Joachim Faulhaber An Introduction to the **Interval Template Library** Lecture held at the Boost Library Conference 2009 2009-05-08 Copyright © Joachim Faulhaber 2009 Slide Design by Chih-Hao Tsai Distributed under Boost Software Licence 1.0 http://www.chtsai.org

Lecture Outline

- Background and Motivation
- Characteristics of interval containers
- Examples
- Semantics
- Implementation
- Future Works
- Availability

Background and Motivation

- Interval containers simplified the implementation of date and time related tasks
 - Decomposing a stream of attributed events into segments with constant attributes.
 - Working with time grids, e.g. a grid of months.
 - Aggregations of values associated to date or time intervals.
- ... that occurred frequently in programs like
 - Billing modules
 - Therapy scheduling programs
 - Hospital and controlling statistics

- Background is the date time problem domain ...
- ... but the scope of the ItI as a generic library is more general:

an interval_set implements a set via a set of intervals

an interval_map implements a map via a map of interval value pairs

- There are two aspects in the design of interval containers
 - Conceptual aspect

```
interval_set<int> mySet;
mySet.insert(42);
bool has_answer = mySet.contains(42);
```

- On the conceptual aspect an interval_set can be used just as a set of elements
- except for . . .
- . . . iteration
- consider interval_set<double> or interval_set<string>

Iterative aspect

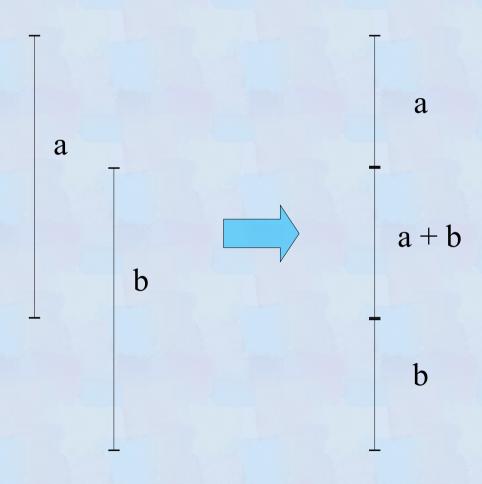
```
// Switch on my favorite telecasts using an interval set.
interval < seconds > news (make seconds ("20:00:00"),
                       make seconds("20:15:00"));
interval < seconds > talk show (make seconds ("22:45:30"),
                             make seconds("23:30:50"));
interval set<seconds> myTvProgram;
myTVProgram.add(news).add(talk show);
// Iterating over elements (seconds) would be silly ...
for(interval set<seconds>::iterator telecast =
   myTvProgram.begin();
    telecast != myTvProgram.end(); ++telecast)
  //...so this iterates over intervals
  TV.switch on(*telecast);
```

- Addability and Subtractability
 - All of itl's (interval) containers are Addable and Subtractable
 - They implement operators +=, +, -= and -

	+=	-=
sets	set union	set difference
maps	?	?

- A possible implementation for maps
 - Propagate addition/subtraction to the associated values
 - ... or aggregate on overlap
 - ... or aggregate on collision

Aggregate on overlap



- Decompositional effect on Intervals
- Accumulative effect on associated values

Aggregate on overlap, a minimal example

```
typedef itl::set<string> quests;
interval map<time, quests> party;
party += make pair(
  interval<time>::rightopen(20:00, 22:00), quests("Mary"));
party += make pair(
  interval<time>::rightopen(21:00, 23:00), guests("Harry"));
// party now contains
[20:00, 21:00) \rightarrow {\text{"Mary"}}
[21:00, 22:00) -> { "Harry", "Mary" } //quest sets aggregated
[22:00, 23:00) \rightarrow {\text{"Harry"}}
```

The Itl's class templates

Granu -larity	Style	Sets	Maps
interval		interval	
	joining	interval_set	interval_map
	separating	separate_interval_set	
	splitting	split_interval_set	split_interval_map
element		set	map

- Interval Combining Styles: Joining
 - Intervals are joined on overlap or on touch
 - ... for maps, if associated values are equal
 - Keeps interval_maps and sets in a minimal form

- Interval Combining Styles: Splitting
 - Intervals are split on overlap and kept separate on touch
 - All interval borders are preserved (insertion memory)

- Interval Combining Styles: Separating
 - Intervals are joined on overlap but kept separate on touch
 - Preserves borders that are never crossed (preserves a hidden grid).

