Context-Aware and Data-Driven Feedback Generation for Programming Assignments

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> 11 Feb 2022 SW 재난 연구센터 워크샵 @ Jeju





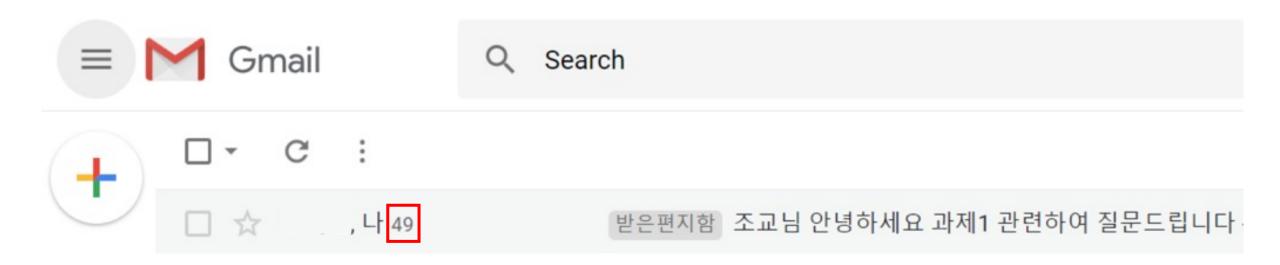
- 프로그래밍 교육에 대한 수요가 커지며, 적절한 피드백에 대한 요구가 증가
- 실제 서비스에서도, 피드백의 양과 질이 학생들의 수요를 따라가지 못함

| 소수구하기 배열에서 자꾸 문제가 생깁니다 | 1929번 질문 | taeyang95 |
|--------------------------------------|-----------|--------------|
| [Python] 최대, 최소 구하기 '틀렸습니다' 질문 | 10818번 질문 | poroli0119 |
| 반례가 무엇인지를 모르겠습니다 | 1158번 질문 | hyunsk77 |
| [java]반례를 찾아주십시오! | 1002번 질문 | dbtmxlsk2007 |
| 연결리스트 시간초과 | 17298번 질문 | y718j |
| node.js 런타임에러(StackSizeExceeded) | 1717번 질문 | heech1013 |
| [Python] 반례를 못찾겠습니다 ㅠ 해결 | 2581번 질문 | dnjstjr245 |
| python 10025번 시간초과입니다. | 10025번 질문 | fblood53 |
| 코드에 무슨 이상이 있는 걸까요 | 2908번 질문 | cho990205 |
| [파이썬] 시간초과가 뜨는데 줄이는 방법이 있을까요? | 18290번 질문 | dhrudgns529 |
| [Python] X보다 작은 수 | 10871번 질문 | poroli0119 |
| (C++) 이분 탐색을 이용한 가장 가까운 수 구하기 | 질문 | 098123 |
| [c++] 계속 틀렸다고 나오는데 어디가 틀렸는지 모르겠어요 해결 | 11022번 질문 | hjungwon034 |
| [C++]BFS 코드 반례 질문입니다. 해결 | 1697번 질문 | Icj207 |
| 메모리 초과 나는 이유 | 2887번 질문 | chaerin0625 |
| 무엇이 틀렸는지 도저히 모르겠습니다,, | 10757번 질문 | tjswo613 |
| 18126 c++ 질문 | 18126번 질문 | fruity |
| 파이썬 메모리 초과 질문입니다 | 7576번 질문 | kms15461 |
| DFS 정상 BFS 시간초과 질문 | 10026번 질문 | codren |
| 데크의 시간복잡도 계산 | 1158번 질문 | nh0903 |

• 온라인 프로그래밍 서비스인 백준의 질의 응답 게시판 상황

• 20개의 질문 중 단 3개의 질문에 대해서만 피드백이 제공된 상황

- 실제 수업환경에서도 많은 학생들이 과제에 어려움을 느낌
 - 조교가 매 학기 평균 학생들로부터 100개의 이메일을 받음
 - 개중 한 질문에 대해서는, 49개의 답변을 주고받았음



• 단순히 모범 답안을 제공하는 것은 학생들에게 도움이 되지 않음

```
let rec do_diff (ae, x) =
 match ae with
 | Const i -> Const 0
 | Var v \rightarrow if (v = x) then Const 1 else Const 0
 | Power (v, i) \rightarrow if (v = x) Times [Const i; Power (v, i-1)] else Const 0
 | Sum (hd::tl) ->
  if (tl = []) then do_diff (hd, x) else Sum [do_diff (hd, x); do_diff (Sum tl, x)]
 | Times (hd::tl) ->
  if (tl = []) then do_diff (hd, x)
   else Sum [Times ((do_diff (hd, x))::tl); Times [hd; (do_diff (Times tl, x))]]
let rec minimize ae =
 let rec minimize_helper ae =
   match ae with
   | Sum 1st ->
    if (1st = \Gamma 1) then Const 0
     else if (List.length lst = 1) then List.hd lst
     else Sum (List.map minimize_helper (List.filter (fun ae -> ae <> Const 0) lst))
   | Times lst ->
    if (lst = []) then Const 0
     else if (List.mem (Const 0)) lst then Const 0
     else if (List.length lst = 1) then List.hd lst
     else Times (List.map minimize_helper (List.filter (fun ae -> ae <> Const 1) lst))
   l -> ae in
 let ae' = minimize helper ae in
 if (ae = ae') then ae else minimize ae'
let diff (ae, str) = minimize (do_diff (ae, str))
```

```
let rec diff (e, x) =
  match e with
  | Const n -> Const 0
  | Var y -> if (x <> y) then Const 0 else Const 1
  | Power (y, n) -> if (x <> y) then Const 0 else Times [Const n; Power (y, n-1)]
  | Sum (hd::tl) -> Sum (List.map (fun e -> diff (e, x)) (hd::tl))
  | Times [hd] -> diff (hd, x)
  | Times (hd::tl) -> Sum [Times ((diff (hd, x))::tl); Times [hd; diff (Times tl, x)]]
  | _ -> raise (Failure "Invalid")
```

