ns = P > 0.05,
           * = P  (0.05,
          ** = P  (0.01,
          *** = P   (0.001,
          **** = P  (0.0001)
           ", escape = F) %>%
  footnote(general = "Kruskal-Wallis test for continuous variables,
          Chi-Square test for categorical variables.
          Bonferroni correction applied.", escape = F)
# Histograms of variable distributions
# Identify numeric columns
numeric_cols <- sapply(data, is.numeric)</pre>
# Create histograms for each numeric column
for (col in names(data)[numeric cols]) {
  hist(data[[col]], main = paste("Histogram of", col), xlab = col)
}
```

```
# Generate psuedo correlation matrix
psuedo_cor_matrix <- psuedo_cor_mat(data[-1])</pre>
# Plot the heatmap (with variable names and values)
ggplot(melt(psuedo\_cor\_matrix), aes(x = Var2, y = Var1, fill = value)) +
  geom_tile(color = "white") +
  geom_text(aes(label = sprintf("%.2f", value)), size = 2.8, color = "black") +
  scale_fill_gradient2(low = "blue",
                       high = "red",
                       mid = "white",
                       midpoint = 0,
                       limits = c(-1, 1),
                       space = "Lab",
                       name = "Correlation") +
  theme minimal() +
  labs(x = "", y = "") +
  theme(axis.title.x = element_blank(),
        axis.text.x = element_text(angle = 45, hjust = 1, size = 9),
        axis.ticks.x = element_blank(),
        axis.title.y = element_blank(),
        axis.text.y = element_text(angle = 45, hjust = 1, size = 9),
        legend.position="none") +
  coord_fixed(ratio = .55)
missing_by_variable <- data %>%
  summarise(across(everything(), ~ sum(is.na(.)))) %>%
  pivot_longer(cols = everything(), names_to = "Variable", values_to = "Missing_Count") %>%
  mutate(Missing_Percentage = round((Missing_Count / nrow(data)) * 100, 2))
missing_by_record <- data %>%
  mutate(Row = row_number()) %>%
  mutate(Missing_Count = rowSums(is.na(across(everything())))) %>%
  select(Row, Missing_Count)
total_complete_cases <- data %>%
  summarise(Complete_Cases = sum(complete.cases(.))) %>%
  pull(Complete_Cases)
# Test for MCAR
naniar::mcar_test(data)
# prep data for analysis
data <- data %>%
  mutate(abst = as.numeric(abst) - 1,
    edu = factor(recode_factor(edu,
                                "Grade School" = "High School or Less",
```

```
"Some High School" = "High School or Less",
                                "High School Graduate/GED" = "High School or Less"),
                 levels = c("High School or Less",
                             "Some College/Technical School",
                             "College Graduate"),
                 ordered = TRUE),
    inc = factor(recode_factor(inc,
                                "$50,001-75,000" = "More than $50,000",
                                "More than $75,000" = "More than $50,000"),
                 levels = c("Less than $20,000",
                             "$20,000-35,000",
                             "$35,001-50,000",
                             "More than $50,000"),
                 ordered = TRUE)
         )
data <- data %>%
  mutate(logNMR = log(NMR)) %>% # Toggle off to test model fit w/o transform
  select(-c(NMR, # Don't drop if toggle log(NMR)
            Hisp,
            NHW))
# --- Validation / Train split ---
set.seed(123)
split_indices <- createDataPartition(y = data$abst, p = 0.8, list = FALSE)</pre>
# split data training / validation sets
train_data <- data[split_indices, ]</pre>
validation_data <- data[-split_indices, ]</pre>
data <- train_data</pre>
#GOOD; Q1; baseline
# Def All Params
B <- 1000
              # num of bootstraps
            # num of multiple imputations per bootstrap
m <- 5
            # num of cv folds for cv.glmnet
poly_degree <- 3 # degree for polynomial terms, set to 1 to test model fit w/o poly
# remove id
data_complete <- data %>% select(-id)
# Flag predictor vars
# exclude 'abst' from predictors
predictor_vars <- setdiff(names(data_complete), c("abst"))</pre>
# Flag trt vars
treatment vars <- c("BA", "Var")</pre>
baseline_vars <- setdiff(predictor_vars, treatment_vars)</pre>
```

```
# Flag numeric and int baseline vars
num_baseline_vars <- baseline_vars[sapply(data_complete[baseline_vars],</pre>
                                             function(x) is.numeric(x) & !is.integer(x))]
non_binary_factor_vars <- baseline_vars[sapply(data_complete[baseline_vars],</pre>
                                                  function(x) is.integer(x))]
# Flag Binary baseline vars
binary_vars <- baseline_vars[sapply(data_complete[baseline_vars],</pre>
                                    function(x) length(unique(na.omit(x))) == 2)]
# Flag factor vars and store levels
factor_vars <- names(data_complete)[sapply(data_complete, is.factor)]</pre>
levels_list <- lapply(data_complete[, factor_vars, drop = FALSE], levels)</pre>
# --- Build Formula ---
# Main Effects
main effects <- paste("BA + Var +",</pre>
                       paste(c(
                          paste0("poly(", non binary factor vars,
                                 ", ", poly_degree, ", raw=TRUE)"),
                         num_baseline_vars,
                          binary_vars
                       ), collapse = " + "))
# Full Model Formula
full_formula <- as.formula(paste("abst ~", main_effects))</pre>
# fix factor levels in the entire dataset (ensure consistency) BUGFIX
if (length(factor_vars) > 0) {
  for (var in factor vars) {
    data_complete[[var]] <- factor(data_complete[[var]], levels = levels_list[[var]])</pre>
}
# Gen master model matrix
master_model_matrix <- model.matrix(full_formula, data = data_complete)</pre>
master_coef_names <- colnames(master_model_matrix)</pre>
total_coeffs <- length(master_coef_names)</pre>
# init storage for coefs
coef_matrix <- matrix(NA, nrow = B, ncol = total_coeffs)</pre>
colnames(coef_matrix) <- master_coef_names</pre>
# init object for nonzero coef indicator
nonzero matrix <- matrix(0, nrow = B, ncol = total coeffs)</pre>
colnames(nonzero_matrix) <- master_coef_names</pre>
```

```
# --- Main estimation and bootstrap loop ---
# --- Primary model fit on original data with imputation ---
# Initial imputation for primary fit
predictor_matrix <- make.predictorMatrix(data_complete)</pre>
predictor_matrix[, "abst"] <- 0</pre>
predictor_matrix["abst", ] <- 0</pre>
imp_primary <- mice(data_complete, m = m, printFlag = FALSE, seed = 123,</pre>
                    predictorMatrix = predictor_matrix, method = 'pmm')
# Stack imputations for primary fit
stacked_data_primary <- complete(imp_primary, action = "long", include = FALSE)
stacked_data_primary <- stacked_data_primary %>% dplyr::select(-.id, -.imp)
# Fix factor levels
if (length(factor_vars) > 0) {
  for (var in factor_vars) {
    stacked_data_primary[[var]] <- factor(stacked_data_primary[[var]],
                                          levels = levels_list[[var]])
  }
}
# Create model matrix for primary fit
model_data full <- model.matrix(full_formula, data = stacked_data_primary)</pre>
x_primary <- model_data_full[, -1]</pre>
y primary <- stacked data primary$abst
# Remove zero variance predictors and align columns
zero_var_cols <- apply(x_primary, 2, function(x) var(x) == 0)</pre>
if (any(zero_var_cols)) {
  x_primary <- x_primary[, !zero_var_cols]</pre>
  current_coef_names <- colnames(x_primary)</pre>
} else {
  current_coef_names <- colnames(x_primary)</pre>
}
# Align columns with master names
master_coef_names_no_intercept <- master_coef_names[-1]</pre>
missing cols <- setdiff(master_coef_names_no_intercept, current_coef_names)
if (length(missing_cols) > 0) {
  zeros matrix <- matrix(0, nrow = nrow(x primary), ncol = length(missing cols))
  colnames(zeros matrix) <- missing cols</pre>
  x_primary <- cbind(x_primary, zeros_matrix)</pre>
}
extra_cols <- setdiff(current_coef_names, master_coef_names_no_intercept)</pre>
if (length(extra_cols) > 0) {
```

```
x_primary <- x_primary[, !(colnames(x_primary) %in% extra_cols)]</pre>
}
x_primary <- x_primary[, master_coef_names_no_intercept]</pre>
# Fit primary Lasso model
cv_lasso_primary <- cv.glmnet(</pre>
  x = x_{primary}
  y = y_primary,
  family = "binomial",
  alpha = 1,
  standardize = TRUE,
  relax = FALSE
)
primary_fit <- glmnet(</pre>
  x = x_{primary}
  y = y_primary,
  family = "binomial",
  alpha = 1,
  lambda = cv_lasso_primary$lambda.min,
  standardize = TRUE,
  relax = FALSE
)
# Get aligned primary coefficients
primary_coef_values <- as.vector(coef(primary_fit))</pre>
primary_coef_names <- rownames(coef(primary_fit))</pre>
names(primary_coef_values) <- primary_coef_names</pre>
aligned_primary_coef <- setNames(rep(0, length(master_coef_names)), master_coef_names)
matched_primary <- names(primary_coef_values) %in% master_coef_names</pre>
aligned_primary_coef[names(primary_coef_values)[matched_primary]] <-</pre>
  primary_coef_values[matched_primary]
primary_nonzero <- abs(aligned_primary_coef) > 1e-8 # New
# --- Bootstrap loop for confidence intervals ---
coef_matrix <- matrix(NA, nrow = B, ncol = length(master_coef_names))</pre>
colnames(coef_matrix) <- master_coef_names</pre>
nonzero_matrix <- matrix(0, nrow = B, ncol = length(master_coef_names))</pre>
```