Examples

A few instances of intervals (interval.cpp)

A way to iterate over months and weeks

```
(month and week grid.cpp)
```

```
#include <boost/itl/gregorian.hpp> //boost::gregorian plus adapter code
#include <boost/itl/split interval set.hpp>
// A split interval set of gregorian dates as date grid.
typedef split interval set < boost::gregorian::date > date grid;
// Compute a date grid of months using boost::gregorian.
date grid month grid(const interval < date > & scope)
    date grid month grid;
    // Compute a date grid of months using boost::gregorian.
    return month grid;
// Compute a date grid of weeks using boost::gregorian.
date grid week grid(const interval < date > & scope)
    date grid week grid;
    // Compute a date grid of weeks using boost::gregorian.
    return week grid;
```

A way to iterate over months and weeks

```
void month and time grid()
    date someday = day clock::local day();
    date thenday = someday + months(2);
    interval < date > scope = interval < date > :: rightopen (someday, thenday);
    // An intersection of the month and week grids ...
    date grid month and week grid
        = month grid(scope) \overline{\&} week grid(scope);
    // ... allows to iterate months and weeks. Whenever a month
    // or a week changes there is a new interval.
    for(date grid::iterator it = month and week grid.begin();
        it != month and week grid.end(); it++)
    // We can also intersect the grid into an interval map to make
    // shure that all intervals are within months and week bounds.
    interval map<boost::gregorian::date, some type> accrual;
    compute some result (accrual, scope);
    accrual &= month and week grid;
```

Aggregating with interval_maps (1) (boost party.cpp)

```
typedef itl::set<string> guests;
interval_map<time, guests> party;

party += make_pair(
   interval<time>::rightopen(20:00, 22:00), guests("Mary"));

party += make_pair(
   interval<time>::rightopen(21:00, 23:00), guests("Harry"));

// party now contains
[20:00, 21:00)->{"Mary"}
[21:00, 22:00)->{"Harry","Mary"} //guest sets aggregated
[22:00, 23:00)->{"Harry"}
```

- Aggregating with interval_maps (2)
 - Computing averages via implementing operator +=
 (partys_guest_average.cpp)

```
class counted sum
public:
   counted sum(): sum(0), count(0){}
   counted sum(int sum): sum(sum), count(1){}
   int sum()const {return sum;}
   int count()const{return count;}
   double average()const
    { return _count==0 ? 0.0 : _sum/static cast<double>( count); }
   counted sum& operator += (const counted sum& right)
    { _sum += right.sum(); _count += right.count(); return *this; }
private:
   int sum;
   int count;
};
bool operator == (const counted sum& left, const counted sum& right)
{ return left.sum() == right.sum() && left.count() == right.count(); }
```

- Aggregating with interval_maps (2)
 - Computing averages via implementing operator +=

```
void partys height average()
    interval map<ptime, counted sum> height sums;
    height sums += (
      make pair (
        interval interval ptime>::rightopen(
          time from string("2008-05-20 19:30"),
          time from string("2008-05-20 23:00")),
          counted sum(165)) // Mary is 1,65 m tall.
    );
    // Add height of more pary quests . . .
    interval map<ptime, counted sum>::iterator height sum =
        height sums.begin();
    while(height sum != height sums.end())
        interval<ptime> when = height sum ->first;
        double height average = (*height sum ++).second.average();
        cout << "[" << when.first() << " - " << when.upper() << ")"
             << ": " << height average << " cm" << endl;
```

