# APSTA-GE: 2003 Intermediate Quantitative Methods

Lab Section 003, Week 12

29 November 2020

# Introduction

In this lab, we will examine various factors that may be associated with student's math performance. The attached dataset, student-mat.csv, is a random sample of student's math scores in secondary education of two Portuguese schools. It was collected by using school reports and quesitonnaires.

Note: the dataset is in csv format with semi-colon as separators.

```
dat <- read.csv("student-mat.csv", sep = ";", header = TRUE)</pre>
```

### **Dimensions**

```
dim(dat)
## [1] 395 33
table(is.na(dat))
##
## FALSE
## 13035
```

The dataset contains 395 records with 33 columns. No data point is missing.

#### **Variables**

Here is a list of column names.

```
as.data.frame(colnames(dat))
```

```
##
      colnames(dat)
## 1
            school
## 2
                sex
## 3
                age
            address
## 5
            famsize
## 6
            Pstatus
## 7
               Medu
## 8
               Fedu
## 9
               Mjob
## 10
               Fjob
## 11
             reason
           guardian
## 12
## 13
         traveltime
## 14
          studytime
```

```
## 15
           failures
## 16
          schoolsup
## 17
             famsup
## 18
               paid
## 19
         activities
## 20
            nursery
## 21
             higher
           internet
## 22
## 23
           romantic
## 24
             famrel
## 25
           freetime
## 26
              goout
## 27
               Dalc
## 28
               Walc
## 29
             health
## 30
           absences
## 31
                 G1
## 32
                 G2
## 33
                 G3
```

### **Distributions**

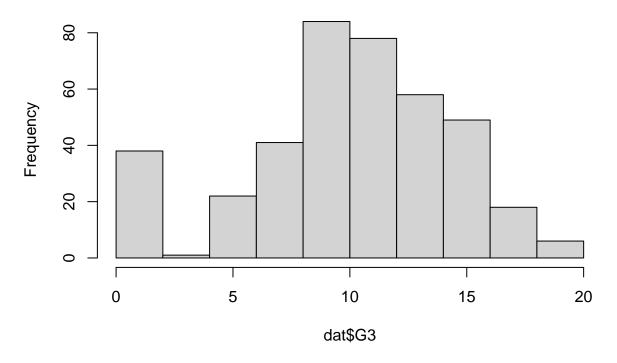
Plot distribution of numeric variables.

# Math Score (Label) Range: 0 - 20

summary(dat\$G3)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.00 8.00 11.00 10.42 14.00 20.00
hist(dat$G3)
```

# Histogram of dat\$G3



# **Regression Models**

### **Baseline models**

```
mod_BL \leftarrow lm(G3 \sim 1, data = dat)
summary(mod_BL)
##
## Call:
## lm(formula = G3 ~ 1, data = dat)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    ЗQ
                                             Max
                                3.5848
## -10.4152 -2.4152
                       0.5848
                                          9.5848
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.4152
                            0.2305
                                     45.18 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.581 on 394 degrees of freedom
Y~Age
mod_age <- lm(G3 ~ age, data = dat)</pre>
summary(mod_age)
##
```

```
## Call:
## lm(formula = G3 ~ age, data = dat)
## Residuals:
       Min
                 1Q
                      Median
                                   3Q
## -11.3992 -1.6588
                     0.3412
                               3.1809
                                        9.5014
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 20.1011
                           2.9928 6.717 6.54e-11 ***
## age
               -0.5801
                           0.1787 -3.246 0.00127 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.527 on 393 degrees of freedom
## Multiple R-squared: 0.02611, Adjusted R-squared: 0.02363
## F-statistic: 10.54 on 1 and 393 DF, p-value: 0.001271
Y~age+sex
mod_age_sex <- lm(G3 ~ age + factor(sex), data = dat)</pre>
summary(mod_age_sex)
##
## Call:
## lm(formula = G3 ~ age + factor(sex), data = dat)
## Residuals:
       Min
                      Median
                                   3Q
                                            Max
                 1Q
## -11.8593 -1.8593
                     0.2806
                               3.1407
                                        9.7571
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            2.9966 6.508 2.33e-10 ***
## (Intercept)
                19.5024
                -0.5700
                            0.1781 -3.200 0.00149 **
## age
## factor(sex)M 0.9065
                            0.4547
                                    1.994 0.04688 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.51 on 392 degrees of freedom
## Multiple R-squared: 0.03588,
                                   Adjusted R-squared: 0.03097
## F-statistic: 7.295 on 2 and 392 DF, p-value: 0.0007751
Model with All Predictors
for (col in 1:ncol(dat)) {
  if (class(dat[, col]) == "character") {
   dat[, col] <- as.factor(dat[, col])</pre>
  }
mod_full \leftarrow lm(G3 \sim ., data = dat)
summary(mod_full)
```