```
colnames(nonzero_matrix) <- master_coef_names</pre>
set.seed(1)
for (b in 1:B) {
  cat("Bootstrap iteration:", b, "of", B, "\n")
  bootstrap_sample <- data_complete %>%
    group_by(abst) %>%
    sample_frac(size = 1, replace = TRUE) %>%
    ungroup()
  predictor_matrix <- make.predictorMatrix(bootstrap_sample)</pre>
  predictor_matrix[, "abst"] <- 0</pre>
  predictor_matrix["abst", ] <- 0</pre>
  imp <- mice(bootstrap_sample, m = m, printFlag = FALSE, seed = b,</pre>
              predictorMatrix = predictor_matrix, method = 'pmm')
  stacked_data <- complete(imp, action = "long", include = FALSE)</pre>
  stacked_data <- stacked_data %>% dplyr::select(-.id, -.imp)
  if (length(factor_vars) > 0) {
    for (var in factor_vars) {
      stacked data[[var]] <- factor(stacked data[[var]], levels = levels_list[[var]])</pre>
    }
  }
  model_data_full <- model.matrix(full_formula, data = stacked_data)</pre>
  x <- model_data_full[, -1]
  y_impute <- stacked_data$abst</pre>
  zero_var_cols <- apply(x, \frac{2}{2}, function(x) var(x) == \frac{0}{2}
  if (any(zero_var_cols)) {
    x <- x[, !zero_var_cols]
    current_coef_names <- colnames(x)</pre>
  } else {
    current_coef_names <- colnames(x)</pre>
  }
  missing_cols <- setdiff(master_coef_names_no_intercept, current_coef_names)</pre>
  if (length(missing_cols) > 0) {
    zeros_matrix <- matrix(0, nrow = nrow(x), ncol = length(missing_cols))</pre>
    colnames(zeros_matrix) <- missing_cols</pre>
    x <- cbind(x, zeros_matrix)</pre>
  }
  extra_cols <- setdiff(current_coef_names, master_coef_names_no_intercept)</pre>
  if (length(extra cols) > 0) {
    x <- x[, !(colnames(x) %in% extra_cols)]</pre>
  }
```

```
x <- x[, master_coef_names_no_intercept]</pre>
  # Fit bootstrap model using same lambda as primary fit
  boot_fit <- tryCatch({</pre>
    glmnet(
      x = x
      y = y_impute,
      family = "binomial",
      alpha = 1,
      lambda = cv_lasso_primary$lambda.min,
      standardize = TRUE,
      relax = FALSE
    )
  }, error = function(e) {
    cat("Error in glmnet for bootstrap", b, ":", e$message, "\n")
    return(NULL)
  })
  if (is.null(boot_fit)) {
    next
  }
  coef_values <- as.vector(coef(boot_fit))</pre>
  coef_names <- rownames(coef(boot_fit))</pre>
  names(coef_values) <- coef_names</pre>
  aligned coef values <- setNames(rep(0, length(master coef names)), master coef names)
  matched <- names(coef_values) %in% master_coef_names</pre>
  aligned coef values [names (coef values) [matched]] <- coef values [matched]
  coef_matrix[b, ] <- aligned_coef_values</pre>
  nonzero_matrix[b, ] <- ifelse(aligned_coef_values != 0, 1, 0)</pre>
}
saveRDS(coef_matrix, file = "baseline_coef_CI-fix_6k.rds")
saveRDS(nonzero_matrix, file = "baseline_nonzero_CI-fix_6k.rds")
coef_matrix <- readRDS(file = "baseline_coef_CI-fix_6k.rds")</pre>
nonzero matrix <- readRDS(file = "baseline nonzero_CI-fix_6k.rds")</pre>
coef matrix[, !primary nonzero] <- 0</pre>
# --- Pool coefs ---
# identify bad runs
bad_runs <- apply(coef_matrix, 1, function(x) all(is.na(x)) | all(x == 0)) &</pre>
             apply(nonzero_matrix, 1, function(x) all(is.na(x)) | all(x == 0))
```

```
# rm bad runs from objects
coef_matrix <- coef_matrix[!bad_runs, ]</pre>
nonzero_matrix <- nonzero_matrix[!bad_runs, ]</pre>
# make coef data frame
coef_mean <- colMeans(coef_matrix, na.rm = TRUE)</pre>
coef_median <- apply(coef_matrix, 2, median, na.rm = TRUE)</pre>
coef_lower <- apply(coef_matrix, 2, quantile, probs = 0.025, na.rm = TRUE)</pre>
coef_upper <- apply(coef_matrix, 2, quantile, probs = 0.975, na.rm = TRUE)</pre>
proportion nonzero <- colSums(nonzero_matrix, na.rm = TRUE) / sum(nonzero_matrix[,1])
coef ci <- data.frame(</pre>
  Predictor = colnames(coef_matrix),
 Mean = coef mean,
 Median = coef_median,
 Lower_2.5 = coef_lower,
 Upper_97.5 = coef_upper,
 Proportion_Nonzero = proportion_nonzero
)
coef_ci$Primary_Estimate <- aligned_primary_coef</pre>
# plot the CIs
ggplot(coef_ci[-1,], aes(x = Predictor, y = Median)) +
  geom point() +
  geom_point(aes(y=Primary_Estimate), color = "red") +
  geom_errorbar(aes(ymin = Lower_2.5, ymax = Upper_97.5), width = 0.2) +
  coord flip() +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
    y = "Coefficient Estimate",
    x = "Predictors"
  )
# plot nonzero prop
ggplot(coef_ci, aes(x = Predictor, y = Proportion_Nonzero)) +
  geom_bar(stat = "identity", fill = "skyblue") +
  theme_bw() +
  labs(
    title = "Proportion of Bootstrap Samples with Non-Zero Coefficients",
    y = "Proportion",
    x = "Predictors"
```

```
# --- Placeholder for: Enforce Sparsity (not done for main effects model) ---
coef_matrix_sparse <- coef_matrix</pre>
coef_mean <- colMeans(coef_matrix_sparse, na.rm = TRUE)</pre>
coef_median <- apply(coef_matrix_sparse, 2, median, na.rm = TRUE)</pre>
coef_lower <- apply(coef_matrix_sparse, 2, quantile, probs = 0.025, na.rm = TRUE)</pre>
coef_upper <- apply(coef_matrix_sparse, 2, quantile, probs = 0.975, na.rm = TRUE)</pre>
proportion nonzero <- colSums(nonzero_matrix, na.rm = TRUE) / sum(nonzero_matrix[,1])
coef ci sparse <- data.frame(</pre>
  Predictor = colnames(coef_matrix_sparse),
  Primary Estimate = aligned primary coef,
 Mean = coef_mean,
 Median = coef_median,
 Lower_2.5 = coef_lower,
 Upper_97.5 = coef_upper,
  Proportion_Nonzero = proportion_nonzero
)
# Results Table
coef_ci_sparse <- coef_ci_sparse %>%
  mutate(
    #Odds_Ratio = exp(Median) # Odds Ratio
    Odds_Ratio = exp(Primary_Estimate) # Odds Ratio (now using main lasso est.)
  )
coef_ci_sparse <- coef_ci_sparse %>%
  mutate(
    Rounded_Lower_2.5 = round(Lower_2.5, 4),
    Rounded_Upper_97.5 = round(Upper_97.5, 4),
    # Determine significance
    Significant = ifelse(
      Rounded_Lower_2.5 > 0 | Rounded_Upper_97.5 < 0,</pre>
      "Yes",
      "No"
    )
  ) %>%
  select(-Rounded Lower 2.5, -Rounded Upper 97.5)
table_data <- coef_ci_sparse %>%
  select(
    Predictor,
   Primary_Estimate,
    Mean,
```

```
Median,
    Odds Ratio,
    Lower_2.5,
    Upper 97.5,
    Proportion_Nonzero,
    Significant
  ) %>%
  rename(
    "Estimate (Primary)" = Primary_Estimate,
    "Estimate (Mean)" = Mean,
    "Estimate (Median)" = Median,
    "Odds Ratio" = Odds_Ratio,
    "Lower 2.5\%" = Lower_2.5,
    "Upper 97.5%" = Upper_97.5,
    "Proportion Non-Zero" = Proportion_Nonzero,
        "Sig." = Significant
  )
table_data_significant <- table_data %>%
  filter(`Sig.` == "Yes")
table_data_significant %>%
  kbl(row.names = F,
    booktabs = TRUE,
    longtable = TRUE,
    escape = TRUE,
    align = "c",
    digits = 3,
    caption = "Lasso Regression Coefficient Estimates"
  ) %>%
  column spec(1, width = "3.2cm", latex valign = "m") %>%
  column_spec(2, width = "1.5cm", latex_valign = "m") %>%
  column_spec(3, width = "1.5cm", latex_valign = "m") %>%
  column_spec(4, width = "1.5cm", latex_valign = "m") %>%
  column_spec(5, width = "1.5cm", latex_valign = "m") %>%
  column_spec(6, width = "1.5cm", latex_valign = "m") %>%
  column_spec(7, width = "1.5cm", latex_valign = "m") %>%
  column_spec(8, width = "1.5cm", latex_valign = "m") %>%
  column_spec(9, width = ".5cm", latex_valign = "m") %>%
  kable_styling(
    font_size = 7.6,
    latex_options = c("repeat_header", "striped"),
    full_width = FALSE,
    position = "center"
  )
# FTCD
```

```
ftcd_coefs <- coef_ci[grep("poly\\(ftcd_score, 3, raw = TRUE\\)", coef_ci$Predictor), ]</pre>
ftcd_range <- seq(min(na.omit(data$ftcd_score)),</pre>
                   max(na.omit(data$ftcd_score)), length.out = 100)
# calc predicted log odds
predicted_log_odds <- coef_ci$Median[coef_ci$Predictor == "(Intercept)"] +</pre>
                      ftcd_coefs$Median[1] * ftcd_range +
                      ftcd_coefs$Median[2] * ftcd_range^2 +
                      ftcd_coefs$Median[3] * ftcd_range^3
# convert to probabilities
predicted_probs <- 1/(1 + exp(-predicted_log_odds))</pre>
plot_data <- data.frame(</pre>
  ftcd_score = ftcd_range,
  log_odds = predicted_log_odds,
  probability = predicted_probs
)
# plot log odds
p1 <- ggplot(plot_data, aes(x = ftcd_score, y = log_odds)) +
  geom_line() +
  theme bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(x = "FTCD Score",
       y = "Predicted Log Odds",
       title = "")
# plot probabilities
p2 <- ggplot(plot_data, aes(x = ftcd_score, y = probability)) +
  geom_line() +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(x = "FTCD Score",
       y = "Predicted Probability",
       title = "")
ftcd_plot <- ggarrange(</pre>
  p1,
  p2,
  ncol = 2,
  nrow = 1
)
```

