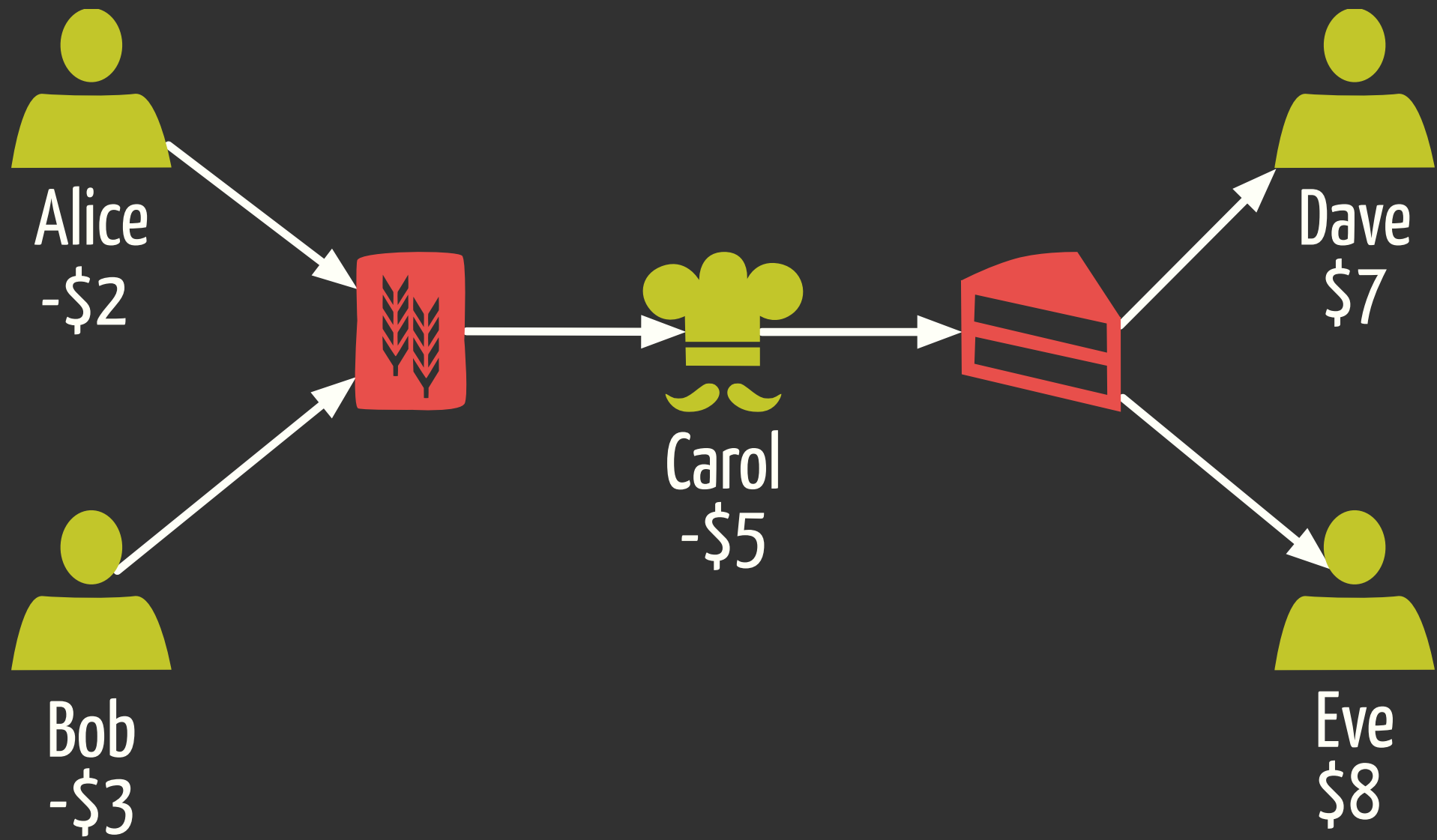
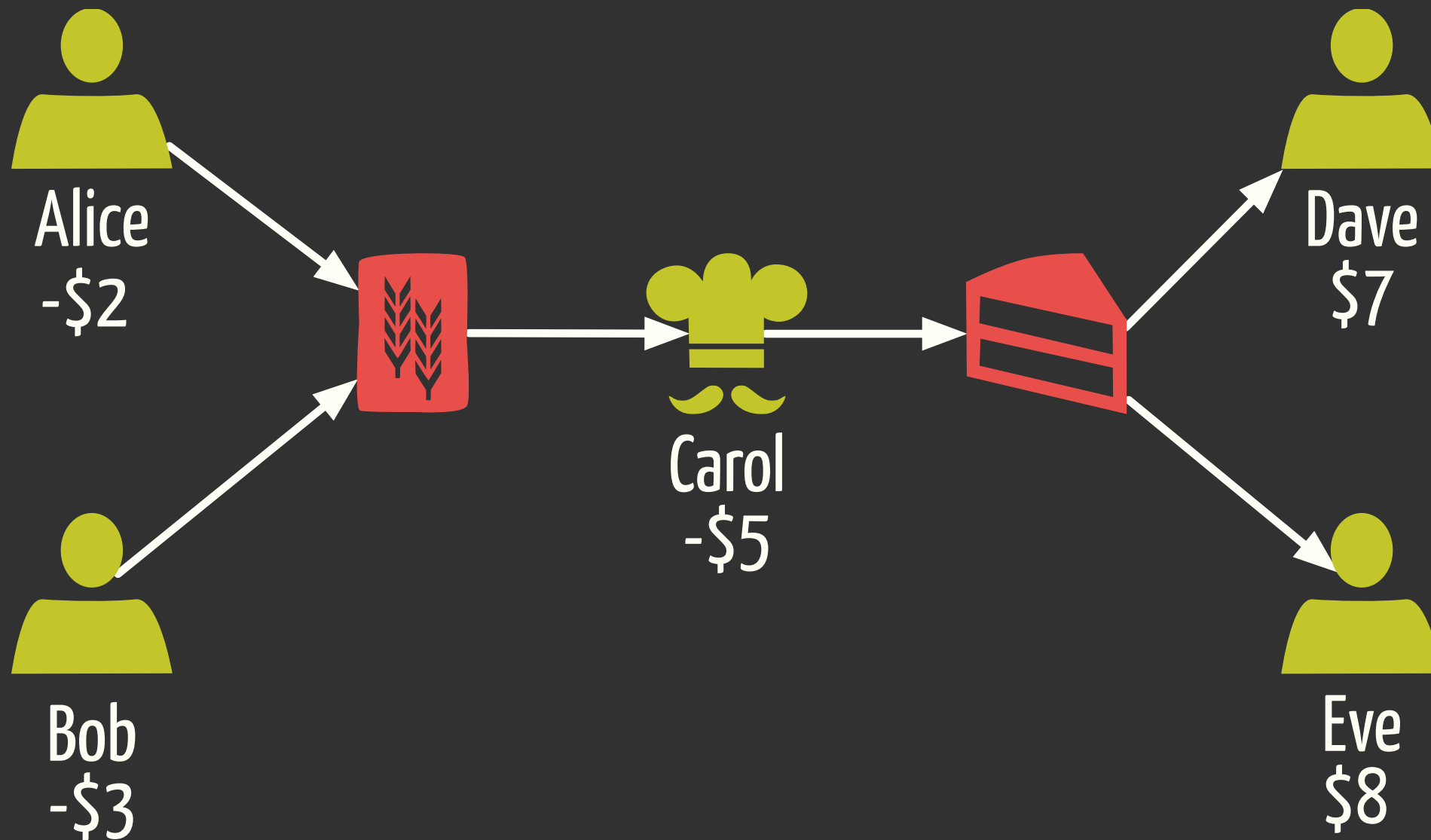


# Social Value Propagation for Supply Chain Formation

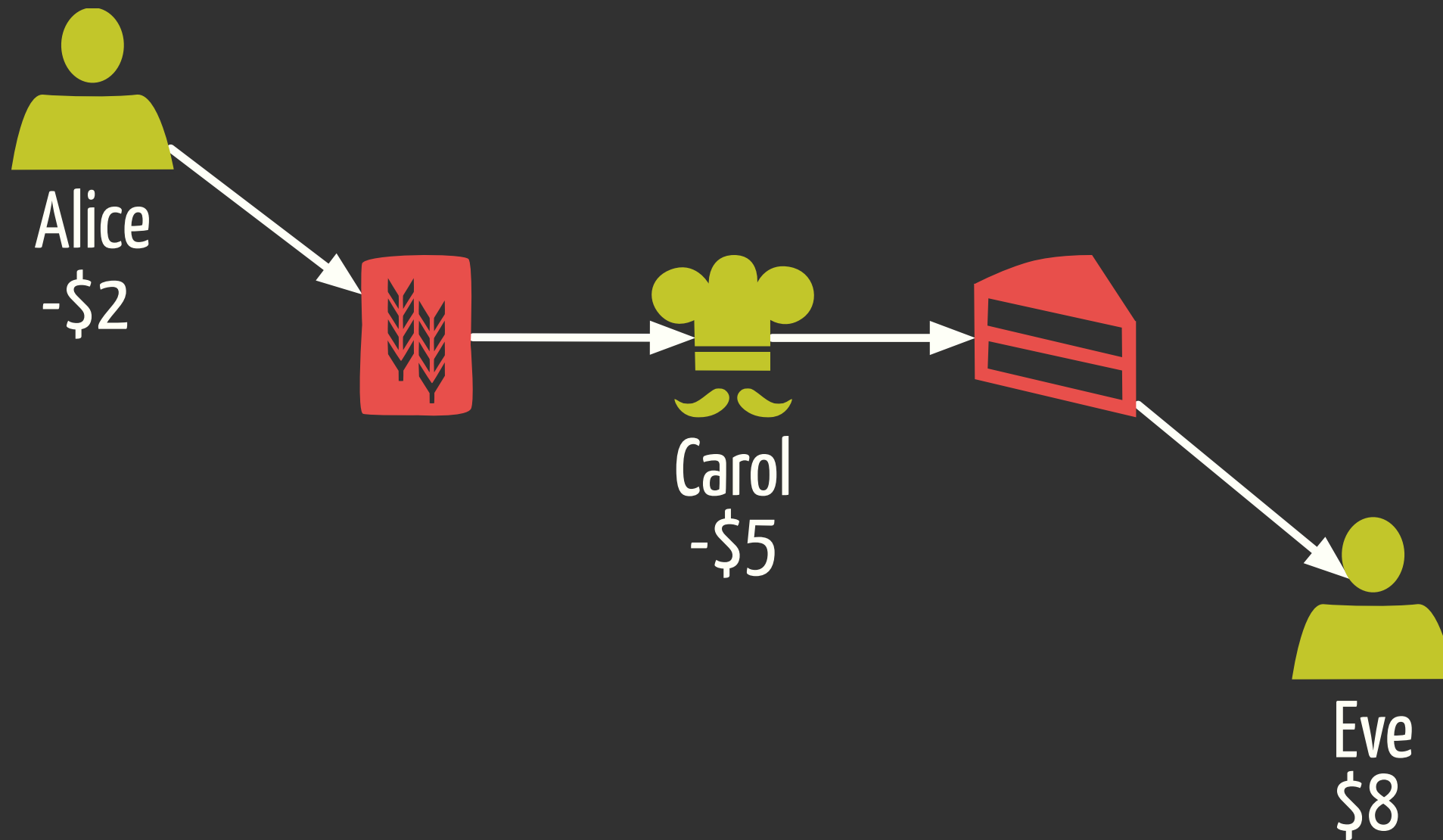
by Toni Peña-Alba, Meritxell Vinyals,  
Jesus Cerquides and Juan A. Rodriguez-Aguilar  
for the 6th International OPTMAS Workshop

The problem





The Supply Chain Formation problem is that of **finding** the **feasible configuration** with **maximum** value.



Supply Chain **Value** = \$8 - \$5 - \$2 = **\$1**

## CONTRIBUTION

Decentralized algorithm for SCF  
based on **social value** propagation.

## BENEFITS

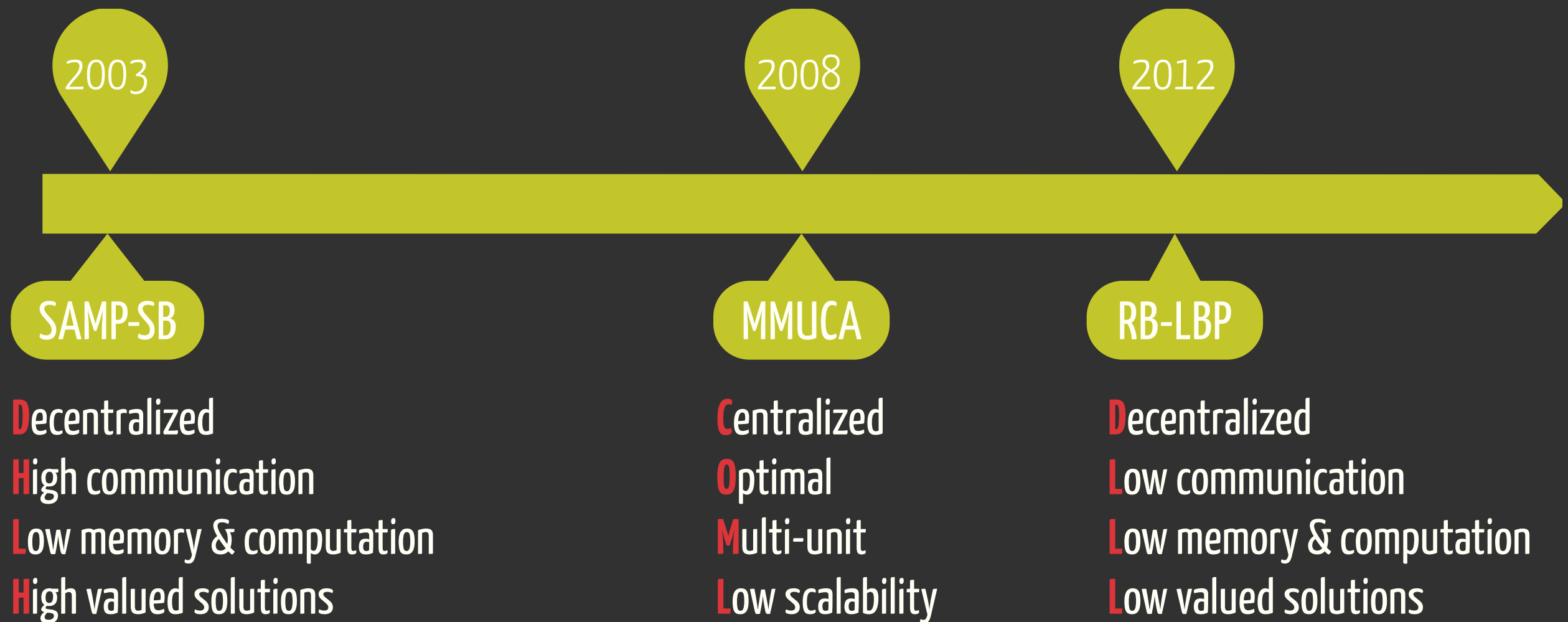
Reduces computation.