T.A's Solution

Student's Submission

```
let rec diff : aexp * string -> aexp
= fun (exp, x) ->
  match exp with
   | Const(i) -> Const(0)
   | Var(s) -> if s=x then Const(1) else Var(s)
   | Power(s, i) ->
     if s=x then if i>2 then Times[Const(i): Power(s. i-1)] else Times[Const(i): Var(s)]
          else Power(s, i)
    | Times(al) ->
     let rec timeiter lst =
       match 1st with
        [] -> []
         |hd::tl ->
           (match hd with
           |Const(i1) -> Const(i1)
           |_{-} -> diff(hd, x)
           )::(timeiter tl)
     Times(timeiter al)
    | Sum(al) ->
     let rec sumeval lst =
       match 1st with
        [] <> []
         |hd::tl -> if hd=Const(0) then sumeval tl else hd::sumeval tl
     in
     let rec sumiter lst =
       match 1st with
        [] -> []
         |hd::tl -> diff(hd, x)::(sumiter tl)
     in
     Sum(sumeval(sumiter al))
```

```
let rec diff (e, x) =
  match e with
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  | Power (y, n) -> if (x <> y) then Const 0 else Times [Const n; Power (y, n-1)]
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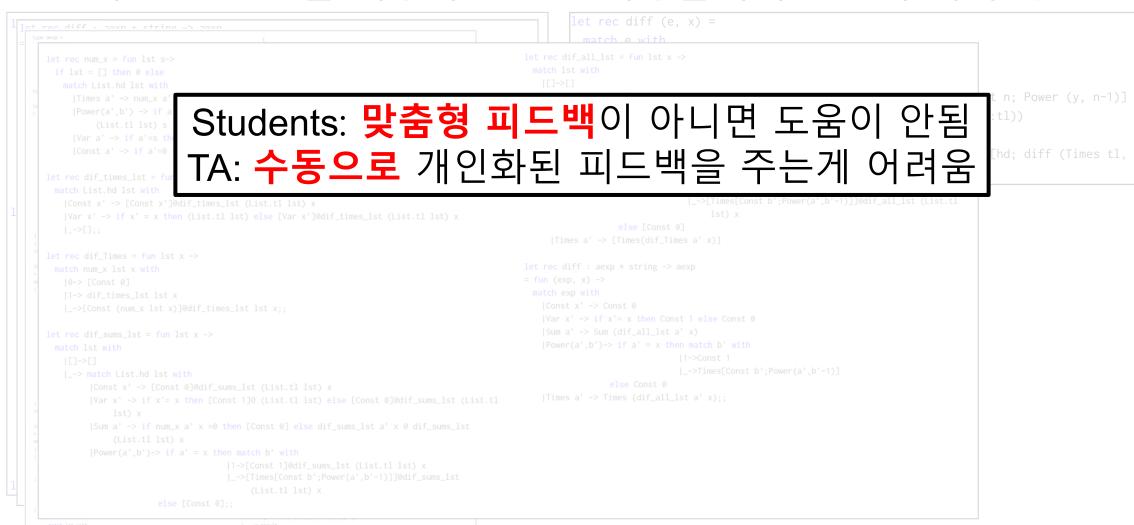
T.A's Solution

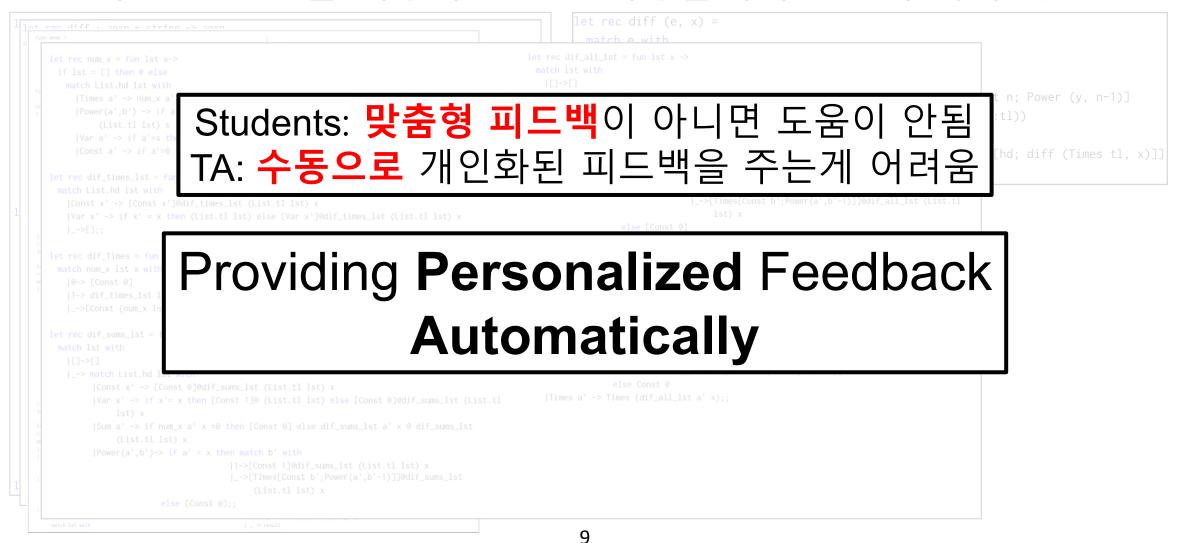
```
type aexp =
  ICONST of int
                                                                                    match (hd, diff_hd, tl, diff_tl) with
  I VAR of string
                                                                                   I (CONST p. CONST s. [CONST r], CONST q) -> CONST (p*q + r*s)
  I POWER of string * int
                                                                                   | (CONST p, _, _, CONST q) ->
  | TIMES of aexp list
                                                                                      if (diff_hd = CONST 0 || tl = [CONST 0]) then CONST (p*q)
                                                                                      else SUM [CONST(p*q); TIMES(diff_hd::tl)]
                                                                                   | (_, CONST s, [CONST r], _) ->
type env = (string * int * int) list
                                                                                      if (hd = CONST 0 || diff tl = CONST 0) then CONST (r*s)
                                                                                      else SUM [TIMES [hd: diff_tl]: CONST(r*s)]
let diff : aexp * string -> aexp
 fun (aexp, x) ->
                                                                                      if (hd = CONST 0 || diff tl = CONST 0) then TIMES(diff hd::tl)
                                                                                      else if (t1 = [CONST 0] || diff_hd = CONST 0) then TIMES [hd; diff_t1] |Var(s)]
  let rec deployEnv : env -> int -> aexp list
                                                                                      else SUM [TIMES [hd; diff_tl]; TIMES (diff_hd::tl)]
 = fun env flag ->
  match env with
                                                                              | [] -> CONST 0
 | hd::tl ->
                                                                         | SUM 1st -> SUM(List.map (fun aexp -> doDiff(aexp, x)) 1st)
   match hd with
     if (flag = 0 && c = 0) then deployEnv tl flag
                                                                         let rec simplify : aexp -> env -> int -> aexp list
     else if (x = "const" && flag = 1 && c = 1) then deployEnv tl flag = fun aexp env flag ->
     else if (p = 0) then (CONST c)::(deployEnv tl flag)
                                                                         match aexp with
     else if (c = 1 && p = 1) then (VAR x)::(deployEnv tl flag)
                                                                         | SUM 1st ->
     else if (n = 1) then TIMES[CONST c: VAR x]: (denloyEnv tl flag)
     else if (c = 1) then POWER(x, p)::(deployEnv tl flag)
     else TIMES [CONST c; POWER(x, p)]::(deployEnv tl flag)
                                                                              | (CONST c)::tl -> simplify (SUM tl) (updateEnv ("const", c, 0) env 0) 0
                                                                              | (VAR x)::tl -> simplify (SUM tl) (updateEnv (x, 1, 1) env 0) 0
| [] -> []
                                                                               | (POWER (x, p))::tl -> simplify (SUM tl) (updateEnv (x, 1, p) env 0) 0
                                                                               | (SUM lst)::tl -> simplify (SUM (List.append lst tl)) env 0
                                                                              | (TIMES lst)::tl ->
let rec updateEnv : (string \star int \star int) -> env -> int -> env
= fun elem env flag ->
                                                                                   let 1 = simplify (TIMES 1st) [] 1 in
                                                                                   match 1 with
| (hd::t1) ->
                                                                                      if (t = []) then List.append 1 (simplify (SUM tl) env 0)
  match hd with
                                                                                      else List.append (TIMES 1::[]) (simplify (SUM tl) env θ)
  | (x, c, p) ->
                                                                                   | [] -> []
     match elem with
                                                                              | [] -> deployEnv env 0
     |(x2, c2, p2) ->
       if (flag = 0) then
                                                                         | TIMES 1st ->
          if (x = x2 && p = p2) then (x, (c + c2), p)::t1
          else hd::(updateEnv elem tl flag)
                                                                              | (CONST c)::tl -> simplify (TIMES tl) (updateEnv ("const", c, 0) env 1) 1
          if (x = x2) then (x, (c*c2), (p + p2))::tl
                                                                              | (VAR x)::tl -> simplify (TIMES tl) (updateEnv (x, 1, 1) env 1) 1
          else hd::(updateEnv elem tl flag)
                                                                               | (POWER (x, p))::tl -> simplify (TIMES tl) (updateEnv (x, 1, p) env 1) 1
| [] -> elem::[]
                                                                                    let 1 = simplify (SUM 1st) [] 0 in
                                                                                    match 1 with
let rec doDiff : aexp * string -> aexp
                                                                                      if (t = []) then List.append 1 (simplify (TIMES t1) env 1)
= fun (aexp. x) ->
                                                                                       else List.append (SUM 1::[]) (simplify (TIMES tl) env 1)
match sevn with
                                                                                    | [] -> []
 | CONST _ -> CONST @
                                                                               | (TIMES lst)::tl -> simplify (TIMES (List.append lst tl)) env 1
  if (x = v) then CONST 1
                                                                               | [] -> deployEnv env 1
  else CONST 0
 I POWER (v. p) ->
   if (p = 0) then CONST 0
   else if (x = v) then TIMES ((CONST p)::POWER (v, p-1)::[])
                                                                          let result = doDiff (aexp, x) in
   else CONST 0
 TIMES 1st ->
                                                                          | SUM _ -> SUM (simplify result [] 0)
                                                                          | TIMES _ -> TIMES (simplify result [] 1)
     match 1st with
                                                                         | _ -> result
```