```
print(ftcd_plot)
### Note: interesting dynamic where when B \leq 1000 this is no longer significant,
### but when B <- 6000 it is. Volitile results.
# Hedonsum
hedon_coefs <- coef_ci[grep("poly\\(hedonsum_y_pq1, 3, raw = TRUE\\)", coef_ci$Predictor), ]</pre>
hedon_range <- seq(min(na.omit(data$hedonsum_y_pq1)),
                    max(na.omit(data$hedonsum_y_pq1)), length.out = 100)
# calc predicted log odds
predicted_log_odds <- coef_ci$Median[coef_ci$Predictor == "(Intercept)"] +</pre>
                      hedon_coefs$Median[1] * hedon_range +
                      hedon_coefs$Median[2] * hedon_range^2 +
                      hedon_coefs$Median[3] * hedon_range^3
# convert to probabilities
predicted_probs <- 1/(1 + exp(-predicted_log_odds))</pre>
plot_data <- data.frame(</pre>
  hedonsum_score = hedon_range,
  log_odds = predicted_log_odds,
  probability = predicted_probs
)
# plot log odds
p1 <- ggplot(plot_data, aes(x = hedonsum_score, y = log_odds)) +
  geom line() +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(x = "Hedonsum Score",
       y = "Predicted Log Odds",
       title = "")
# plot probabilities
p2 <- ggplot(plot_data, aes(x = hedonsum_score, y = probability)) +</pre>
  geom_line() +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(x = "Hedonsum Score",
       y = "Predicted Probability",
       title = "")
hedon_plot <- ggarrange(</pre>
  p1,
  p2,
  ncol = 2,
```

```
nrow = 1
)
print(hedon_plot)
# --- Generate Predictions ---
# fix factor levels in the entire dataset (ensure consistency) BUGFIX
if (length(factor_vars) > 0) {
  for (var in factor_vars) {
    validation_data[[var]] <- factor(validation_data[[var]], levels = levels_list[[var]])</pre>
  }
}
# compute ROC for valid data
# prepare valid data
model data valid full <- model.matrix(full formula, data = validation data)
current_coef_names_valid <- colnames(model_data_valid_full) # align cols</pre>
missing cols <- setdiff(master_coef_names, current_coef_names_valid)
if (length(missing_cols) > 0) {
  zeros_matrix <- matrix(0,</pre>
                          nrow = nrow(model_data_valid_full),
                          ncol = length(missing_cols))
  colnames(zeros_matrix) <- missing_cols</pre>
  model_data_valid_full <- cbind(model_data_valid_full, zeros_matrix)</pre>
}
extra_cols <- setdiff(current_coef_names_valid, master_coef_names)</pre>
if (length(extra_cols) > 0) {
  model_data_valid_full <-</pre>
    model_data_valid_full[, !(colnames(model_data_valid_full) %in% extra_cols)]
}
model_data_valid_full <- model_data_valid_full[, master_coef_names] # reorder</pre>
#predictor_coefs <- coef_ci_sparse$Median</pre>
predictor_coefs <- coef_ci_sparse$Primary_Estimate # NOTE: changed from using $Median
names(predictor_coefs) <- coef_ci_sparse$Predictor</pre>
predictor_coefs <- predictor_coefs[master_coef_names] # ensure match</pre>
# predictions for valid data
linear_predictor <- as.vector(model_data_valid_full %*% predictor_coefs)</pre>
pred_prob <- 1 / (1 + exp(-linear_predictor))</pre>
# BUGFIX
if (length(validation_data) < length(pred_prob)) {</pre>
  validation_data <- validation_data[complete.cases(validation_data),]</pre>
}
validation_data$pred_prob <- pred_prob</pre>
```

```
# compute ROC for training data
# prepare training data
data_complete_cc <- data_complete[complete.cases(data_complete),]</pre>
model_data_train <- model.matrix(full_formula, data = data_complete_cc)</pre>
current_coef_names_train <- colnames(model_data_train)</pre>
missing cols_train <- setdiff(master_coef_names, current_coef_names_train)
if (length(missing_cols_train) > 0) {
  zeros matrix_train <- matrix(0, nrow = nrow(model_data_train),</pre>
                                ncol = length(missing_cols_train))
  colnames(zeros matrix train) <- missing cols train</pre>
  model_data_train <- cbind(model_data_train, zeros_matrix_train)</pre>
}
extra_cols_train <- setdiff(current_coef_names_train, master_coef_names)</pre>
if (length(extra_cols_train) > 0) {
  model_data_train <-</pre>
    model_data_train[, !(colnames(model_data_train) %in% extra_cols_train)]
}
model_data_train <- model_data_train[, master_coef_names]</pre>
# predictions for training data
linear_predictor_train <- as.vector(model_data_train %*% predictor_coefs)</pre>
pred_prob_train <- 1 / (1 + exp(-linear_predictor_train))</pre>
data_complete_cc$pred_prob <- pred_prob_train</pre>
# ROCs
roc_valid <- roc(validation_data$abst, validation_data$pred_prob)</pre>
roc_train <- roc(data_complete_cc$abst, data_complete_cc$pred_prob)</pre>
# plot ROC curves
plot(roc_train, col = "red", main = "")
plot(roc_valid, add = TRUE, col = "blue")
legend("bottomright",
       legend = c(paste("Validation, AUC=", round(roc_valid$auc, 4)),
                   paste("Training, AUC=", round(roc_train$auc, 4))),
       fill = c("blue", "red"))
# calc residuals
data_complete_cc$residuals <- data_complete_cc$abst - data_complete_cc$pred_prob
# plot residuals v. fitted
ggplot(data_complete_cc, aes(x = pred_prob, y = residuals)) +
  geom_point() +
  geom_hline(yintercept = 0, color = "red", linetype = "dashed") +
  labs(x = "Predicted Probability", y = "Residuals") +
  ggtitle("Residuals vs. Predicted Probabilities")
```

```
# Histogram of Residuals
hist(data_complete_cc$residuals, main = "Histogram of Residuals")
# Q-Q Plot of Residuals
qqnorm(data_complete_cc$residuals)
qqline(data_complete_cc$residuals)
# calibration plot
num_cuts <- 24
# calibration for validation data
test calib <- data.frame(</pre>
  prob = validation_data$pred_prob,
  bin = cut(validation data$pred prob, breaks = num cuts),
  class = as.numeric(as.character(validation_data$abst))
test_calib <- test_calib %>%
  group_by(bin) %>%
  summarize(observed = sum(class)/n(),
            expected = sum(prob)/n(),
            se = sqrt(observed * (1-observed) / n()))
cols <- c("Ideal"="red","Loess Smooth"="black","LM Smooth"="blue")</pre>
ggplot(test_calib) +
  geom abline(aes(intercept = 0, slope = 1, color="Ideal")) +
  geom_smooth(aes(x = expected,
                  y = observed,
                  color="Loess Smooth"), se=TRUE) +
  geom_smooth(aes(x = expected,
                  y = observed,
                  color="LM Smooth"), se=FALSE, method="lm") +
  scale_color_manual(values=cols) +
  labs(x = "Expected Proportion",
       y = "Observed Proportion",
       title="") +
  theme_bw() + theme(legend.position = "bottom")
#GOOD; Q2; Moderator
# Def All Params
B <- 1000
              # num of bootstraps
m <- 5
           # num of multiple imputations per bootstrap
           # num of cv folds for cv.glmnet
poly_degree <- 3  # degree for polynomial terms, set to 1 to test model fit w/o poly</pre>
# remove id
data_complete <- data %>% select(-id)
```

```
# Flag predictor vars
# exclude 'abst' from predictors
predictor_vars <- setdiff(names(data_complete), c("abst"))</pre>
# Flag trt vars
treatment_vars <- c("BA", "Var")</pre>
baseline_vars <- setdiff(predictor_vars, treatment_vars)</pre>
# Flag numeric and int baseline vars
num_baseline_vars <- baseline_vars[sapply(data_complete[baseline_vars],</pre>
                                            function(x) is.numeric(x) & !is.integer(x))]
non_binary_factor_vars <- baseline_vars[sapply(data_complete[baseline_vars],</pre>
                                                  function(x) is.integer(x))]
# Flag Binary baseline vars
binary_vars <- baseline_vars[sapply(data_complete[baseline_vars],</pre>
                                    function(x) length(unique(na.omit(x))) == 2)]
# Flag factor vars and store levels
factor_vars <- names(data_complete)[sapply(data_complete, is.factor)]</pre>
levels_list <- lapply(data_complete[, factor_vars, drop = FALSE], levels)</pre>
# --- Build Formula ---
# Main Effects
main_effects <- paste("BA + Var +",</pre>
                       paste(c(
                         paste0("poly(", non_binary_factor_vars,
                                 ", ", poly_degree, ", raw=TRUE)"),
                         num_baseline_vars,
                         binary_vars
                       ), collapse = " + "))
# Interaction Terms
interaction terms <- paste(c(</pre>
  paste0("BA:", c(paste0("poly(", non_binary_factor_vars,
                          ", ", poly_degree, ", raw=TRUE)"), num_baseline_vars, binary_vars))
), collapse = " + ")
# Full Model Formula
full_formula <- as.formula(paste("abst ~", main_effects, "+", interaction_terms))</pre>
# fix factor levels in the entire dataset (ensure consistency) BUGFIX
if (length(factor_vars) > 0) {
  for (var in factor_vars) {
    data_complete[[var]] <- factor(data_complete[[var]], levels = levels_list[[var]])</pre>
  }
}
# Gen master model matrix
```

