## k-means exercise using Wine Data

Tom Thorpe Aug 15, 2018

## Objective

## 2

0.26

Use clustering for wine data

```
# This mini-project is based on the K-Means exercise from 'R in Action'
# Go here for the original blog post and solutions
# http://www.r-bloggers.com/k-means-clustering-from-r-in-action/
# Exercise 0: Install these packages if you don't have them already
# install.packages(c("cluster", "rattle.data", "NbClust"))
# Now load the data and look at the first few rows
data(wine, package="rattle.data")
str(wine)
                   178 obs. of 14 variables:
## 'data.frame':
  $ Type
                    : Factor w/ 3 levels "1", "2", "3": 1 1 1 1 1 1 1 1 1 1 ...
## $ Alcohol
                     : num 14.2 13.2 13.2 14.4 13.2 ...
## $ Malic
                     : num 1.71 1.78 2.36 1.95 2.59 1.76 1.87 2.15 1.64 1.35 ...
## $ Ash
                    : num 2.43 2.14 2.67 2.5 2.87 2.45 2.45 2.61 2.17 2.27 ...
## $ Alcalinity
                    : num 15.6 11.2 18.6 16.8 21 15.2 14.6 17.6 14 16 ...
## $ Magnesium
                    : int 127 100 101 113 118 112 96 121 97 98 ...
## $ Phenols
                     : num 2.8 2.65 2.8 3.85 2.8 3.27 2.5 2.6 2.8 2.98 ...
## $ Flavanoids
                     : num 3.06 2.76 3.24 3.49 2.69 3.39 2.52 2.51 2.98 3.15 ...
## $ Nonflavanoids : num 0.28 0.26 0.3 0.24 0.39 0.34 0.3 0.31 0.29 0.22 ...
## $ Proanthocyanins: num 2.29 1.28 2.81 2.18 1.82 1.97 1.98 1.25 1.98 1.85 ...
                    : num 5.64 4.38 5.68 7.8 4.32 6.75 5.25 5.05 5.2 7.22 ...
## $ Color
## $ Hue
                     : num 1.04 1.05 1.03 0.86 1.04 1.05 1.02 1.06 1.08 1.01 ...
## $ Dilution
                     : num 3.92 3.4 3.17 3.45 2.93 2.85 3.58 3.58 2.85 3.55 ...
## $ Proline
                     : int 1065 1050 1185 1480 735 1450 1290 1295 1045 1045 ...
nrow(wine)
## [1] 178
head(wine)
     Type Alcohol Malic Ash Alcalinity Magnesium Phenols Flavanoids
## 1
        1
            14.23 1.71 2.43
                                  15.6
                                              127
                                                     2.80
           13.20 1.78 2.14
                                   11.2
                                              100
                                                     2.65
                                                                2.76
        1
## 3
            13.16 2.36 2.67
                                   18.6
                                                     2.80
                                                                3.24
                                              101
## 4
            14.37
                  1.95 2.50
                                   16.8
                                              113
                                                     3.85
                                                                3.49
## 5
           13.24 2.59 2.87
                                  21.0
                                              118
                                                     2.80
                                                                2.69
           14.20 1.76 2.45
                                  15.2
                                              112
                                                     3.27
                                                                3.39
    Nonflavanoids Proanthocyanins Color Hue Dilution Proline
## 1
             0.28
                             2.29 5.64 1.04
                                                  3.92
                                                          1065
```