Examples

- Aggregating with interval_maps (3)
 - Computing maxima via instantiation of a template parameter (partys tallest guests.cpp)

```
typedef interval map<ptime, int, partial absorber, less, inplace max>
   PartyHeightHistoryT;
void partys height()
   PartyHeightHistoryT tallest quest;
   tallest guest += (
     make pair (
       time from string("2008-05-20 19:30"),
         time from string("2008-05-20 23:00")),
         180) // Max of Mary & Harry: Harry is 1,80 m tall.
   );
```

- Interval containers allow to express a variety of date and time operations in an easy way.
 - Example man_power.cpp ...
 - Subtract weekends and holidays from an interval_set worktime -= weekends(scope) worktime -= german reunification day
 - Intersect an interval_map with an interval_set
 claudias_working_hours &= worktime
 - Subtract and interval_set from an interval map claudias_working_hours -= claudias_absense_times
 - Adding interval_maps
 interval_map<date,int> manpower;
 manpower += claudias_working_hours;
 manpower += bodos working hours;

Interval_maps can also be intersected Example user_groups.cpp

```
typedef boost::itl::set<string> MemberSetT;
typedef interval map<date, MemberSetT> MembershipT;
void user groups()
    MembershipT med users;
    // Compute membership of medical staff
    med users += make pair(member interval 1, MemberSetT("Dr.Jekyll"));
    med users += . . .
    MembershipT admin users;
    // Compute membership of administation staff
    med users += make pair(member interval 2, MemberSetT("Mr.Hyde"));
    MembershipT all users = med users + admin users;
    MembershipT super users = med users ← admin users;
```

The semantics of itl sets is based on a concept itl::Set

itl::set, interval_set, split_interval_set
and separate_interval_set are models of concept
itl::Set

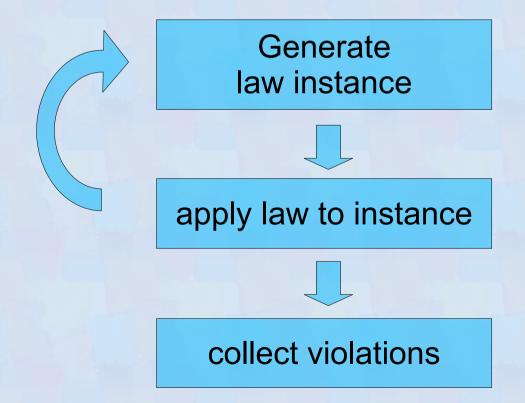
```
// Abstract or conceptual part
               Set::Set()
empty set:
subset relation: bool Set::contained in(const Set& s2)const
equality: bool is element equal(const Set& s1, const Set& s2)
set union:
                Set& operator += (Set& s1, const Set& s2)
                 Set operator + (const Set& s1, const Set& s2)
set difference: Set& operator -= (Set& s1, const Set& s2)
                 Set operator - (const Set& s1, const Set& s2)
set intersection: Set& operator &= (Set& s1, const Set& s2)
                 Set operator & (const Set& s1, const Set& s2)
// Part related to sequence and iteration
sorting order: bool operator < (const Set& s1, const Set& s2)
lexicographical equality:
                 bool operator == (const Set& s1, const Set& s2)
```

The semantics of itl maps is based on a concept itl::Map

```
itl::map, interval_map and split_interval_map
are models of concept
itl::Map
```

```
// Abstract or conceptual part
empty map:
                Map::Map()
submap relation: bool Map::contained in(const Map& m2)const
             bool is element equal(const Map& m1, const Map& m2)
equality:
map union:
                 Map& operator += (Map& m1, const Map& m2)
                 Map operator + (const Map& m1, const Map& m2)
map difference:
                Map& operator -= (Map& m1, const Map& m2)
                 Map operator - (const Map& m1, const Map& m2)
map intersection: Map& operator &= (Map& m1, const Map& m2)
                 Map operator & (const Map& m1, const Map& m2)
// Part related to sequence and iteration
sorting order: bool operator < (const Map& m1, const Map& m2)
lexicographical equality:
                 bool operator == (const Map& m1, const Map& m2)
```

- Defining semantics of itl concepts via sets of laws
 - aka c++0x axioms
- Checking law sets via automatic testing:
 - A Law Based Test Automaton LaBatea



- Lexicographical Ordering and Equality
 - For all itl containers operator < implements a strict weak ordering.</p>
 - The induced equivalence of this ordering is lexicographical equality which is implemented as operator ==
 - This is in line with the semantics of SortedAssociativeContainers

- Subset Ordering and Element Equality
 - For all itl containers function contained_in implements a partial ordering.
 - The induced equivalence of this ordering is equality of elements which is implemented as function is element equal.

