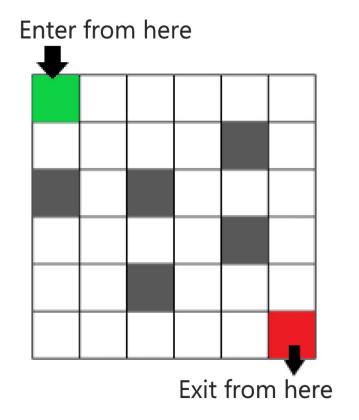
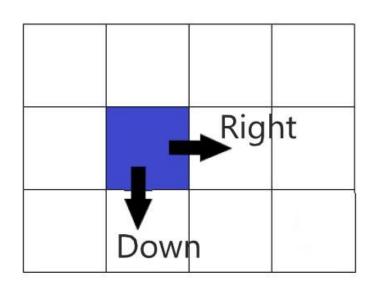
Dynamic Programming

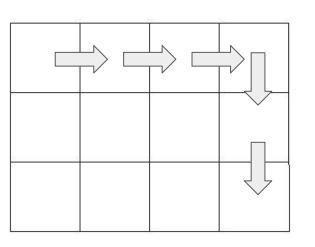
Q.NO. How many ways to go from start to end of maze with some boxes blocked and we can only move to right or down.

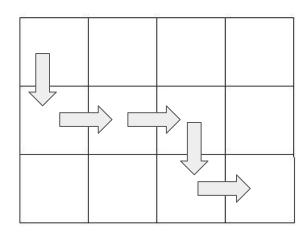


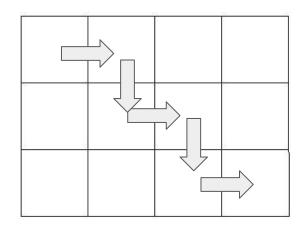


Left and down movements

Let's start with easy version (without any box blocked)







Observation

One thing to observe was every figure had-3 Arrows with this shape

And 2 Arrows with this shape

So we can calculate our answer via P&C....

Q. No. of ways to arrange $3 \Longrightarrow$ and $2 \downarrow \downarrow$ is

Ans. (3+2)!/(3!*2!)

So Basically for M x N Grid no. of ways is equal to

```
(M-1 + N-1)!
----(M-1)! (N-1)!
```

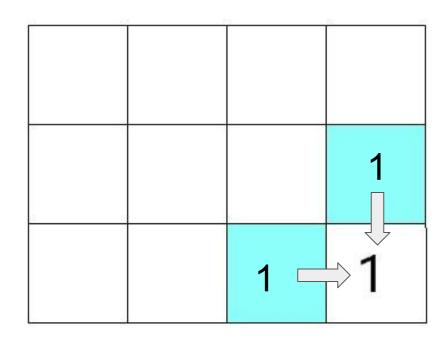
DP Approach

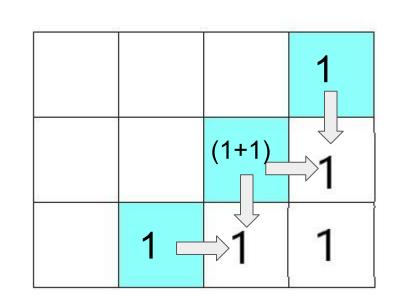
Lets Calculate for each cell the no. ways from there to exit

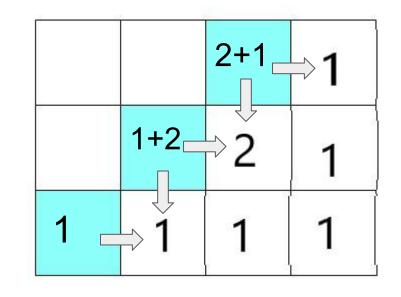
BASE CASE-

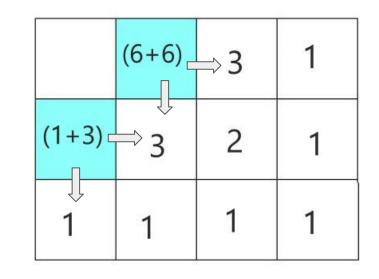
If I am in last cell then I have only one move that is exit this cell. So for last cell answer is 1

	2	
ž.		
		1









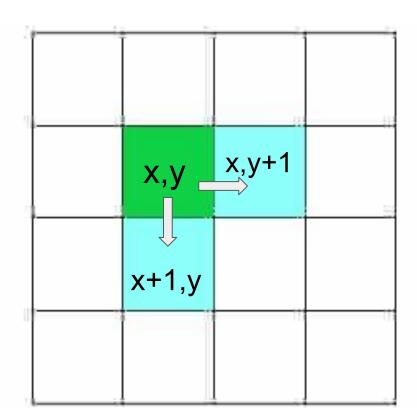
(4+6)	_⇒ 6	3	1
4	3	2	1
1	1	1	1

So for a general Case

$$ans(x,y) = ans(x+1,y) + ans(x,y+1)$$

Let's say I want to calculate answer for (X,Y).

Then I will first Calculate for them - (X+1,Y) and (X,Y+1)



Recurrence relation

(Pseudo Code)

```
// Assume N * M Grid
    Calculate Ways ( X,Y )
 4
 5
         // Base Case
 6
         if( X==N && Y== M )
             return 1;
8
 9
10
         Ans=0;
11
         if(X+1 <= N)
12
             Ans += Calculate Ways(X+1,Y);
13
14
15
         if(Y+1 <= M)
             Ans += Calculate Ways(x,Y+1);
16
17
18
         return Ans;
19
```

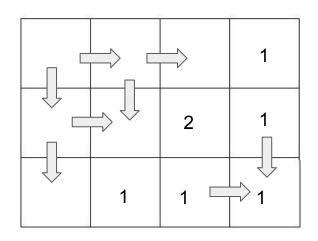
What happens

We are in block (1,1).. So to find answer for it we need to calculate anser for (1,2) and (2,1).