3.40

1050

1.28 4.38 1.05

```
2.81 5.68 1.03
## 3
             0.30
                                                 3.17
                                                         1185
## 4
             0.24
                             2.18 7.80 0.86
                                                 3.45
                                                         1480
## 5
             0.39
                             1.82 4.32 1.04
                                                 2.93
                                                          735
## 6
             0.34
                             1.97 6.75 1.05
                                                 2.85
                                                         1450
#knitr::knit_exit()
# Exercise 1: Remove the first column from the data and scale
# it using the scale() function
# the following are some calculations to understand the scale function
avgAlc=mean(wine$Alcohol)
sdAlc=sd(wine$Alcohol)
avgAlc
## [1] 13.00062
sdAlc
## [1] 0.8118265
(wine$Alcohol[1]-avgAlc)/sdAlc
## [1] 1.514341
\# scale(x, center = TRUE, scale = TRUE)
# wine[-1] removes the first column, so the remaining columns are scaled
# center with default = true, subracts the mean of the column
# scale with default = true, divides by the standard deviation
df <- scale(wine[-1]) # remove first column and scale
str(df)
## num [1:178, 1:13] 1.514 0.246 0.196 1.687 0.295 ...
## - attr(*, "dimnames")=List of 2
   ..$ : NULL
    ..$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## - attr(*, "scaled:center")= Named num [1:13] 13 2.34 2.37 19.49 99.74 ...
   ..- attr(*, "names")= chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## - attr(*, "scaled:scale")= Named num [1:13] 0.812 1.117 0.274 3.34 14.282 ...
   ..- attr(*, "names")= chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
head(df)
##
         Alcohol
                       Malic
                                    Ash Alcalinity Magnesium
## [1,] 1.5143408 -0.56066822 0.2313998 -1.1663032 1.90852151 0.8067217
## [2,] 0.2455968 -0.49800856 -0.8256672 -2.4838405 0.01809398 0.5670481
## [3,] 0.1963252 0.02117152 1.1062139 -0.2679823 0.08810981 0.8067217
## [4,] 1.6867914 -0.34583508 0.4865539 -0.8069748 0.92829983 2.4844372
## [5,] 0.2948684 0.22705328 1.8352256 0.4506745 1.27837900 0.8067217
## [6,] 1.4773871 -0.51591132 0.3043010 -1.2860793 0.85828399 1.5576991
##
       Flavanoids Nonflavanoids Proanthocyanins
                                                     Color
## [1,] 1.0319081 -0.6577078
                                      1.2214385 0.2510088 0.3611585
## [2,] 0.7315653
                     -0.8184106
                                     -0.5431887 -0.2924962 0.4049085
## [3,] 1.2121137
                     -0.4970050
                                      2.1299594 0.2682629 0.3174085
## [4,] 1.4623994
                                      1.0292513 1.1827317 -0.4263410
                    -0.9791134
## [5,] 0.6614853
                                      0.4002753 -0.3183774 0.3611585
                     0.2261576
## [6,] 1.3622851
                    -0.1755994
                                      0.6623487 0.7298108 0.4049085
```