```
master_model_matrix <- model.matrix(full_formula, data = data_complete)</pre>
master_coef_names <- colnames(master_model_matrix)</pre>
total_coeffs <- length(master_coef_names)</pre>
# --- Main estimation and bootstrap loop ---
# --- Primary model fit with imputation ---
# Initial imputation for primary fit
predictor_matrix <- make.predictorMatrix(data_complete)</pre>
predictor matrix[, "abst"] <- 0</pre>
predictor_matrix["abst", ] <- 0</pre>
imp_primary <- mice(data_complete, m = m, printFlag = FALSE, seed = 123,</pre>
                    predictorMatrix = predictor_matrix, method = 'pmm')
# Stack imputations for primary fit
stacked_data_primary <- complete(imp_primary, action = "long", include = FALSE)</pre>
stacked_data_primary <- stacked_data_primary %>% dplyr::select(-.id, -.imp)
# Fix factor levels
if (length(factor_vars) > 0) {
  for (var in factor vars) {
    stacked_data_primary[[var]] <- factor(stacked_data_primary[[var]],</pre>
                                           levels = levels_list[[var]])
  }
}
# Create model matrix for primary fit
model_data_full <- model.matrix(full_formula, data = stacked_data_primary)</pre>
x_primary <- model_data_full[, -1]</pre>
y_primary <- stacked_data_primary$abst</pre>
# Remove zero variance predictors and align columns
zero_var_cols <- apply(x_primary, 2, function(x) var(x) == 0)</pre>
if (any(zero_var_cols)) {
  x_primary <- x_primary[, !zero_var_cols]</pre>
  current_coef_names <- colnames(x_primary)</pre>
} else {
  current_coef_names <- colnames(x_primary)</pre>
}
# Align columns with master names
master_coef_names_no_intercept <- master_coef_names[-1]</pre>
missing_cols <- setdiff(master_coef_names_no_intercept, current_coef_names)</pre>
if (length(missing_cols) > 0) {
  zeros matrix <- matrix(0, nrow = nrow(x primary), ncol = length(missing cols))
  colnames(zeros_matrix) <- missing_cols</pre>
  x_primary <- cbind(x_primary, zeros_matrix)</pre>
```

```
}
extra_cols <- setdiff(current_coef_names, master_coef_names_no_intercept)</pre>
if (length(extra_cols) > 0) {
  x_primary <- x_primary[, !(colnames(x_primary) %in% extra_cols)]</pre>
}
x_primary <- x_primary[, master_coef_names_no_intercept]</pre>
# Set up penalty factors for primary fit
penalty_factors_primary <- ifelse(grepl(":", colnames(x_primary)), 1, 0)</pre>
# Verify penalty factor dimensions
if (ncol(x_primary) != length(penalty_factors_primary)) {
  stop("Mismatch between x columns and penalty_factors length in primary fit")
}
# Fit primary Lasso model with penalty factors
cv_lasso_primary <- cv.glmnet(</pre>
  x = x_{primary}
  y = y_primary,
  family = "binomial",
  alpha = 1,
  penalty.factor = penalty_factors_primary,
  standardize = TRUE,
  relax = FALSE
)
primary_fit <- glmnet(</pre>
  x = x_{primary}
  y = y_primary,
  family = "binomial",
  alpha = 1,
  lambda = cv_lasso_primary$lambda.min,
  penalty.factor = penalty_factors_primary,
  standardize = TRUE,
  relax = FALSE
)
# Get aligned primary coefficients
primary_coef_values <- as.vector(coef(primary_fit))</pre>
primary_coef_names <- rownames(coef(primary_fit))</pre>
names(primary_coef_values) <- primary_coef_names</pre>
aligned_primary_coef <- setNames(rep(0, length(master_coef_names)), master_coef_names)</pre>
matched_primary <- names(primary_coef_values) %in% master_coef_names</pre>
aligned_primary_coef[names(primary_coef_values)[matched_primary]] <-</pre>
  primary_coef_values[matched_primary]
```

```
primary nonzero <- abs(aligned primary coef) > 1e-8 # New
# --- Bootstrap loop for confidence intervals ---
coef_matrix <- matrix(NA, nrow = B, ncol = length(master_coef_names))</pre>
colnames(coef_matrix) <- master_coef_names</pre>
nonzero_matrix <- matrix(0, nrow = B, ncol = length(master_coef_names))</pre>
colnames(nonzero_matrix) <- master_coef_names</pre>
set.seed(1)
for (b in 1:B) {
  cat("Bootstrap iteration:", b, "of", B, "\n")
  bootstrap_sample <- data_complete %>%
    group_by(abst) %>%
    sample_frac(size = 1, replace = TRUE) %>%
    ungroup()
  predictor_matrix <- make.predictorMatrix(bootstrap_sample)</pre>
  predictor_matrix[, "abst"] <- 0</pre>
  predictor_matrix["abst", ] <- 0</pre>
  imp <- mice(bootstrap_sample, m = m, printFlag = FALSE, seed = b,</pre>
              predictorMatrix = predictor_matrix, method = 'pmm')
  stacked data <- complete(imp, action = "long", include = FALSE)
  stacked_data <- stacked_data %>% dplyr::select(-.id, -.imp)
  if (length(factor_vars) > 0) {
    for (var in factor_vars) {
      stacked_data[[var]] <- factor(stacked_data[[var]], levels = levels_list[[var]])</pre>
    }
  }
  model_data_full <- model.matrix(full_formula, data = stacked_data)</pre>
  x <- model_data_full[, -1]
  y_impute <- stacked_data$abst</pre>
  zero_var_cols <- apply(x, 2, function(x) var(x) == 0)
  if (any(zero_var_cols)) {
    x <- x[, !zero var cols]
    current_coef_names <- colnames(x)</pre>
  } else {
    current_coef_names <- colnames(x)</pre>
  missing_cols <- setdiff(master_coef_names_no_intercept, current_coef_names)</pre>
```

```
if (length(missing_cols) > 0) {
  zeros_matrix <- matrix(0, nrow = nrow(x), ncol = length(missing_cols))</pre>
 colnames(zeros_matrix) <- missing_cols</pre>
 x <- cbind(x, zeros_matrix)</pre>
}
extra_cols <- setdiff(current_coef_names, master_coef_names_no_intercept)</pre>
if (length(extra_cols) > 0) {
 x <- x[, !(colnames(x) %in% extra_cols)]</pre>
x <- x[, master_coef_names_no_intercept]</pre>
# Set penalty factors for bootstrap iterations
penalty_factors <- ifelse(grepl(":", colnames(x)), 1, 0)</pre>
# Verify penalty factor dimensions
if (ncol(x) != length(penalty_factors)) {
  stop("Mismatch between x columns and penalty factors length in bootstrap")
}
# Fit bootstrap model using same lambda as primary fit and penalty factors
boot_fit <- tryCatch({</pre>
 glmnet(
   x = x
    y = y_impute,
   family = "binomial",
   alpha = 1,
   lambda = cv_lasso_primary$lambda.min,
   penalty.factor = penalty_factors,
   standardize = TRUE,
   relax = FALSE
  )
}, error = function(e) {
 cat("Error in glmnet for bootstrap", b, ":", e$message, "\n")
 return(NULL)
})
if (is.null(boot_fit)) {
 next
}
coef_values <- as.vector(coef(boot_fit))</pre>
coef_names <- rownames(coef(boot_fit))</pre>
names(coef_values) <- coef_names</pre>
aligned_coef_values <- setNames(rep(0, length(master_coef_names)), master_coef_names)
matched <- names(coef_values) %in% master_coef_names</pre>
aligned_coef_values[names(coef_values)[matched]] <- coef_values[matched]
```

```
coef_matrix[b, ] <- aligned_coef_values</pre>
  nonzero_matrix[b, ] <- ifelse(aligned_coef_values != 0, 1, 0)</pre>
}
saveRDS(coef_matrix, file = "moderators_coef_CI-fix_6k.rds")
saveRDS(nonzero matrix, file = "moderators nonzero CI-fix 6k.rds")
coef_matrix <- readRDS(file = "moderators_coef_CI-fix_6k.rds")</pre>
nonzero_matrix <- readRDS(file = "moderators_nonzero_CI-fix_6k.rds")</pre>
coef_matrix[, !primary_nonzero] <- 0</pre>
# --- Pool coefs ---
# identify bad runs
bad_runs <- apply(coef_matrix, 1, function(x) all(is.na(x)) | all(x == 0)) &</pre>
             apply(nonzero_matrix, 1, function(x) all(is.na(x)) | all(x == 0))
# rm bad runs from objects
coef_matrix <- coef_matrix[!bad_runs, ]</pre>
nonzero_matrix <- nonzero_matrix[!bad_runs, ]</pre>
# make coef data frame
coef_mean <- colMeans(coef_matrix, na.rm = TRUE)</pre>
coef median <- apply(coef matrix, 2, median, na.rm = TRUE)</pre>
coef_lower <- apply(coef_matrix, 2, quantile, probs = 0.025, na.rm = TRUE)</pre>
coef_upper <- apply(coef_matrix, 2, quantile, probs = 0.975, na.rm = TRUE)</pre>
proportion_nonzero <- colSums(nonzero_matrix, na.rm = TRUE) / sum(nonzero_matrix[,1])
coef_ci <- data.frame(</pre>
  Predictor = colnames(coef_matrix),
  Mean = coef_mean,
  Median = coef_median,
  Lower_2.5 = coef_lower,
  Upper_97.5 = coef_upper,
  Proportion_Nonzero = proportion_nonzero
coef_ci$Primary_Estimate <- aligned_primary_coef</pre>
# plot the CIs
ggplot(coef_ci[-1,], aes(x = Predictor, y = Median)) +
  geom point() +
  geom_point(aes(y=Primary_Estimate), color = "red") +
```

