

In this assignment reverse time migration (RTM) is performed on data with and without signal with a direct wave arrival. The earth model for velocity and density shown in Figures 1 and 2 was utilized to construct data shown in Figures 3 and 4 with and without a direct arrival, respectively.

Figure 1: Velocity.

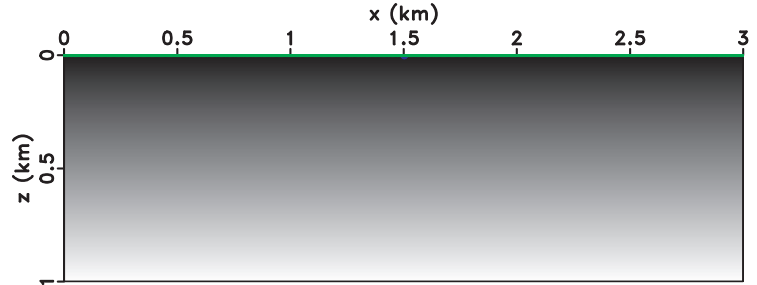


Figure 2: Density.

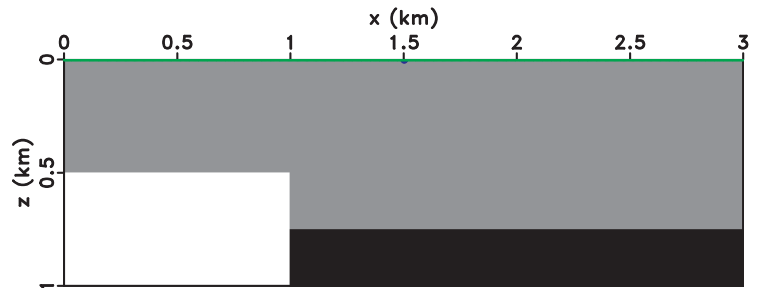
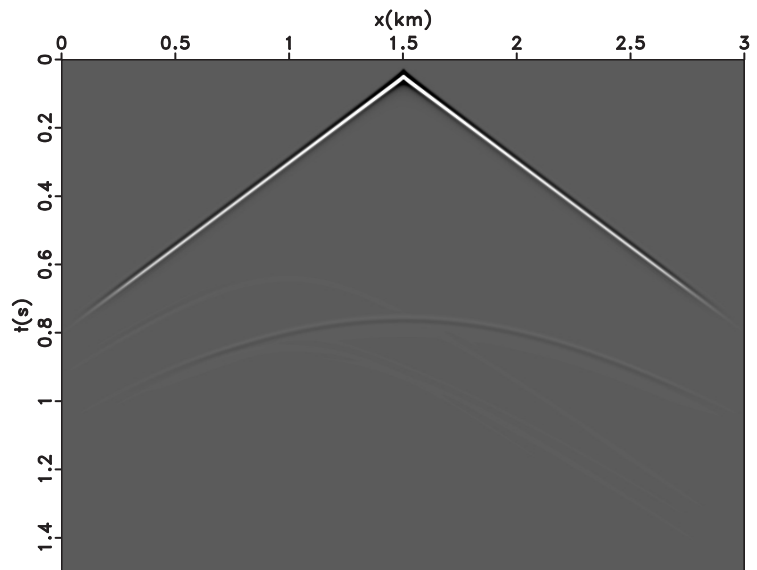


Figure 3: Data w/ direct arrival.



APPENDIX

The plots below were computed using the program `sfciold2d` which implements cross-correlation between receiver and source wavefields for the imaging condition. The plots from `sfciold2d` don't exactly match the plots above using a "homebrewed" CIC implementation. The images in the previous section were deduced using "Interferometric cross-correlation" according to the documentation of `sftcor`. Honestly, I don't know exactly how the interferometric cross-correlation works, but it appears to suppress the backscattering effects that contaminate the CIC image using `sfciold2d` (especially in the case of variable density without a direct wave in the model).

Figure 4: Data w/o direct arrival.