```
let rec diff (e, x) =
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T.A's Solution

```
let rec diff (e, x) =
at rac diff . savn + etring -> savn
  type aexp =
                                                                                                                                                                                                                         match e with
                                                                                                                                                                                                  let rec dif_all_lst = fun lst x ->
       let rec num x = fun lst s->
                                                                                                                                                                                                     match 1st with
          if lst = [] then 0 else
                                                                                                                                                                                                         1[]->[]
             match List.hd 1st with
                                                                                                                                                                                                         I ->match List.hd lst with
                                                                                                                                                                                                                                                                                                                                                                                     hst n; Power (y, n-1)]
                 |Times a' -> num_x a' s + num_x (List.tl lst) s
                                                                                                                                                                                                            |Const x' -> [Const 0]@dif_all_lst (List.tl lst) x
                 |Power(a',b') -> if a' = s && b' <> 0 then b' + num_x (List.tl lst) s else 0 +num_x
                                                                                                                                                                                                                                                                                                                                                                                     d::tl))
                                                                                                                                                                                                            |Var x'| \rightarrow |Var x'| + |Var x'| 
                           (List.tl lst) s
                 |Var a' -> if a'=s then 1 + num_x (List.tl lst) s else 0 +num_x (List.tl lst) s
                                                                                                                                                                                                            |Sum a' -> if num_x a' x =0 then [Const 0] else dif_sums_lst a' x @ dif_all_lst (List.tl
                 | IConst a' -> if a'=0 then 0 else 0 +num_x (List.tl lst) s::
                                                                                                                                                                                                                                                                                                                                                                                        [ Thd: diff (Times tl. x)]]
                                                                                                                                                                                                                     lst) x
                                                                                                                                                                                                            |Power(a',b')-> if a' = x then match b' with
       let rec dif times lst = fun lst x ->
                                                                                                                                                                                                                                                                 |1->[Const 1]@dif_all_lst (List.tl lst) x
          match List.hd 1st with
                                                                                                                                                                                                                                                                 |_->[Times[Const b';Power(a',b'-1)]]@dif_all_lst (List.tl
              |Const x' -> [Const x']@dif_times_lst (List.tl lst) x
                                                                                                                                                                                                                                                                           lst) x
             |Var x' -> if x' = x then (List.tl lst) else [Var x']@dif_times_lst (List.tl lst) x
                                                                                                                                                                                                                                       else [Const 0]
             [_->[];;
                                                                                                                                                                                                            |Times a' -> [Times(dif_Times a' x)]
       let rec dif_Times = fun lst x ->
                                                                                                                                                                                                  let rec diff : aexp * string -> aexp
          match num_x lst x with
                                                                                                                                                                                                  = fun (exp, x) ->
             10-> [Const 0]
                                                                                                                                                                                                     match exp with
             11-> dif times lst lst x
                                                                                                                                                                                                         |Const x' -> Const 0
             |_->[Const (num_x lst x)]@dif_times_lst lst x;;
                                                                                                                                                                                                         |Var x' -> if x'= x then Const 1 else Const 0
                                                                                                                                                                                                         |Sum a' -> Sum (dif_all_lst a' x)
       let rec dif sums lst = fun lst x ->
                                                                                                                                                                                                         |Power(a',b')-> if a' = x then match b' with
          match 1st with
                                                                                                                                                                                                                                                              |1->Const 1
             []->[]
                                                                                                                                                                                                                                                              |_->Times[Const b';Power(a',b'-1)]
              I_-> match List.hd 1st with
                                                                                                                                                                                                                                   else Const 0
                       |Const x' -> [Const 0]@dif_sums_lst (List.tl lst) x
                                                                                                                                                                                                         |Times a' -> Times (dif_all_lst a' x);;
                        |Var x' -> if x'= x then [Const 1]@ (List.tl lst) else [Const 0]@dif_sums_lst (List.tl
                                lst) x
                       |Sum a' -> if num_x a' x =0 then [Const 0] else dif_sums_lst a' x @ dif_sums_lst
                                 (List.tl 1st) x
                        [Power(a',b')\rightarrow if a' = x then match b' with]
                                                                             [1->[Const 1]@dif_sums_lst (List.tl lst) x
                                                                             |_->[Times[Const b';Power(a',b'-1)]]@dif_sums_lst
                                                                                       (List.tl 1st) x
                                                  else [Const 0];;
                                                                                  | _ -> result
         match 1st with
```





Data-Driven Feedback Generation

• 최근의 연구 동향은 **많은 정답 코드**를 활용하여 피드백을 생성. e.g., CLARA (PLDI 18), SARFGEN (PLDI 18)

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• 이러한 연구들은 주어진 오답과 **아주 비슷한** 정답 프로그램의 존재를 가정함. e.g., exact CFG matching

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• 이런 강한 가정은 **초급 난이도의 문제를 벗어나면** 거의 만족되지 않음.

| Difficulty | # Submissions | # Error | # Matching | Matching Rate |
|--------------|---------------|---------|------------|---------------|
| Introductory | 1,185 | 105 | 87 | 83% |
| Intermediate | 1,107 | 116 | 42 | 36% |
| Advanced | 1,919 | 443 | 80 | 18% |

```
let rec timediff (tst,x) =
    match tst with
     | [] -> [] | h::t ->
       (match h with
       Int n -> (Int n)::timediff(t.x)
        Var v -> if v=x then (Int 1)::timediff(t,x)
                  else (Int 0)::timediff(t,x)
       | Pow (v,c) ->
         if v=x then (Mul [Int n;Pow(v,c-1)])::timediff(t,x)
10
         else (Int 0)::timediff(t,x))
11 and sumdiff (slst,x) =
    match slst with
12
     | [] -> [] | h::t ->
14
       (match h with
15
       | Int n -> (Int 0)::sumdiff(t,x)
       | Var v -> if v=x then (Int 1)::sumdiff(t,x)
17
                  else (Int 0)::sumdiff(t,x)
18
       | Pow (v.c) ->
        if v=x then (Mul [Int n;Pow(v,c-1)])::sumdiff(t,x)
20
         else (Int 0)::sumdiff(t,x)
21
       | Sum lst -> Sum (sumdiff (lst,x))::sumdiff(t,x)
        Time lst -> Mul (timediff (lst,x))::sumdiff(t,x))
23 and diff (e, x) =
    match e with
25
      Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
      Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
      Sum lst -> Sum (sumdiff(lst,x))
28
      Mul lst -> Mul (timediff(lst.x))
```