```
geom_errorbar(aes(ymin = Lower_2.5, ymax = Upper_97.5), width = 0.2) +
  coord_flip() +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(
   y = "Coefficient Estimate",
    x = "Predictors"
  )
# plot nonzero prop
ggplot(coef_ci, aes(x = Predictor, y = Proportion_Nonzero)) +
  geom bar(stat = "identity", fill = "skyblue") +
  theme bw() +
  labs(
    title = "Proportion of Bootstrap Samples with Non-Zero Coefficients",
    y = "Proportion",
    x = "Predictors"
# --- Enforce Sparsity ---
# first criteria
\# note: from experimentation we see (for the B <- 6000 case) when threshold is set
# to .60, no additional variables are zeroed (no additional sparsity). the model
# over-fits in this case. however, when threshold is moved to even .605, just one
# variable is zeroed out which causes the calibration to improve but destroys the
# AUC / discriminative ability. very interesting behavior to study later.
threshold <- .60
predictors_to_keep <- names(proportion_nonzero)[proportion_nonzero >= threshold]
coef_matrix_sparse <- coef_matrix</pre>
# columns (predictors) to zero out
predictors_to_zero <- setdiff(colnames(coef_matrix_sparse), predictors_to_keep)</pre>
# second criteria
# note: from experimentation we know this second criteria doesn't cause any coefs
# to go to zero in the tested setting (B = 6000).
zero_ci_predictors <- coef_ci$Predictor[</pre>
  round(coef_ci$Median, 4) == 0 &
  round(coef ci$Lower 2.5, 4) == 0 &
  round(coef_ci$Upper_97.5, 4) == 0]
predictors_to_zero <- union(predictors_to_zero, zero_ci_predictors)</pre>
# zero out the coefs
if(length(predictors_to_zero) > 0){
```

```
coef_matrix_sparse[, predictors_to_zero] <- 0</pre>
  aligned_primary_coef[predictors_to_zero] <- 0</pre>
}
# coef_matrix_sparse <- coef_matrix # Uncomment to test not enforcing sparsity
coef_mean <- colMeans(coef_matrix_sparse, na.rm = TRUE)</pre>
coef_median <- apply(coef_matrix_sparse, 2, median, na.rm = TRUE)</pre>
coef_lower <- apply(coef_matrix_sparse, 2, quantile, probs = 0.025, na.rm = TRUE)</pre>
coef_upper <- apply(coef_matrix_sparse, 2, quantile, probs = 0.975, na.rm = TRUE)</pre>
proportion_nonzero <- colSums(nonzero_matrix, na.rm = TRUE) / sum(nonzero_matrix[,1])</pre>
coef_ci_sparse <- data.frame(</pre>
  Predictor = colnames(coef_matrix_sparse),
  Primary Estimate = aligned primary coef,
 Mean = coef_mean,
 Median = coef median,
  Lower_2.5 = coef_lower,
  Upper_97.5 = coef_upper,
  Proportion_Nonzero = proportion_nonzero
)
# Results Table
coef_ci_sparse <- coef_ci_sparse %>%
  mutate(
    #Odds_Ratio = exp(Median) # Odds Ratio
    Odds_Ratio = exp(Primary_Estimate) # Odds Ratio (now using main lasso est.)
  )
coef_ci_sparse <- coef_ci_sparse %>%
  mutate(
    Rounded_Lower_2.5 = round(Lower_2.5, 4),
    Rounded_Upper_97.5 = round(Upper_97.5, 4),
    # Determine significance
    Significant = ifelse(
      Rounded_Lower_2.5 > 0 | Rounded_Upper_97.5 < 0,
      "Yes",
      "No"
    )
  ) %>%
  select(-Rounded_Lower_2.5, -Rounded_Upper_97.5)
table_data <- coef_ci_sparse %>%
  select(
    Predictor,
    Primary_Estimate,
    Mean,
```

```
Median,
    Odds Ratio,
    Lower_2.5,
    Upper 97.5,
    Proportion_Nonzero,
    Significant
  ) %>%
  rename(
    "Estimate (Primary)" = Primary_Estimate,
    "Estimate (Mean)" = Mean,
    "Estimate (Median)" = Median,
    "Odds Ratio" = Odds_Ratio,
    "Lower 2.5\%" = Lower 2.5,
    "Upper 97.5%" = Upper_97.5,
    "Proportion Non-Zero" = Proportion_Nonzero,
        "Sig." = Significant
  )
table_data_significant <- table_data %>%
  filter(`Sig.` == "Yes")
table_data_significant %>%
  kbl(row.names = F,
    booktabs = TRUE,
    longtable = TRUE,
    escape = TRUE,
    align = "c",
    digits = 3,
    caption = "Lasso Regression Coefficient Estimates"
  ) %>%
  column spec(1, width = "3.2cm", latex valign = "m") %>%
  column_spec(2, width = "1.5cm", latex_valign = "m") %>%
  column_spec(3, width = "1.5cm", latex_valign = "m") %>%
  column_spec(4, width = "1.5cm", latex_valign = "m") %>%
  column_spec(5, width = "1.5cm", latex_valign = "m") %>%
  column_spec(6, width = "1.5cm", latex_valign = "m") %>%
  column_spec(7, width = "1.5cm", latex_valign = "m") %>%
  column_spec(8, width = "1.5cm", latex_valign = "m") %>%
  column_spec(9, width = ".5cm", latex_valign = "m") %>%
  kable_styling(
    font_size = 7.6,
    latex_options = c("repeat_header", "striped"),
    full_width = FALSE,
    position = "center"
  )
### Plot omitted in revision as this is no longer significant
```

```
# polynomial coefficients
shaps_coefs <- coef_ci[grep("poly\\(shaps_score_pq1, 3, raw = TRUE\\)", coef_ci$Predictor), ]</pre>
# interaction coefficients
shaps_baba_coefs <- coef_ci[grep("BABA:poly\\(shaps_score_pq1, 3, raw = TRUE\\)", coef_ci$Predict</pre>
# BABA main effect
baba_coef <- coef_ci$Median[coef_ci$Predictor == "BABA"]</pre>
shaps_range <- seq(min(na.omit(data$shaps_score_pq1)),</pre>
                    max(na.omit(data$shaps_score_pq1)), length.out = 100)
# Function to calculate predicted values for a given BABA value
calculate_predictions <- function(baba_value) {</pre>
    predicted_log_odds <- coef_ci$Median[coef_ci$Predictor == "(Intercept)"] +</pre>
                          baba_coef * baba_value +
                          shaps_coefs$Median[1] * shaps_range +
                          shaps_coefs$Median[2] * shaps_range^2 +
                          shaps_coefs$Median[3] * shaps_range^3 +
                          baba_value * shaps_baba_coefs$Median[1] * shaps_range +
                          baba_value * shaps_baba_coefs$Median[2] * shaps_range^2 +
                          baba_value * shaps_baba_coefs$Median[3] * shaps_range^3
    predicted_probs <- 1/(1 + exp(-predicted_log_odds))</pre>
    return(data.frame(
        shaps_score = shaps_range,
        log_odds = predicted_log_odds,
        probability = predicted_probs,
        BABA = as.factor(baba_value)
    ))
}
plot_data <- rbind(</pre>
    calculate_predictions(0),
    calculate_predictions(1)
)
# plot log odds
p1 <- ggplot(plot_data, aes(x = shaps_score, y = log_odds, color = BABA)) +
    geom_line() +
    theme_minimal() +
    scale_color_discrete(labels = c("Standard", "BA")) +
    labs(x = "SHAPS Score",
         y = "Predicted Log Odds",
         title = "")
# plot probabilities
p2 \leftarrow ggplot(plot_data, aes(x = shaps_score, y = probability, color = BABA)) +
    geom_line() +
    theme_minimal() +
```

```
scale_color_discrete(labels = c("Standard", "BA")) +
    labs(x = "SHAPS Score",
         y = "Predicted Probability",
         title = "")
shaps_plot <- ggarrange(</pre>
    p1,
    p2,
    ncol = 2,
    nrow = 1,
    common.legend = TRUE,
    legend = "bottom"
)
print(shaps_plot)
# --- Generate Predictions ---
# fix factor levels in the entire dataset (ensure consistency) BUGFIX
if (length(factor_vars) > 0) {
  for (var in factor_vars) {
    validation_data[[var]] <- factor(validation_data[[var]], levels = levels_list[[var]])</pre>
  }
}
# compute ROC for valid data
# prepare valid data
model_data_valid_full <- model.matrix(full_formula, data = validation_data)</pre>
current coef names valid <- colnames(model data valid full) # align cols
missing_cols <- setdiff(master_coef_names, current_coef_names_valid)
if (length(missing cols) > 0) {
  zeros_matrix <- matrix(0,</pre>
                          nrow = nrow(model_data_valid_full),
                          ncol = length(missing_cols))
  colnames(zeros_matrix) <- missing_cols</pre>
  model_data_valid_full <- cbind(model_data_valid_full, zeros_matrix)</pre>
}
extra_cols <- setdiff(current_coef_names_valid, master_coef_names)</pre>
if (length(extra_cols) > 0) {
  model_data_valid_full <-</pre>
    model_data_valid_full[, !(colnames(model_data_valid_full) %in% extra_cols)]
}
model_data_valid_full <- model_data_valid_full[, master_coef_names] # reorder</pre>
#predictor_coefs <- coef_ci_sparse$Median</pre>
predictor_coefs <- coef_ci_sparse$Primary_Estimate # NOTE: changed from using $Median
names(predictor_coefs) <- coef_ci_sparse$Predictor</pre>
predictor_coefs <- predictor_coefs[master_coef_names] # ensure match</pre>
```