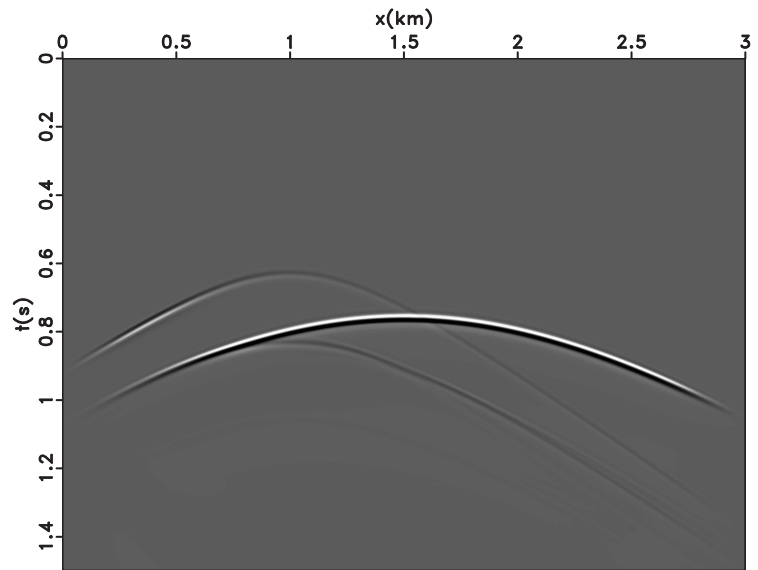


Figure 5: CIC using a constant density model (the incorrect density model) for imaging with direct arrival in data.

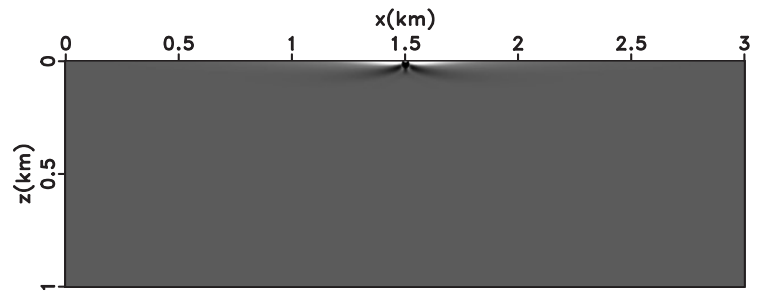


Figure 6: CIC using a constant density model (the incorrect density model) for imaging with-out direct arrival in data.

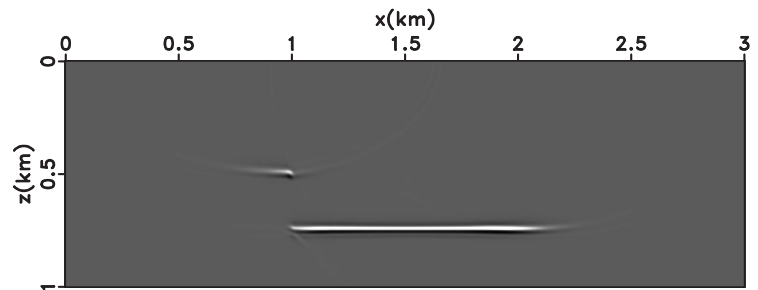


Figure 7: CIC using a variable density model (the correct density model) for imaging with direct arrival in data.

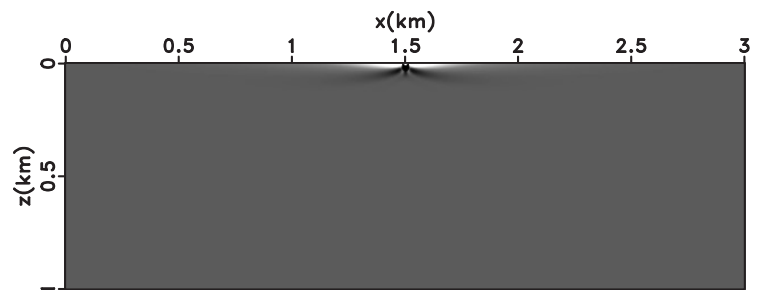


Figure 8: CIC using a variable density model (the correct density model) for imaging without direct arrival in data.