- 3가지의 함수를 사용해 작성된 오답 코드
 - 세개의 함수 모두 오류가 존재
 - 최소로 수정하기 위해선 각 함수를 수정해야함

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let rec timediff (tst,x) =
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 - 최소로 수정하기 위해선 각 함수를 수정해야함
- 218개의 정답 코드 중 **같은 CFG구조**가 하나도 없음

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       | Var v -> if v=x then (Int 1)::sumdiff(t,x)
17
                  else (Int 0)::sumdiff(t,x)
18
       | Pow (v.c) ->
        if v=x then (Mul [Int n;Pow(v,c-1)])::sumdiff(t,x)
20
         else (Int 0)::sumdiff(t,x)
21
       | Sum lst -> Sum (sumdiff (lst,x))::sumdiff(t,x)
        Time lst -> Mul (timediff (lst,x))::sumdiff(t,x))
23 and diff (e, x) =
    match e with
     | Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
25
      Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
      Sum lst -> Sum (sumdiff(lst,x))
      Mul lst -> Mul (timediff(lst.x))
```

- 3가지의 함수를 사용해 작성된 오답 코드
 - 세개의 함수 모두 오류가 존재
 - 최소로 수정하기 위해선 각 함수를 수정해야함
- 218개의 정답 코드 중 **같은 CFG구조**가 하나도 없음
- 하지만 해당 프로그램과 부분적으로 비슷한 정답은 존재함

```
let rec timediff (tst,x) =
    match tst with
     | [] -> [] | h::t ->
       (match h with
        Int n -> (Int n)::timediff(t.x)
        Var v -> if v=x then (Int 1)::timediff(t,x)
                  else (Int 0)::timediff(t,x)
       | Pow (v,c) ->
        if v=x then (Mul [Int n;Pow(v,c-1)])::timediff(t,x)
10
         else (Int 0)::timediff(t,x))
11 and sumdiff (slst,x) =
12
     match slst with
     | [] -> [] | h::t ->
14
       (match h with
15
       | Int n -> (Int 0)::sumdiff(t,x)
       | Var v -> if v=x then (Int 1)::sumdiff(t,x)
16
17
                  else (Int 0)::sumdiff(t,x)
18
       | Pow (v.c) ->
19
        if v=x then (Mul [Int n;Pow(v,c-1)])::sumdiff(t,x)
20
         else (Int 0)::sumdiff(t,x)
21
       | Sum lst -> Sum (sumdiff (lst,x))::sumdiff(t,x)
22
        Time lst -> Mul (timediff (lst,x))::sumdiff(t,x))
23 and diff (e, x) =
    match e with
25
      Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
      Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
      Sum lst -> Sum (sumdiff(lst,x))
28
      Mul lst -> Mul (timediff(lst,x))
```

```
let rec check (l,v) =
     match l with
     | [] -> false | h::t ->
       (match h with
         Var x -> if x=v then true else check(t,v)
         Pow (x,i) \rightarrow if x=v then true else check(t,v)
         Sum lst | Mul lst -> check(lst,v) || check(t,v)
         -> check(t,v))
  let rec times (l,v) =
     match l with
11
     | [] -> [] | h::t ->
      if t=[] then [diff(h,v)]
12
       else [Mul ([diff(h,v)]@t)]@[Mul ([h]@[Sum (times(t,v))])]
14 and sum (l,v) =
     match l with
     | [] -> [] | h::t -> [diff(h,v)]@(sum(t,v))
17 and diff (aexp,v) =
     match aexp with
     | Int n -> Int 0 | Var x -> if x=v then Int 1 else Int 0
20
     | Pow (s,i) ->
21
       if s=str then (
22
        if i=1 then Int 1
23
         else if i=0 then Int 0
24
         else Mul ([Int i; Pow (s,i-1)]))
25
       else Int 0
26
      Mul l \rightarrow if check(l,v) then Sum (times(l,v)) else Int 0
27
      Sum l \rightarrow Sum (sum (l,v))
```

```
let rec check (l,v) =
   let rec timediff (tst,x) =
    match tst with
                                                                       match l with
    | [] -> [] | h::t ->
                                                                        | [] -> false | h::t ->
                                                                          (match h with
                                                                           Var x -> if x=v then true else check(t,v)
                                                                           Pow (x,i) \rightarrow if x=v then true else check(t,v)
                                                                           Sum lst | Mul lst -> check(lst,v) || check(t,v)
                                                                           -> check(t,v))
                                                                  9 let rec times (l,v) =
11 and sumdiff (slst,x) =
                                                                       | [] -> [] | h::t ->
                                                                         if t=[] then [diff(h,v)]
    match slst with
     | [] -> [] | h::t ->
                                                                         else [Mul ([diff(h,v)]@t)]@[Mul ([h]@[Sum (times(t,v))])]
                          오답 코드에는 없는 다른 함수들을 사용함
                                                                                                        sum(t,v))
                                                                   1/ and diff (aexp, v)
                                                                        | Int n -> Int 0 | Var x -> if x=v then Int 1 else Int 0
23 and diff (e, x) =
                                                                           else if i=0 then Int 0
                                                                          else Mul ([Int i; Pow (s,i-1)]))
     | Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
                                                                         else Int 0
      Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
                                                                        Mul l -> if check(l,v) then Sum (times(l,v)) else Int 0
      Sum lst -> Sum (sumdiff(lst,x))
      Mul lst -> Mul (timediff(lst,x))
```

```
let rec timediff (tst,x) =
                                                                      let rec check (l,v) =
    match tst with
     | [] -> [] | h::t ->
                                                                          [] -> false | h::t ->
      (match h with
        Int n -> (Int n)::timediff(t.x)
                                                                           Var x -> if x=v then true else check(t,v)
        Var v -> if v=x then (Int 1)::timediff(t,x)
                                                                            Pow (x,i) \rightarrow if x=v then true else check(t,v)
                 else (Int 0)::timediff(t,x)
                                                                            Sum lst | Mul lst -> check(lst,v) || check(t,v)
        Pow (v,c) ->
                                                                              -> check(t,v))
        if v=x then (Mul [Int n;Pow(v,c-1)])::timediff(t,x)
                                                                      let rec times (l,v) =
10
        else (Int 0)::timediff(t,x))
                                                                   10
                                                                        match l with
11 and sumdiff (slst,x) =
                                                                   11
                                                                        | [] -> [] | h::t ->
    match slst with
                                                                   12
                                                                          if t=[] then [diff(h,v)]
     | [] -> [] | h::t ->
                                                                          else [Mul ([diff(h,v)]@t)]@[Mul ([h]@[Sum (times(t,v))])]
                         오류 함수와 비슷한 기능을 갖는 함수 존재
                                                                                                           um(t,v))
                                                                         | Int n -> Int 0 | Var x -> if x=v then Int 1 else Int 0
23 and diff (e, x) =
                                                                            else if i=0 then Int 0
                                                                           else Mul ([Int i; Pow (s,i-1)]))
     | Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
                                                                          else Int 0
      Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
                                                                         Mul l -> if check(l,v) then Sum (times(l,v)) else Int 0
      Sum lst -> Sum (sumdiff(lst,x))
      Mul lst -> Mul (timediff(lst,x))
```

