

Problem 1

I have twelve books.

- In how many ways can I line them up on a single shelf?

$$12! = 479,001,600$$

- In how many ways can I choose seven of them and line them up on a single shelf?

$$\frac{12!}{5!} = 3,991,680$$

- In how many ways can I choose seven to take to school?

$$\binom{12}{7} = \frac{12!}{7!5!} = 792$$

Problem 2

An ogre has n captives to eat, one captive per day.

1. How many ways are there to make a menu for n days?

$$n!$$

2. How many ways are there to pick k captives to freeze them for winter season?

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

3. How many ways are there to buy n bottles of sauce for the captives, out of k kinds?

$$\binom{k}{n} = \frac{k!}{n!(k-n)!}$$

Problem 3

- An ice-cream vendor sells eleven kinds of ice-cream. In how many different ways can I buy six cones, some or even all of which could be the same.
- An icecream vendor sells six kinds of ice-cream. In how many different ways can I buy eleven cones, some or even all of which could be the same.