```
# predictions for valid data
linear_predictor <- as.vector(model_data_valid_full %*% predictor_coefs)</pre>
pred_prob <- 1 / (1 + exp(-linear_predictor))</pre>
# BUGFIX
if (length(validation_data) < length(pred_prob)) {</pre>
  validation_data <- validation_data[complete.cases(validation_data),]</pre>
}
validation_data$pred_prob <- pred_prob</pre>
# compute ROC for training data
# prepare training data
data_complete_cc <- data_complete[complete.cases(data_complete),]</pre>
model_data_train <- model.matrix(full_formula, data = data_complete_cc)</pre>
current_coef_names_train <- colnames(model_data_train)</pre>
missing_cols_train <- setdiff(master_coef_names, current_coef_names_train)</pre>
if (length(missing_cols_train) > 0) {
  zeros_matrix_train <- matrix(0, nrow = nrow(model_data_train),</pre>
                                 ncol = length(missing_cols_train))
  colnames(zeros_matrix_train) <- missing_cols_train</pre>
  model_data_train <- cbind(model_data_train, zeros_matrix_train)</pre>
}
extra cols train <- setdiff(current coef names train, master coef names)
if (length(extra_cols_train) > 0) {
  model data train <-
    model_data_train[, !(colnames(model_data_train) %in% extra_cols_train)]
}
model_data_train <- model_data_train[, master_coef_names]</pre>
# predictions for training data
linear_predictor_train <- as.vector(model_data_train %*% predictor_coefs)</pre>
pred_prob_train <- 1 / (1 + exp(-linear_predictor_train))</pre>
data_complete_cc$pred_prob <- pred_prob_train</pre>
# ROCs
roc_valid <- roc(validation_data$abst, validation_data$pred_prob)</pre>
roc_train <- roc(data_complete_cc$abst, data_complete_cc$pred_prob)</pre>
# plot ROC curves
plot(roc train, col = "red", main = "")
plot(roc_valid, add = TRUE, col = "blue")
legend("bottomright",
       legend = c(paste("Validation, AUC=", round(roc_valid$auc, 4)),
```

```
paste("Training, AUC=", round(roc_train$auc, 4))),
       fill = c("blue", "red"))
# calc residuals
data_complete_cc$residuals <- data_complete_cc$abst - data_complete_cc$pred_prob</pre>
# plot residuals v. fitted
ggplot(data_complete_cc, aes(x = pred_prob, y = residuals)) +
  geom_point() +
  geom_hline(yintercept = 0, color = "red", linetype = "dashed") +
  labs(x = "Predicted Probability", y = "Residuals") +
  ggtitle("Residuals vs. Predicted Probabilities")
# Histogram of Residuals
hist(data_complete_cc$residuals, main = "Histogram of Residuals")
# Q-Q Plot of Residuals
qqnorm(data_complete_cc$residuals)
qqline(data_complete_cc$residuals)
# calibration plot
num_cuts <- 24
# calibration for validation data
test_calib <- data.frame(</pre>
  prob = validation_data$pred_prob,
  bin = cut(validation_data$pred_prob, breaks = num_cuts),
  class = as.numeric(as.character(validation_data$abst))
)
test_calib <- test_calib %>%
  group by(bin) %>%
  summarize(observed = sum(class)/n(),
            expected = sum(prob)/n(),
            se = sqrt(observed * (1-observed) / n()))
cols <- c("Ideal"="red","Loess Smooth"="black","LM Smooth"="blue")</pre>
ggplot(test_calib) +
  geom_abline(aes(intercept = 0, slope = 1, color="Ideal")) +
  geom_smooth(aes(x = expected,
                  y = observed,
                  color="Loess Smooth"), se=TRUE) +
  geom_smooth(aes(x = expected,
                  y = observed,
                  color="LM Smooth"), se=FALSE, method="lm") +
  scale color manual(values=cols) +
  labs(x = "Expected Proportion",
       y = "Observed Proportion",
```

```
title="") +
theme_bw() + theme(legend.position = "bottom")
```

Appendix II: Functions Code

```
# Helper Functions for Smoking Cessation Project
# --- Preamble ---
# Date of last update: Oct. 17, 2024
# R Version: 4.3.1
# Package Versions:
  outliers: 0.15
# tidyverse: 2.0.0
# reshape2: 1.4.4
# moments: 0.14.1
# vcd: 1.4-12
# Libraries for functions
suppressMessages(library(tidyverse))
library(outliers) # for grubbs.test()
library(reshape2) # for melt()
library(moments) # for skewness() and kurtosis()
library(vcd) # for assocstats()
# -- BEGIN Psuedo-correlation Matrix Section --
# Helper function to calculate Eta^2
eta_squared <- function(aov_model) {</pre>
  #' This function calculates the Eta^2 stat from an anova model. Eta^2 is a measure
  #' of effect size. Eta^2 describes the proportion of the total variance attributable
  #' to a given factor
  #'
  #' @param aov_model An aov object
  #' @return A numeric value of Eta^2 (proportion of the total variance explained)
  # '
  sum_of_squares_model <- summary(aov_model)[[1]]$"Sum Sq"[1]</pre>
  sum_of_squares_total <- sum(summary(aov_model)[[1]]$"Sum Sq")</pre>
  eta_sq <- sum_of_squares_model / sum_of_squares_total</pre>
  return(eta_sq)
}
# Main function to compute correlations or psuedo-correlations
# NOTE: Below still does not work with logical variables, but now fixed for NAs
```

```
psuedo_cor_mat <- function(data) {</pre>
  #' Builds a pseudo correlation matrix for a given dataset, flexible for numerical
  #' and categorical variables. Uses Pearson correlation for numerical-numerical pairs,
  #' Cramer's V for categorical-categorical pairs, point biserial correlation for
  #' numerical-binary categorical pairs, and the square root of Eta^2 for
  #' numerical-multi-category pairs.
  #'
  #' Oparam data A df with any mix of numerical and categorical variables.
  #' @return A symmetric matrix with correlation coefficients
  #' (or equivalent measures) for all variable pairs.
  variables <- names(data)</pre>
  n <- length(variables)</pre>
  cor_matrix <- matrix(NA, n, n, dimnames = list(variables, variables))</pre>
  for (i in 1:n) {
    for (j in i:n) {
      if (i == j) {
        cor_matrix[i, j] <- 1</pre>
      } else {
        var_i <- data[[i]]</pre>
        var_j <- data[[j]]</pre>
        if (is.numeric(var_i) && is.numeric(var_j)) {
          # Pearson correlation for continuous-continuous
          cor_matrix[i, j] <- cor_matrix[j, i] <- cor(var_i, var_j,</pre>
                                                          use = "pairwise.complete.obs")
        } else if (is.factor(var_i) && is.factor(var_j)) {
          # Remove NAs for both variables
          valid_idx <- !is.na(var_i) & !is.na(var_j)</pre>
          var_i_clean <- var_i[valid_idx]</pre>
          var_j_clean <- var_j[valid_idx]</pre>
          # Drop unused levels
          var_i_clean <- droplevels(var_i_clean)</pre>
          var_j_clean <- droplevels(var_j_clean)</pre>
          # Cramer's V for categorical-categorical
          if (length(var_i_clean) > 0 && length(var_j_clean) > 0) {
            cramers_v <- sqrt(assocstats(table(var_i_clean, var_j_clean))$cramer)</pre>
            cor_matrix[i, j] <- cor_matrix[j, i] <- cramers_v</pre>
          } else {
             cor_matrix[i, j] <- cor_matrix[j, i] <- NA</pre>
          }
        } else {
          # Continuous-categorical pairs
          if (is.numeric(var_i) && (is.factor(var_j) || is.character(var_j))) {
```

```
continuous <- var_i</pre>
             factor var <- as.factor(var j)</pre>
           } else if ((is.factor(var_i) || is.character(var_i)) && is.numeric(var_j)) {
             continuous <- var_j</pre>
             factor_var <- as.factor(var_i)</pre>
           } else {
             next # Skip if variables are not appropriate types
          }
           # Remove NAs in both variables
          valid_idx <- !is.na(continuous) & !is.na(factor_var)</pre>
           continuous <- continuous[valid_idx]</pre>
           factor_var <- factor_var[valid_idx]</pre>
           # Drop unused levels
           factor_var <- droplevels(factor_var)</pre>
           if (length(unique(factor_var)) == 2) {
             # Point biserial correlation for binary factors
             factor_numeric <- as.numeric(factor_var) - 1</pre>
             cor_matrix[i, j] <- cor_matrix[j, i] <- cor(continuous, factor_numeric)</pre>
           } else if (length(unique(factor_var)) > 2) {
             # Eta-squared for multi-category factors
             if (length(factor_var) > 0) {
               aov_result <- aov(continuous ~ factor_var)</pre>
               eta_sq <- eta_squared(aov_result)</pre>
               cor_matrix[i, j] <- cor_matrix[j, i] <- sqrt(eta_sq)</pre>
             } else {
               cor_matrix[i, j] <- cor_matrix[j, i] <- NA</pre>
             }
          } else {
             # Cannot compute correlation if factor_var has insufficient levels
             cor_matrix[i, j] <- cor_matrix[j, i] <- NA</pre>
        }
      }
    }
  return(cor_matrix)
}
# -- END Psuedo-correlation Matrix Section --
```

```
# NOTE: Does not like the following variable types: Date, `hms` num / difftime
# NOTE: Will likely need custom subroutines to handle dates / hms / difftime
summary table <- function(df, stratify var = NULL) {</pre>
  #' Create summary table for a data frame with option for stratification. It
  #' summarizes numeric variables by mean, standard deviation, and IQR.
  #' Categorical variables by count and percentage. Optionally stratifies by a
  #' specified variable.
  # '
  #' @param df A data frame
  #' @param stratify_var (Optional) A variable on which to stratify the summaries.
  # '
  #' @return A data frame (or tibble) containing the summarized statistics.
  # Internal function to handle the actual summarization
  summarize_internal <- function(df, stratify_var = NULL, is_recursive_call = FALSE) {</pre>
    # --- SUMMARIZER SECTION ---
    # Function to summarize continuous variable
    summarize_continuous <- function(data, var) {</pre>
      var_data <- data[[var]]</pre>
      mean_sd <- paste0(round(mean(var_data, na.rm = TRUE), 2),</pre>
                         " (",
                         round(sd(var_data, na.rm = TRUE), 2),
                         ")")
      quantiles \leftarrow quantile(var_data, probs = c(0.25, 0.75), na.rm = TRUE)
      quantile_range <- paste0("(",
                                round(quantiles[1], 2),
                                " - ",
                                round(quantiles[2], 2),
      paste(mean_sd, quantile_range)
    # Func to summarize categorical variable
    summarize_categorical <- function(data, var) {</pre>
      var_data <- table(data[[var]])</pre>
      percentages <- prop.table(var_data) * 100</pre>
```

Function to generate summary table aka "Table 1"