Reduces communication.

Produces (near)**optimal** solutions.

Related work

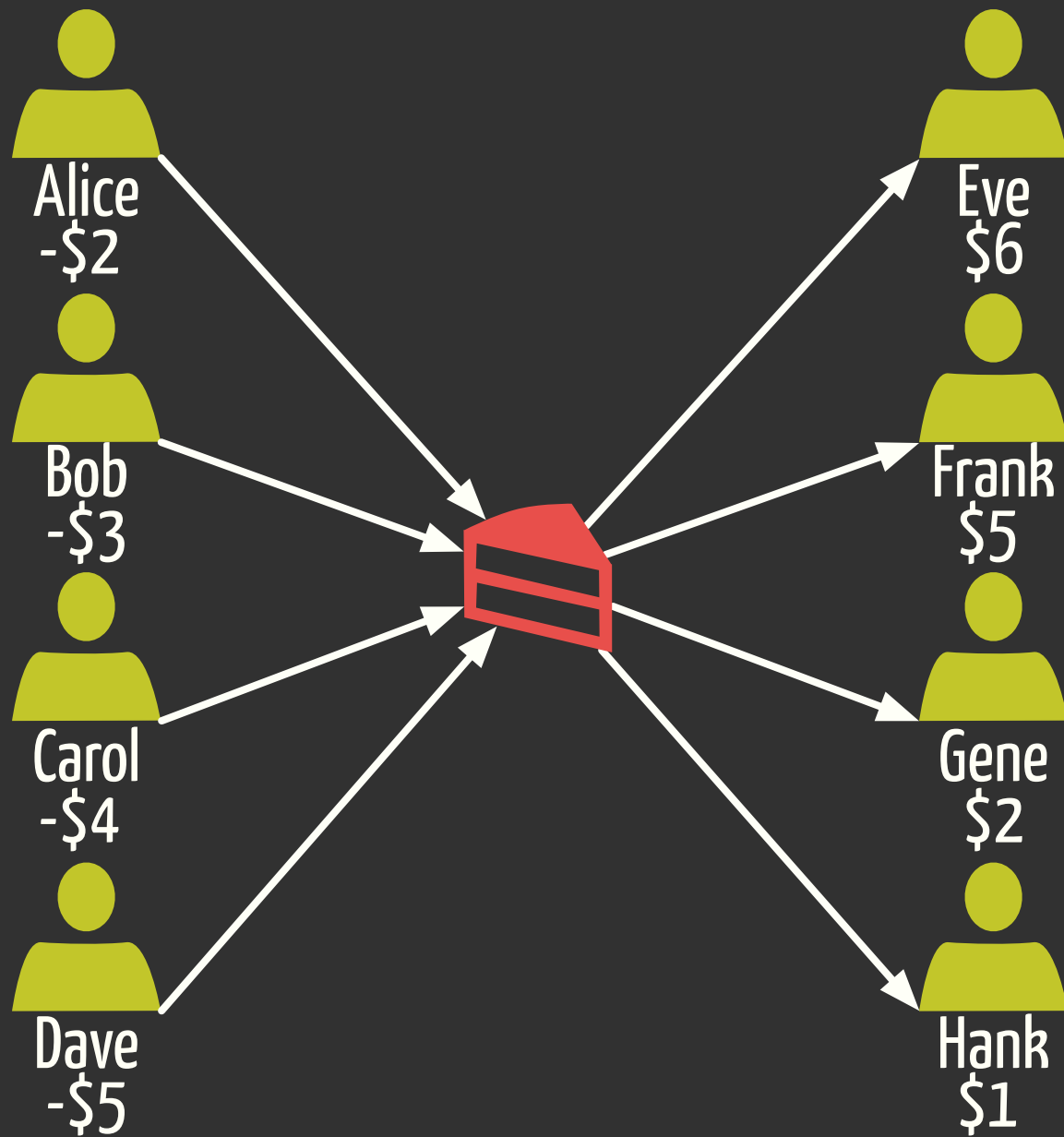
# SUPPLY CHAIN FORMATION TIMELINE



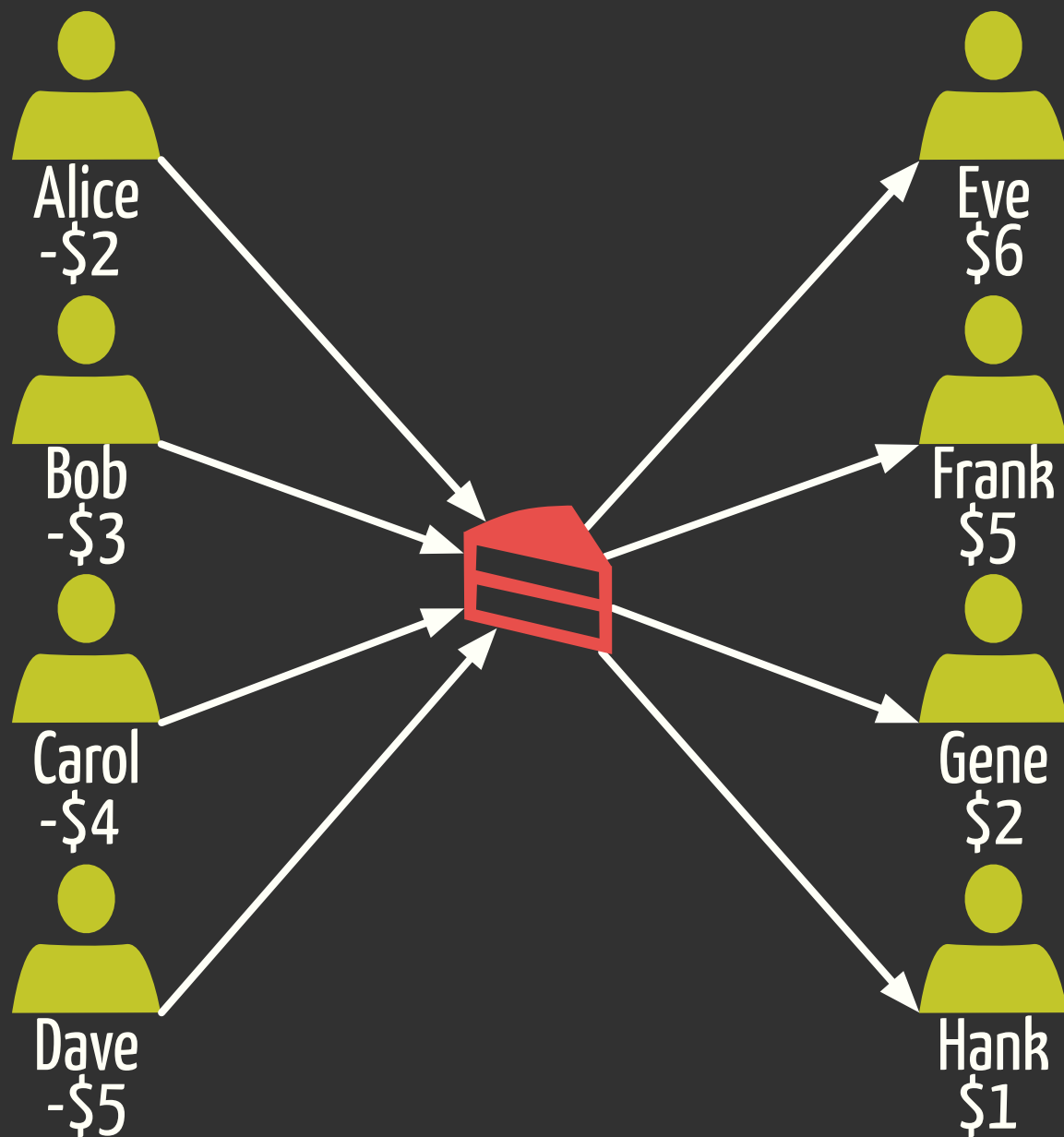


# Social Value Propagation

# PARTICIPANT'S SOCIAL VALUE

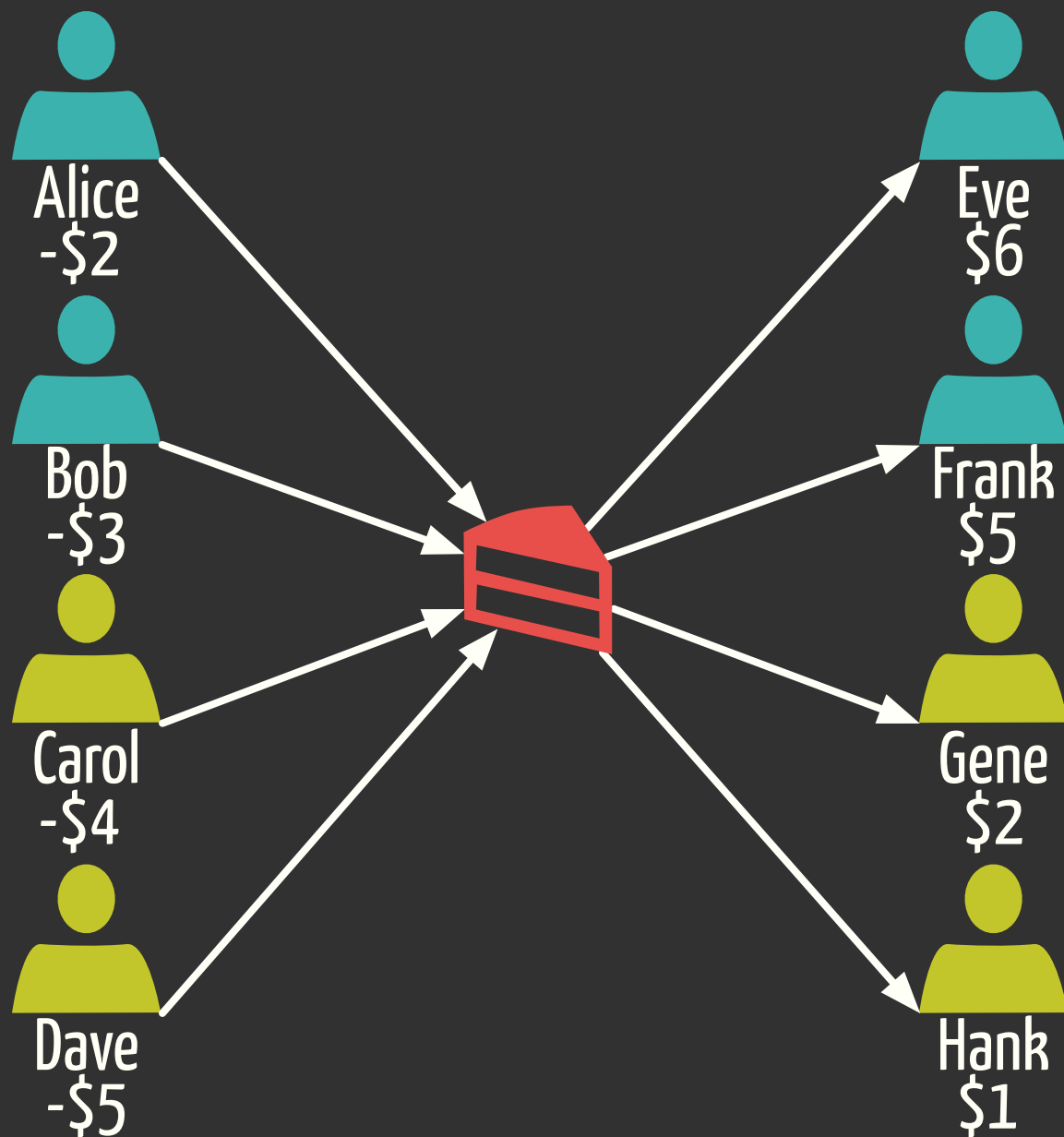


# PARTICIPANT'S SOCIAL VALUE



**Social value** for participant p  
how much better is for the  
other agents that p is active  
over p being inactive.

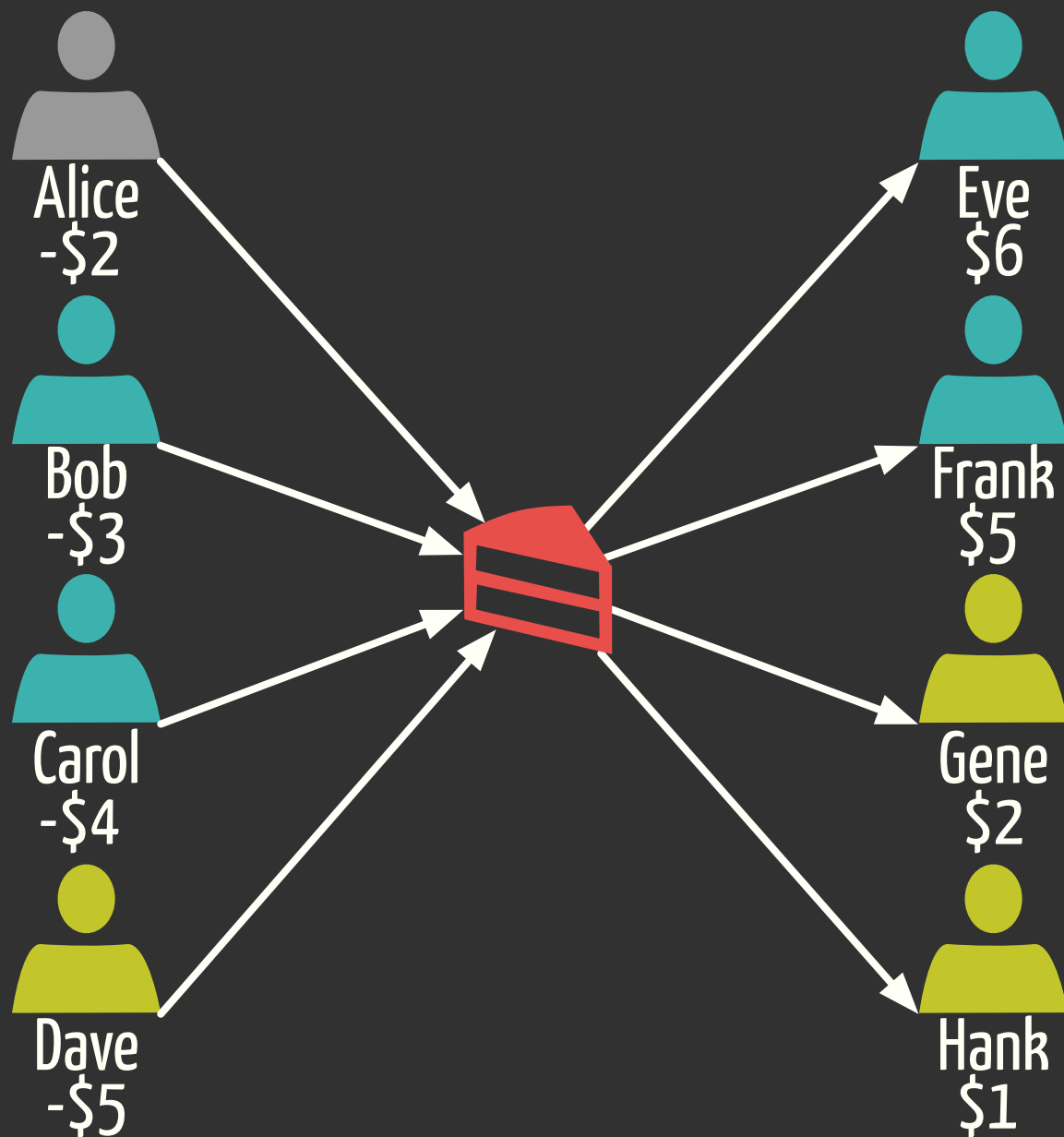
# PARTICIPANT'S SOCIAL VALUE



**Social value** for participant p  
how much better is for the  
other agents that p is active  
over p being inactive.

$$\text{With Alice} = 6 + 5 - 2 - 3 = 6$$

