

# Graph Theory Cheat Sheet

## Chordality

**Chordal graph:** one in which all cycles of 4 or more vertices have a chord.

**Chord:** an edge that is **NOT** part of the cycle but connect two vertices of the cycle.

**Remark:** every induced cycle in the graph should have **EXACTLY 3** vertices!

## Perfect Elimination

**Perfect elimination ordering:** ordering of vertices  $\Theta$  such that for every vertex  $\theta \in \Theta$ ,  $\theta$  and its neighbors  $\text{Ne}(\theta)$  that occur after  $\theta$  in the ordering form a clique.

**Lexicographic breadth-first search:** linear time algorithm for ordering the vertices of a graph.