```
let rec timediff (tst,x) =
    match tst with
     | [] -> [] | h::t ->
                                                                        [] -> false | h::t ->
      if t=[] then [diff(h,v)] else
        [Mul ([diff(h,x)]@t)]@[Mul ([h]@[Sum (timediff(t,x))])]
                                                                         Var x -> if x=v then true else check(t,v)
                                                                          Pow (x,i) \rightarrow if x=v then true else check(t,v)
                                                                          Sum lst | Mul lst -> check(lst,v) || check(t,v)
    match slst with
                                                                            -> check(t,v))
    | [] -> [] | h::t ->
                                                                    let rec times (l,v) =
                                                                      match l with
                                                                  11
                                                                       | [] -> [] | h::t ->
                                                                        if t=[] then [diff(h,v)]
                                                                  12
                                                                        else [Mul ([diff(h,v)]@t)]@[Mul ([h]@[Sum (times(t,v))])]
                                                                  14 and sum (l,v) =
                                                                      [] -> [] | h::t -> [diff(h,v)]@(sum(t,v))
                                                                  17 and diff (aexp,v) =
18 and diff (e, x) =
                                                                                                          en Int 1 else Int 0
                       CAFE: 해당 함수만을 이용해 오류 함수 수정
      Int n -> Int 0
      Sum lst -> Sum (Sumuling ts
      Mul lst -> Mul (timediff(lst.x))
                                                                          else if i=0 then Int 0
                                                                          else Mul ([Int i; Pow (s,i-1)]))
                                                                        else Int 0
                                                                       Mul l -> if check(l,v) then Sum (times(l,v)) else Int 0
```

```
let rec timediff (tst,x) =
     match tst with
     | [] -> [] | h::t ->
       if t=[] then [diff(h,v)] else
         [Mul ([diff(h,x)]@t)]@[Mul ([h]@[Sum (timediff(t,x))])]
   and sumdiff (slst,x) =
     match slst with
     | [] -> [] | h::t ->
       (match h with
        Int n -> (Int 0)::sumdiff(t,x)
       | Var v -> if v=x then (Int 1)::sumdiff(t,x)
11
                  else (Int 0)::sumdiff(t,x)
12
13
       | Pow (v,c) ->
         if v=x then (Mul [Int n;Pow(v,c-1)])::sumdiff(t,x)
14
15
         else (Int 0)::sumdiff(t,x)
        Sum lst -> Sum (sumdiff (lst,x))::sumdiff(t,x)
16
        Time lst -> Mul (timediff (lst,x))::sumdiff(t,x))
17
18 and diff (e, x) =
     match e with
20
      Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
       Pow (v,c) \rightarrow if v=x then Mul [Int n;Pow(v,c-1)] else Int 0
22
       Sum lst -> Sum (sumdiff(lst,x))
23
      Mul lst -> Mul (timediff(lst,x))
```

```
let rec timediff (tst,x) =
     match tst with
     | [] -> [] | h::t ->
       if t=[] then [diff(h,v)] else
         [Mul ([diff(h,x)]@t)]@[Mul ([h]@[Sum (timediff(t,x))])]
   and sumdiff (slst,x) =
     match slst with
     | [] -> [] | h::t ->
       (match h with
        Int n -> (Int 0)::sumdiff(t,x)
11
        | Var v -> if v=x then (Int 1)::sumdiff(t,x)
                  else (Int 0)::sumdiff(t,x)
12
13
       | Pow (v,c) ->
14
         if v=x then (Mul [Int n;Pow(v,c-1)])::sumdiff(t,x)
15
         else (Int 0)::sumdiff(t,x)
         Sum lst -> Sum (sumdiff (lst,x))::sumdiff(t,x)
16
17
         Time lst -> Mul (timediff (lst,x))::sumdiff(t,x))
18 and diff (e, x) =
     match e with
20
      Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
21
       Pow (v,c) \rightarrow if v=x then Mul [Int n;Pow(v,c-1)] else Int 0
22
       Sum lst -> Sum (sumdiff(lst,x))
23
       Mul lst -> Mul (timediff(lst,x))
```

```
let rec timediff (tst,x) =
     match tst with
     | [] -> [] | h::t ->
       if t=[] then [diff(h,v)] else
         [Mul ([diff(h,x)]@t)]@[Mul ([h]@[Sum (timediff(t,x))])]
   and sumdiff (slst,x) =
     match slst with
     | [] -> [] | h::t ->
       (match h with
        Int n -> (Int 0)::sumdiff(t,x)
10
11
       | Var v -> if v=x then (Int 1)::sumdiff(t,x)
                  else (Int 0)::sumdiff(t,x)
12
13
       | Pow (v,c) ->
14
         if v=x then (Mul [Int n;Pow(v,c-1)])::sumdiff(t,x)
15
         else (Int 0)::sumdiff(t,x)
         Sum lst -> Sum (sumdiff (lst,x))::sumdiff(t,x)
16
17
         Time lst -> Mul (timediff (lst,x))::sumdiff(t,x))
18 and diff (e, x) =
     match e with
20
      Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
21
       Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
       Sum lst -> Sum (sumdiff(lst,x))
       Mul lst -> Mul (timediff(lst,x))
```

```
1 let rec length lst = List.length lst
  let rec diff sum (l, k) = match l with
     [] \rightarrow [] | h::t \rightarrow (diff(h,k))::(diff sum(t,k))
   let rec f (l, k, p, q) = match l with
     | [] -> [] | h::t ->
       if p=q then diff(h,k)::f(t,k,p+1,q)
       else hd::(f(t,k,p+1,q))
8 let rec diff time (l, k, x, y) =
     if x>y then [] else Mul (f(l,k,1,x))::diff_time(l,k,x+1,y)
10 let rec diff (e, x) = match e with
       Sum lst -> Sum (diff sum(lst,x))
12
       Mul lst -> Sum (diff_time(lst,x,1,(length lst))) | ...
  let rec differ (a, x) =
     match a with
       Int a -> Int 0 | Var v -> if x=v then Int 1 else Int 0
      Pow (v, a) ->
       if x=v then Mul ([Int a]@[Pow (v,a-1)]) else Int 0
       Sum l \rightarrow Sum (sum(l,x)) \mid Mul l \rightarrow Sum (times(l,x,[]))
   and times (a, x, acc) =
     match a with
```

```
| Sum l -> Sum (sum(l,x)) | Mul l -> Sum (times(l,x,[]))

| and times (a, x, acc) = | match a with | | [] -> [] | hd::tl -> | if List.length a = List.length acc then acc | else (times((tl@[hd]),x,acc@[Mul ([diff(hd,x)]@tl)]))

| and sum (a, x) = match a with | | [] -> [] | hd::tl -> ([(diff(hd,x))]@(sum(tl,x)))