Now similary (1,2) calls (1,3) and (2,2)... and (2,1) calls (1,2) and (1,3) and this goes on....

Sometime we reach base Case and then we actually have answers.

In actual this happens...

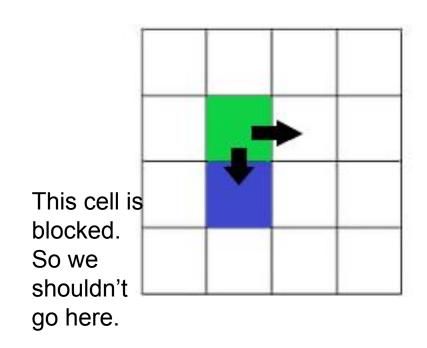


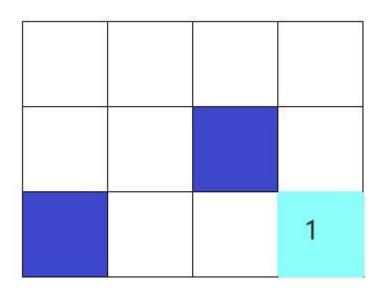
This Goes on....
In some time, we reach end.

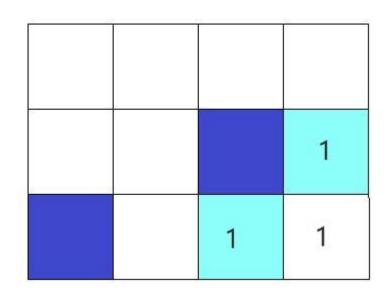
So, now I will soon have answers

So.. soon I will have answer for every box.

Now Let's move on to block cells.







		1
		1
1	1	1

	1	1
1		1
1	1	1

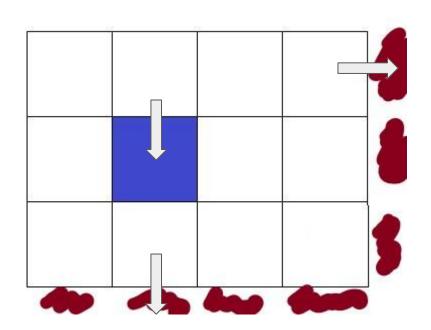
	1	1	1
1	1		1
	1	1	1

2	1	1	1
1	1		1
	1	1	1

Like we are checking for boundary condition, Similarly check for if the cell is blocked

```
// Assume N * M Grid
     // Assume Is blocked [X][Y] is 1 if cell is blocked otherwise 0.
     Calculate Ways ( X,Y )
         // Base Case
         if( X==N && Y== M )
             return 1;
10
         Ans=0;
11
12
         if(X+1 \le N \&\& Is blocked [X+1][y] == 0)
             Ans += Calculate Ways(X+1,Y);
13
14
         if(Y+1 \le M \&\& Is_blocked [X][Y+1] == 0)
15
             Ans += Calculate Ways(X,Y+1);
16
17
18
         return Ans;
19
```

More better way to write code....



Invalid Blocks have following property

X>N

Y>M

Is_blocked [X] [Y] == 1

I have 0 way to reach to the end from these places.

More better way to write code....

```
Assume N * M Grid
     // Assume Is blocked [X][Y] is 1 if cell is blocked otherwise 0.
     Calculate Ways ( X,Y )
         // check if block is invalid
         if( X > N | | Y > M | | Is_blocked[X][Y] ==1 )
             return 0;
9
10
        // Base Case
11
        if( X==N && Y== M )
12
             return 1;
13
14
15
         Ans = Calculate Ways(X+1,Y) + Calculate Ways(X,Y+1);
16
17
         return Ans;
18
```

Relation to PMI (just for understanding)

Dynamic Programming

Base Case- Like Ans[M][N] =1

Or Our invalid Cases X>N,Y>M or if the cell is blocked Ans is 0.

Recursion Step - We want answer for (X,Y), so we first find for (X+1,Y) and (X,Y+1)

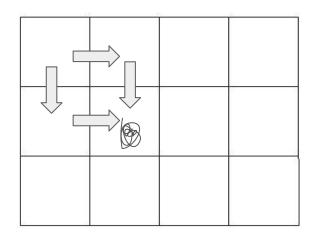
PMI

Base Case- Like we had for k=0, or k=1, we had proof.

Recursion Step - If we want to prove for K+1, then we need to have proof for K.

Memoization...

Problem is we might be reaching the same Box again... like...



So why calculate again and again... Lets store the answer...

If ans[X][Y] == -1then we have not calculated for it yet otherwise we had.

```
// Assume N * M Grid
     // Assume Is blocked [X][Y] is 1 if cell is blocked otherwise 0.
     // Lets Store Answer in DP[X][Y]
     Calculate Ways ( X,Y )
         // check if block is invalid
         if( X > N || Y > M || Is_blocked[X][Y] ==1 )
10
             return 0:
11
12
         if( DP[X][Y] != -1 )
13
14
             return DP[X][Y];
15
         // Base Case
17
         if( X==N && Y== M )
             return 1;
19
20
21
         Ans = Calculate_Ways(X+1,Y) + Calculate_Ways(X,Y+1);
22
23
         return DP[X][Y] = Ans;
      }
25
```