```
paste(names(var_data), ": ",
        var_data, " (",
        round(percentages, 2),
        "%)",
        sep = "",
        collapse = ", ")
}
# Handler for strata
variable_names <- names(df)</pre>
if (!is.null(stratify_var) && stratify_var %in% variable_names) {
  variable_names <- variable_names[variable_names != stratify_var]</pre>
# Summarize all into a list for table
summary_list <- map(variable_names, ~ {</pre>
  var_type <- ifelse(is.numeric(df[[.x]]) | is.integer(df[[.x]]),</pre>
                      "Numeric", "Categorical")
  summarizer <- ifelse(var_type == "Numeric",</pre>
                         summarize_continuous,
                         summarize_categorical)
  summary <- summarizer(df, .x)</pre>
  variable_name <- ifelse(var_type == "Numeric",</pre>
                            paste(.x, "[Mean (SD) (Quantile)]"),
                            paste(.x, "[n (%)]"))
  tibble(Variable = variable_name, Type = var_type, Summary = summary)
})
# Bind to table
summary_table <- bind_rows(summary_list)</pre>
# --- NORMALITY AND OUTLIERS SECTION ---
# Perform Shapiro-Wilk and Grubbs tests only if it's not a recursive call
# and no stratify_var is given
if (!is_recursive_call && is.null(stratify_var)) {
  # Get numeric variables
  numeric_vars <- variable_names[sapply(df[variable_names],</pre>
                                           function(x) is.numeric(x) | is.integer(x))]
  # Init object for S-W / Grubbs results
  test_results <- map(numeric_vars, ~ {</pre>
    x \leftarrow df[[.x]]
    x \leftarrow na.omit(x)
    n <- length(x)</pre>
    normality <- NA
    outlier <- NA
    skewness label <- NA
    kurtosis_label <- NA</pre>
```

```
# Shapiro-Wilk test (Note: now accommodates n > 5000)
# NOTE: Consider in future -- KS test, AD test, Jarque-Bera test
if (n >= 3) {
  if (n > 5000) {
    shapiro_test <- shapiro.test(sample(x, 4999))</pre>
  } else {
    shapiro_test <- shapiro.test(x)</pre>
  normality <- ifelse(shapiro_test$p.value < 0.05, "No", "Yes")</pre>
} else {
  normality <- "Insufficient data"</pre>
}
# Grubbs test
if (n >= 3) {
  grubbs_test <- grubbs.test(x)</pre>
  outlier <- ifelse(grubbs_test$p.value < 0.05, "Yes", "No")
} else {
  outlier <- "Insufficient data"
# Skewness and Kurtosis
if (n >= 2) {
  skewness <- skewness(x)</pre>
  kurtosis <- kurtosis(x)</pre>
  # Skewness label
  if (abs(skewness) < 0.5) {
    skewness_label <- "Centered"</pre>
  } else if (skewness > 0.5) {
    skewness_label <- "Right-skewed"</pre>
  } else {
    skewness_label <- "Left-skewed"</pre>
  }
  # Kurtosis label
  if (kurtosis < 2.5) {
    kurtosis_label <- "Platykurtic"</pre>
  } else if (kurtosis > 3.5) {
    kurtosis_label <- "Leptokurtic"</pre>
  } else {
    kurtosis_label <- "Mesokurtic"</pre>
  }
} else {
  skewness_label <- "Insufficient data"</pre>
  kurtosis_label <- "Insufficient data"</pre>
}
tibble(Variable = .x,
```

```
`Normal Distribution` = normality,
           `Outlier(s) Present` = outlier,
           `Skewness` = skewness label,
           `Kurtosis` = kurtosis_label)
 })
 # Bind test results into df
 test_results_df <- bind_rows(test_results)</pre>
 # Get actual variable names from summary_table for merge
 # Note: this could break in some datasets if the variable names include "["
 # therefore a more general solution later is preferred
 summary_table$ActualVariable <- gsub(" \\[.*\\]", "", summary_table$Variable)</pre>
 # Merge summary_table with test_results_df
  summary_table <- left_join(summary_table,</pre>
                              test results df,
                              by = c("ActualVariable" = "Variable"))
 # Remove temp matching ActualVariable column
 summary_table <- summary_table %>% dplyr::select(-ActualVariable)
} else if (!is.null(stratify_var)) {
 # --- STRATA SECTION ---
 # Stratification handling
 stratified_summaries <- df %>%
    group_by(!!sym(stratify_var)) %>%
    do(summarize_internal(., stratify_var = NULL, is_recursive_call = TRUE))
 summary_table <- stratified_summaries %>%
    ungroup() %>%
    dplyr::select(-group cols()) %>% # This doesn't seem necessary, why'd I do it?
    pivot_wider(names_from = !!sym(stratify_var), values_from = Summary)
 # Function for significance testing (numeric variables)
 test_continuous <- function(data, var, group_var) {</pre>
    formula <- as.formula(paste0("`", var, "` ~ `", group_var, "`")) #BUGFIX: spaces</pre>
   num_groups <- length(unique(data[[group_var]]))</pre>
    if (num_groups == 2) {
     test_result <- t.test(formula, data = data)</pre>
     p_value <- test_result$p.value</pre>
    } else {
     test result <- kruskal.test(formula, data = data)</pre>
      p_value <- test_result$p.value</pre>
   p_value
 # Function for significance testing (categorical variables)
```

```
test_categorical <- function(data, var, group_var) {</pre>
  table_data <- table(data[[var]], data[[group_var]])</pre>
  table_data <- table_data[rowSums(table_data) > 0, # This prevents NaN error
                            colSums(table_data) > 0, # in ChiSq test.
                            drop = FALSE]
  test_result <- chisq.test(table_data)</pre>
  p_value <- test_result$p.value</pre>
  p_value
# Perform significance testing (if stratify_var is specified)
significance_tests <- map(variable_names, ~ {</pre>
  var_type <- ifelse(is.numeric(df[[.x]]) | is.integer(df[[.x]]),</pre>
                      "Numeric", "Categorical")
  tester <- ifelse(var_type == "Numeric",</pre>
                    test_continuous,
                    test_categorical)
 p_value <- tester(df, .x, stratify_var)</pre>
 tibble(Variable = .x, `P-value` = p_value)
})
significance_table <- bind_rows(significance_tests)</pre>
# Adjust p-values using Bonferroni correction
significance_table$`Adjusted P-value` <- p.adjust(significance_table$`P-value`,</pre>
                                                     method = "bonferroni")
# Get actual variable names from summary_table for merge
# Note: this could break in some datasets if the variable names include "["
# therefore a more general solution later is preferred
summary_table$ActualVariable <- gsub(" \\[.*\\]", "", summary_table$Variable)</pre>
# Merge summary_table with significance_table on actual variable names
summary_table <- left_join(summary_table,</pre>
                            significance_table,
                            by = c("ActualVariable" = "Variable"))
# Remove rows corresponding to stratify_var
summary_table <- summary_table %>% filter(ActualVariable != stratify_var)
# Create 'Sig.' column based on Adjusted P-value
summary_table$`Sig.` <- case_when(</pre>
  summary_table$`Adjusted P-value` <= 0.0001 ~ "****",</pre>
  summary_table$`Adjusted P-value` <= 0.001 ~ "***",</pre>
  summary table$`Adjusted P-value` <= 0.01 ~ "**",</pre>
  summary_table$`Adjusted P-value` <= 0.05 ~ "*",</pre>
  TRUE
                                               ~ "ns"
)
```

```
# Remove temp matching ActualVariable, adjusted/unadjusted P-Values
      summary_table <- dplyr::select(summary_table,</pre>
                                      c(-ActualVariable,
                                        -`P-value`,
                                        - `Adjusted P-value`))
    }
    # Remove "Type" column for stratified tables
    if (!is.null(stratify_var) && !is_recursive_call) {
      summary_table <- summary_table %>% dplyr::select(-Type)
    return(summary_table)
  }
  # Call internal function to initiate procedure
  summarize_internal(df, stratify_var)
}
# Function to count number of variables where missing data occours
count_missing_vars <- function(df) {</pre>
  #' Calc the number of variables in a data frame that have at least one missing
  #' value.
  #'
  #' @param df A data frame
  #' @return A data frame with a single row and column indicating the count
  #' of variables with any missing values.
  missing_count <- df %>%
    summarise_all(~ sum(is.na(.))) %>%
    pivot_longer(everything()) %>%
    filter(value > 0) %>%
```

nrow()

```
return(data.frame(Num_Missing_Vars = missing_count))
}
# Count by variable type
summarize_variables_types <- function(data) {</pre>
  #' Summarizes the types of variables in a dataset by type. Possible types:
  #' Numeric, or Categorical (factors or logical).
  #'
  #' Oparam data A data frame
  #' @return A table with the counts of variables categorized by type
  # '
  var_types <- sapply(data, function(x) {</pre>
    if(is.numeric(x) | is.integer(x)) {
      return("Numeric")
    }
    else {
      return("Categorical")
    }
  })
  var_counts <- table(var_types)</pre>
  return(var_counts)
}
```