```
##
## Call:
## lm(formula = G3 \sim ., data = dat)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
  -7.9339 -0.5532 0.2680 0.9689
                                     4.6461
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                    -1.115488
                                 2.116958
                                           -0.527 0.598573
                                 0.366512
##
   schoolMS
                      0.480742
                                             1.312 0.190485
##
  sexM
                      0.174396
                                 0.233588
                                            0.747 0.455805
                                 0.100780
## age
                    -0.173302
                                           -1.720 0.086380
                                            0.386 0.699922
## addressU
                      0.104455
                                 0.270791
## famsizeLE3
                      0.036512
                                 0.226680
                                            0.161 0.872128
                    -0.127673
## PstatusT
                                 0.335626
                                           -0.380 0.703875
## Medu
                     0.129685
                                 0.149999
                                            0.865 0.387859
## Fedu
                    -0.133940
                                 0.128768
                                           -1.040 0.298974
## Mjobhealth
                    -0.146426
                                 0.518491
                                            -0.282 0.777796
## Mjobother
                      0.074088
                                 0.332044
                                            0.223 0.823565
                                            0.127 0.898973
## Mjobservices
                      0.046956
                                 0.369587
                                           -0.055 0.956522
## Mjobteacher
                    -0.026276
                                 0.481632
## Fjobhealth
                      0.330948
                                 0.666601
                                             0.496 0.619871
## Fjobother
                    -0.083582
                                 0.476796
                                           -0.175 0.860945
## Fjobservices
                    -0.322142
                                 0.493265
                                           -0.653 0.514130
                                           -0.187 0.851907
## Fjobteacher
                    -0.112364
                                 0.601448
## reasonhome
                    -0.209183
                                 0.256392
                                           -0.816 0.415123
## reasonother
                      0.307554
                                 0.380214
                                            0.809 0.419120
                     0.129106
                                 0.267254
                                            0.483 0.629335
## reasonreputation
## guardianmother
                      0.195741
                                 0.252672
                                            0.775 0.439046
## guardianother
                      0.006565
                                 0.463650
                                            0.014 0.988710
## traveltime
                      0.096994
                                 0.157800
                                            0.615 0.539170
                                            -0.777 0.437667
                    -0.104754
                                 0.134814
## studytime
                    -0.160539
                                 0.161006
                                            -0.997 0.319399
## failures
## schoolsupyes
                     0.456448
                                 0.319538
                                             1.428 0.154043
## famsupyes
                      0.176870
                                 0.224204
                                            0.789 0.430710
                                 0.222100
                                            0.341 0.733211
## paidyes
                     0.075764
                                           -1.680 0.093774 .
## activitiesyes
                    -0.346047
                                 0.205938
## nurseryyes
                    -0.222716
                                 0.254184
                                            -0.876 0.381518
## higheryes
                     0.225921
                                 0.500398
                                            0.451 0.651919
                    -0.144462
                                            -0.502 0.615679
## internetyes
                                 0.287528
## romanticyes
                    -0.272008
                                 0.219732
                                           -1.238 0.216572
                                            3.127 0.001912 **
## famrel
                      0.356876
                                 0.114124
## freetime
                      0.047002
                                 0.110209
                                            0.426 0.670021
                                            0.114 0.909224
## goout
                      0.012007
                                 0.105230
## Dalc
                    -0.185019
                                 0.153124
                                           -1.208 0.227741
## Walc
                      0.176772
                                 0.114943
                                             1.538 0.124966
## health
                      0.062995
                                 0.074800
                                            0.842 0.400259
## absences
                      0.045879
                                 0.013412
                                             3.421 0.000698 ***
## G1
                      0.188847
                                 0.062373
                                             3.028 0.002645 **
## G2
                      0.957330
                                 0.053460
                                           17.907 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 1.901 on 353 degrees of freedom
## Multiple R-squared: 0.8458, Adjusted R-squared: 0.8279
## F-statistic: 47.21 on 41 and 353 DF, p-value: < 2.2e-16</pre>
```

# **Model Selection: Step-wise AIC**

### **Additive Terms Only**

Start from the full model. Run stepAIC by going "backward". You can also use the baseline model and go "forward" or use any model and go with "both" directions.

```
stepAIC(mod_full, scope = . ~ 1, direction = "backward")
## Start: AIC=547.02
## G3 ~ school + sex + age + address + famsize + Pstatus + Medu +
      Fedu + Mjob + Fjob + reason + guardian + traveltime + studytime +
##
      failures + schoolsup + famsup + paid + activities + nursery +
      higher + internet + romantic + famrel + freetime + goout +
##
##
      Dalc + Walc + health + absences + G1 + G2
##
               Df Sum of Sq
                              RSS
                                    AIC
## - Mjob
                      1.18 1276.7 539.39
## - Fjob
               4
                      7.60 1283.1 541.37
## - reason
               3
                      8.85 1284.3 543.75
## - guardian 2
                      2.57 1278.1 543.82
              1
                      0.05 1275.5 545.04
## - goout
                    0.09 1275.6 545.05
## - famsize
              1
## - paid
              1
                    0.42 1275.9 545.15
## - Pstatus
              1
                    0.52 1276.0 545.19
## - address 1 0.54 1276.0 545.19
## - freetime 1 0.66 1276.2 545.23
## - higher
                      0.74 1276.2 545.25
## - internet 1
                      0.91 1276.4 545.31
## - traveltime 1
                      1.37 1276.9 545.45
## - sex 1
                      2.01 1277.5 545.65
                      2.18 1277.7 545.70
## - studytime 1
## - famsup
                     2.25 1277.8 545.72
              1
## - health
                      2.56 1278.1 545.82
               1
## - Medu
              1
                      2.70 1278.2 545.86
## - nursery
              1
                      2.77 1278.3 545.88
## - failures 1
                      3.59 1279.1 546.14
## - Fedu
              1
                      3.91 1279.4 546.23
## - Dalc
              1
                    5.28 1280.8 546.65
## - romantic 1 5.54 1281.0 546.74
## - school 1 6.22 1281.7 546.94
## <none>
                           1275.5 547.02
## - schoolsup 1 7.37 1282.9 547.30
## - Walc 1
                      8.55 1284.0 547.66
## - activities 1
                     10.20 1285.7 548.17
## - age 1 10.68 1286.2 548.32
## - G1
              1
                   33.12 1308.6 555.15
## - famrel
              1
                    35.33 1310.8 555.82
                   42.28 1317.8 557.91
## - absences
              1
## - G2
        1 1158.72 2434.2 800.31
```