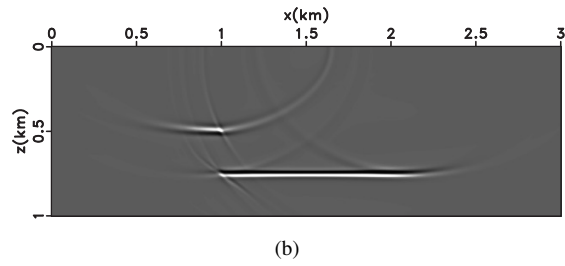
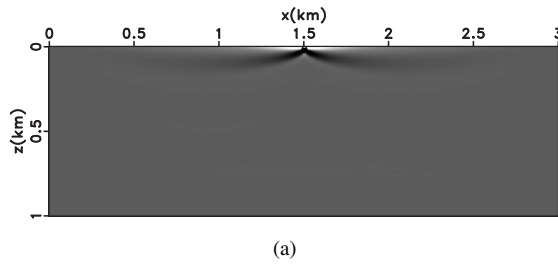
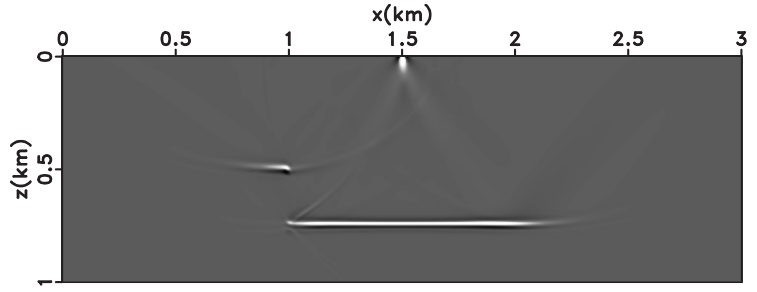


Figure 9: Images using `sfciold2d` to implement CIC with a constant density model (the incorrect density model) with and without direct arrival in data.

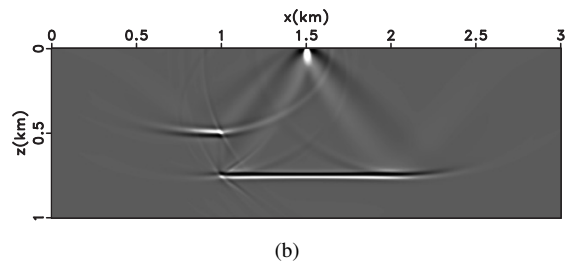
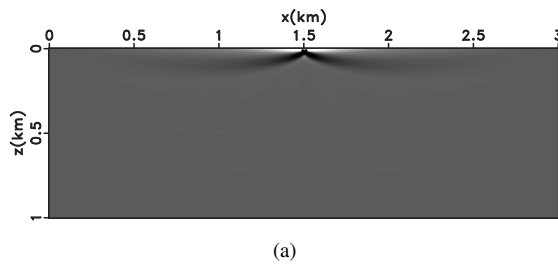


Figure 10: Images using `sfciold2d` to implement CIC with a variable density model (the correct density model) with and without direct arrival in data.

EXERCISE

In this homework, you will use a finite-differences modeling code, similar to the one you wrote in the preceding homework, to implement basic reverse time migration. I do not expect you to be concerned with the efficiency of your implementation at this time. This implementation of reverse-time migration does not require that you write any new C code. You will use pre-existing Madagascar programs, but you will modify the `SConstruct` file to combine those programs.

This is an individual assignment and absolutely no collaboration on code is allowed.

Using the finite-differences modeling function `awefd`, construct an image of the subsurface. This function takes the following parameters:

`awefd(odat, owfl, idat, velo, dens, sou, rec, custom, par)`

- `odat`: output data $d(x, t)$
- `owfl`: output wavefield $u(z, x, t)$
- `idat`: input data (wavelet)
- `velo`: velocity model $v(z, x)$
- `dens`: density model $\rho(z, x)$
- `sou`: source coordinates
- `rec`: receiver coordinates
- `custom`: custom parameters
- `par`: parameter dictionary

Design an imaging procedure following the generic scheme developed in class. Your task is to identify Madagascar programs necessary to implement reverse-time migration in two different ways and generate the appropriate `Flows` in the `SConstruct`. Explain in detail how your imaging procedures work.

1. Use your imaging procedure to generate images based on recorded data in Figures 3 and 4. For this exercise, use the constant density `rb.rsfc` for imaging. Include those two images in this document. Are the images different from each-other? How? Why?
2. Use your imaging procedure to generate images based on recorded data in Figures 3 and 4. For this exercise, use the variable density `ra.rsfc` for imaging. Include those two images in this document. Are the images different from each-other? How? Why? How do your images compare with the ones from the preceding exercise?

WRAP-UP

After you are satisfied that your document looks ok, print it from the PDF viewer and bring it to class.