```
# Function to find groups of correlated variables
findCorrelatedGroups <- function(corr_matrix, threshold) {</pre>
  #' Find Groups of Correlated Variables
  #' This function identifies groups of variables in a correlation matrix that
  #' exceed a specified correlation threshold.
  #' Oparam corr matrix A square symmetric matrix representing variable correlations.
  #' Oparam threshold A numeric threshold for defining significant correlation.
  #' @return A list of numeric vectors, each containing indices of a group of
  #' correlated variables.
  correlation <- abs(corr matrix)</pre>
  diag(correlation) <- 0 # blank out diagonal to ignore self-correlation
  groups <- list()</pre>
  visited <- rep(FALSE, ncol(correlation))</pre>
  for (i in 1:ncol(correlation)) {
    if (!visited[i]) {
      # Find index of variables correlated w/ the current var
      high_cor_vars <- which(correlation[, i] > threshold)
      if (length(high_cor_vars) > 0) {
        group <- unique(c(i, high_cor_vars)) # include current var in the group</pre>
        groups[[length(groups) + 1]] <- group</pre>
        visited[group] <- TRUE</pre>
      else {
        visited[i] <- TRUE</pre>
    }
  }
  return(groups)
# Function to drop select highly correlated vars
reduceDataset <- function(df, corr_matrix, threshold) {</pre>
  #' Reduce Dataset by Dropping Highly Correlated Variables
  # '
  #' This function reduces a dataset by identifying and dropping highly correlated
  #' variables based on the provided correlation matrix and threshold.
  #' Oparam of A dataframe containing the dataset to be reduced.
  #' @param corr_matrix A square symmetric matrix of correlations between
  #' variables in `df`.
  #' @param threshold A numeric threshold to identify high correlations.
  #' @return A dataframe with reduced variables.
```

```
groups <- findCorrelatedGroups(corr_matrix, threshold)</pre>
  to_drop <- numeric()</pre>
  for (group in groups) {
    # Subroutine to select which to drop (inverse of variance explained)
    variances <- sapply(group, function(index) {</pre>
      # Below is to fix bug with fread/data.table (depending on how data is read in)
      if (is.data.table(df)) {
        var(as.vector(df[[index]]))
      } else {
        var(df[, index, drop = FALSE])
      }
    })
    # Drop variable with minimum variance
    min_variance_index <- which.min(variances)</pre>
    to_drop_var <- group[min_variance_index]</pre>
    to_drop <- c(to_drop, to_drop_var)</pre>
  to_drop <- unique(to_drop)</pre>
  # only drop columns that exist in the dataset (bug fix)
  to_drop <- to_drop[to_drop <= ncol(df)]</pre>
  if (length(to_drop) > 0) {
    reduced_df <- dplyr::select(df, -to_drop)</pre>
  else {
    reduced_df <- df # If nothing to drop, return the original dataset (bug fix)
  }
  return(reduced_df)
}
check_mar <- function(data) {</pre>
  #' Check Missing At Random (MAR) in Data
  # '
```

```
#' This function tests each variable in the dataset for missingness being at
#' random, conditional on all other variables, using logistic regression models.
#' @param data A dataframe with variables to test for MAR.
#' @return A list where each entry corresponds to a variable in `data` and
#' contains results of MAR tests.
all_vars <- names(data)</pre>
# Init object for results
results <- list()
for (var in all_vars) {
  # Generate missing indicator
 missing_var_name <- paste0("missing_", make.names(var))</pre>
  data[[missing_var_name]] <- as.integer(is.na(data[[var]]))</pre>
  # formula for GLM
  formula_vars <- sapply(all_vars[all_vars != var], function(v) paste0("`", v, "`"))</pre>
  formula_str <- paste0(missing_var_name, " ~ ", paste(formula_vars, collapse = " + "))</pre>
  formula <- as.formula(formula_str)</pre>
 model <- tryCatch(</pre>
      glm(formula, data = data, family = binomial())
    },
    error = function(e) {
     return(NULL)
    }
  )
  if (!is.null(model)) {
    # check for sig. variables
    summary_model <- summary(model)</pre>
    pvalues <- summary_model$coefficients[, "Pr(>|z|)"]
    significant_vars <- names(pvalues[pvalues < 0.05 & !is.na(pvalues)])
    # removve intercept from significant vars (if present)
    significant_vars <- significant_vars[significant_vars != "(Intercept)"]</pre>
    # rm backticks from significant vars for cleaner output
    significant_vars <- gsub("`", "", significant_vars)</pre>
    results[[var]] <- list(
      is_mar = length(significant_vars) == 0,
      significant vars = significant vars
    )
  } else {
```

```
results[[var]] <- list(
        is_mar = NA,
        significant_vars = NA,
        error = "Error in fitting GLM"
      )
    }
    # remove temporary missing indicator col
    data[[missing_var_name]] <- NULL</pre>
  }
  return(results)
}
calculate_mse <- function(actual, predicted) {</pre>
  #' Calculate Mean Squared Error
  #' This function computes the mean squared error between actual and predicted
  #' numerical values.
  # '
  #' @param actual A numeric vector of actual values.
  #' @param predicted A numeric vector of predicted values.
  #' Oreturn Numeric value representing the mean squared error.
  # inputs must be numeric
  actual <- as.numeric(actual)</pre>
  predicted <- as.numeric(predicted)</pre>
  # calc squared differences
  squared_diff <- (actual - predicted)^2</pre>
  # Remove NA / infinite values
  valid_diff <- squared_diff[is.finite(squared_diff) & !is.na(squared_diff)]</pre>
  # calc MSE
  mse <- sum(valid_diff) / length(valid_diff)</pre>
  return(mse)
}
variable_importance_reg <- function(model, data, target_column, n_iterations = 20) {</pre>
  #' Calculate Variable Importance for Linear Regression Models
  #' This function estimates the importance of each predictor variable in a
```

```
#' regression model by measuring the increase in prediction error after
  #' permuting each predictor variable.
  #' Oparam model A regression model object (e.g., lm, lmer).
  #' @param data A dataframe containing the data used in the model.
  #' @param target_column The name of the target (dependent) variable in `data`.
  #' @param n_iterations The number of iterations to perform for estimating
  #' importance (default is 20).
  #' @return A dataframe with variables and their relative importance scores.
  predictor_vars <- all.vars(formula(model))[-1]</pre>
  original_preds <- as.numeric(predict(model, data))</pre>
  original_mse <- calculate_mse(data[[target_column]], original_preds)</pre>
  importance_scores <- matrix(0, nrow = n_iterations, ncol = length(predictor_vars))</pre>
  colnames(importance_scores) <- predictor_vars</pre>
  for (i in 1:n_iterations) {
    for (var in predictor_vars) {
      data_shuffled <- data</pre>
      data_shuffled[[var]] <- sample(data_shuffled[[var]])</pre>
      shuffled_preds <- as.numeric(predict(model, data_shuffled))</pre>
      shuffled_mse <- calculate_mse(data_shuffled[[target_column]], shuffled_preds)
      importance_scores[i, var] <- shuffled_mse - original_mse</pre>
    }
  }
  avg_importance <- abs(colMeans(importance_scores))</pre>
  se_importance <- apply(importance_scores, 2, sd) / sqrt(n_iterations)</pre>
  result <- data.frame(
    Variable = predictor vars,
    Importance = avg_importance,
    SE = se_importance
  )
  result <- result[order(-result$Importance), ]</pre>
  result$`Relative Importance` <- result$Importance / max(result$Importance) * 100</pre>
 return(result)
}
```

```
select_best_model <- function(model_backward, model_forward) {</pre>
  #TODO: INSERT ROXYGEN
  # Compare the formulas of the two models
  if ((formula(model backward) == formula(model forward))) {
    # Formulas are the same, models are the same
    return(model_backward)
  } else {
    # --- Formulas are different ---
    # Extract terms from models
    terms_backward <- attr(terms(model_backward), "term.labels")</pre>
    terms_forward <- attr(terms(model_forward), "term.labels")</pre>
    # Check if models are nested -- BUG FIX 10/17/24
    if (all(terms_backward %in% terms_forward)) {
      # Backward model is nested within forward model
      smaller_model <- model_backward</pre>
      larger model <- model forward
    } else if (all(terms_forward %in% terms_backward)) {
      # Forward model is nested within backward model
      smaller_model <- model_forward</pre>
      larger_model <- model_backward</pre>
    } else {
      # Models are not nested; cannot perform LRT therefore we compare BIC to
      # select the best model
      aic_backward <- BIC(model_backward)</pre>
      aic_forward <- AIC(model_forward)</pre>
      if (aic_backward < aic_forward) {</pre>
        return(model_backward)
      } else {
        return(model_forward)
      }
    }
    # Perform LRT
    lrt_result <- tryCatch({</pre>
```

```
anova(smaller_model, larger_model, test = "LRT")
}, error = function(e) {
   stop("Error in performing LRT: ", e$message)
})

p_value <- lrt_result$`Pr(>Chi)`[2]

if (is.na(p_value)) {
   stop("LRT failed: p-value is NA")
}

# Decide which model to choose based on LRT
if (p_value < 0.05) {
   return(larger_model) # Larger model is significantly better
} else {
   return(smaller_model) # Smaller model is sufficient
}
}</pre>
```

```
create_cross_table <- function(data) {
  vars <- names(data)
  n_vars <- length(vars)

results <- list()

for (i in 1:(n_vars-1)) {
  for (j in (i+1):n_vars) {
    var1 <- vars[i]
    var2 <- vars[j]

  # variable types
    type1 <- class(data[[var1]])[1]
    type2 <- class(data[[var2]])[1]

# result based on variable types</pre>
```

```
if (type1 %in% c("factor", "character") && type2 %in% c("factor", "character")) {
        result <- table(data[[var1]], data[[var2]])</pre>
      } else if (type1 %in% c("numeric", "integer") && type2 %in% c("numeric", "integer")) {
        result <- cor(data[[var1]], data[[var2]], use = "complete.obs")</pre>
      } else {
        if (type1 %in% c("factor", "character")) {
          result <- tapply(data[[var2]], data[[var1]], mean, na.rm = TRUE)</pre>
        } else {
          result <- tapply(data[[var1]], data[[var2]], mean, na.rm = TRUE)</pre>
        }
      }
      # result
      results[[paste(var1, "x", var2)]] <- result</pre>
    }
  }
  return(results)
}
```