```
##
## Step: AIC=539.39
## G3 ~ school + sex + age + address + famsize + Pstatus + Medu +
       Fedu + Fjob + reason + guardian + traveltime + studytime +
       failures + schoolsup + famsup + paid + activities + nursery +
##
      higher + internet + romantic + famrel + freetime + goout +
##
      Dalc + Walc + health + absences + G1 + G2
##
##
                Df Sum of Sq
                                RSS
                                        AIC
                        7.59 1284.3 533.73
## - Fjob
## - reason
                 3
                        8.73 1285.4 536.08
                        2.61 1279.3 536.20
## - guardian
                 2
## - goout
                        0.05 1276.7 537.40
                 1
## - famsize
                 1
                        0.06 1276.8 537.41
## - paid
                        0.36 1277.0 537.50
                 1
## - address
                 1
                        0.56 1277.2 537.56
## - freetime
                        0.65 1277.3 537.59
                 1
## - Pstatus
                        0.67 1277.4 537.60
                        0.76 1277.5 537.63
## - higher
                 1
## - internet
                 1
                        0.99 1277.7 537.70
## - traveltime 1
                        1.41 1278.1 537.83
## - studytime
                        1.96 1278.7 538.00
## - famsup
                        2.01 1278.7 538.01
                 1
## - sex
                        2.20 1278.9 538.07
                 1
## - health
                 1
                        2.54 1279.2 538.18
## - Medu
                 1
                        2.76 1279.5 538.24
## - nursery
                        2.91 1279.6 538.29
                 1
                        3.72 1280.4 538.54
## - failures
                 1
## - Fedu
                        3.82 1280.5 538.57
                 1
## - Dalc
                        4.64 1281.3 538.82
                 1
## - romantic
                 1
                        5.53 1282.2 539.10
## - school
                        6.33 1283.0 539.34
## <none>
                             1276.7 539.39
## - schoolsup
                        7.83 1284.5 539.81
                1
## - Walc
                 1
                        7.90 1284.6 539.83
## - activities 1
                       10.48 1287.2 540.62
## - age
                       10.70 1287.4 540.69
## - G1
                       32.86 1309.5 547.43
                 1
## - famrel
                 1
                       36.93 1313.6 548.65
## - absences
                       44.45 1321.1 550.91
                 1
## - G2
                    1177.44 2454.1 795.52
##
## Step: AIC=533.73
## G3 ~ school + sex + age + address + famsize + Pstatus + Medu +
       Fedu + reason + guardian + traveltime + studytime + failures +
       schoolsup + famsup + paid + activities + nursery + higher +
##
       internet + romantic + famrel + freetime + goout + Dalc +
##
       Walc + health + absences + G1 + G2
##
                Df Sum of Sq
                                RSS
                 3
                        9.66 1294.0 530.69
## - reason
                 2
## - guardian
                        3.16 1287.4 530.70
## - goout
                 1
                        0.12 1284.4 531.77
## - famsize
                 1
                        0.16 1284.4 531.78
```

```
## - paid
          1
                      0.46 1284.8 531.88
## - address
                      0.51 1284.8 531.89
                      0.98 1285.3 532.03
## - Pstatus
                      0.98 1285.3 532.03
## - freetime
                1
## - higher
                1
                      1.09 1285.4 532.07
## - traveltime 1
                    1.51 1285.8 532.20
## - internet
                     1.60 1285.9 532.22
                1
## - studytime 1
                    1.84 1286.1 532.30
                      2.44 1286.7 532.48
## - sex
                1
## - famsup
                1
                      2.47 1286.8 532.49
                      2.81 1287.1 532.60
## - Medu
                1
## - nursery
                      3.21 1287.5 532.72
                1
## - health
                1
                      3.47 1287.8 532.80
## - Fedu
                     4.01 1288.3 532.96
               1
## - failures
                    4.12 1288.4 533.00
              1
                    5.23 1289.5 533.34
## - school
               1
## - Dalc
                      5.45 1289.7 533.40
              1
## - romantic 1
                      5.54 1289.8 533.43
## <none>
                           1284.3 533.73
## - Walc
                      7.11 1291.4 533.91
                      9.10 1293.4 534.52
## - schoolsup
              1
                   10.65 1294.9 534.99
## - age
                1
                    12.66 1297.0 535.61
## - activities 1
## - famrel
                     34.67 1319.0 542.26
                1
## - G1
                    36.47 1320.8 542.79
                1
## - absences
                1
                    44.08 1328.4 545.06
## - G2
                  1190.12 2474.4 790.77
                1
## Step: AIC=530.69
## G3 ~ school + sex + age + address + famsize + Pstatus + Medu +
##
      Fedu + guardian + traveltime + studytime + failures + schoolsup +
##
      famsup + paid + activities + nursery + higher + internet +
##
      romantic + famrel + freetime + goout + Dalc + Walc + health +
##
      absences + G1 + G2
##
##
              Df Sum of Sq
                              RSS
## - guardian
              2 3.26 1297.2 527.69
## - goout
                      0.06 1294.0 528.71
               1
## - address
                1
                      0.08 1294.0 528.72
## - famsize
                      0.16 1294.1 528.74
               1
## - paid
                      0.49 1294.4 528.84
               1
## - higher
              1
                      0.50 1294.4 528.85
                      0.88 1294.8 528.96
## - Pstatus
                1
## - freetime
                    1.46 1295.4 529.14
                1
## - sex
                      1.47 1295.4 529.14
                1
                    1.50 1295.4 529.15
## - traveltime 1
## - internet
                1
                      1.75 1295.7 529.23
## - studytime
                      1.77 1295.7 529.23
## - famsup
                1
                      2.46 1296.4 529.44
## - health
                1
                     2.94 1296.9 529.59
## - nursery
                     3.23 1297.2 529.68
                1
## - Medu
              1
                    3.66 1297.6 529.81
## - Fedu
              1
                     4.35 1298.3 530.02
## - failures
                   4.75 1298.7 530.14
             1
```

