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Title...

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Declaration

I hereby declare that this report has been composed by me. I also declare that all sources of information have been specifically acknowledged and all quotations distinguished by quotation marks.

(signed)

Abstract

Abstract....

Acknowledgments

Acknowledgments....

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CHAPTER 1

Introduction

1. Overview
2. Motivation
3. Primary Goals
4. Secondary Goals

CHAPTER 2

Background

In order to expand and adapt existing Particles Swarm Optimisation methods an initial background research has to be done to fully understand the concepts involved. Similarly to fully

1. Particle Swarm Optimisation

Particle Swarm Optimisation (PSO) [3, 7, 2, 5] is a metaheuristic inspired on the social behavior of flocks of birds when flying and on the movement of shoals of fish. A population of entities moves in the search space during the execution on the algorithm. These entities perform local interactions (with other particles as well as the environment).

Assuming worker bees are searching for a patch of flowers with the most pollen, also assume that the bees

2. Portfolio Management

3. Multi-objective Optimisation

CHAPTER 3

Related Work

1. Markowitz Model

One of the first contributions to the portfolio problem was made by Markowitz [4] which was later described in more detail in his book [1]. Markowitz introduced the mean-variance model which considers the variance of the portfolio as the measure of the investor's risk under a set of assumptions. According to Markowitz, the portfolio selection problem can be expressed as an objective function subject to linear constraints.

Following Markowitz, the investment horizon includes a single period whereas the investment strategy is to select an optimal portfolio at the beginning of the period which will be held unchanged until the date of termination. The joint distribution of one-period security returns is assumed to be a multivariate normal distribution, which in turn follows that the distribution of the portfolio return is also normal.

Let $S = (S_1, S_2, S_3, \dots, S_N)$ be the set of N assets where each asset S_i has a rate of return represented by a variable R_i with a expected return r_i and each pair of assets (S_i, S_j) has a covariance σ_{ij} . The variance-covariance matrix $\sigma_{n \times n}$ contains all the covariance values, furthermore, it is a symmetric matrix and every diagonal element σ_{ii} represents the variance of asset S_i . Let π be a positive value which represents the investor's required expected return. Generally the values r_i σ_{ij} are estimated from past data and are fixed during the period of investment.

According to Markowitz, a portfolio is a real valued vector $X = (x_1, x_2, x_3, \dots, x_i)$ where each variable x_i represents the percentage invested in a corresponding asset S_i . The value $\sum_{i=1}^N \sum_{j=1}^N x_i x_j \sigma_{ij}$ is the variance of the portfolio and it is the measure of risk associated with the portfolio. From this, we may obtain a constrained portfolio

optimisation problem:

$$\begin{aligned}
 & \text{Minimise} \\
 & \sum_{i=1}^N \sum_{j=1}^N x_i x_j \sigma_{ij} \\
 & \text{Constraints :} \\
 & \sum_{i=1}^N x_i r_i = \pi \\
 & \sum_{i=1}^N x_i = 1 \\
 & x_i \geq 0, i \in \{1, 2, \dots, N\}
 \end{aligned} \tag{3.1}$$

Here, the objective function minimises the total variance (risk) associated with a portfolio whilst the constraints ensure that the portfolio meets the expected required return of π and the proportions of all the assets sum to 1. The non-negative constraint means that no short-selling is allowed.

This framework presumes that the investor uses a quadratic utility function or that asset returns follow a multivariate normal distribution. This implies that the rate of return of a portfolio of assets can be completely explained by the expected return or variance of assets. The efficient-frontier is the set of assets which provide minimum risk for a specified level of return. Solving the Markowitz portfolio optimisation problems for different specified expected portfolio returns will give us a set which represents the efficient-frontier, it is a smooth semi-increasing curve which represents the best possible trade-off between risk and expected return, also called the set of Pareto-optimal portfolios.

2. Portfolio in Excel

3. Something PSO

4. PSO applied

CHAPTER 4

Problem Domain

1. Approach

CHAPTER 5

Requirements

This section describes the requirements for this project. Table 1 refers to the functional requirements from technical point of view. Section 2 focuses on the non-functional requirements of the system.