- itl::Sets
- All itl sets implement a Set Algebra, which is to say satisfy a "classical" set of laws . . .
 - ... using is_element_equal as equality
 - Associativity, Neutrality, Commutativity
 - Distributivity, DeMorgan, Symmetric Difference
- Most of the itl sets satisfy the classical set of laws even if . . .
 - in lexicographical equality: operator == is used
 - The differences reflect proper inequalities in sequence that occur for separate_interval_set and split_interval_set.

itl::Maps

- Two major use cases
 - Maps of Sets: Collectors
 - Maps of Numbers: Quantifiers

- Map Traits:
 - Definedness
 - partial
 - total
 - Neutron semantics: Given a value pair (k,0), the associated neutron value codes
 - non existence. (k,0) will be deleted: neutron absorber
 - O-quantification. (k,0) will not be deleted: neutron enricher

	neutron absorber	neutron enricher
partial	partial_absorber	partial_enricher
total	total_absorber	total_enricher

- Collectors: Maps of Sets . . .
 - Condition: Trait == partial_absorber.
 interval_map<int, itl::set<int>, partial_absorber>
 - partial: only value pairs exist that have been added
 - neutron absorber: If a value pair carries a neutron (k,0), it is deleted (0 codes non existence).
 - ... then an itl Map of Sets is model of itl::Set
 - ... it satisfies the same set of laws that itl sets do.

- Concepts induction / concept transition
 - The semantics of itl Maps appears to be determined by the codomain type of the map
 - Itl Maps are mapping the semantics of the codomain type on themselves.

Implementation

- Itl containers are implemented simply based on std::set and std::map
 - Basic operations like adding and subtracting intervals have a best case complexity of O(lg n), if the added or subtracted intervals are relatively small.
 - Worst case complexity of adding or subtracting intervals for interval_set is O(n).
 - For all other interval containers adding or subtracting intervals has a worst case performance of O(n lg(n)).
 - There is a potential for optimization . . .

Implementation

- A segment_tree implementaion: A balanced tree, where . . .
 - an interval represents a perfectly balanced subtree
 - large intervals are rotated towards the root
- First results
 - much better worst case performance O(n) instead of O(n lg(n))
 - but slower for best case due to heavier bookkeeping and recursive algorithms.

Future Works

- Completing and optimizing the segment_tree implementation of interval containers
- Implementing interval_maps of sets more efficiently
- Revision of features of the extended itl (itl_plus.zip)
 - Decomposition of histories: k histories h_k with attribute types $A_1, ..., A_k$ are "decomposed" to a product history of tuples of attribute sets: $(h_1 < T, A_1 >, ..., h < T, A_k >) \rightarrow h < T, (set < A_1 >, ..., set < A_k >) >$
 - Cubes (generalized crosstables): Applying aggregate on collision to maps of tuple value pairs in order to organize hierachical data and their aggregates.

Availability

- Itl project on sourceforge (version 2.0.1) http://sourceforge.net/projects/itl
- Latest version on boost vault/Containers (3.0.0) http://www.boostpro.com/vault/ → containers
 - itl.zip : Core itl in preparation for boost
 - itl_plus.zip : Extended itl including product histories, cubes and automatic validation (LaBatea).
- Online documentation at http://www.herold-faulhaber.de/
 - Doxygen generated docs for (version 2.0.1) http://www.herold-faulhaber.de/itl/
 - Latest boost style documentation (version 3.0.0) http://www.herold-faulhaber.de/boost_itl/doc/libs/itl/doc/html/