```
5.22 1299.2 530.28
## - Dalc
## - school
                       5.28 1299.2 530.30
                1
## - romantic 1
                       5.41 1299.3 530.34
## <none>
                            1294.0 530.69
## - Walc
                1
                       7.59 1301.5 531.00
## - schoolsup 1
                       9.16 1303.1 531.48
                    10.84 1304.8 531.99
## - age
                1
                    11.28 1305.2 532.12
## - activities 1
## - famrel
                1
                      35.01 1329.0 539.24
## - G1
                1
                    36.35 1330.3 539.64
## - absences
                1
                     43.30 1337.2 541.70
                   1210.19 2504.1 789.49
## - G2
                1
## Step: AIC=527.69
## G3 ~ school + sex + age + address + famsize + Pstatus + Medu +
       Fedu + traveltime + studytime + failures + schoolsup + famsup +
##
      paid + activities + nursery + higher + internet + romantic +
##
      famrel + freetime + goout + Dalc + Walc + health + absences +
##
      G1 + G2
##
##
               Df Sum of Sq
                               RSS
                                      AIC
## - address
                       0.00 1297.2 525.69
## - famsize
                       0.21 1297.4 525.75
                1
## - goout
                       0.22 1297.4 525.75
                1
                       0.33 1297.5 525.79
## - higher
                1
                       0.63 1297.8 525.88
## - paid
                1
## - Pstatus
                       1.07 1298.3 526.01
                1
                       1.09 1298.3 526.02
## - traveltime 1
## - freetime
                     1.28 1298.5 526.07
              1
## - sex
                1
                     1.32 1298.5 526.09
## - internet
                1
                     1.87 1299.1 526.26
## - studytime
               1
                       2.19 1299.4 526.35
## - famsup
                       2.27 1299.5 526.38
## - nursery
                       2.76 1300.0 526.53
                1
## - health
                1
                      2.89 1300.1 526.57
                     5.03 1302.2 527.22
## - Medu
                1
## - school
               1
                     5.25 1302.5 527.28
## - romantic 1
                     5.66 1302.9 527.40
## - Dalc
                1
                       5.70 1302.9 527.42
## - Fedu
                       6.15 1303.3 527.55
               1
## - failures 1
                       6.42 1303.6 527.64
## <none>
                            1297.2 527.69
## - Walc
                       7.85 1305.0 528.07
                1
## - schoolsup
                       8.88 1306.1 528.38
              1
## - activities 1
                    11.11 1308.3 529.06
## - age
                     14.39 1311.6 530.04
                1
## - famrel
                1
                      34.83 1332.0 536.15
## - G1
                    36.97 1334.2 536.79
                1
## - absences
                1
                     44.05 1341.2 538.88
                   1207.82 2505.0 785.63
## - G2
                1
##
## Step: AIC=525.69
## G3 ~ school + sex + age + famsize + Pstatus + Medu + Fedu + traveltime +
      studytime + failures + schoolsup + famsup + paid + activities +
```

```
##
       nursery + higher + internet + romantic + famrel + freetime +
##
       goout + Dalc + Walc + health + absences + G1 + G2
##
##
                Df Sum of Sq
                                RSS
                                       AIC
## - famsize
                1
                        0.21 1297.4 523.75
                        0.23 1297.4 523.76
## - goout
                1
## - higher
                        0.33 1297.5 523.79
                 1
                        0.63 1297.8 523.88
## - paid
                 1
                        1.07 1298.3 524.01
## - Pstatus
                 1
## - traveltime 1
                       1.16 1298.4 524.04
                        1.28 1298.5 524.07
## - freetime
                 1
                       1.33 1298.5 524.09
## - sex
                 1
## - internet
                 1
                        1.92 1299.1 524.27
                        2.22 1299.4 524.36
## - studytime
                 1
## - famsup
                        2.27 1299.5 524.38
                 1
## - nursery
                 1
                        2.76 1300.0 524.53
## - health
                        2.89 1300.1 524.57
                 1
## - Medu
                        5.04 1302.2 525.22
## - school
                        5.49 1302.7 525.35
                1
## - romantic
                1
                        5.66 1302.9 525.41
## - Dalc
                 1
                        5.70 1302.9 525.42
## - Fedu
                        6.16 1303.4 525.56
                 1
## - failures
                        6.42 1303.6 525.64
                1
## <none>
                             1297.2 525.69
## - Walc
                        7.91 1305.1 526.09
                 1
                        8.88 1306.1 526.38
## - schoolsup
                1
## - activities 1
                       11.22 1308.4 527.09
                       14.40 1311.6 528.05
## - age
                 1
## - famrel
                 1
                       34.84 1332.0 534.16
                      37.04 1334.2 534.81
## - G1
                 1
## - absences
                 1
                     44.30 1341.5 536.95
## - G2
                    1214.11 2511.3 784.62
##
## Step: AIC=523.75
## G3 ~ school + sex + age + Pstatus + Medu + Fedu + traveltime +
       studytime + failures + schoolsup + famsup + paid + activities +
##
       nursery + higher + internet + romantic + famrel + freetime +
##
       goout + Dalc + Walc + health + absences + G1 + G2
##
##
                Df Sum of Sq
                                RSS
                                       AIC
                       0.23 1297.6 521.82
## - goout
                1
## - higher
                        0.34 1297.8 521.85
                 1
                        0.63 1298.0 521.94
## - paid
                 1
                        1.20 1298.6 522.12
## - traveltime 1
## - Pstatus
                        1.25 1298.7 522.13
                 1
## - freetime
                        1.27 1298.7 522.14
                 1
## - sex
                 1
                        1.37 1298.8 522.17
## - internet
                       1.89 1299.3 522.33
                 1
## - famsup
                 1
                        2.20 1299.6 522.42
## - studytime
                1
                        2.29 1299.7 522.45
## - nursery
                        2.62 1300.0 522.55
                 1
## - health
                 1
                        2.85 1300.3 522.62
## - Medu
                 1
                      4.96 1302.4 523.26
## - school
                       5.58 1303.0 523.45
               1
```

