



**UiO** : **Centre for Educational Measurement**  
Det utdanningsvitenskapelige fakultet

# Missing Data Treatment

A hand-on illustration using  package [mice](#)  
(Version 3.14.0)

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# Overview

- Complete-case analyses:

- ✗ Wasteful

- ✗ Biased

- Two approaches:

- ① Joint modelling (JM, Schafer, 1997, R package [jomo](#))

- ② Fully conditional specification (FCS)

- 👉 FCS aka **m**ultivariate **i**mputation by **c**hained **e**quations (MICE, van Buuren & Groothuis-Oudshoorn, 2011)

- Existing R packages:


- [Amelia](#), [Hmisc](#), [jomo](#), [mi](#), [mice](#), [norm](#), [norm2](#), [pan](#)

- 📖 See Table 5.1, Kleinke et al. (2020) (p. 134) for popularity contest across various MI packages

- 📖 See Table 6, Grund et al. (2018) (pp. 134–135) for missing data treatment for multilevel models

# Data Missing Mechanism (Rubin, 1976)

## ■ Missing completely at random (**MCAR**)

-  missingness of variables is independent of the variables considered in the study
- ✓ no treatment required, complete-case analyses valid and unbiased

## ■ Missing at random (**MAR**)

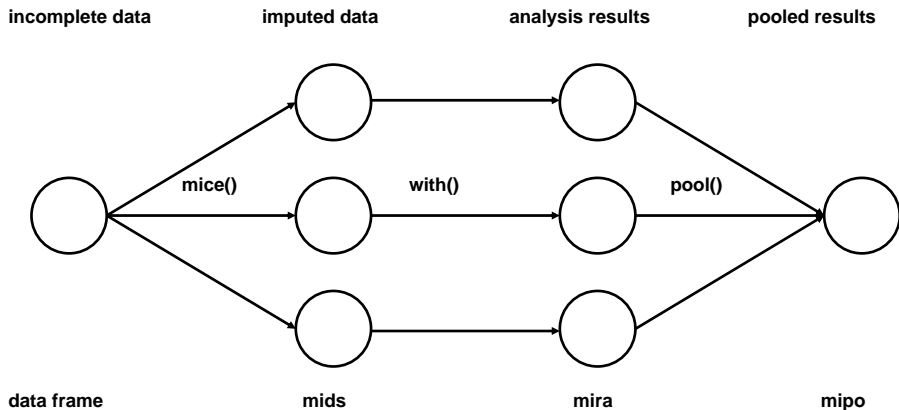
-  missingness depends exclusively on observable variables
- ✓ the assumption behind most MI procedures, including [mice](#)

## ■ Missing not at random (**MNAR**)

-  missingness depends on unobservable but important variables of interest in the study
- ✓ exact treatment rather complicated (Rose, 2013)
- ✓ in practice: introduce lots of covariates and hope  $MNAR \cong MAR$

● Ignorable = { MCAR, MAR }; Nonignorable = { MNAR }

# mice Workflow (van Buuren & Groothuis-Oudshoorn, 2011)



## mice Imputation Methods

Method	Description	Scale type	Default
pmm	Predictive mean matching	numeric	Y
norm	Bayesian linear regression	numeric	
norm.nob	Linear regression, non-Bayesian	numeric	
mean	Unconditional mean imputation	numeric	
2L.norm	Two-level linear model	numeric	
logreg	Logistic regression	factor, 2 levels	Y
polyreg	Multinomial logit model	factor, >2 levels	Y
polr	Ordered logit model	ordered, >2 levels	Y
lda	Linear discriminant analysis	factor	
sample	Random sample from the observed data	any	

## Further Readings

(Hox et al., 2018)

The classical guide *Statistical analysis with missing data* has recently been updated to its 3rd edition (Little & Rubin, 2019). Two alternative textbooks are *Applied missing data analysis* (Enders, 2010) and *Multiple imputation and its application* (Carpenter & Kenward, 2013).

# References

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