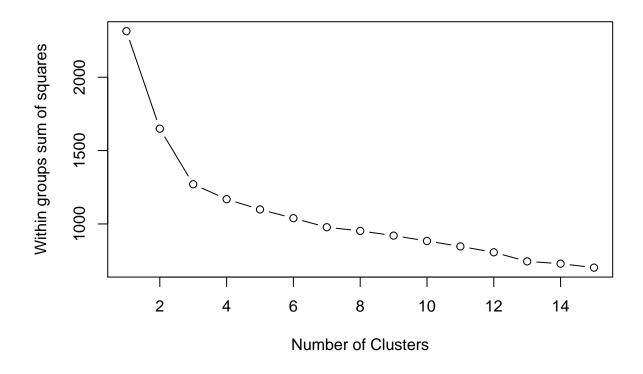
```
Dilution
                      Proline
## [1,] 1.8427215 1.01015939
## [2,] 1.1103172 0.96252635
## [3,] 0.7863692 1.39122370
## [4,] 1.1807407 2.32800680
## [5,] 0.4483365 -0.03776747
## [6,] 0.3356589 2.23274072
# Now we'd like to cluster the data using K-Means.
# How do we decide how many clusters to use if you don't know that already?
# We'll try two methods.
# Method 1: A plot of the total within-groups sums of squares against the
# number of clusters in a K-means solution can be helpful. A bend in the
# graph can suggest the appropriate number of clusters.
wssplot <- function(data, nc=15, seed=1234){</pre>
    wss <- (nrow(data)-1)*sum(apply(data,2,var))
  for (i in 2:nc){
     set.seed(seed)
    wss[i] <- sum(kmeans(data, centers=i)$withinss)</pre>
    plot(1:nc, wss, type="b", xlab="Number of Clusters",
                              ylab="Within groups sum of squares")
}
sumVal=sum(apply(df,2,var))
sumVal
## [1] 13
str(sumVal)
## num 13
wss<-(nrow(df-1))*sumVal
WSS
## [1] 2314
for (i in 2:15) {
  set.seed(1234)
  km = kmeans(df, centers=i)
  str(km)
  wss[i] <- sum(km$withinss)</pre>
  print(wss[i])
## List of 9
## $ cluster
                 : int [1:178] 1 1 1 1 1 1 1 1 1 1 ...
## $ centers : num [1:2, 1:13] 0.3249 -0.3106 -0.3529 0.3374 0.0521 ...
   ..- attr(*, "dimnames")=List of 2
   .. ..$ : chr [1:2] "1" "2"
##
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
```

```
: num 2301
## $ totss
## $ withinss
               : num [1:2] 765 884
## $ tot.withinss: num 1649
## $ betweenss : num 652
## $ size
                 : int [1:2] 87 91
## $ iter
                : int 1
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 1649.44
## List of 9
## $ cluster
                : int [1:178] 1 1 1 1 1 1 1 1 1 1 ...
                : num [1:3, 1:13] 0.833 -0.923 0.164 -0.303 -0.393 ...
## $ centers
   ..- attr(*, "dimnames")=List of 2
   .. ..$ : chr [1:3] "1" "2" "3"
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
                : num 2301
## $ withinss
                : num [1:3] 386 559 326
## $ tot.withinss: num 1271
## $ betweenss : num 1030
                : int [1:3] 62 65 51
## $ size
                : int 3
## $ iter
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 1270.749
## List of 9
## $ cluster
                : int [1:178] 1 1 1 1 2 1 1 1 1 1 ...
                : num [1:4, 1:13] 0.958 -0.787 0.186 -0.905 -0.377 ...
## $ centers
   ..- attr(*, "dimnames")=List of 2
   .. ..$ : chr [1:4] "1" "2" "3" "4"
   ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
                : num 2301
## $ withinss
                : num [1:4] 269 307 303 290
## $ tot.withinss: num 1169
## $ betweenss : num 1132
## $ size
                 : int [1:4] 56 28 49 45
## $ iter
                : int 4
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 1168.614
## List of 9
## $ cluster
                : int [1:178] 1 1 1 1 4 1 1 1 1 1 ...
## $ centers
                : num [1:5, 1:13] 0.982 -0.772 -0.909 -0.669 0.186 ...
    ..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:5] "1" "2" "3" "4" ...
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
                : num 2301
                 : num [1:5] 243 201 247 105 303
## $ withinss
## $ tot.withinss: num 1099
## $ betweenss : num 1202
                 : int [1:5] 54 30 37 8 49
## $ size
## $ iter
                : int 5
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 1098.739
```