| det rec diff (a, x) = differ(a,x)
```

```
let rec timediff (tst,x) =
     match tst with
     | [] -> [] | h::t ->
       if t=[] then [diff(h,v)] else
         [Mul ([diff(h,x)]@t)]@[Mul ([h]@[Sum (timediff(t,x))])]
   and sumdiff (slst,x) =
     match slst with
     | [] -> [] | h::t ->
       (diff(hd,key))::(sumdiff(t,x))
9 and diff (e, x) =
     match e with
      Int n -> Int 0 | Var v -> if v=x then Int 1 else Int 0
11
       Pow (v,c) \rightarrow if v=x then Mul [Int n; Pow(v,c-1)] else Int 0
       Sum lst -> Sum (sumdiff(lst,x))
13
       Mul lst -> Sum (timediff(lst,x))
```

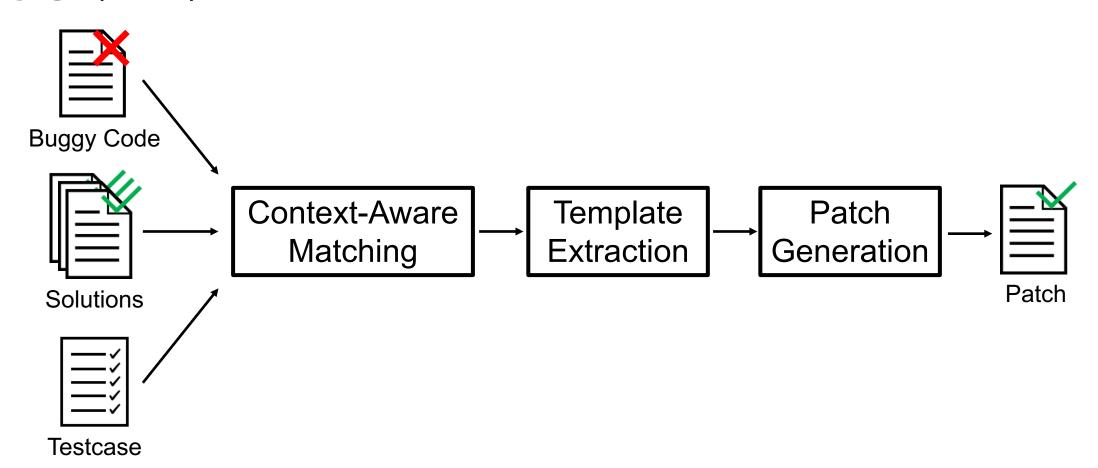
(((x))

3개의 **서로 다른** 정답을 이용해 **5초내에** 패치를 생성

14 let rec diff (a, x) = differ(a, x)

Overview of CAFE

• **함수 단위**의 context-aware matching을 활용하여 피드백을 생성하는 기술



How CAFE Works: Running Example

• 입력 연산자에 따라 주어진 리스트의 값을 1씩 증가 혹은 감소시키는 함수

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

- I/O examples:
 - apply ([1; 2; 3], ADD) => [2; 3; 4]
 - apply ([1; 2; 3], SUB) => [0; 1; 2]

How CAFE Works: Running Example

• 입력 연산자에 따라 주어진 리스트의 값을 1씩 증가 혹은 감소시키는 함수

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

- I/O examples:
 - apply ([1; 2; 3], ADD) => [2; 3; 4]
 - apply ([1; 2; 3], SUB) => [1; 3; 4]
- 입력 연산자가 "SUB" 일 때 오류 발생

How CAFE Works: Running Example

• 덧셈 함수, 뺄셈 함수를 각각 하나씩만 사용하여 구현된 두개의 정답 코드

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)

5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)

9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
2
3
4
5 let rec sub_list lst =
6    match lst with
7    | [] -> []
8    | h::t -> (h-1)::(sub_list t)

9 let rec apply1 (l, o) =
10    match l with
11    | [] -> id []
12    | hd::tl -> (match o with
13    | ADD -> (hd+1)::(apply1(tl,o))
14    | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11  | [] -> []
12  | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

"dec_all" 함수를 수정하기 위해, "sub_list" 함수를 사용해야 함

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
2
3
4
5 let rec sub_list lst =
6    match lst with
7    | [] -> []
8    | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10    match l with
11    | [] -> id []
12    | hd::tl -> (match o with
13    | ADD -> (hd+1)::(apply1(tl,o))
14    | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)

5
6
7
8

9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

Syntax 혹은 semantic에 기반한 매칭은 잘못된 함수를 매칭

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
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3
4
5 let rec sub_list lst =
6   match lst with
7   | [] -> []
8   | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10  match l with
11  | [] -> id []
12  | hd::tl -> (match o with
13  | ADD -> (hd+1)::(apply1(tl,o))
14  | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10  match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
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3
4
5 let rec sub_list lst =
6   match lst with
7   | [] -> []
8   | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10   match l with
11  | [] -> id []
12  | hd::tl -> (match o with
13  | ADD -> (hd+1)::(apply1(tl,o))
14  | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10  match l with
11  | [] -> []
12  | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14  | SUB -> (h-1)::(apply2(t,o)))
```

 $Ctx_{dec_all} = (l = hd :: tl) \land o = SUB$

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
2
3
4
5 let rec sub_list lst =
6   match lst with
7   | [] -> []
8   | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10   match l with
11   | [] -> id []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(apply1(tl,o))
14   | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10  match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

```
Ctx_{dec\ all} = (l = hd :: tl) \land o = SUB
```

$$Ctx_{sub}$$
 list= $(l=hd::tl) \land o=SUB$

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)

9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
2
3
4
5 let rec sub_list lst =
6    match lst with
7    | [] -> []
8    | h::t -> (h-1)::(sub_list t)

9 let rec apply1 (l, o) =
10    match l with
11    | [] -> id []
12    | hd::tl -> (match o with
13    | ADD -> (hd+1)::(apply1(tl,o))
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```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
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5
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7
8
9 let rec apply2 (l, o) =
10  match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

```
Ctx_{dec\_all} = (l = hd :: tl) \land o = SUB
```

$$Ctx_{sub\ list} = (l = hd::tl) \land o = SUB$$

Ctx_{dec_all} ∧ Ctx_{sub_list}이 SAT, "dec_all" 과 "sub_list"를 매칭

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
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11   | [] -> []
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13   | ADD -> (hd+1)::(inc_all tl)
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```

```
1 let id x = x
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3
4
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6   match lst with
7   | [] -> []
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9 let rec apply1 (l, o) =
10 match l with
11  | [] -> id []
12  | hd::tl -> (match o with
13   | ADD -> (hd+1)::(apply1(tl,o))
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```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

```
Ctx_{dec\ all} = (l = hd::tl) \land o = SUB
```

$$Ctx_{add\ list} = (l = hd::tl) \land o = ADD$$

• 각 함수의 context에 기반하여 **패치에 유용하게 사용 될 것 같은** 정답 함수를 탐색

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)

5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)

9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
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```

```
1 let id x = x
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12  | hd::tl -> (match o with
13  | ADD -> (hd+1)::(apply1(tl,o))
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```

```
1 let rec add_list lst =
2   match lst with
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4   | h::t -> (h+1)::(add_list t)

5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

```
Ctx_{dec\ all} = (l = hd::tl) \land o = SUB
```

```
Ctx_{add\ list} = (l = hd::tl) \land o = ADD
```

Ctx_{dec_all} ∧ Ctx_{add_list} 이 UNSAT, "dec_all" 과 "add_list"는 매칭되지 않음.

Step2: Template Extraction

• 서로 매칭된 함수 사이의 syntactic difference를 통해 패치 템플릿 추출

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
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```

```
1 let id x = x
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5 let rec sub_list lst =
6    match lst with
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8    | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10    match l with
11    | [] -> id []
12    | hd::tl -> (match o with
13    | ADD -> (hd+1)::(apply1(tl,o))
14    | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

Context-aware matching에서 다음의 결과가 나왔다고 가정: [apply → apply2, dec_all → sub_list]

Step2: Template Extraction

• 서로 매칭된 함수 사이의 syntactic difference를 통해 패치 템플릿 추출

```
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4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10  match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

$$T = \{ \text{Modify } (8, hd + 1 \rightarrow h - 1) \}$$

Step2: Template Extraction

• 서로 매칭된 함수 사이의 syntactic difference를 통해 패치 템플릿 추출