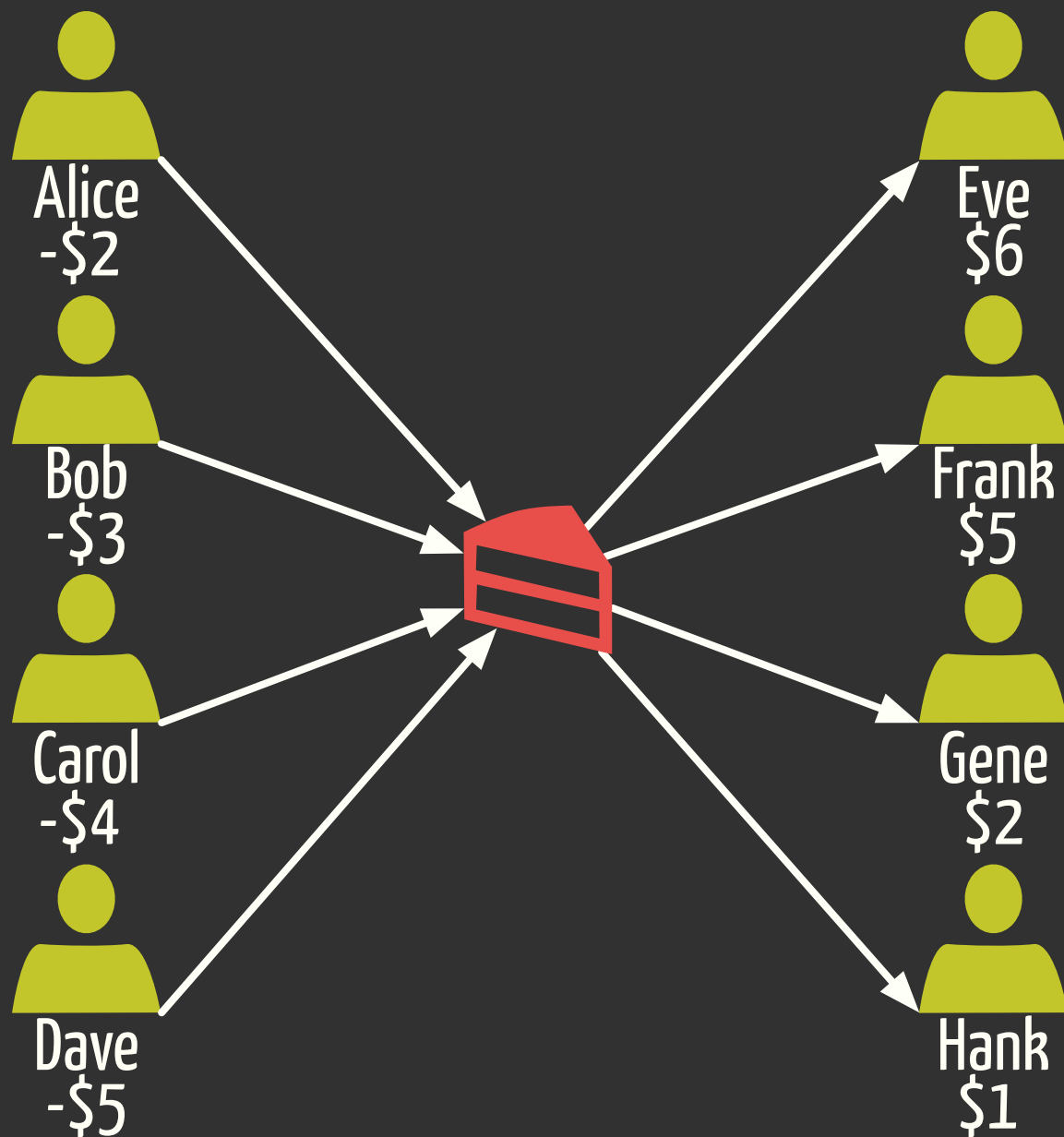
# PARTICIPANT'S SOCIAL VALUE



**Social value** for participant  $p$   
how much better is for the  
other agents that  $p$  is active  
over  $p$  being inactive.

$$\text{Without Alice} = 6 + 5 - 3 - 4 = 4$$

# PARTICIPANT'S **SOCIAL VALUE**



**Social value** for participant  $p$   
how much better is for the  
other agents that  $p$  is active  
over  $p$  being inactive.

Alice's **social value** =  $6 - 4 = 2$

# CHAINME

CHaining Agents IN  
Mediated Environments

**CHAINME** is a message passing algorithm

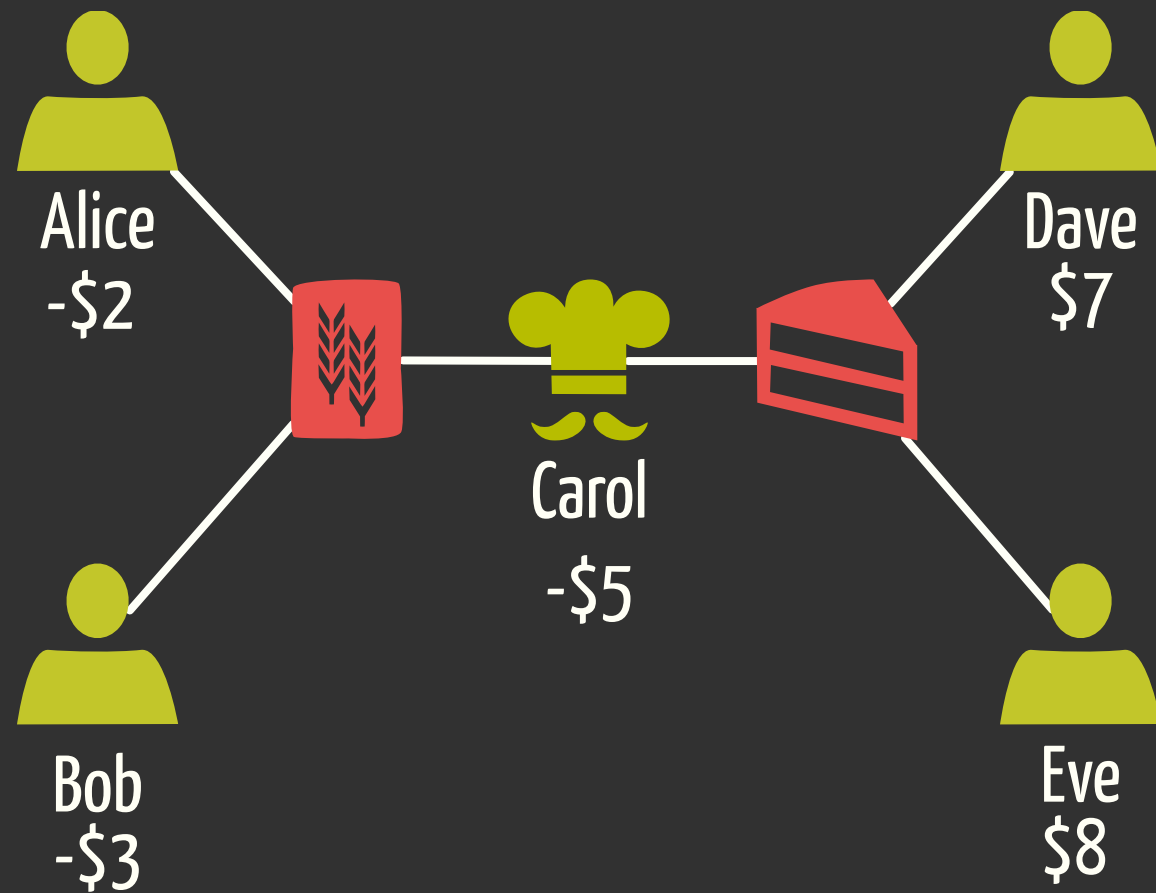
Two phases:

- Assess participants **social value**.
- Assess the **supply chain configuration**.