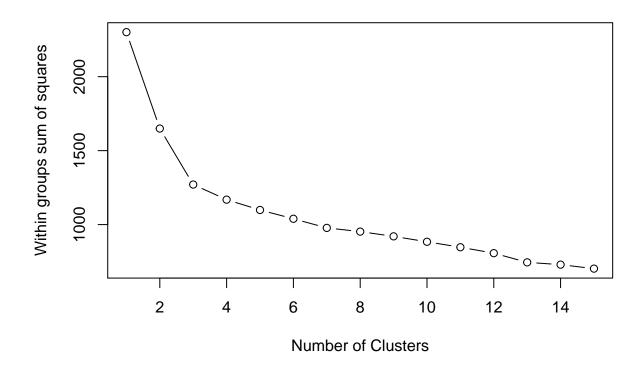
```
## List of 9
## $ cluster
               : int [1:178] 1 1 1 1 4 1 1 1 1 1 ...
                : num [1:6, 1:13] 0.982 -0.758 -0.926 -0.669 -0.105 ...
    ..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:6] "1" "2" "3" "4" ...
##
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
              : num 2301
               : num [1:6] 243 193 236 105 177 ...
## $ withinss
## $ tot.withinss: num 1039
## $ betweenss : num 1262
## $ size
                : int [1:6] 54 29 36 8 33 18
## $ iter
                : int 5
                : int 0
## $ ifault
## - attr(*, "class")= chr "kmeans"
## [1] 1039.296
## List of 9
## $ cluster
                : int [1:178] 1 1 1 1 4 1 1 1 1 1 ...
                : num [1:7, 1:13] 0.9998 -0.7509 -1.0165 -0.3738 -0.0639 ...
   ..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:7] "1" "2" "3" "4" ...
##
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
               : num 2301
               : num [1:7] 227.2 130.2 132.6 73.4 169 ...
## $ withinss
## $ tot.withinss: num 978
## $ betweenss : num 1323
## $ size
                : int [1:7] 52 20 24 7 32 19 24
## $ iter
                : int 3
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 977.541
## List of 9
## $ cluster
                : int [1:178] 1 1 1 1 4 1 1 1 1 1 ...
## $ centers
                : num [1:8, 1:13] 0.9683 -0.9171 -1.0269 -0.592 -0.0639 ...
   ..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:8] "1" "2" "3" "4" ...
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
             : num 2301
## $ withinss
               : num [1:8] 209.9 115.5 128.1 63.6 169 ...
## $ tot.withinss: num 953
## $ betweenss : num 1348
## $ size
               : int [1:8] 49 18 23 6 32 19 24 7
## $ iter
                : int 4
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 952.5328
## List of 9
## $ cluster
                : int [1:178] 1 1 1 1 4 1 1 1 1 1 ...
## $ centers
                : num [1:9, 1:13] 0.968 -0.951 -0.895 -0.592 -0.054 ...
   ..- attr(*, "dimnames")=List of 2
    ....$: chr [1:9] "1" "2" "3" "4" ...
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
##
## $ totss
              : num 2301
## $ withinss
               : num [1:9] 209.9 53.4 84.5 63.6 159.8 ...
## $ tot.withinss: num 920
```

```
## $ betweenss
                : num 1381
## $ size
               : int [1:9] 49 8 16 6 31 18 14 7 29
## $ iter
                : int 4
                : int 0
## $ ifault
## - attr(*, "class")= chr "kmeans"
## [1] 920.4558
## List of 9
## $ cluster
                : int [1:178] 1 7 1 1 4 1 7 1 7 7 ...
   $ centers
                : num [1:10, 1:13] 1.145 -0.951 -0.895 -0.592 -0.054 ...
   ..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:10] "1" "2" "3" "4" ...
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
##
## $ totss
              : num 2301
## $ withinss : num [1:10] 101.1 53.4 84.5 63.6 159.8 ...
## $ tot.withinss: num 884
## $ betweenss : num 1417
## $ size
                : int [1:10] 26 8 16 6 31 18 24 7 32 10
## $ iter
                : int 4
                : int 0
## $ ifault
## - attr(*, "class")= chr "kmeans"
## [1] 883.7607
## List of 9
## $ cluster
                : int [1:178] 1 7 1 1 4 1 7 1 7 7 ...
                : num [1:11, 1:13] 1.145 -0.951 -0.526 -0.592 -0.042 ...
## $ centers
   ..- attr(*, "dimnames")=List of 2
   ....$ : chr [1:11] "1" "2" "3" "4" ...
##
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
               : num 2301
## $ totss
## $ withinss : num [1:11] 101.1 53.4 75.6 63.6 137.4 ...
## $ tot.withinss: num 847
## $ betweenss : num 1454
## $ size
                : int [1:11] 26 8 12 6 29 18 24 7 19 15 ...
## $ iter
                : int 4
                : int 0
## $ ifault
   - attr(*, "class")= chr "kmeans"
## [1] 846.7963
## List of 9
## $ cluster
                : int [1:178] 1 7 1 1 4 1 7 1 7 7 ...
             : num [1:12, 1:13] 1.145 -0.951 0.086 -0.417 -0.203 ...
   $ centers
   ..- attr(*, "dimnames")=List of 2
   ....$ : chr [1:12] "1" "2" "3" "4" ...
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
##
## $ totss
               : num 2301
## $ withinss : num [1:12] 101.1 53.4 90.1 48.2 53.1 ...
## $ tot.withinss: num 807
## $ betweenss : num 1494
## $ size
                : int [1:12] 26 8 23 5 11 15 24 7 22 12 ...
## $ iter
                : int 4
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 806.6972
## List of 9
## $ cluster : int [1:178] 8 7 13 13 4 13 7 7 8 8 ...
## $ centers : num [1:13, 1:13] -0.818 -0.812 0.086 -0.358 -0.203 ...
```

```
..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:13] "1" "2" "3" "4" ...
##
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
##
## $ totss
                 : num 2301
## $ withinss
                 : num [1:13] 9.16 59.02 90.08 24.64 53.09 ...
## $ tot.withinss: num 745
## $ betweenss : num 1556
                 : int [1:13] 3 9 23 4 11 15 22 14 18 12 ...
## $ size
## $ iter
                 : int 6
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 744.7018
## List of 9
## $ cluster
                : int [1:178] 8 7 13 13 4 13 7 8 7 7 ...
## $ centers
                : num [1:14, 1:13] -0.818 -0.951 0.18 -0.358 0.138 ...
    ..- attr(*, "dimnames")=List of 2
##
##
    ....$ : chr [1:14] "1" "2" "3" "4" ...
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
## $ totss
                 : num 2301
                 : num [1:14] 9.16 53.45 65.57 24.64 55.23 ...
## $ withinss
## $ tot.withinss: num 729
## $ betweenss : num 1572
## $ size
                 : int [1:14] 3 8 18 4 16 6 21 15 18 12 ...
## $ iter
                 : int 5
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 729.1297
## List of 9
## $ cluster
                : int [1:178] 8 8 15 15 4 15 8 7 8 8 ...
## $ centers
                : num [1:15, 1:13] -0.8178 -0.984 0.0675 -0.358 0.4575 ...
    ..- attr(*, "dimnames")=List of 2
##
    ....$ : chr [1:15] "1" "2" "3" "4" ...
##
    ....$ : chr [1:13] "Alcohol" "Malic" "Ash" "Alcalinity" ...
##
## $ totss
                 : num 2301
## $ withinss
                 : num [1:15] 9.16 50.79 87.51 24.64 48.71 ...
## $ tot.withinss: num 702
## $ betweenss : num 1599
## $ size
                 : int [1:15] 3 11 22 4 15 2 20 18 6 13 ...
## $ iter
                 : int 5
## $ ifault
                : int 0
## - attr(*, "class")= chr "kmeans"
## [1] 702.2454
plot(1:15, wss, type="b", xlab="Number of Clusters",
                             ylab="Within groups sum of squares")
```