1. Functional

No.	Description	Priority
1	Optimisation of Portfolio	
1.1	PSO	
1.1.1	Initialisation of particle population	High
1.1.2	Processing swarm optimisation	High
1.1.3	Updating the local and global (at each step) particle values	
1.1.4	Calculating an optimal solution	High
1.1.5	Presenting the results	High
1.2	PSO for portfolio problem	
1.2.1	Minimise portfolio variance	High
1.2.2	Maximise portfolio expected return	Low
1.2.3	Use multi-objective for optimum solution	Low
1.2.4	Refining results output	High
1.2.5	Make results for readable for user	High
2	User Input	
2.1	Allow the user to enter the name of the data file	High
2.2	Allow the user to change the expected portfolio return	High
2.3	Allow the user to select the name for the output file	Low
2.4	Allow the user to change the PSO particle size	Low
2.5	Allow the user to change the PSO iteration number	Low
3	Output format	
3.1	Display the results during run-time	High
3.2	Make results more readable for output file	High
3.3	Store results into a separate file	High

TABLE 1. Functional requirements for system.

2. Non-functional

As this system is an extension on a PSO module by Fernando Rubio et. al [6], it is crucially important to devote a considerable amount of time to testing. This is to ensure that the alterations do not affect the performance of the overall efficiency of the algorithm and quality of the optimisation.

The system's scalability is something not to be overlooked. As each asset in a portfolio represents one dimension in the fitness function (not to be confused with just another linear factor of the same coefficient in a function), optimising a function in, for example, 100 dimensions (100 assets) might be too much for the system to cope with.

Running the PSO requires setting up various parameters and thresholds for optimisation (size of the particle population, number of iterations, inertia weights and convergence coefficients). These parameters need to be optimised for the algorithm to be computationally effective and produce accurate results.

CHAPTER 6

Methodology and Technologies

This chapter describes the methodology used in the project for the research, design, implementation and testing. It also mentions the technologies used to achieve the goals.

1. Methodology

This sections is basically an extension to the project plan which had to be made during the first week of the project. An approximate guideline to follow the project was set focusing on the project deadlines. I left a few weeks for margin for error in case something takes slightly longer than planned for whatever reason.

—Project timeline—

For this project to be successful I am planning on spending the initial weeks researching relevant literature and becoming familiar with the concepts of Particle Swarm Optimisation. This is a completely new field to me and understanding the key ideas and models will be critically important. Not only will I need to understand PSO's background I will also need to study previous implementations and applications in order to become absolutely comfortable with it. Finally, as I am planning on improving an existing algorithm, I will have to spend some time becoming familiar enough with the code so that I will be able to modify it with ease.

The implementation stage will consist of designing the future system and the realisation of the plans. Key design decisions will have to be made during this stage and the solutions might be obtained from the analysis of previous work.

To complete this project test driven development will be carried out. I plan to test after every implementation or modification. This will be done to ensure that changes won't affect any previous functionality. The tests will evaluate the efficiency as well as the accuracy of my system. Given the nature of PSO's 'random' initialisation, I want to make sure that the results are consistent.

The writing of this result will be flexible, the sections will be written as needed or when the section arises naturally throughout the project.

2. Technology

2.1. Haskell. Coming from a strong mathematical background I find functional languages easier to understand. Also one huge advantage of pure functional languages is that the absence of side-effects allow them to offer a clear semantic framework to analyse the correctness of programs.

As Haskell is the functional language I am more familiar with, I didn't see the point in learning a new language as it would only restrict my project process, so Haskell was a clear winner.

There are other PSO implementations in other languages such as C and Ruby but as already mentioned, Haskell is my preferred language.

2.2. Operating System. As Haskell is platform independent (in the sense that it can be compiled in Windows, Linux or Mac) I have chosen to use Ubuntu 12.04 as it is my preferred OS and I feel the most comfortable with it. In addition, I wouldn't be affected in the about of software needed for the project as it is provided for all three OSs already mentioned.

The work was carried out on my personal laptop (Intel CORETM i3 @ 2.6GHZ, 4Gb RAM). If required due to any reasons, the university provide classroom PCs (Intel CORETM i3-2100 CPU @3.10 GHz, 3 Gb RAM) although I have faith that my own machine will be reliable enough for me not to have to change machines. Sublime Text 2 was chosen as the IDE for the project. It has many useful functions [8] and similarly for the choice of OS, I am happy with this editor.

CHAPTER 7

System Design and Architecture

CHAPTER 8

Experimentation and Testing

CHAPTER 9

Financial Data

1. Data Description
2. Problem Domain
3. Assets and their Weights
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8. Results

CHAPTER 10

Future Work

1. PSO Parameters
2. Asset's Covariance
3. Market Relationships

CHAPTER 11

Discussion and Conclusion

1. Discussion
2. Future Work
3. Conclusion

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