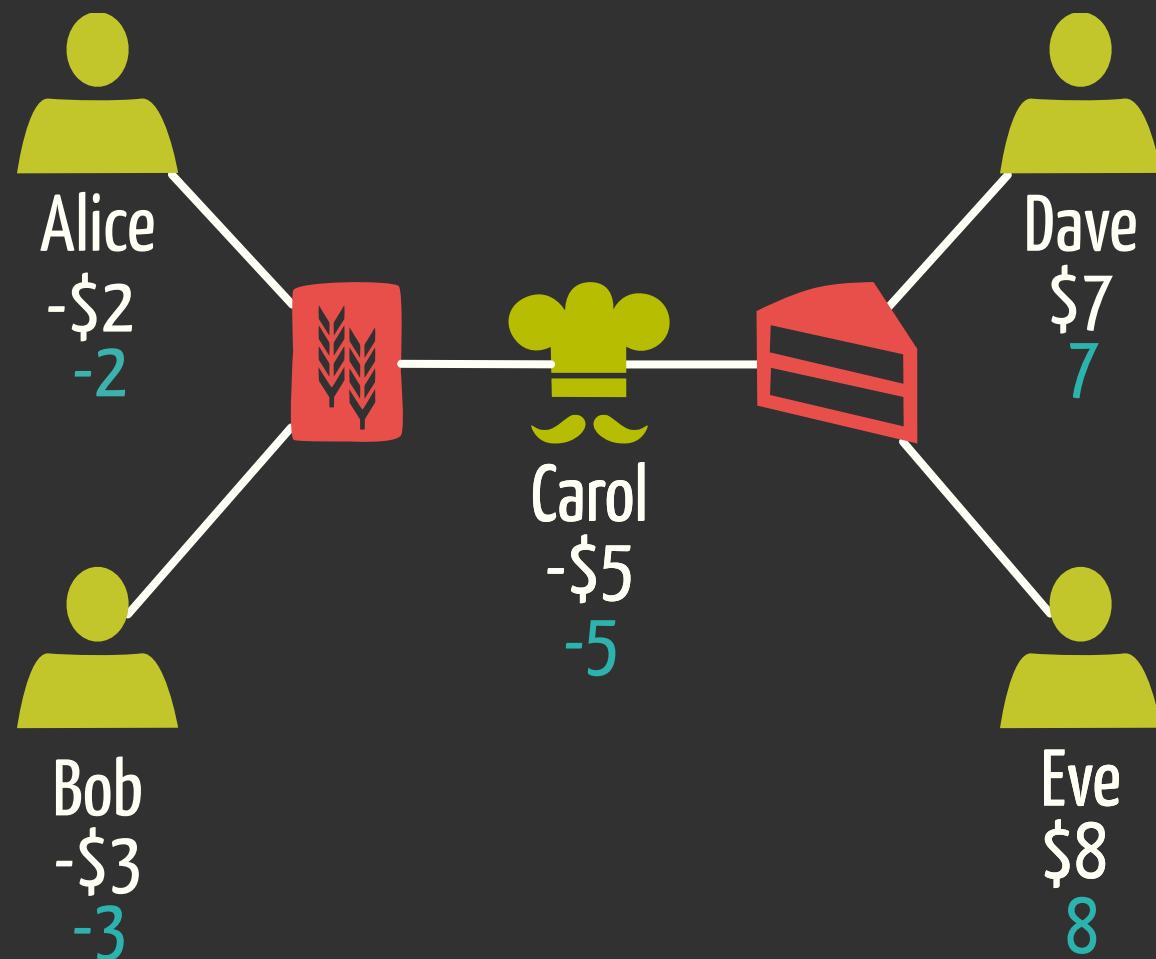


# Assessing participants' Social Value

# ASSESSING PARTICIPANTS' SOCIAL VALUE



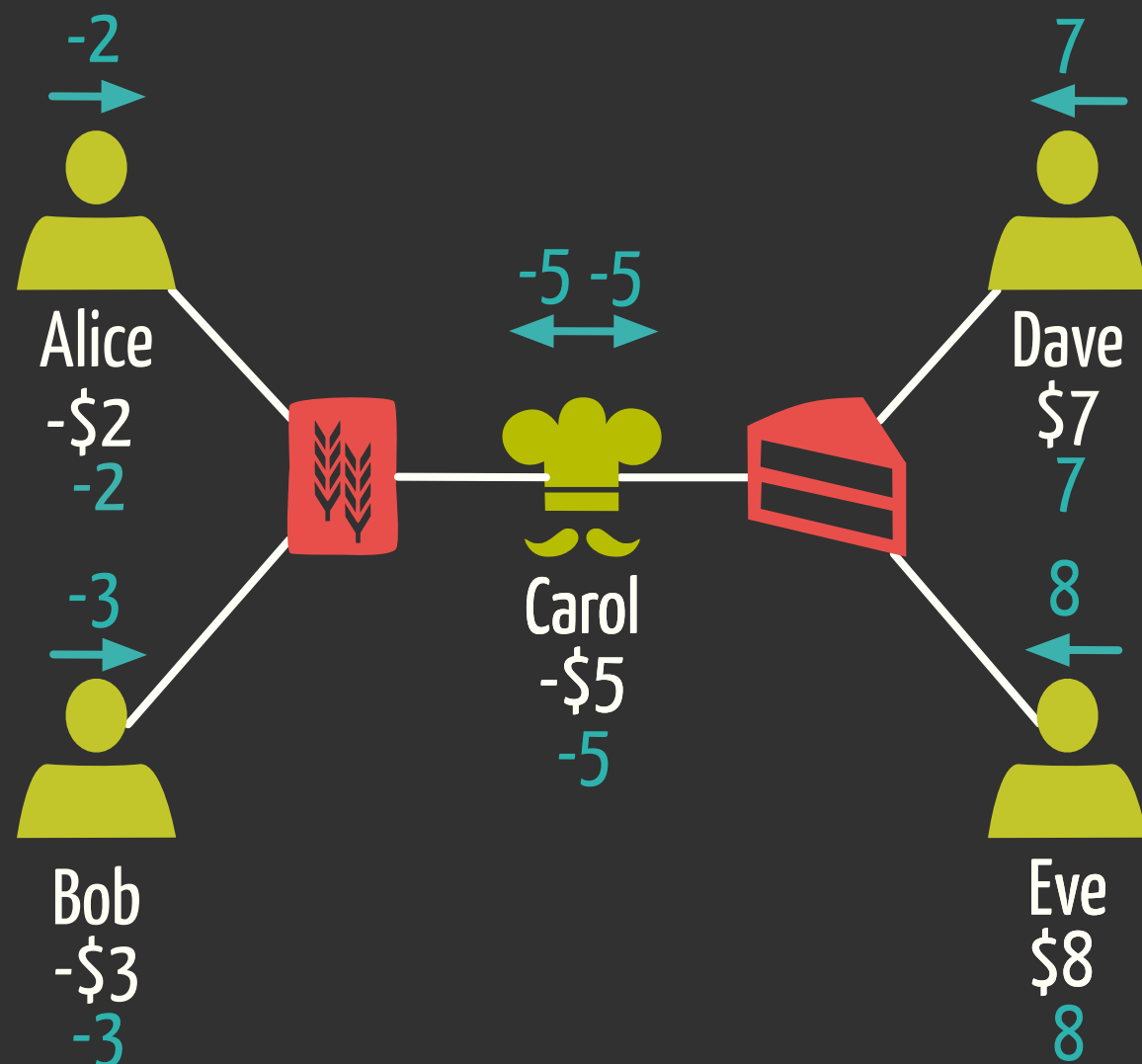
# ASSESSING PARTICIPANTS' SOCIAL VALUE



Determine **agent value**

$$V_a = C_a + \sum_{g \in G_a} S_a^g$$

# ASSESSING PARTICIPANTS' SOCIAL VALUE



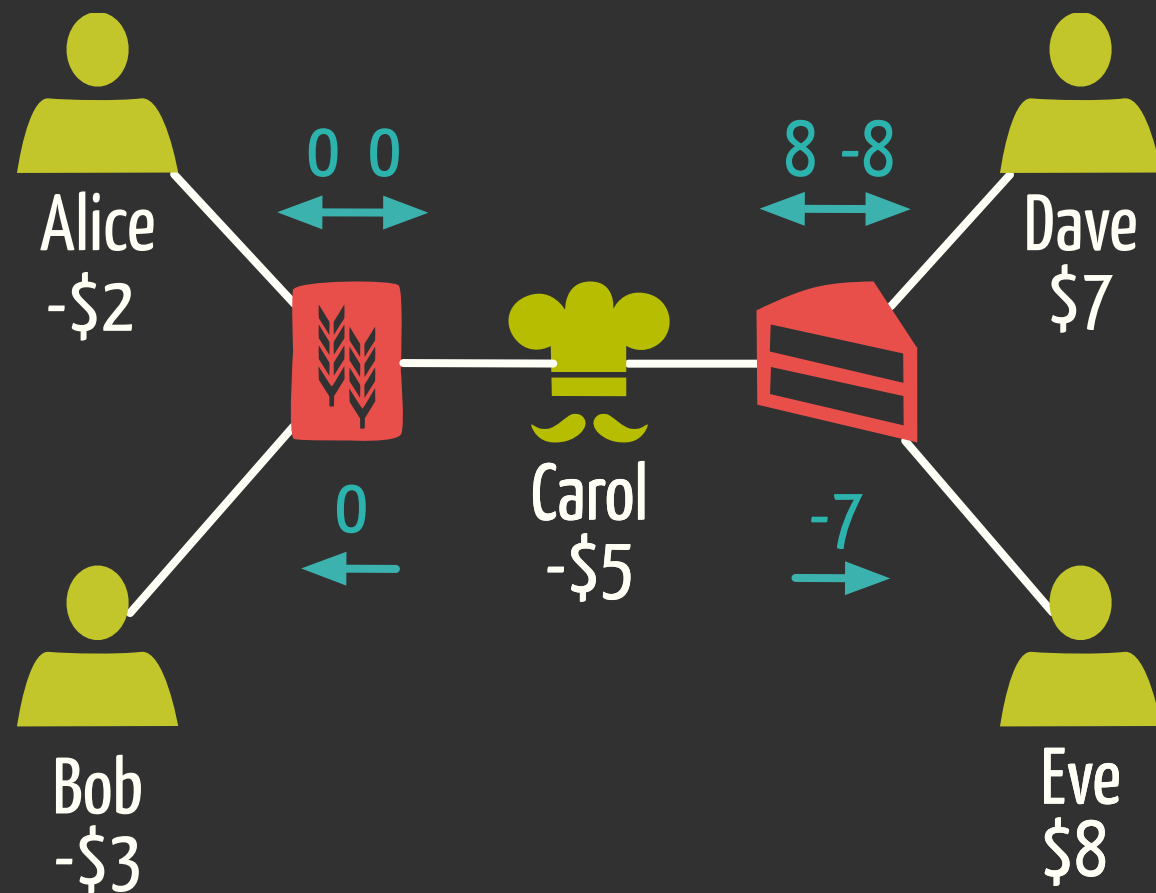
Determine **agent value**

$$V_a = C_a + \sum_{g \in G_a} S_a^g$$

**Send offer** to mediators

$$O_a^g \leftarrow V_a - S_a^g$$

# ASSESSING PARTICIPANTS' SOCIAL VALUE



Determine **agent value**

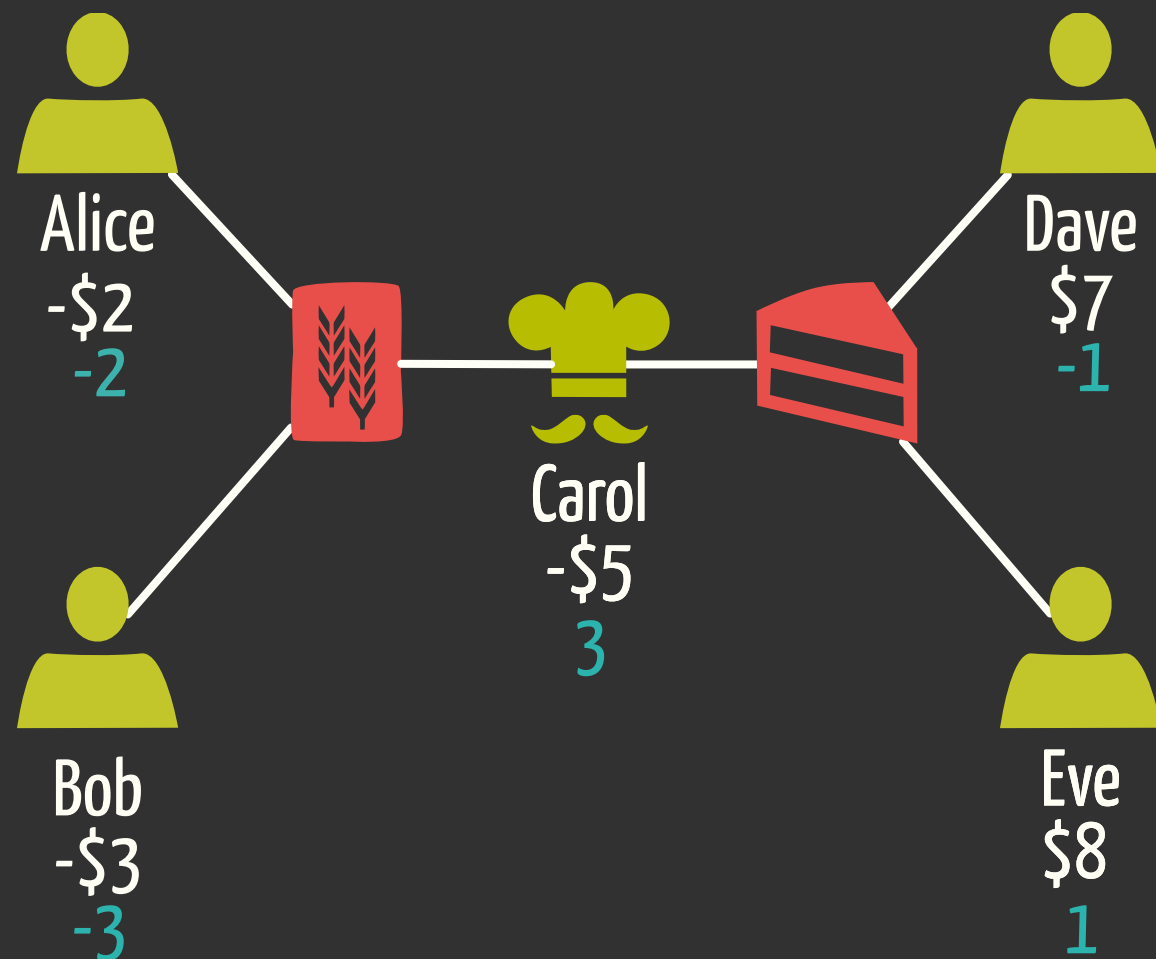
$$V_a = C_a + \sum_{g \in G_a} S_a^g$$

**Send offer** to mediators

$$O_a^g \leftarrow V_a - S_a^g$$

Send updated **social value**

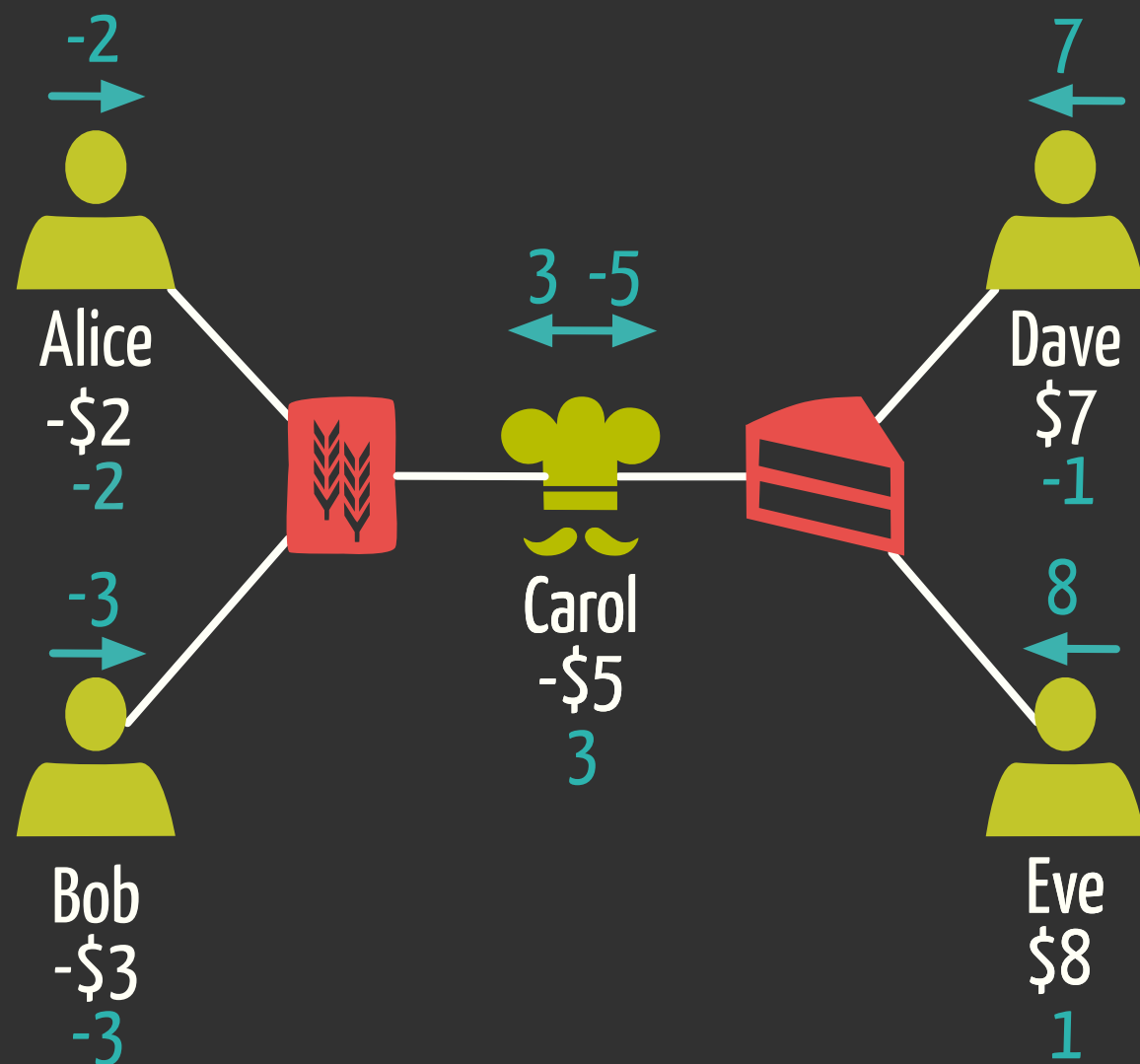
# ASSESSING PARTICIPANTS' SOCIAL VALUE



Determine **agent value**

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# ASSESSING PARTICIPANTS' SOCIAL VALUE



