

In[53]:=

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(* Defining B(0,T) *)
B = E^(-r*T)
(* Defining k *)
k = Log[(V)/(B*K)]
(* Defining Pt{No Default} *)
t = CDF[(k+(0.5*q))/(q^(1/2))] - E^(-2k)*(CDF[(-k + (0.5*q))/(q^(1/2))])
(* Defining Pv{No Default} *)
v = CDF[(k-(0.5*q))/(q^(1/2))] - E^(-2k)*(CDF[(-k - (0.5*q))/(q^(1/2))])

(* Partial Derivative of E, w.r.t V *)
a = D[(K*B*t) - (V*v),V]

(* Simplify this result *)
Simplify[a]
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Out[53]=

$$e^{-rT}$$

Out[54]=

$$\text{Log}\left[\frac{e^{rT}V}{K}\right]$$

Out[55]=

$$-\frac{e^{-2rT}K^2\text{CDF}\left[\frac{0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{V^2} + \text{CDF}\left[\frac{0.5q+\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]$$

Out[56]=

$$-\frac{e^{-2rT}K^2\text{CDF}\left[\frac{-0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{V^2} + \text{CDF}\left[\frac{-0.5q+\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]$$

Out[57]=

$$\begin{aligned} & \frac{e^{-2rT}K^2\text{CDF}\left[\frac{-0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{V^2} - \text{CDF}\left[\frac{-0.5q+\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right] - \\ & V \left(\frac{2e^{-2rT}K^2\text{CDF}\left[\frac{-0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{V^3} + \frac{e^{-2rT}K^2\text{CDF}'\left[\frac{-0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{\sqrt{q}V^3} + \frac{\text{CDF}'\left[\frac{-0.5q+\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{\sqrt{q}V} \right) + \\ & e^{-rT}K \left(\frac{2e^{-2rT}K^2\text{CDF}\left[\frac{0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{V^3} + \frac{e^{-2rT}K^2\text{CDF}'\left[\frac{0.5q-\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{\sqrt{q}V^3} + \frac{\text{CDF}'\left[\frac{0.5q+\text{Log}\left[\frac{e^{rT}V}{K}\right]}{\sqrt{q}}\right]}{\sqrt{q}V} \right) \end{aligned}$$

Out[58]=

$$\begin{aligned}
& -\frac{1}{\sqrt{q} V^3} e^{-3 r^T} \left(e^{r^T} K^2 \sqrt{q} V \operatorname{CDF} \left[\frac{-0.5 q - \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] - \right. \\
& \quad 2 K^3 \sqrt{q} \operatorname{CDF} \left[\frac{0.5 q - \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] + e^{3 r^T} \sqrt{q} V^3 \operatorname{CDF} \left[\frac{-0.5 q + \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] + \\
& \quad e^{r^T} K^2 V \operatorname{CDF}' \left[\frac{-0.5 q - \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] - K^3 \operatorname{CDF}' \left[\frac{0.5 q - \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] + \\
& \quad \left. e^{3 r^T} V^3 \operatorname{CDF}' \left[\frac{-0.5 q + \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] - e^{2 r^T} K V^2 \operatorname{CDF}' \left[\frac{0.5 q + \operatorname{Log} \left[\frac{e^{r^T} V}{K} \right]}{\sqrt{q}} \right] \right)
\end{aligned}$$