wssplot(df)

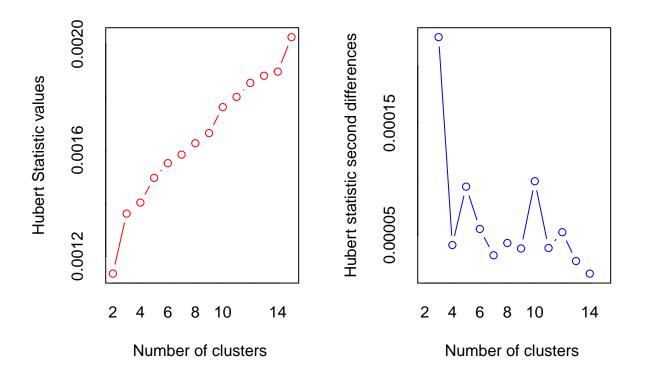


```
# Exercise 2:
# * How many clusters does this method suggest?
# * Why does this method work? What's the intuition behind it?
# * Look at the code for wssplot() and figure out how it works
```

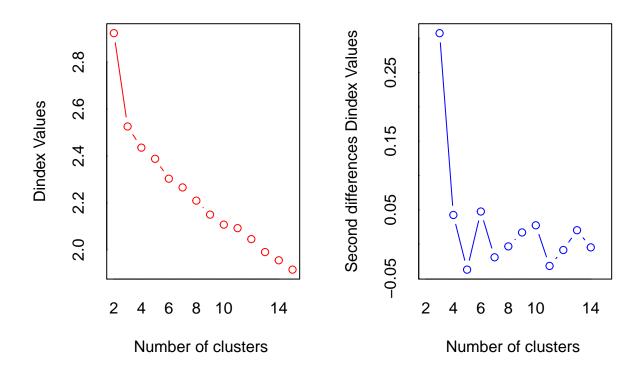
This method suggests 3 clusters. I am not really sure how it works. Need to investigate.

```
# Method 2: Use the NbClust library, which runs many experiments
# and gives a distribution of potential number of clusters.

library(NbClust)
set.seed(1234)
nc <- NbClust(df, min.nc=2, max.nc=15, method="kmeans")</pre>
```