```
## - romantic
                       5.59 1303.0 523.45
## - Dalc
                       5.63 1303.0 523.46
                1
## - Fedu
                       6.30 1303.7 523.66
                1
## - failures
                       6.50 1303.9 523.73
              1
## <none>
                            1297.4 523.75
## - Walc
                       8.03 1305.5 524.19
                1
## - schoolsup 1
                       8.90 1306.3 524.45
                     11.13 1308.5 525.13
## - activities 1
                      14.36 1311.8 526.10
## - age
                1
## - famrel
                1
                      34.81 1332.2 532.21
                      37.12 1334.5 532.89
## - G1
                1
                      44.34 1341.8 535.03
## - absences
                1
                    1216.66 2514.1 783.06
                1
##
## Step: AIC=521.82
## G3 ~ school + sex + age + Pstatus + Medu + Fedu + traveltime +
##
       studytime + failures + schoolsup + famsup + paid + activities +
##
       nursery + higher + internet + romantic + famrel + freetime +
##
      Dalc + Walc + health + absences + G1 + G2
##
               Df Sum of Sq
                               RSS
##
                                       AIC
## - higher
                       0.35 1298.0 519.93
                       0.61 1298.3 520.01
## - paid
                1
## - traveltime 1
                       1.20 1298.8 520.19
## - Pstatus
                       1.26 1298.9 520.20
               1
## - sex
                1
                       1.29 1298.9 520.21
## - freetime
                       1.65 1299.3 520.32
                1
                       1.81 1299.5 520.37
## - internet
                1
## - famsup
                       2.17 1299.8 520.48
                1
## - studytime
                       2.22 1299.9 520.50
                1
## - nursery
                1
                       2.55 1300.2 520.59
## - health
                1
                       2.75 1300.4 520.66
## - Medu
                1
                       5.17 1302.8 521.39
## - school
                       5.46 1303.1 521.48
                1
## - romantic
                1
                       5.65 1303.3 521.54
## - Dalc
                       5.73 1303.4 521.56
                1
## - Fedu
               1
                       6.24 1303.9 521.72
## - failures
                       6.42 1304.1 521.77
                1
## <none>
                             1297.6 521.82
                       8.88 1306.5 522.51
## - schoolsup 1
## - Walc
                      10.43 1308.1 522.98
                1
## - activities 1
                      11.02 1308.7 523.16
                      14.14 1311.8 524.10
## - age
                1
## - famrel
                      35.48 1333.1 530.47
                1
## - G1
                      37.06 1334.7 530.94
                1
## - absences
                     44.14 1341.8 533.03
                1
## - G2
                    1221.43 2519.1 781.84
##
## Step: AIC=519.93
## G3 ~ school + sex + age + Pstatus + Medu + Fedu + traveltime +
##
      studytime + failures + schoolsup + famsup + paid + activities +
##
      nursery + internet + romantic + famrel + freetime + Dalc +
##
      Walc + health + absences + G1 + G2
##
```

```
Df Sum of Sq
                             RSS AIC
## - paid
                       0.73 1298.7 518.15
                1
## - sex
                       1.14 1299.1 518.27
                       1.15 1299.1 518.28
## - traveltime 1
## - Pstatus
                1
                       1.33 1299.3 518.33
## - freetime
                       1.63 1299.6 518.42
                1
## - internet
                 1
                       1.85 1299.8 518.49
## - studytime
                      2.11 1300.1 518.57
                 1
## - famsup
                 1
                       2.19 1300.2 518.59
## - nursery
                 1
                       2.57 1300.6 518.71
## - health
                 1
                       2.81 1300.8 518.78
## - Medu
                       5.28 1303.3 519.53
                 1
## - Dalc
                1
                       5.65 1303.6 519.64
## - school
                       5.73 1303.7 519.67
                1
## - romantic
                     5.97 1304.0 519.74
                1
## - Fedu
                       6.13 1304.1 519.79
## <none>
                             1298.0 519.93
                      7.05 1305.0 520.07
## - failures
## - schoolsup
                       8.93 1306.9 520.64
                1
## - Walc
                 1
                      10.40 1308.4 521.08
                     10.76 1308.8 521.19
## - activities 1
## - age
                1
                     15.08 1313.1 522.49
## - famrel
                     35.70 1333.7 528.64
                1
## - G1
                      37.71 1335.7 529.24
                1
## - absences
                      44.06 1342.0 531.11
                 1
## - G2
                 1
                   1221.11 2519.1 779.85
##
## Step: AIC=518.15
## G3 ~ school + sex + age + Pstatus + Medu + Fedu + traveltime +
       studytime + failures + schoolsup + famsup + activities +
##
       nursery + internet + romantic + famrel + freetime + Dalc +
##
       Walc + health + absences + G1 + G2
##
               Df Sum of Sq
##
                             RSS
                       0.97 1299.7 516.45
## - sex
                       1.06 1299.8 516.47
## - traveltime 1
## - Pstatus
                1
                       1.22 1300.0 516.52
## - freetime
                 1
                       1.50 1300.2 516.60
## - internet
                 1
                       1.66 1300.4 516.65
## - studytime
                       1.92 1300.6 516.73
                 1
## - nursery
                       2.35 1301.1 516.86
                1
## - health
                       2.66 1301.4 516.96
                 1
                       3.14 1301.9 517.10
## - famsup
                1
## - Dalc
                       5.44 1304.2 517.80
                 1
## - Medu
                       5.63 1304.4 517.86
                 1
## - school
                       5.95 1304.7 517.95
                 1
                       5.95 1304.7 517.96
## - romantic
                1
## - Fedu
                       6.40 1305.1 518.09
## <none>
                            1298.7 518.15
                       7.86 1306.6 518.53
## - failures
## - schoolsup
                       8.68 1307.4 518.78
                1
## - activities 1
                     10.87 1309.6 519.44
## - Walc
                 1
                     11.14 1309.9 519.53
## - age
                1
                     14.99 1313.7 520.68
```