```
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3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
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3
4
5 let rec sub_list lst =
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7    | [] -> []
8    | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10    match l with
11    | [] -> id []
12    | hd::tl -> (match o with
13    | ADD -> (hd+1)::(apply1(tl,o))
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```

```
1 let rec add_list lst =
2   match lst with
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5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

$$T = \begin{cases} & \text{Modify (8, } hd+1 \rightarrow h-1) \\ & \text{Modify (14, } dec_all \ tl \rightarrow (h-1) :: (apply2(t,o)))} \end{cases}$$

Step3: Patch Generation

• 추출한 템플릿을 원본에서 사용 가능하게 수정 후, 명세를 만족가능하게 하는 **최소 패치**를 찾음

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

$$T = \left\{ \begin{array}{c} \text{Modify (8, } hd+1 \rightarrow h-1) \\ \text{Modify (14, } dec_all \ tl \rightarrow (h-1) :: (apply2(t,o)))} \end{array} \right\}$$

Step3: Patch Generation

• 추출한 템플릿을 원본에서 사용 가능하게 수정 후, 명세를 만족가능하게 하는 **최소 패치**를 찾음

```
1 let rec inc_all l =
2   match l with
3   | [] -> []
4   | hd::tl -> (hd+1)::(inc_all tl)
5 let rec dec_all l =
6   match l with
7   | [] -> []
8   | hd::tl -> (hd+1)::(dec_all tl)
9 let apply (l, o) =
10   match l with
11   | [] -> []
12   | hd::tl -> (match o with
13   | ADD -> (hd+1)::(inc_all tl)
14   | SUB -> (dec_all tl))
```

```
1 let id x = x
2
3
4
5 let rec sub_list lst =
6    match lst with
7    | [] -> []
8    | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10    match l with
11    | [] -> id []
12    | hd::tl -> (match o with
13    | ADD -> (hd+1)::(apply1(tl,o))
14    | SUB -> (hd-1)::(sub_list tl))
```

```
1 let rec add_list lst =
2   match lst with
3   | [] -> []
4   | h::t -> (h+1)::(add_list t)
5
6
7
8
9 let rec apply2 (l, o) =
10   match l with
11   | [] -> []
12   | h::t -> (match o with
13   | ADD -> (h+1)::(inc_all t)
14   | SUB -> (h-1)::(apply2(t,o)))
```

$$T = \begin{cases} \operatorname{Modify}(8, \ hd + 1 \rightarrow hd - 1) \\ \operatorname{Modify}(14, \operatorname{dec_all} \ tl \rightarrow (hd - 1) :: (\operatorname{dec_all} \ tl)) \\ \operatorname{Modify}(14, \operatorname{dec_all} \ tl \rightarrow (hd - 1) :: (\operatorname{dec_all} \ l)) \\ \operatorname{Modify}(14, \operatorname{dec_all} \ tl \rightarrow (hd - 1) :: (\operatorname{inc_all} \ tl)) \\ \operatorname{Modify}(14, \operatorname{dec_all} \ tl \rightarrow (hd - 1) :: (\operatorname{inc_all} \ l)) \end{cases}$$

Step3: Patch Generation

• 추출한 템플릿을 원본에서 사용 가능하게 수정 후, 명세를 만족가능하게 하는 **최소 패치**를 찾음

```
1 let rec inc all l =
    match l with
   | [] -> []
     | hd::tl -> (hd+1)::(inc all tl)
5 let rec dec all l =
    match l with
     | [] -> []
      hd::tl -> (hd+1)::(dec all tl)
9 let apply (l, o) =
   match l with
     [] -> []
     | hd::tl -> (match o with
        ADD -> (hd+1)::(inc all tl)
14
        SUB -> (dec all tl))
```

```
1 let id x = x
5 let rec sub list lst =
     match lst with
      | [] -> []
      | h::t -> (h-1)::(sub_list t)
9 let rec apply1 (l, o) =
10 match l with
    | [] -> id []
    | hd::tl -> (match o with
       ADD -> (hd+1)::(apply1(tl,o))
        SUB -> (hd-1)::(sub list tl))
```

```
1 let rec add list lst =
    match lst with
    | [] -> []
     | h::t -> (h+1)::(add list t)
9 let rec apply2 (l, o) = \frac{1}{2}
    match l with
     [] -> []
     h::t -> (match o with
        ADD -> (h+1)::(inc all t)
        SUB \rightarrow (h-1)::(apply2(t,o)))
```