SCONSTRUCT

```
##
# GPCN 658 — reverse—time migration
##
from rsf.proj import *
import fdm

# -----
par = dict(
    nt=1500, ot=0, dt=0.001, lt='t', ut='s',
    nx=601, ox=0, dx=0.005, lx='x', ux='km',
    nz=201, oz=0, dz=0.005, lz='z', uz='km',
    kt=50, nb=100, jsnap=50, jdata=1, frq=35
)
fdm.param(par)

par['xk']=50
par['xl']=par['nx']-50

par['xsou']=par['ox']+par['nx']/2*par['dx']
par['zsou']=par['oz']

# -----
# wavelet
fdm.wavelet('wav.', par['frq'], par)
Flow('wav', 'wav.', 'transp')
Result('wav', 'window n2=500 |' + fdm.waveplot('', par))

# -----
# sources coordinates
fdm.point('ss', par['xsou'], par['zsou'], par)
Plot('ss', fdm.ssplot('', par))

# receivers coordinates
fdm.horizontal('rr', 0, par)
Plot('rr', fdm.rrplot('', par))

# -----
# velocity
Flow('vo', None,
    '',
    math output="2.0+0.25*x1"
    n1=(nz)d o1=(oz)g d1=(dz)g
    n2=(nx)d o2=(ox)g d2=(dx)g
    '' % par)

Plot('vo', fdm.cgrey('allpos=y bias=2.0 pclip=100', par))
Result('vo', ['vo', 'ss', 'rr'], 'Overlay')

# -----
# density
Flow('ra', None,
    '',
    spike nsp=2 mag=+0.5, -0.5
    n1=(nz)d o1=(oz)g d1=(dz)g k1=101,151 l1=(nz)d,(nz)d
    n2=(nx)d o2=(ox)g d2=(dx)g k2=1,201 l2=200,(nx)d |
    add add=2
    '' % par)
Plot('ra', fdm.cgrey('allpos=y bias=1.5 pclip=100', par))
Result('ra', ['ra', 'ss', 'rr'], 'Overlay')

Flow('rb', 'ra', 'math output=1')

# -----
# edge taper
Flow('taper', None,
    '',
    spike nsp=1 mag=1
    n1=(nx)d d1=(dx)g o1=(ox)g k1=(xk)d l1=(xl)d
    n2=(nt)d d2=(dt)g o2=(ot)g |
    smooth rectl=50
    '' % par)
Result('taper', 'transp |'+fdm.dgrey('pclip=99', par))

# -----
# finite—differences modeling
fdm.awefd('dd', 'ww', 'wav', 'vo', 'ra', 'ss', 'rr', 'jsnap=1 fsrf=n', par)
fdm.awefd('do', 'wo', 'wav', 'vo', 'rb', 'ss', 'rr', 'jsnap=1 fsrf=n', par)

Result('ww', 'window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9', par))
Result('wo', 'window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9', par))

# data w/ direct arrivals
Flow('dr0', 'dd taper',
    'add mode=p ${SOURCES[1]}')

# data w/o direct arrivals
Flow('drl', 'dd do taper',
    'math r=${SOURCES[0]} d=${SOURCES[1]} t=${SOURCES[2]} output="(r-d)*t"')

for j in range(2):
    dtag="%d"%j
    Result('dr'+dtag, 'transp |' + fdm.dgrey('pclip=99.9', par))

# -----
##
## Here add rules for your assignment.
#
# use Flow()
# use Result()
#
# find Madagascar programs using the command "sfdoc -k ."
# find the documentation of Madagascar programs by typing the program name
##

# -----
## Construct source wavefields
# This step was performed when data was constructed
# ww is wavefield with vertically varying density
```

```

# wo is wavefield with constant density=1

#-----
## Construct receiver wavefields (four total)
# wb0.reverse — constant density with direct wave
# wb1.reverse — constant density without direct wave
# wa0.reverse — varying density with direct wave
# wa1.reverse — varying density without direct wave
# (takes about 30 seconds a pop at 1500 time steps...)

# flip the data along the time axis both with and without direct wave
# *** ensure that opt=i flag is used to prevent swapping of offset and step
Flow('dr0.reverse','dr0','reverse which=2 opt=i'); # with direct wave
Flow('dr1.reverse','dr1','reverse which=2 opt=i'); # without
Result('dr0.reverse','transp |' + fdm.dgrey('pclip=99.9',par))
Result('dr1.reverse','transp |' + fdm.dgrey('pclip=99.9',par))