```
## - famrel
              1 36.22 1334.9 527.01
## - G1
                      37.08 1335.8 527.27
                1
## - absences
                1
                    43.75 1342.5 529.24
## - G2
                1 1239.93 2538.7 780.90
## Step: AIC=516.45
## G3 ~ school + age + Pstatus + Medu + Fedu + traveltime + studytime +
      failures + schoolsup + famsup + activities + nursery + internet +
##
      romantic + famrel + freetime + Dalc + Walc + health + absences +
##
      G1 + G2
##
##
               Df Sum of Sq
                               RSS
                                      AIC
                       1.17 1300.9 514.80
## - traveltime 1
## - Pstatus
               1
                       1.20 1300.9 514.81
## - internet
                1
                       1.54 1301.2 514.91
## - freetime
                1
                       1.85 1301.5 515.01
                       2.25 1302.0 515.13
## - nursery
                1
## - famsup
                1
                       2.77 1302.5 515.29
## - studytime 1
                       2.86 1302.5 515.31
## - health
                1
                       3.08 1302.8 515.38
## - Dalc
                1
                       4.98 1304.7 515.96
## - school
                1
                     5.67 1305.4 516.17
## - Medu
                     6.13 1305.8 516.31
                1
## - romantic
                       6.43 1306.1 516.39
                1
## - Fedu
                       6.59 1306.3 516.44
                1
## <none>
                            1299.7 516.45
## - failures
              1
                       7.67 1307.4 516.77
                       8.21 1307.9 516.93
## - schoolsup
               1
## - activities 1
                    10.27 1310.0 517.56
## - Walc
                1
                    11.92 1311.6 518.05
## - age
                1
                    15.11 1314.8 519.01
## - famrel
                1
                      36.95 1336.7 525.52
## - G1
               1
                    37.72 1337.4 525.75
## - absences
                     42.86 1342.6 527.26
              1
                   1242.31 2542.0 779.42
## - G2
                1
##
## Step: AIC=514.8
## G3 ~ school + age + Pstatus + Medu + Fedu + studytime + failures +
      schoolsup + famsup + activities + nursery + internet + romantic +
      famrel + freetime + Dalc + Walc + health + absences + G1 +
##
##
##
               Df Sum of Sq
                             RSS
## - Pstatus
                       1.20 1302.1 513.17
                1
## - freetime
                       1.65 1302.5 513.30
                1
                       1.69 1302.6 513.32
## - internet
                1
## - nursery
                1
                       2.15 1303.0 513.45
## - health
                       2.99 1303.9 513.71
                1
## - studytime
               1
                       3.11 1304.0 513.74
## - famsup
                1
                       3.12 1304.0 513.75
## - Dalc
                       4.67 1305.5 514.22
                1
## - Medu
                1
                       5.86 1306.7 514.58
## - romantic
                1
                       6.38 1307.2 514.73
## <none>
                            1300.9 514.80
```

```
## - Fedu
                       7.24 1308.1 515.00
## - school
                       7.32 1308.2 515.02
                 1
## - failures
                       7.59 1308.5 515.10
                       8.30 1309.2 515.31
## - schoolsup
                 1
## - activities 1
                       9.89 1310.8 515.79
## - Walc
                     12.47 1313.3 516.57
                 1
## - age
                     15.89 1316.8 517.60
                 1
## - famrel
                       37.31 1338.2 523.97
                 1
                       39.82 1340.7 524.71
## - G1
                 1
## - absences
                 1
                      42.93 1343.8 525.63
                 1
                   1257.83 2558.7 780.01
##
## Step: AIC=513.17
## G3 ~ school + age + Medu + Fedu + studytime + failures + schoolsup +
      famsup + activities + nursery + internet + romantic + famrel +
##
      freetime + Dalc + Walc + health + absences + G1 + G2
##
##
                Df Sum of Sq
                                RSS
## - freetime
                       1.60 1303.7 511.65
                1
## - nursery
                1
                        1.97 1304.0 511.76
## - internet
                1
                        2.06 1304.1 511.79
## - health
                 1
                       2.92 1305.0 512.05
## - famsup
                       2.93 1305.0 512.05
                 1
## - studytime
                       3.14 1305.2 512.12
                1
## - Dalc
                 1
                       4.49 1306.5 512.52
## - romantic
                1
                        6.15 1308.2 513.03
## - Medu
                        6.34 1308.4 513.08
                 1
                             1302.1 513.17
## <none>
## - Fedu
                 1
                       7.06 1309.1 513.30
                       7.14 1309.2 513.33
## - school
                 1
## - failures
                 1
                       7.39 1309.5 513.40
## - schoolsup
                 1
                        8.48 1310.5 513.73
## - activities 1
                       10.80 1312.9 514.43
                      12.21 1314.3 514.85
## - Walc
                 1
## - age
                 1
                       16.23 1318.3 516.06
## - famrel
                      37.32 1339.4 522.33
                 1
## - G1
                 1
                     39.35 1341.4 522.93
## - absences
                     45.40 1347.5 524.70
                 1
## - G2
                    1265.76 2567.8 779.41
##
## Step: AIC=511.65
## G3 ~ school + age + Medu + Fedu + studytime + failures + schoolsup +
      famsup + activities + nursery + internet + romantic + famrel +
##
      Dalc + Walc + health + absences + G1 + G2
##
##
                Df Sum of Sq
                                RSS
                                       AIC
## - internet
                 1
                        1.89 1305.5 510.22
                        1.94 1305.6 510.24
## - nursery
                 1
## - health
                 1
                        3.06 1306.7 510.58
## - famsup
                 1
                        3.18 1306.8 510.61
## - studytime
                        3.79 1307.5 510.80
                 1
## - Dalc
                 1
                        3.82 1307.5 510.81
## - romantic
                 1
                        6.19 1309.8 511.52
## <none>
                             1303.7 511.65
```