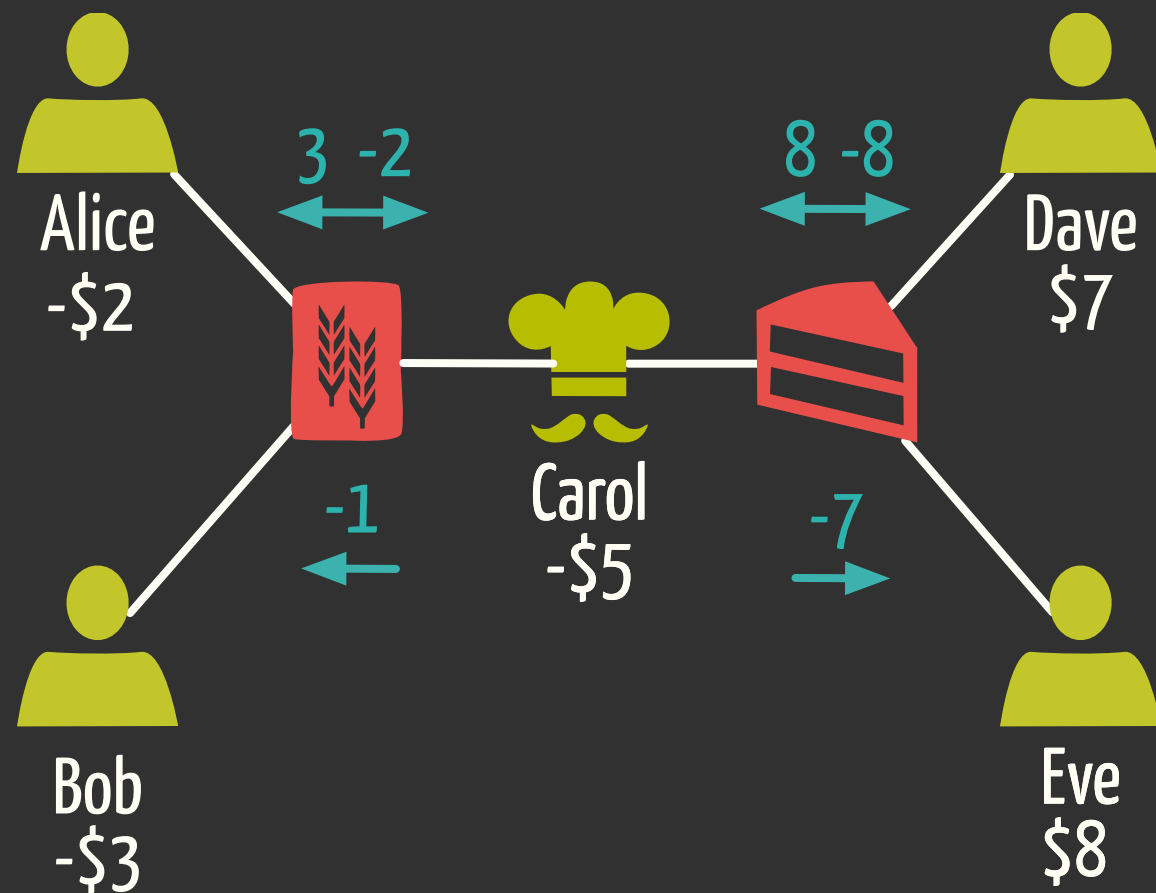
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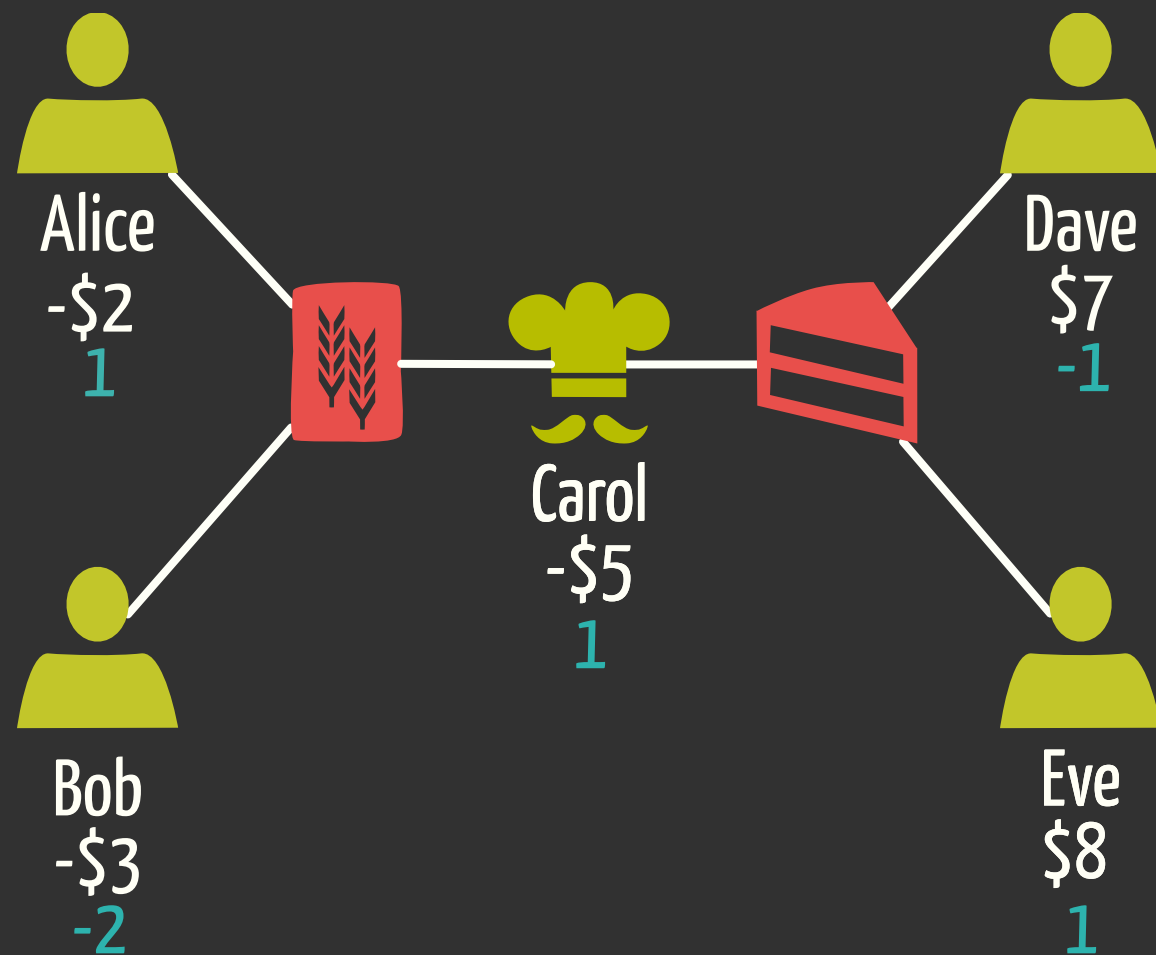
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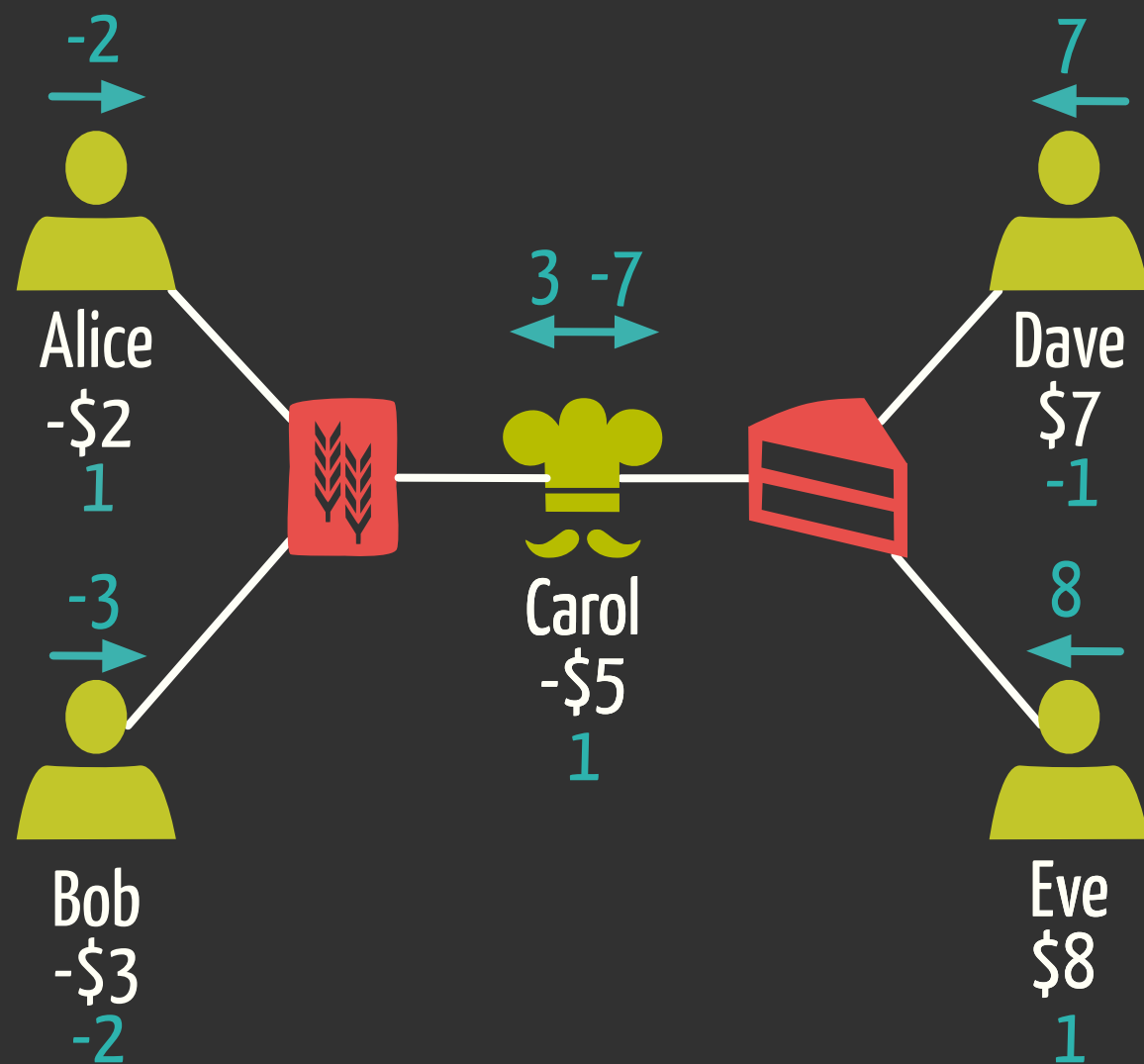
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# ASSESSING PARTICIPANTS' SOCIAL VALUE



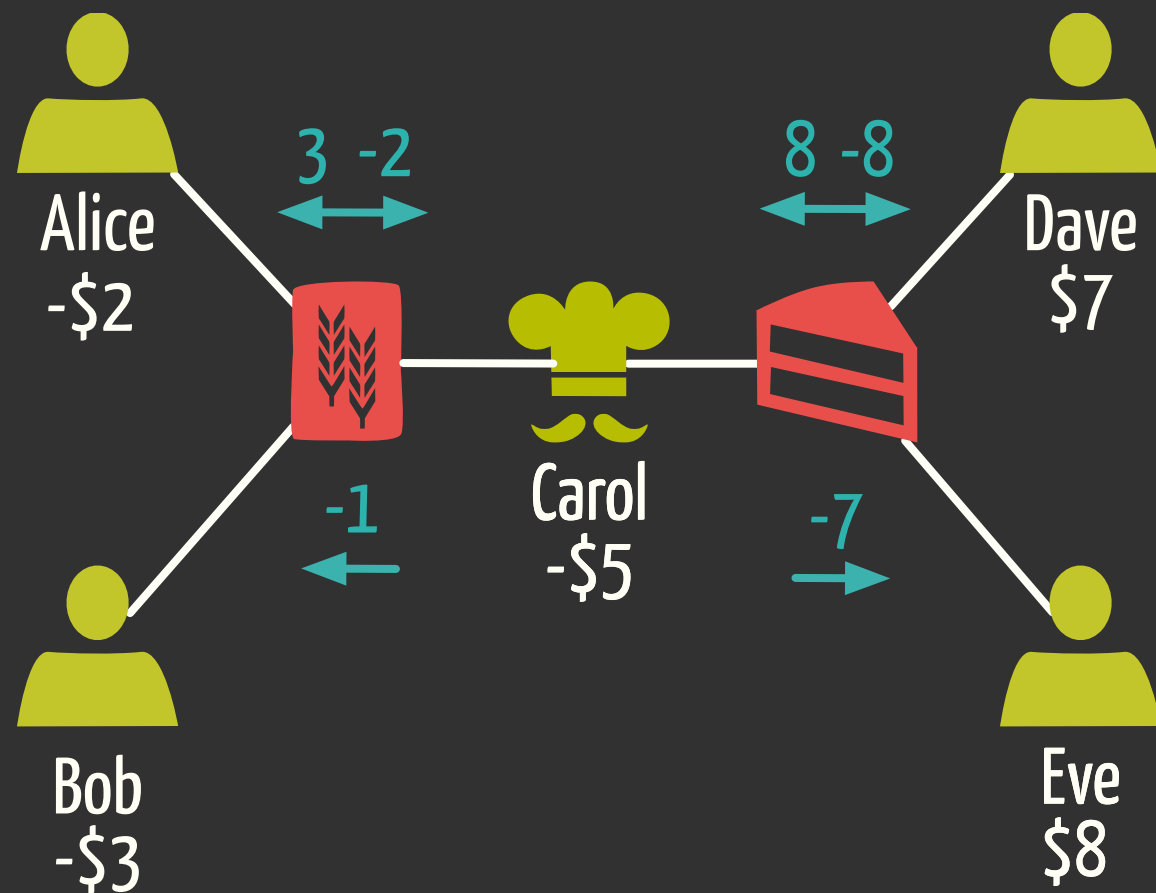
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Determine **agent value**