# inject data into model
# *** Make sure the source locations are changed to the locations where
# the data were recorded.
# (i.e. the receiver locations used to generate data)

# varying density (use ra)
fdm.awefd('dda0','wa0','dr0.reverse','vo','ra','rr','rr','jsnap=1 fsrf=n',par)
fdm.awefd('ddal','wal','dr1.reverse','vo','ra','rr','rr','jsnap=1 fsrf=n',par)
Result('wa0','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))
Result('wal','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))

# constant density (use rb)
fdm.awefd('ddb0','wb0','dr0.reverse','vo','rb','rr','rr','jsnap=1 fsrf=n',par)
fdm.awefd('ddb1','wb1','dr1.reverse','vo','rb','rr','rr','jsnap=1 fsrf=n',par)
Result('wb0','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))
Result('wb1','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))

# transpose wavefields along time axis again (remove later for speed)
Flow('wa0.reverse','wa0','reverse which=4');
Flow('wa1.reverse','wa1','reverse which=4');
Flow('wb0.reverse','wb0','reverse which=4');
Flow('wb1.reverse','wb1','reverse which=4');
Result('wa0.reverse','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))
Result('wa1.reverse','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))
Result('wb0.reverse','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))
Result('wb1.reverse','window j3=(jsnap)d |'%par + fdm.wgrey('pclip=99.9',par))

#-----
## Imaging condition 1: Homebrew correlation (CIC)
# note that "ww" has vertically varying density contrast
# note that "wo" has a constant density contrast
# modifying ompchunk doesn't seem to speed things up . . . why?...

##### varying density
##### with direct arrival
Flow('Ra01',['ww','wa0.reverse'],'sftcor ur=${SOURCES[1]} ompchunk=1')
##### without direct arrival
Flow('Ra11',['ww','wa1.reverse'],'sftcor ur=${SOURCES[1]} ompchunk=1')

##### constant density
##### with direct arrival
Flow('Rb01',['wo','wb0.reverse'],'sftcor ur=${SOURCES[1]} ompchunk=1')
##### without direct arrival
Flow('Rb11',['wo','wb1.reverse'],'sftcor ur=${SOURCES[1]} ompchunk=1')

#-----
## Imaging condition 2: CIC using sfcicold2d
#### *** sfcicop2d was seg-faulting

##### varying density
##### with direct arrival
Flow('Ra02',['ww','wa0'],'sfcicold2d ur=${SOURCES[1]}')
##### without direct arrival
Flow('Ra12',['ww','wa1'],'sfcicold2d ur=${SOURCES[1]}')

##### constant density
##### with direct arrival
Flow('Rb02',['wo','wb0'],'sfcicold2d ur=${SOURCES[1]}')
Flow('Rb02',['wo','wb0.reverse'],'sfcicold2d ur=${SOURCES[1]} isreversed=y')
##### without direct arrival
Flow('Rb12',['wo','wb1'],'sfcicold2d ur=${SOURCES[1]}')

#-----

# Placeholder results

#varying density
#Flow('Ra01','Rtemp','math x=${SOURCES[0]} output=x')
#Flow('Ra02','Rtemp','math x=${SOURCES[0]} output=x')
#Flow('Ra11','Rtemp','math x=${SOURCES[0]} output=x')
#Flow('Ra12','Rtemp','math x=${SOURCES[0]} output=x')

#constant density
#Flow('Rb01','Rtemp','math x=${SOURCES[0]} output=x')
#Flow('Rb02','Rtemp','math x=${SOURCES[0]} output=x')
#Flow('Rb11','Rtemp','math x=${SOURCES[0]} output=x')
#Flow('Rb12','Rtemp','math x=${SOURCES[0]} output=x')

#plot
Result('Ra01',fdm.wgrey('pclip=99.9',par))
Result('Ra02',fdm.wgrey('pclip=99.9',par))
Result('Ra11',fdm.wgrey('pclip=99.9',par))
Result('Ra12',fdm.wgrey('pclip=99.9',par))
Result('Rb01',fdm.wgrey('pclip=99.9',par))
Result('Rb02',fdm.wgrey('pclip=99.9',par))
Result('Rb11',fdm.wgrey('pclip=99.9',par))
Result('Rb12',fdm.wgrey('pclip=99.9',par))

End()

```