```
6.75 1310.4 511.69
## - Medu
               1
## - failures
                       6.89 1310.6 511.73
                1
## - school
                1
                       7.35 1311.0 511.87
                       7.53 1311.2 511.92
## - Fedu
                 1
## - schoolsup
                1
                       8.37 1312.0 512.18
## - activities 1
                     10.01 1313.7 512.67
## - Walc
                1
                     12.44 1316.1 513.40
                      16.39 1320.1 514.59
## - age
                 1
## - G1
                 1
                      40.81 1344.5 521.83
## - famrel
                 1
                      41.09 1344.8 521.91
## - absences
                1
                       44.23 1347.9 522.83
## - G2
                   1264.31 2568.0 777.44
                 1
##
## Step: AIC=510.22
## G3 ~ school + age + Medu + Fedu + studytime + failures + schoolsup +
##
       famsup + activities + nursery + romantic + famrel + Dalc +
##
       Walc + health + absences + G1 + G2
##
               Df Sum of Sq
##
                               RSS
## - nursery
                1
                    1.78 1307.3 508.76
## - famsup
                1
                       2.92 1308.5 509.10
## - health
                1
                       3.54 1309.1 509.29
## - studytime
                       4.01 1309.6 509.43
                1
## - Dalc
                1
                       4.06 1309.6 509.45
## - Medu
                1
                        6.11 1311.7 510.06
## <none>
                             1305.5 510.22
## - failures
              1
                        6.99 1312.5 510.33
                       7.01 1312.6 510.34
## - romantic
                1
## - Fedu
                1
                       7.63 1313.2 510.52
## - school
                 1
                       7.92 1313.5 510.61
## - schoolsup
                 1
                       8.75 1314.3 510.86
## - activities 1
                       10.13 1315.7 511.28
## - Walc
                 1
                      12.36 1317.9 511.94
## - age
                      15.57 1321.1 512.91
                 1
## - famrel
                 1
                       40.11 1345.7 520.17
## - G1
                      42.19 1347.8 520.78
                 1
## - absences
                1
                     43.07 1348.6 521.04
## - G2
                 1
                    1267.44 2573.0 776.21
##
## Step: AIC=508.76
## G3 ~ school + age + Medu + Fedu + studytime + failures + schoolsup +
##
      famsup + activities + romantic + famrel + Dalc + Walc + health +
##
       absences + G1 + G2
##
                Df Sum of Sq
                                RSS
                        2.94 1310.3 507.65
## - famsup
                1
## - health
                1
                        3.54 1310.9 507.83
## - Dalc
                        3.89 1311.2 507.93
                 1
## - studytime
                1
                        4.25 1311.6 508.04
## - Medu
                 1
                        5.49 1312.8 508.41
## <none>
                             1307.3 508.76
## - failures
                        6.81 1314.1 508.81
## - romantic
                1
                       7.22 1314.6 508.94
## - Fedu
                       7.97 1315.3 509.16
                 1
```

```
## - school 1
                       8.25 1315.6 509.25
                      8.48 1315.8 509.31
## - schoolsup 1
## - activities 1
                      9.82 1317.2 509.72
                     12.69 1320.0 510.57
## - Walc
                1
## - age
                1
                      15.40 1322.7 511.39
## - famrel
                    40.31 1347.7 518.76
                1
## - G1
                     42.09 1349.4 519.28
                1
## - absences
                    42.86 1350.2 519.50
                1
## - G2
                   1267.41 2574.8 774.48
##
## Step: AIC=507.65
## G3 ~ school + age + Medu + Fedu + studytime + failures + schoolsup +
      activities + romantic + famrel + Dalc + Walc + health + absences +
##
      G1 + G2
##
##
               Df Sum of Sq
                             RSS
                                      AIC
## - studytime
                       3.34 1313.6 506.65
                1
## - Dalc
                       3.64 1313.9 506.74
## - health
                       3.77 1314.0 506.78
                1
## - Medu
                1
                       6.13 1316.4 507.49
## <none>
                            1310.3 507.65
## - failures
                       6.88 1317.2 507.72
## - Fedu
                       7.01 1317.3 507.75
                1
## - romantic
                       7.16 1317.4 507.80
                1
## - school
                1
                       7.36 1317.6 507.86
## - schoolsup 1
                      8.77 1319.0 508.28
## - activities 1
                    10.44 1320.7 508.78
                    11.93 1322.2 509.23
## - Walc
                1
## - age
                1
                    16.22 1326.5 510.51
## - famrel
                1
                    39.68 1350.0 517.43
                     40.55 1350.8 517.69
## - G1
                1
## - absences
                1
                     43.39 1353.7 518.51
## - G2
                1
                  1267.34 2577.6 772.91
##
## Step: AIC=506.65
## G3 ~ school + age + Medu + Fedu + failures + schoolsup + activities +
##
      romantic + famrel + Dalc + Walc + health + absences + G1 +
##
##
##
               Df Sum of Sq
                               RSS
                                      AIC
                   3.40 1317.0 505.67
## - Dalc
               1
## - health
                       4.03 1317.6 505.86
                1
## - Medu
                       5.61 1319.2 506.33
                1
## - failures
                       5.84 1319.5 506.40
                1
## - Fedu
                1
                       6.22 1319.8 506.52
## <none>
                            1313.6 506.65
                       7.92 1321.5 507.03
## - romantic
                1
## - schoolsup
               1
                       8.09 1321.7 507.08
## - school
                1
                       8.42 1322.0 507.18
## - activities 1
                      11.31 1324.9 508.04
## - Walc
                    14.02 1327.6 508.84
                1
## - age
                1
                    17.96 1331.6 510.02
## - G1
                1
                    39.40 1353.0 516.33
## - famrel
              1 39.69 1353.3 516.41
```

```
## - absences
              1 45.29 1358.9 518.04
## - G2
                1 1267.13 2580.8 771.39
##
## Step: AIC=505.67
## G3 ~ school + age + Medu + Fedu + failures + schoolsup + activities +
      romantic + famrel + Walc + health + absences + G1 + G2
##
##
               Df Sum of Sq
                             RSS
                                   AIC
## - health
                1
                       3.74 1320.8 504.80
## - Medu
                      4.83 1321.8 505.12
                1
## - Fedu
                1
                       5.97 1323.0 505.46
                       6.35 1323.4 505.57
## - failures
                1
## <none>
                           1317.0 505.67
## - schoolsup
                       7.34 1324.3 505.87
              1
## - school
                      7.59 1324.6 505.94
                1
## - romantic
                1
                       8.02 1325.0 506.07
## - activities 1
                   10.73 1327.7 506.88
## - Walc
             1
                    11.05 1328.1 506.97
## - age
                    18.76 1335.8 509.26
                1
## - G1
                1
                     39.42 1356.4 515.32
## - famrel
              1
                    39.75 1356.8 515.42
## - absences
              1
                    44.98 1362.0 516.94
## - G2
                1 1266.03 2583.0 769.75
##
## Step: AIC=504.8
## G3 ~ school + age + Medu + Fedu + failures + schoolsup + activities +
      romantic + famrel + Walc + absences + G1 + G2
##
##
               Df Sum of Sq
                               RSS
                                     AIC
                       4.32 1325.1 504.08
## - Medu
                1
                       5.46 1326.2 504.42
## - Fedu
                1
## - failures
                1
                       5.88 1326.6 504.55
## <none>
                            1320.8 504.80
## - schoolsup
                       6.72 1327.5 504.80
               1
## - school
                1
                       7.35 1328.1 504.99
## - romantic
                1
                      7.62 1328.4 505.07
## - activities 1
                    10.49 1331.2 505.92
## - Walc
                1
                    12.51 1333.3 506.52
## - age
                1
                     20.67 1341.4 508.93
## - G1
                    39.86 1360.6 514.54
                1
## - famrel
                    43.03 1363.8 515.46
               1
## - absences
               1
                    44.39 1365.2 515.85
## - G2
                   1262.31 2583.1 767.75
                1
##
## Step: AIC=504.08
## G3 ~ school + age + Fedu + failures + schoolsup + activities +
      romantic + famrel + Walc + absences + G1 + G2
##
               Df Sum of Sq RSS
## - Fedu
               1
                      1.89 1327.0 502.65
## - schoolsup
                       5.75 1330.8 503.79
               1
## - failures
                1
                       6.51 1331.6 504.02
## - school
                1
                       6.63 1331.7 504.06
## <none>
                            1325.1 504.08
```