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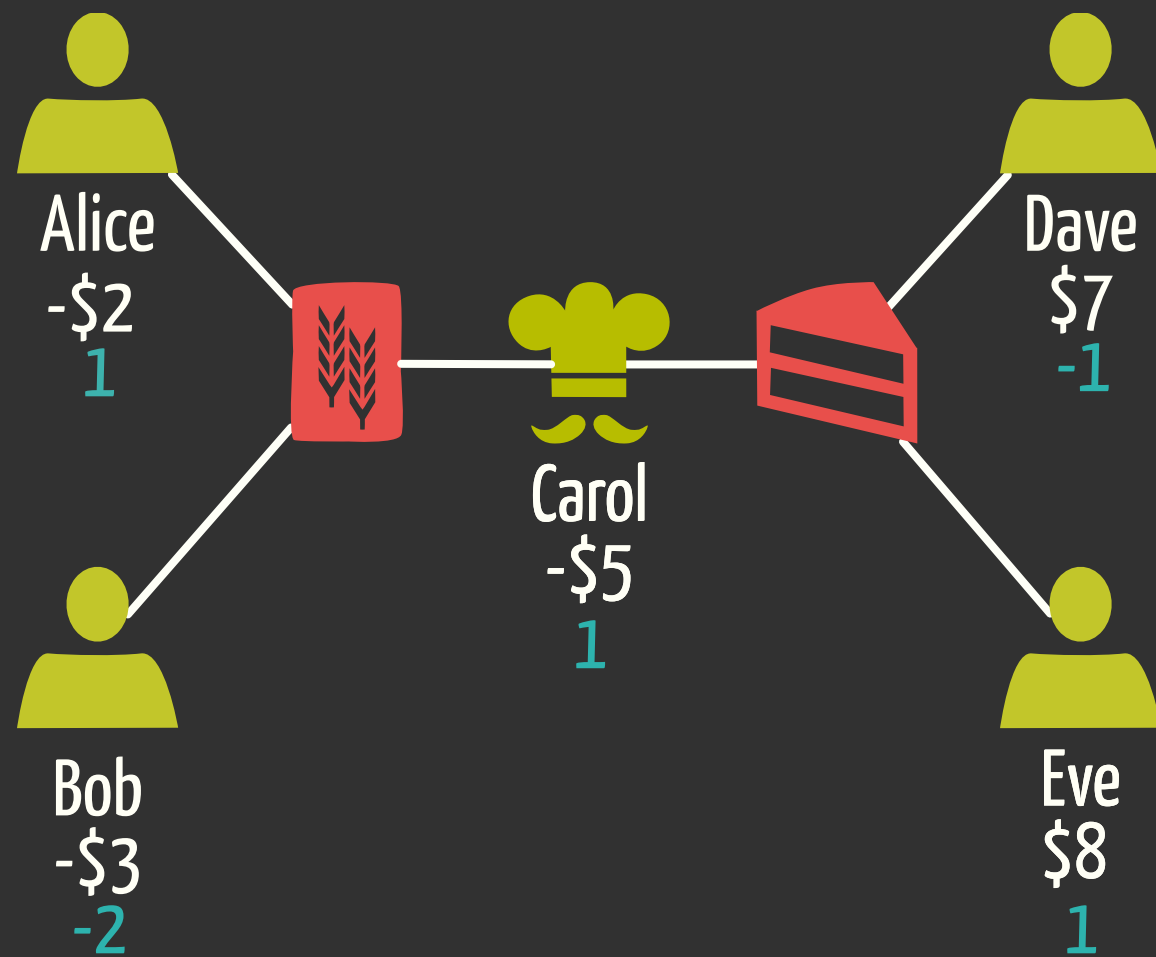
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Send updated **social value**

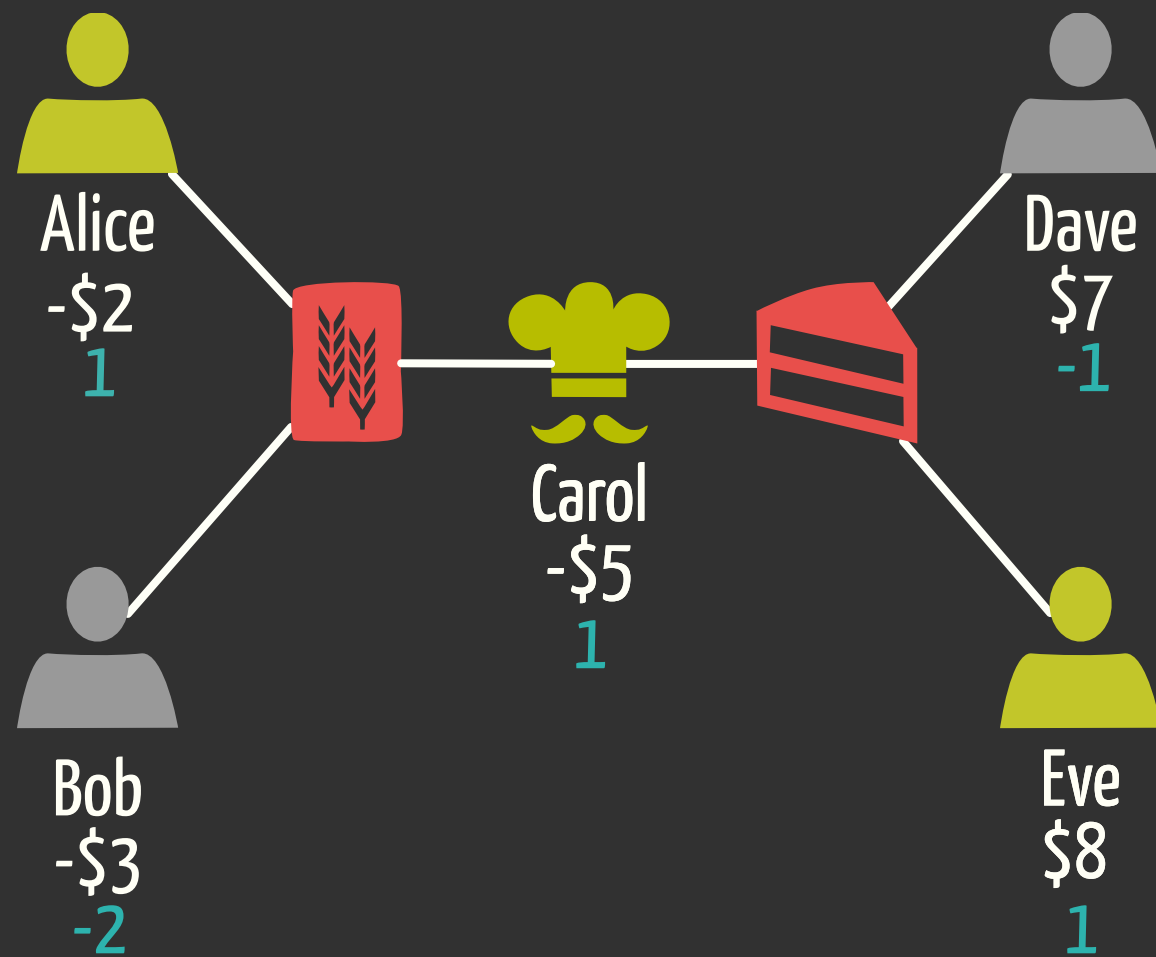
# Determining the supply chain configuration

# ASSESSING PARTICIPANTS' SOCIAL VALUE



1. **Participants** with positive value announce their **availability**.
2. **Mediators choose** active participants out of the available ones.
3. Available participants **remain available** if all their mediators choose them to be active.
4. **Back to 2.**

# ASSESSING PARTICIPANTS' SOCIAL VALUE



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4. **Back to 2.**

Does *it* work?

	SAMP-SB	RB-LBP	CHAINME
participant memory	$O(G)$	$O(G \cdot A)$	$O(G)$
mediator memory	$O(A)$		$O(A)$
participant bandwidth	$O(G)$	$O(G \cdot A)$	$O(G)$
mediator bandwidth	$O(A)$		$O(A)$
participant operations	$O(G)$	$O(G \cdot A^2)$	$O(G)$
mediator operations	$O(\log A)$		$O(A \cdot \log A)$



large networks

50 goods

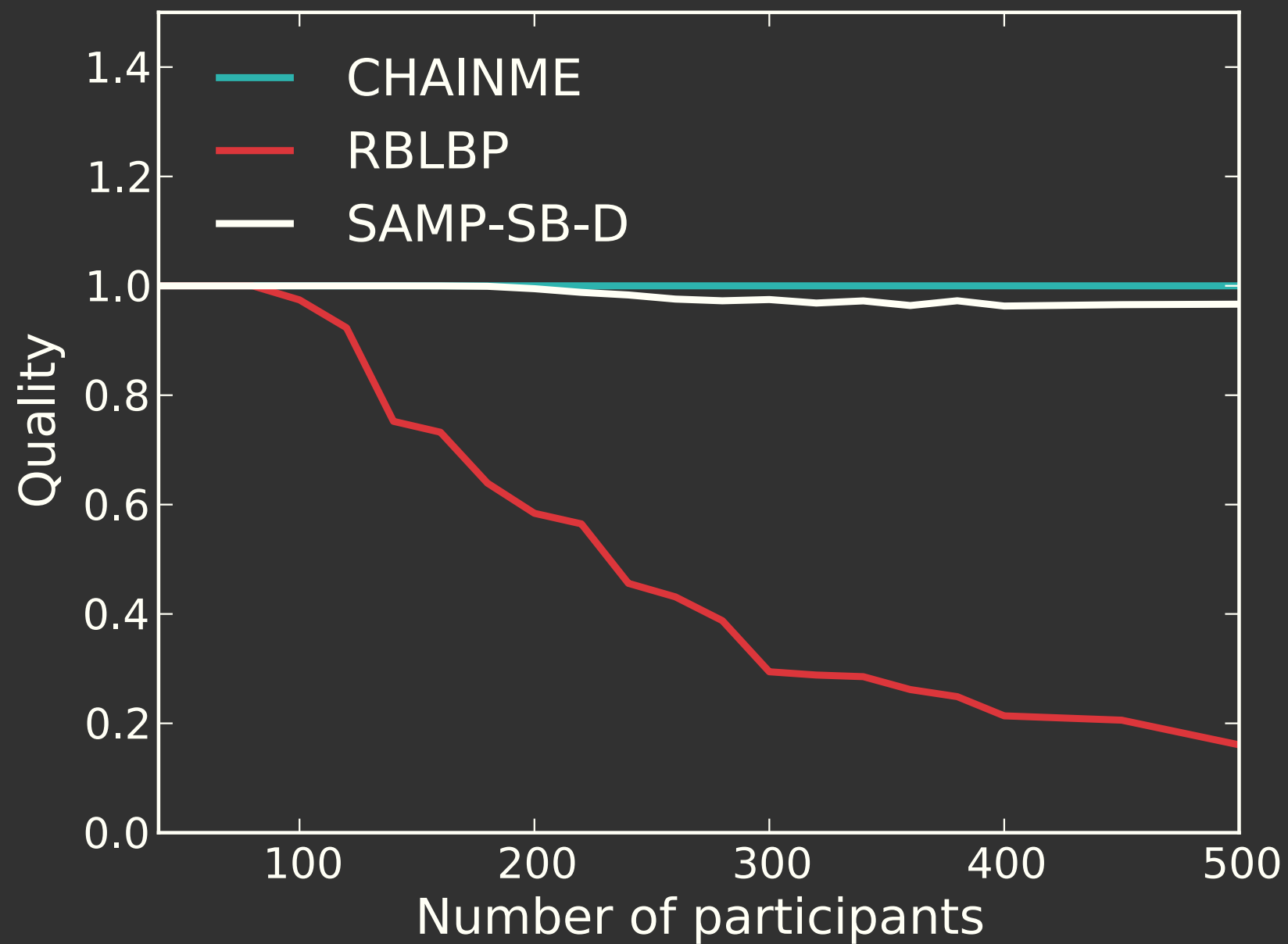
40-500 agents

up to 50 times less bandwidth

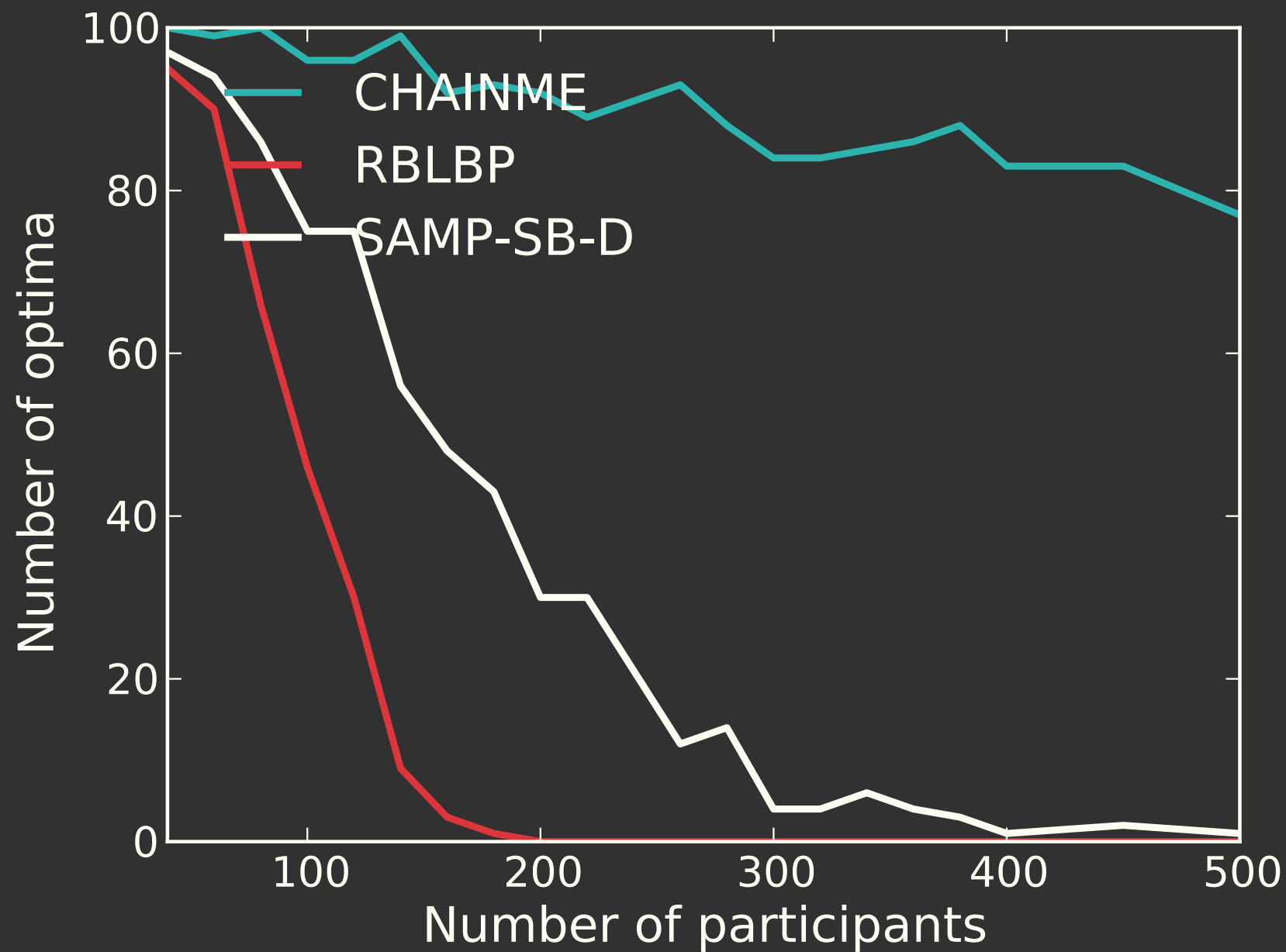
up to  $10^2$  times faster

consistently better solutions

close to 80% optimal solutions



consistently better solutions



close to 80% optimal solutions



Decentralized algorithm for SCF  
based on **social value** propagation.

**Reduces** computation.

**Reduces** communication.

Produces (near)**optimal** solutions.

What's next?