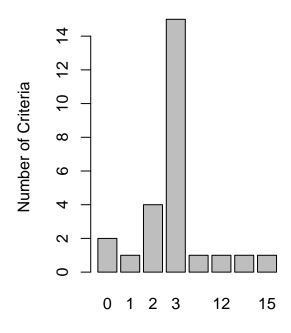


## \*\*\* : The Hubert index is a graphical method of determining the number of clusters.
## In the plot of Hubert index, we seek a significant knee that corresponds to a
## significant increase of the value of the measure i.e the significant peak in Hubert
## index second differences plot.
##



```
*** : The D index is a graphical method of determining the number of clusters.
                In the plot of D index, we seek a significant knee (the significant peak in Dindex
##
                second differences plot) that corresponds to a significant increase of the value of
##
                the measure.
##
##
## * Among all indices:
\#\# * 4 proposed 2 as the best number of clusters
## * 15 proposed 3 as the best number of clusters
## * 1 proposed 10 as the best number of clusters
## * 1 proposed 12 as the best number of clusters
## * 1 proposed 14 as the best number of clusters
## * 1 proposed 15 as the best number of clusters
##
##
                   ***** Conclusion *****
##
## * According to the majority rule, the best number of clusters is 3
##
barplot(table(nc$Best.n[1,]),
            xlab="Numer of Clusters", ylab="Number of Criteria",
                 main="Number of Clusters Chosen by 26 Criteria")
# Exercise 3: How many clusters does this method suggest?
```

## lumber of Clusters Chosen by 26 Ci



**Numer of Clusters** 

This also suggests 3 clusters.

```
# Exercise 4: Once you've picked the number of clusters, run k-means
# using this number of clusters. Output the result of calling kmeans()
\# into a variable fit.km
# fit.km <- kmeans( ... )
fit.km <- kmeans(df,centers=3)</pre>
fit.km
## K-means clustering with 3 clusters of sizes 51, 65, 62
##
## Cluster means:
##
        Alcohol
                     Malic
                                  Ash Alcalinity
                                                   Magnesium
## 1 0.1644436 0.8690954 0.1863726 0.5228924 -0.07526047 -0.97657548
## 2 -0.9234669 -0.3929331 -0.4931257 0.1701220 -0.49032869 -0.07576891
## 3 0.8328826 -0.3029551 0.3636801 -0.6084749 0.57596208
                                                             0.88274724
     Flavanoids Nonflavanoids Proanthocyanins
                                                    Color
                                   -0.77751312 0.9388902 -1.1615122
## 1 -1.21182921
                   0.72402116
## 2 0.02075402
                   -0.03343924
                                    0.05810161 -0.8993770 0.4605046
                                    0.57865427 0.1705823 0.4726504
## 3 0.97506900
                   -0.56050853
      Dilution
                   Proline
## 1 -1.2887761 -0.4059428
## 2 0.2700025 -0.7517257
```

```
## 3 0.7770551 1.1220202
##
## Clustering vector:
  ## [176] 1 1 1
##
## Within cluster sum of squares by cluster:
## [1] 326.3537 558.6971 385.6983
## (between_SS / total_SS = 44.8 %)
## Available components:
##
## [1] "cluster"
              "centers"
                        "totss"
                                  "withinss"
## [5] "tot.withinss" "betweenss"
                       "size"
                                  "iter"
## [9] "ifault"
# Now we want to evaluate how well this clustering does.
# Exercise 5: using the table() function, show how the clusters in fit.km$clusters
# compares to the actual wine types in wine$Type. Would you consider this a good
# clustering?
#table(fit.km$clusters,wine$Type)
table(fit.km$clusters)
## 
# Exercise 6:
# * Visualize these clusters using function clusplot() from the cluster library
# * Would you consider this a good clustering?
library(cluster)
#clusplot( fit.km )
```