```
Modify (8, hd+1 \rightarrow hd-1)
           Modify(14,dec_all tl \rightarrow (hd-1) :: (dec_all \ tl))
             Modify (14 \text{ dec all } t) \rightarrow (hd - 1) \cdots (dec all l)
두 템플릿을 사용하면 최소 수정으로 패치 생성 가능
             Modify (14, dec_all\ tl \rightarrow (hd-1) :: (inc_all\ l))
```

Evaluation: Performance of CAFE

• 벤치마크: 실제 학생들이 수업에서 제출한 4,211 (3,547 correct / 664 incorrect) 개의 OCaml 코드 사용

- 비교 대상:
 - FixML (OOPSLA 18): OCaml을 대상으로 하는 가장 최신의 피드백 생성 기술
 - SARFGEN (PLDI 18): Python을 대상으로 하는 syntax-based data-driven 피드백 생성 기술
- SARFGEN이 Python을 위한 기술이기 때문에, 다음의 두가지 버전의 SARFGEN을 구현해 실험:
 - Prog: SARFGEN의 매칭 기술을 프로그램 단위로 적용한 피드백 생성 기술
 - Func: SARFGEN의 매칭 기술을 **함수 단위**로 적용한 피드백 생성 기술

Evaluation: Performance of CAFE

- 다른 모든 기술에 비해 CAFE의 성능이 뛰어남을 확인
- 문제의 난이도가 어려워져도, 여전히 피드백을 잘 생성함

| No | #Wrong | #Correct | FixML | | Prog | | Func | | Cafe | |
|----|--------|----------|-------|-------------|------|-------------|------|-------------|------|-------------|
| | | | Time | #Fix (Rate) | Time | #Fix (Rate) | Time | #Fix (Rate) | Time | #Fix (Rate) |
| 1 | 45 | 171 | 0.3 | 40 (89%) | 0.0 | 33 (73%) | 0.0 | 45 (100%) | 0.0 | 45 (100%) |
| 2 | 19 | 117 | 3.1 | 12 (63%) | 0.0 | 19 (100%) | 0.0 | 19 (100%) | 0.0 | 19 (100%) |
| 3 | 9 | 88 | 0.1 | 7 (78%) | 0.0 | 8 (89%) | 0.0 | 8 (89%) | 0.0 | 9 (100%) |
| 4 | 32 | 704 | 1.6 | 12 (38%) | 3.2 | 17 (53%) | 3.2 | 17 (53%) | 2.1 | 29 (91%) |
| 5 | 49 | 454 | 11.8 | 26 (53%) | 2.7 | 31 (63%) | 2.6 | 35 (71%) | 1.1 | 42 (86%) |
| 6 | 32 | 125 | 4.1 | 10 (31%) | 1.0 | 8 (25%) | 1.6 | 9 (28%) | 3.0 | 23 (72%) |
| 7 | 35 | 412 | 23.3 | 18 (51%) | 8.7 | 25 (71%) | 3.1 | 23 (66%) | 1.0 | 30 (86%) |
| 8 | 111 | 597 | 1.5 | 44 (40%) | 2.1 | 67 (60%) | 1.8 | 71 (64%) | 0.5 | 78 (70%) |
| 9 | 141 | 661 | 1.5 | 23 (16%) | 0.5 | 71 (50%) | 2.7 | 99 (70%) | 1.8 | 133 (94%) |
| 10 | 191 | 218 | 1.1 | 42 (22%) | 1.6 | 114 (60%) | 2.4 | 118 (62%) | 3.0 | 140 (73%) |
| | 664 | 3,547 | 3.9 | 234 (35%) | 1.9 | 393 (59%) | 2.1 | 444 (67%) | 1.6 | 548 (83%) |

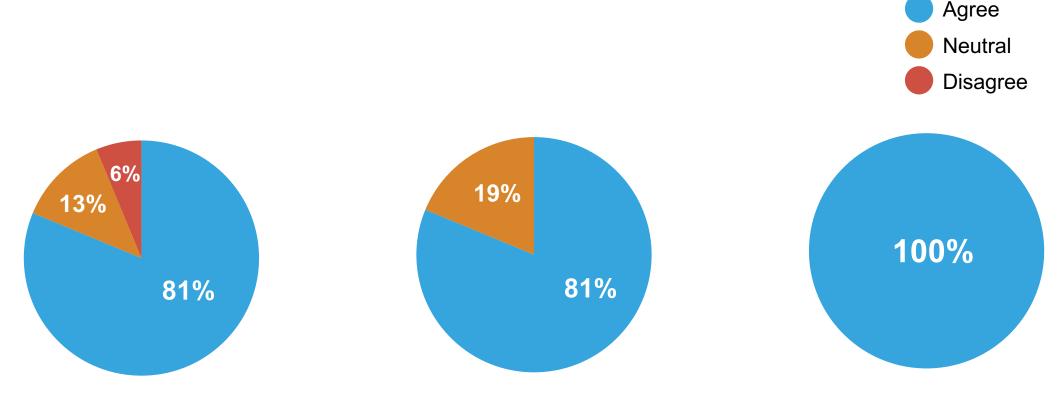
Evaluation: Performance of CAFE

- 다른 모든 기술에 비해 CAFE의 성능이 뛰어남을 확인
- 문제의 난이도가 어려워져도, 여전히 피드백을 잘 생성함

| No | #Wrong | #Correct | FixML | | Prog | | Func | | Cafe | |
|----|---|--|-------|-------------|------|-------------|------|-------------|------|-------------|
| | | | Time | #Fix (Rate) | Time | #Fix (Rate) | Time | #Fix (Rate) | Time | #Fix (Rate) |
| 1 | 45 | 171 | 0.3 | 40 (89%) | 0.0 | 33 (73%) | 0.0 | 45 (100%) | 0.0 | 45 (100%) |
| 2 | 19 | 117 | 3.1 | 12 (63%) | 0.0 | 19 (100%) | 0.0 | 19 (100%) | 0.0 | 19 (100%) |
| 3 | 9 | 88 | 0.1 | 7 (78%) | 0.0 | 8 (89%) | 0.0 | 8 (89%) | 0.0 | 9 (100%) |
| 4 | 32 | 704 | 1.6 | 12 (38%) | 3.2 | 17 (53%) | 3.2 | 17 (53%) | 2.1 | 29 (91%) |
| 5 | 49 | 454 | 11.8 | 26 (53%) | 2.7 | 31 (63%) | 2.6 | 35 (71%) | 1.1 | 42 (86%) |
| 6 | 32 | 125 | 4.1 | 10 (31%) | 1.0 | 8 (25%) | 1.6 | 9 (28%) | 3.0 | 23 (72%) |
| 7 | 35 | 412 | 23.3 | 18 (51%) | 8.7 | 25 (71%) | 3.1 | 23 (66%) | 1.0 | 30 (86%) |
| 8 | 111 | 597 | 1.5 | 44 (40%) | 2.1 | 67 (60%) | 1.8 | 71 (64%) | 0.5 | 78 (70%) |
| 9 | 141 | 661 | 1.5 | 23 (16%) | 0.5 | 71 (50%) | 2.7 | 99 (70%) | 1.8 | 133 (94%) |
| 10 | 주가 ㄴ | 중간 난이도 (82%), 고급 난이도 (79%) 문제도 높은 수치의 피드백 생성 (73%) | | | | | | | | |
| | (02.0), (02.0) , (02.0) , (02.0) , (02.0) | | | | | | | | | |

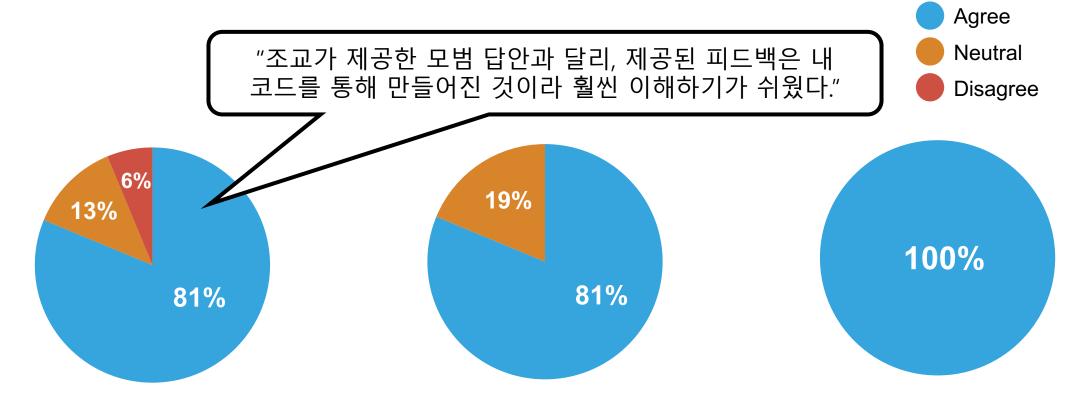
Evaluation: User Study

- 16명의 학부생들을 대상으로 다음의 설문에 대한 응답을 기록:
 - Q1: 제공된 피드백이 올바르며 이해하기 쉬운지?
 - Q2: 제공된 피드백을 통해 자신의 실수를 파악할 수 있었는지?
 - Q3: CAFE가 실제 수업에서 활용이 된다면 유용할 것 같은지?



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Discussion: Limitation of CAFE

- 피드백 생성 실패 가장 주요한 원인: 패치 생성 시간 초과
 - 현재 알고리즘은 가장 적은 수의 템플릿부터 적용을 시도
 - 작은 템플릿을 여러개 적용해야 하는 패치의 경우 패치를 잘 만들지 못함

```
1 let rec eval_exp e =
2  match e with
3  | Int n -> -> n
4  | Add (e1, e2) -> (eval_exp e1) + (eval_exp e2)
5  | Sub (e1, e2) -> (eval_exp e1) - (eval_exp e2)
6 let rec eval f =
7  match f with
8  | True -> true
9  | False -> false
10  | Not f -> if f = True then false else true
11  | AndAlso (f1, f2) -> if f1 = True && f2 = True then true else false
12  | OrElse (f1, f2) -> if f1 = True && f2 = False then false else true
13  | Imply (f1, f2) -> if f1 = True && f2 = False then false else true
14  | Equal (e1, e2) -> (eval_exp e1) = (eval_exp e2)
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Conclusion

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• 이 문제를 해결하기 위해 **함수 단위의 context-aware matching**을 이용한 데이터 기반 피드백 생성 기술 제안

• 실제 학생들이 제출한 OCaml에 대해서 성공적으로 피드백을 생성, 학생들에게도 도움이 됨을 확인함

Tool: https://github.com/kupl/LearnML

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감사합니다!