Payments  
Multiple Unit  
Time constraints  
Multiple Attributes

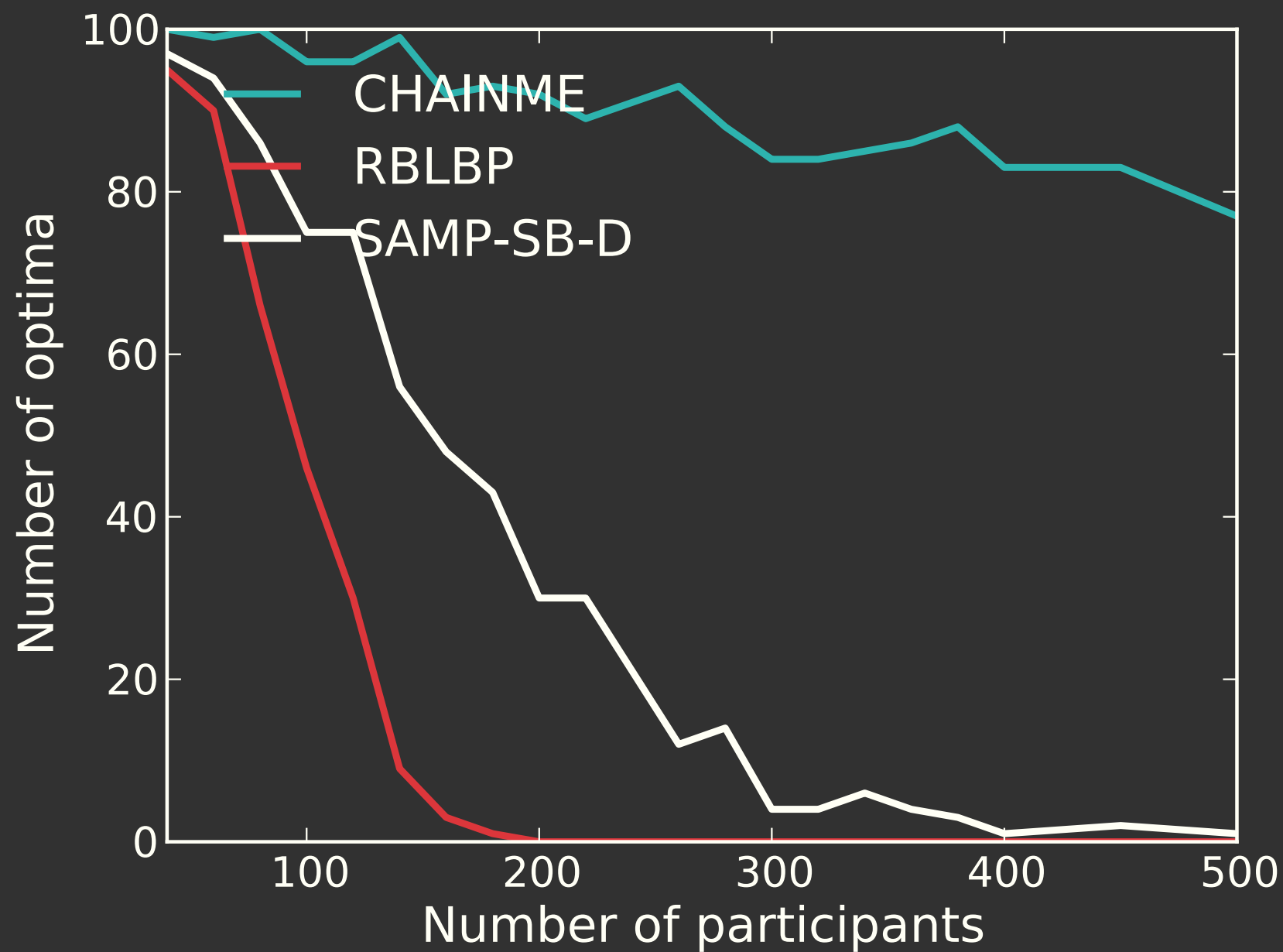
Thank You



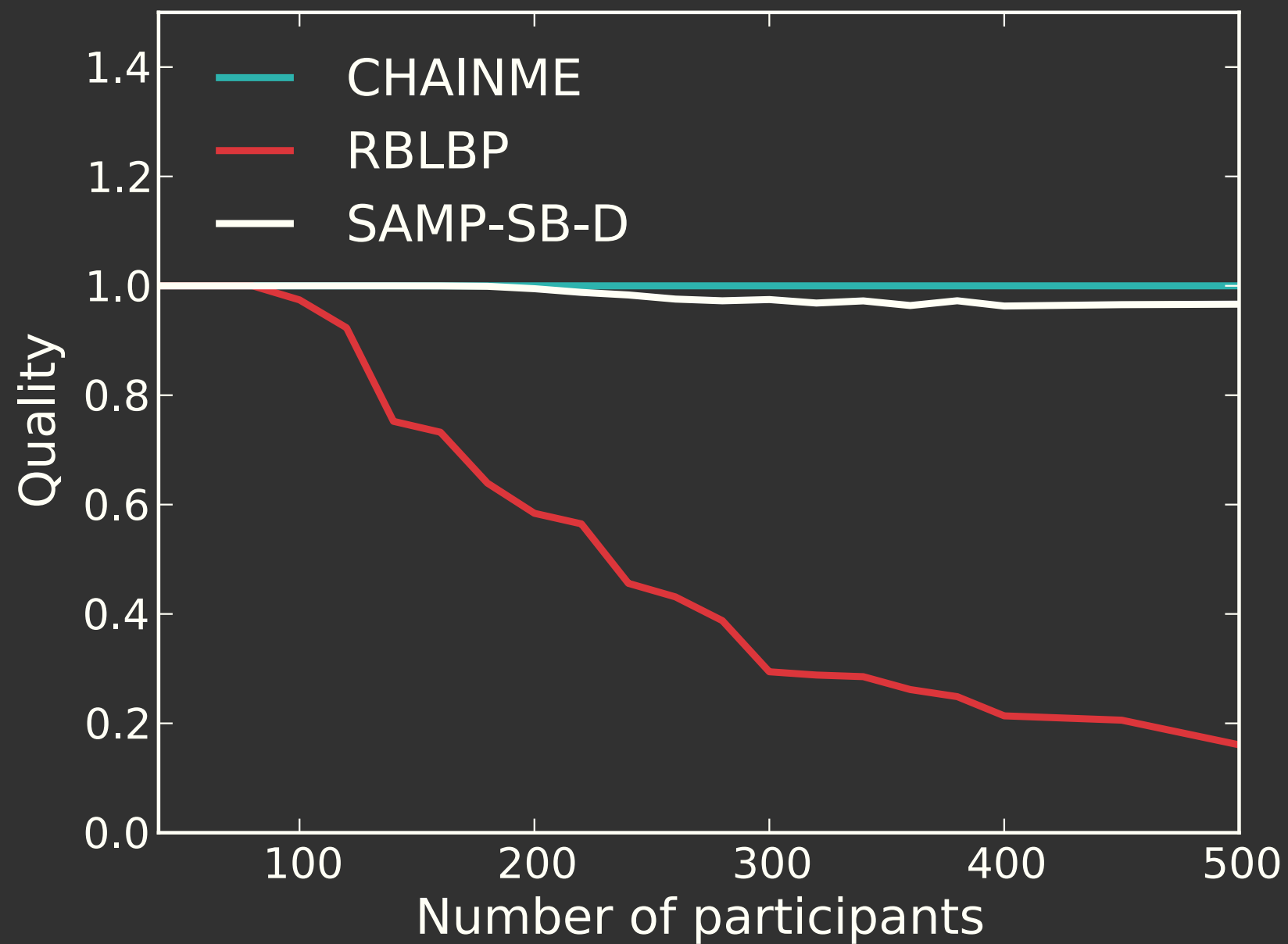
Questions?