```
7.08 1332.2 504.19
10.05 1335.1 505.07
## - romantic 1
## - activities 1
## - Walc
           1
                    11.84 1336.9 505.60
## - age
                      21.91 1347.0 508.56
                1
## - G1
                1
                      38.75 1363.8 513.47
## - famrel
                     43.04 1368.1 514.71
                1
## - absences
                    48.54 1373.6 516.30
                1
## - G2
                1 1288.29 2613.4 770.36
##
## Step: AIC=502.65
## G3 ~ school + age + failures + schoolsup + activities + romantic +
##
      famrel + Walc + absences + G1 + G2
##
               Df Sum of Sq
##
                               RSS
                       5.49 1332.5 502.28
## - schoolsup
                1
## - failures
                1
                       5.50 1332.5 502.28
                       6.71 1333.7 502.64
## - school
                1
## <none>
                            1327.0 502.65
## - romantic 1
                       7.46 1334.4 502.86
## - activities 1
                      10.85 1337.8 503.86
## - Walc
                1
                     11.42 1338.4 504.03
## - age
                1
                    20.86 1347.8 506.81
## - G1
                    37.46 1364.4 511.64
                1
## - famrel
                     43.08 1370.0 513.27
                1
## - absences
              1
                     47.77 1374.7 514.62
## - G2
                1 1293.22 2620.2 769.38
##
## Step: AIC=502.28
## G3 ~ school + age + failures + activities + romantic + famrel +
      Walc + absences + G1 + G2
##
##
               Df Sum of Sq
                             RSS
                                      AIC
## - failures
                      5.54 1338.0 501.92
## - school
                       6.32 1338.8 502.14
                1
## <none>
                            1332.5 502.28
## - romantic
                       8.16 1340.6 502.69
                1
## - Walc
              1
                      9.94 1342.4 503.21
## - activities 1
                    10.38 1342.8 503.34
## - age
                1
                      26.72 1359.2 508.12
## - G1
                    33.28 1365.7 510.02
                1
## - famrel
                    43.34 1375.8 512.92
                1
## - absences
                     50.61 1383.1 515.00
                1
                   1315.78 2648.2 771.59
## - G2
                1
##
## Step: AIC=501.92
## G3 ~ school + age + activities + romantic + famrel + Walc + absences +
##
      G1 + G2
##
               Df Sum of Sq
##
                             RSS
                                      AIC
## <none>
                            1338.0 501.92
## - school
                       6.90 1344.9 501.95
                1
## - romantic
              1
                       8.72 1346.7 502.48
## - Walc
                1
                       8.82 1346.8 502.51
## - activities 1
                       9.90 1347.9 502.83
```

```
## - age
                   33.30 1371.3 509.63
              1
## - G1
                      37.24 1375.2 510.76
                1
## - famrel
                1
                    44.94 1382.9 512.96
## - absences
                    50.88 1388.9 514.66
              1
                1 1336.04 2674.0 773.42
##
## Call:
## lm(formula = G3 ~ school + age + activities + romantic + famrel +
      Walc + absences + G1 + G2, data = dat)
##
## Coefficients:
                                         age activitiesyes
##
     (Intercept)
                      schoolMS
                                                               romanticves
##
        0.65012
                       0.45495
                                    -0.26017
                                                   -0.32049
                                                                  -0.32668
##
         famrel
                          Walc
                                    absences
                                                         G1
                                                                       G2
        0.38361
                                     0.04714
                                                    0.18058
##
                       0.11979
                                                                   0.96153
This is the selected model. It has the lowest AIC score (best prediction performance).
mod_lowest_AIC <- lm(G3 ~ school + age + activities + romantic + famrel + Walc +
                    absences + G1 + G2, data = dat)
summary(mod_lowest_AIC)
##
## Call:
## lm(formula = G3 ~ school + age + activities + romantic + famrel +
      Walc + absences + G1 + G2, data = dat)
##
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
## -8.8416 -0.4534 0.2645 1.0247 4.0315
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 0.65012 1.45806 0.446 0.655933
                                    1.409 0.159693
## schoolMS
                 0.45495
                            0.32293
                ## age
                           0.18989 -1.688 0.092278 .
## activitiesyes -0.32049
                           0.20622 -1.584 0.113989
## romanticyes
              -0.32668
                         0.10668
                                     3.596 0.000365 ***
## famrel
                 0.38361
                 0.11979 0.07521
                                     1.593 0.112050
## Walc
## absences
                 0.04714
                           0.01232
                                     3.826 0.000152 ***
## G1
                 0.18058
                            0.05517
                                     3.273 0.001159 **
## G2
                 0.96153
                            0.04904 19.607 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.864 on 385 degrees of freedom
## Multiple R-squared: 0.8382, Adjusted R-squared: 0.8344
## F-statistic: 221.6 on 9 and 385 DF, p-value: < 2.2e-16
```

### with Interactive Terms

```
# stepAIC(mod_full, scope = . ~ .^2, direction = "both")
```