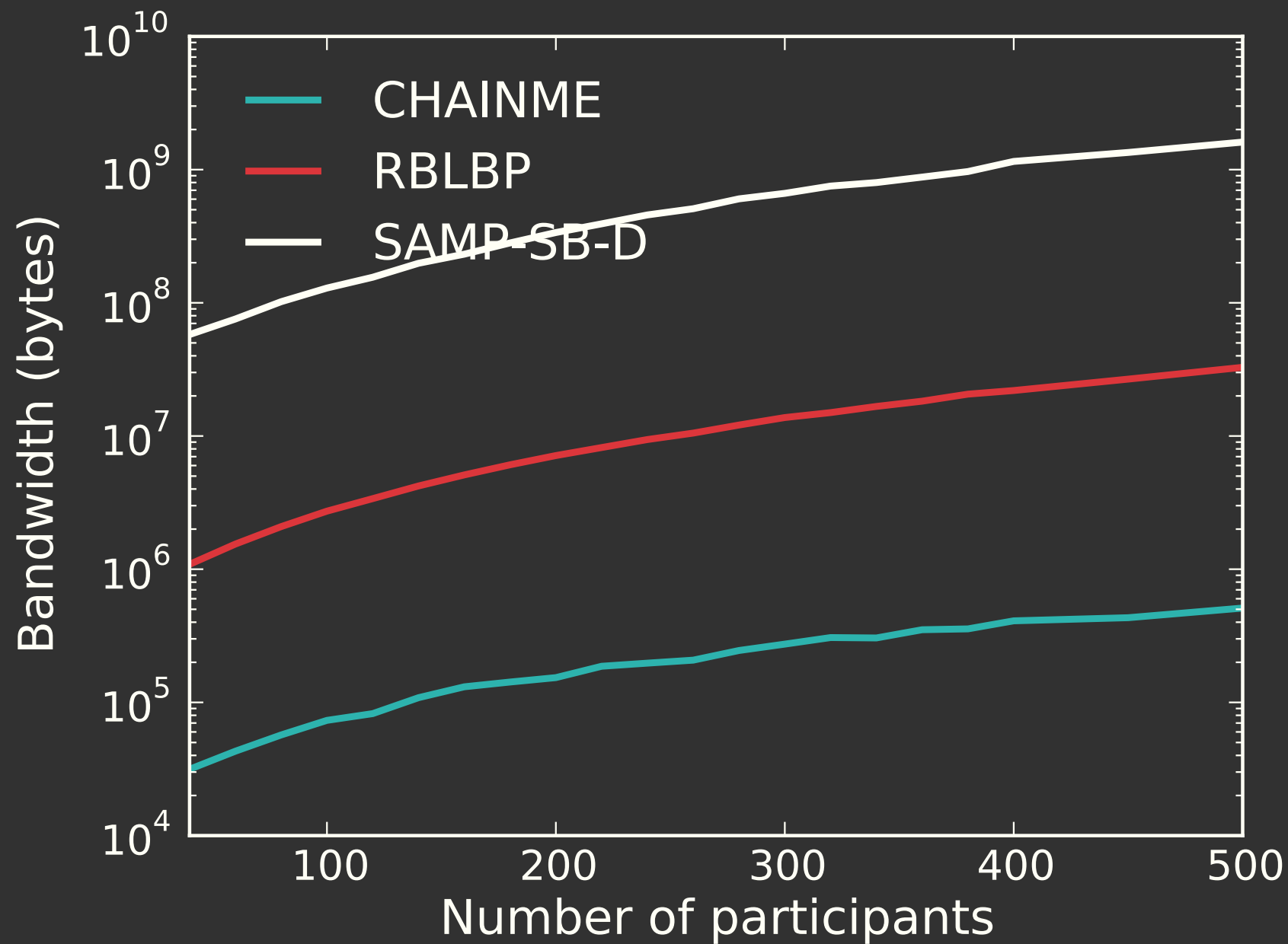
CHAINME plots



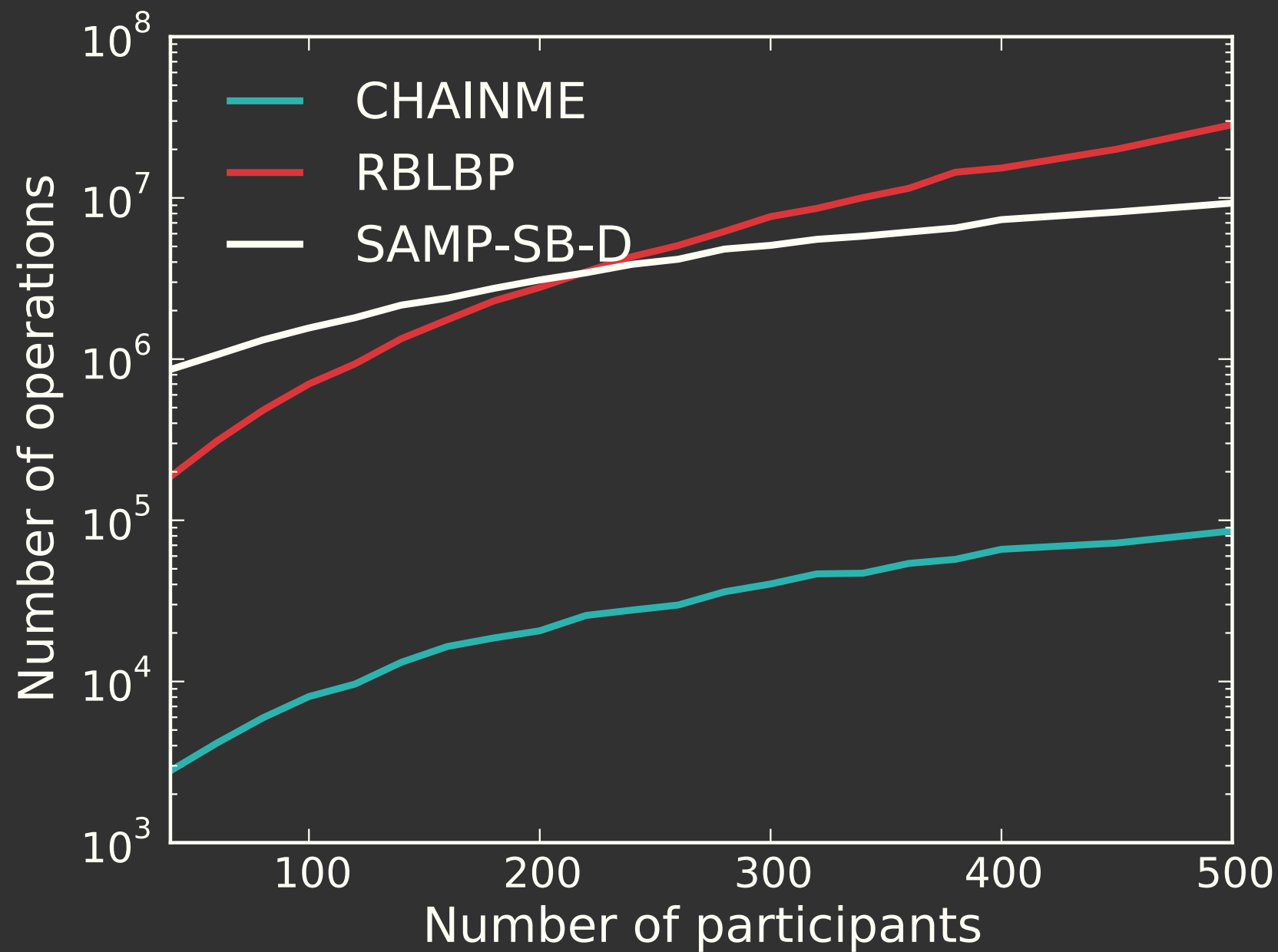
**70%** optimal solutions



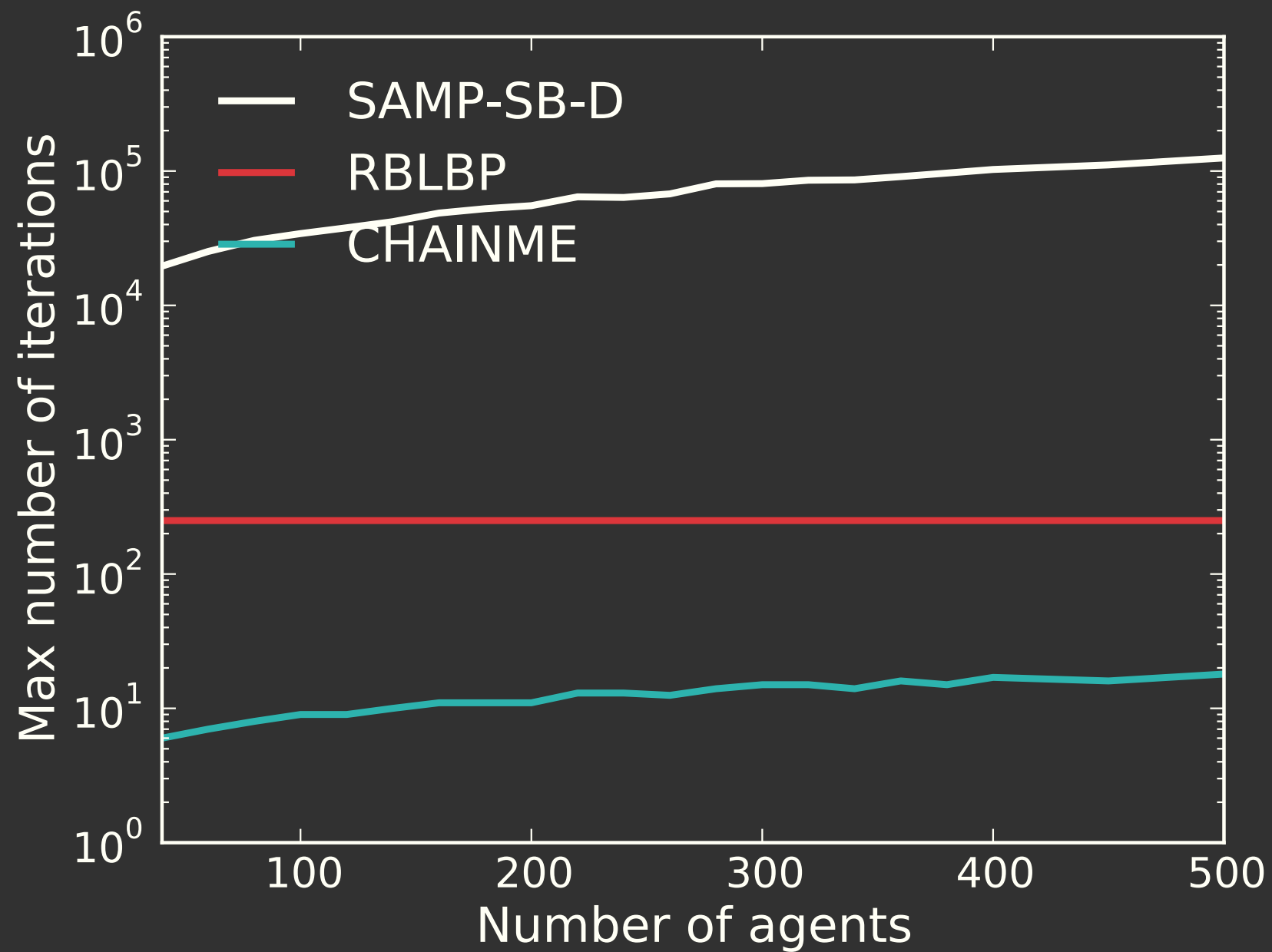
consistently better solutions



up to 50 times less bandwidth



up to  $10^2$  times faster



**better** convergence



CHAINME  
messages

$$\nu_{M \rightarrow s} = \begin{cases} \textcolor{red}{\omega_s}, & \text{if } s \in \textcolor{olive}{active}_s \\ -\textcolor{teal}{\omega_b}, & \text{otherwise} \end{cases}$$

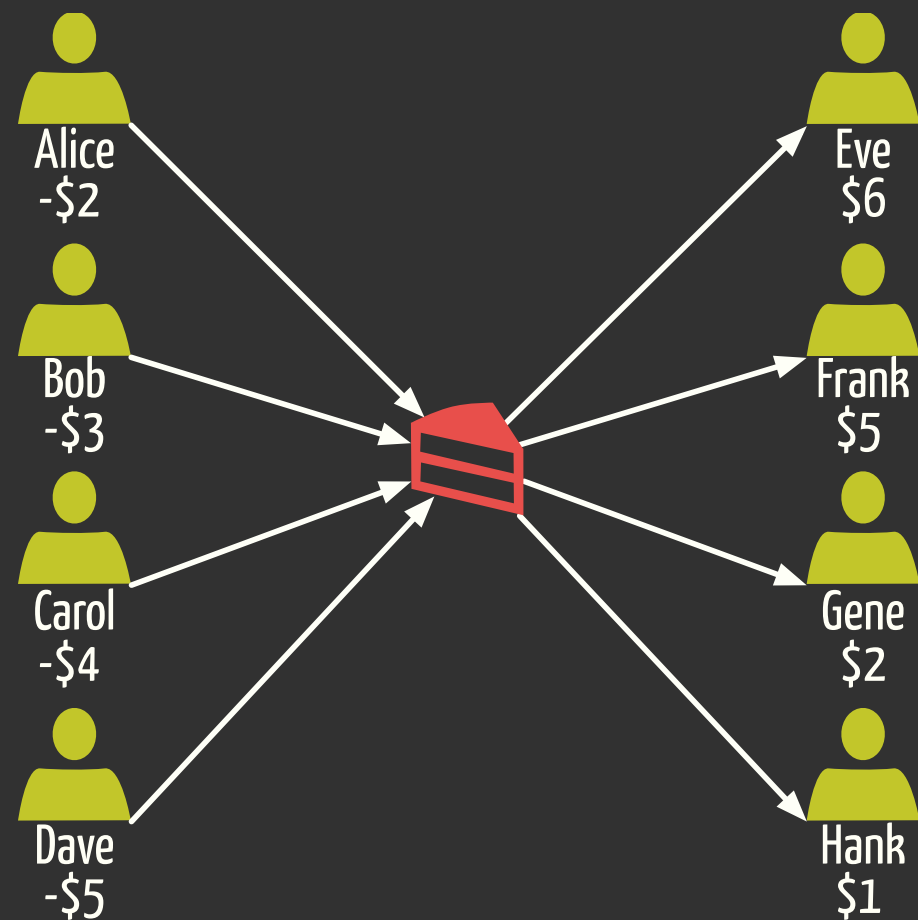
$$\nu_{M \rightarrow b} = \begin{cases} \omega_b, & \text{if } b \in \textcolor{olive}{active}_b \\ -\omega_s, & \text{otherwise} \end{cases}$$

$$\nu_{x \rightarrow F} = \sum_{F' \in \mathcal{N}(x) \setminus F} \nu_{F' \rightarrow x}$$

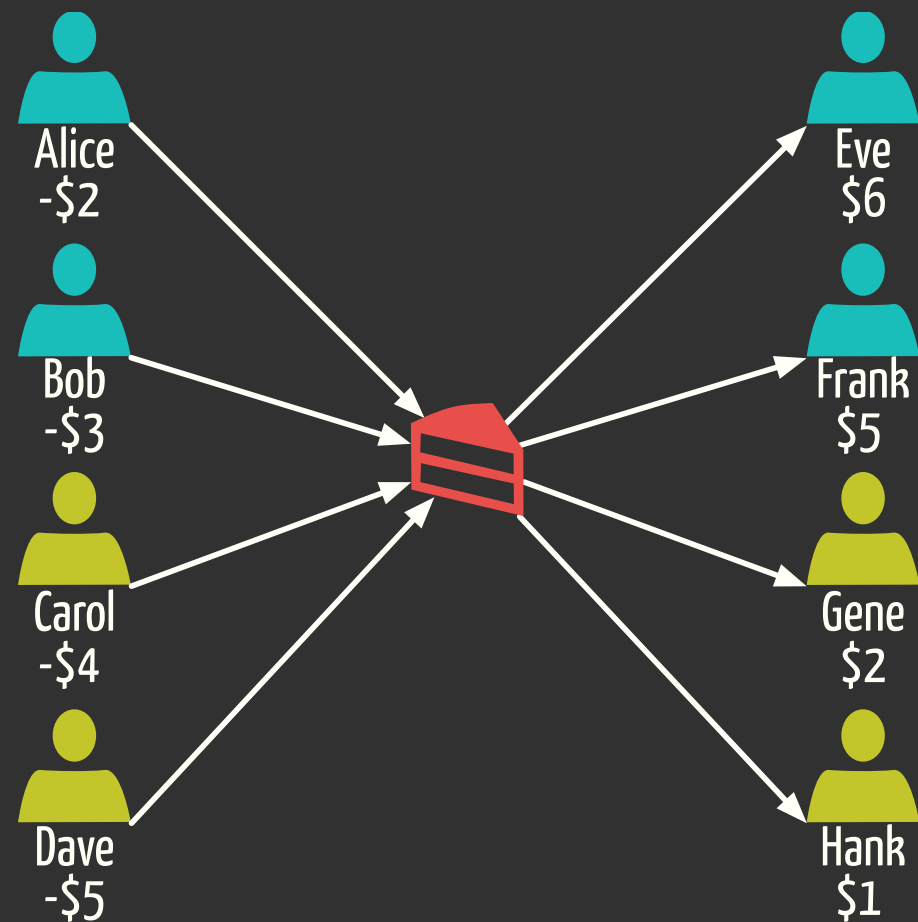
# Background

# Price Rules for Double Auctions

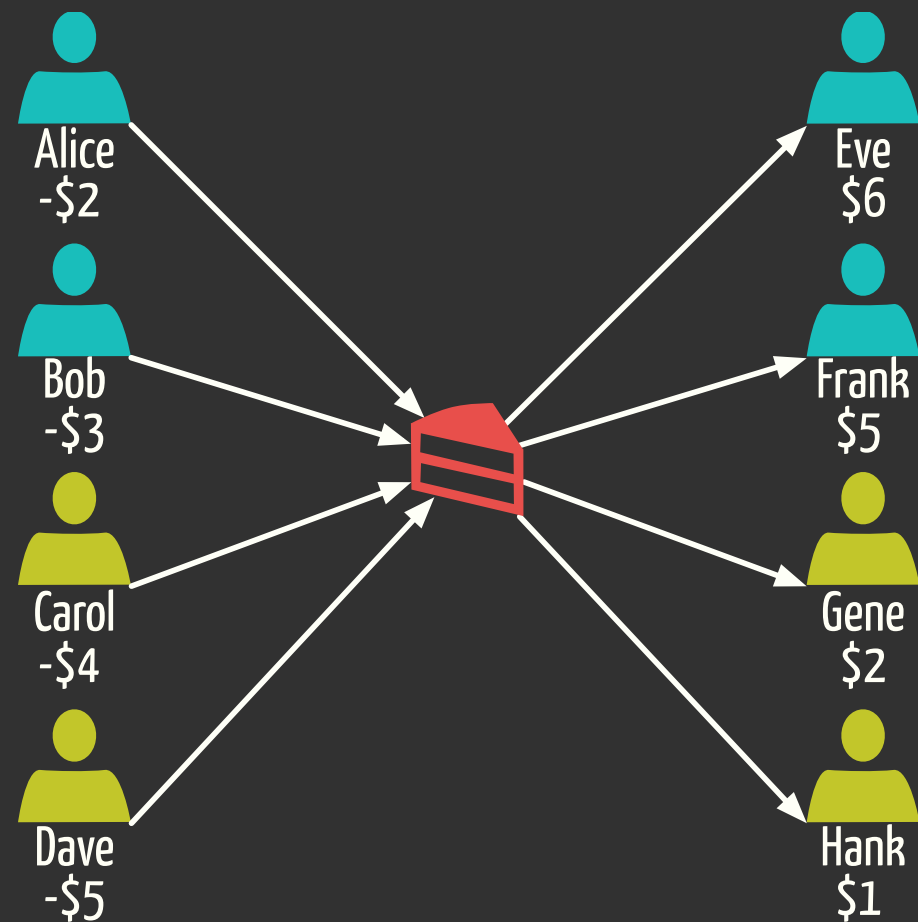
# PRICE RULES FOR DOUBLE AUCTIONS



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## Individual rationality

No seller should be paid less than her bid.

No buyer should pay more than her bid.

## Fairness

The price cannot be larger than the bid of any seller out of trade.

The price cannot be smaller than the bid of any buyer out of trade.

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No seller should be paid less than her bid.

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Sellers	Buyers	Fact
$s^1$	$b^1$	$b^1 + s^1 > 0$
$\vdots$	$\vdots$	
$s^\eta$	$b^\eta$	$b^\eta + s^\eta \geq 0$
$\overline{s^{\eta+1}}$	$\overline{b^{\eta+1}}$	$\overline{b^{\eta+1}} + \overline{s^{\eta+1}} < 0$
$\vdots$	$\vdots$	

## Fairness

The price cannot be larger than the bid of any seller out of trade.

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# PRICE RULES FOR DOUBLE AUCTIONS

$$\tau^- \leq \tau \leq \tau^+$$

$$\tau^- = \max(-s^n, b^{n+1})$$

$$\tau^+ = \max(-s^{n+1}, b^n)$$

## Individual rationality

No seller should be paid less than her bid.

No buyer should pay more than her bid.

## Fairness

The price cannot be larger than the bid of any seller out of trade.

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$s^1$	$b^1$	$b^1 + s^1 > 0$
$\vdots$	$\vdots$	
$s^n$	$b^n$	$b^n + s^n \geq 0$
$s^{n+1}$	$b^{n+1}$	$b^{n+1} + s^{n+1} < 0$
$\vdots$	$\vdots$	

**CONTRIBUTION**

**GOAL**

**GOAL**