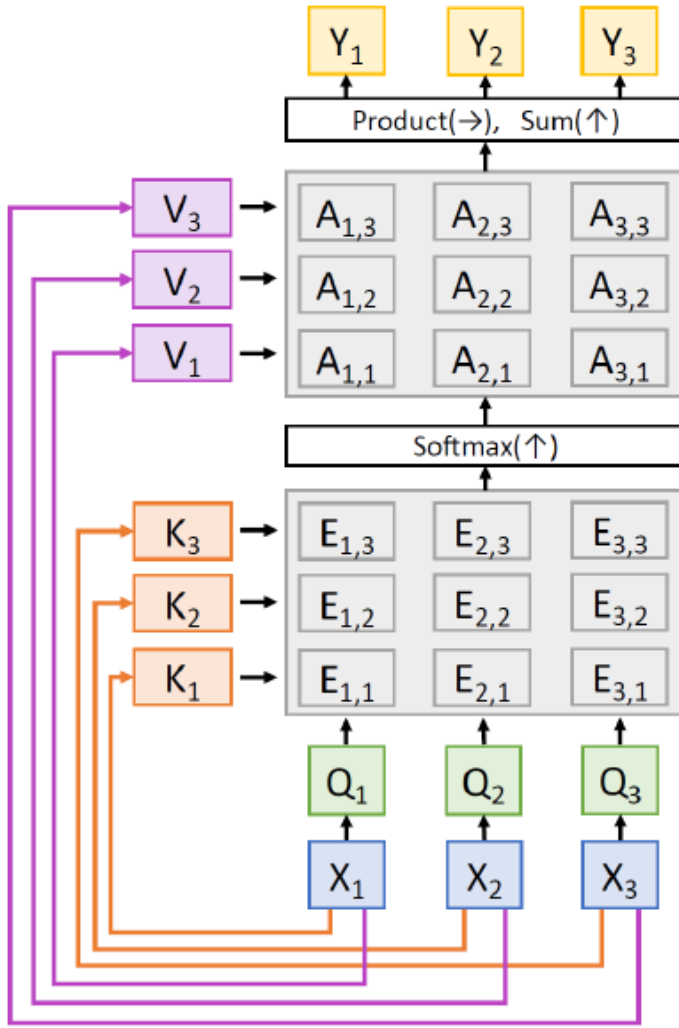


1. Self-attention



(a) Prepare Inouts :

X_1 shap : $1 \times D_x$

$X = [X_1^T, X_2^T, X_3^T]^T$, shape : $N_x \times D_x, N_x = 3$

(b) Initialize weights:

Key matrix W_k , shape : $D_x \times D_Q$

Query matrix W_Q , shape : $D_x \times D_Q$

Value matrix W_V , shape : $D_x \times D_V$

(c) Derive key, query and value:

Key $K = XW_k$, shape : $N_x \times D_Q$

Query $Q = XW_Q$, shape : $N_x \times D_Q$

Value $V = XW_V$, shape : $N_x \times D_V$

(d) Calculate attention scores for input :

$E^T = QK^T / \sqrt{D_Q}$, shape : $N_x \times N_x$

$E_{i,j} = Q_i K_j^T / \sqrt{D_Q}$, shape : 1×1

(e) Calculate softmax:

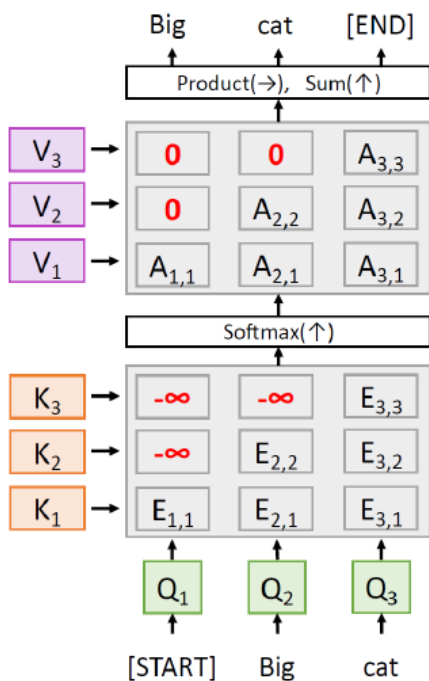
$A = \text{softmax}(E, \text{dim} = 1)$, shape : $N_x \times N_x$

(f) Multiply scores with values

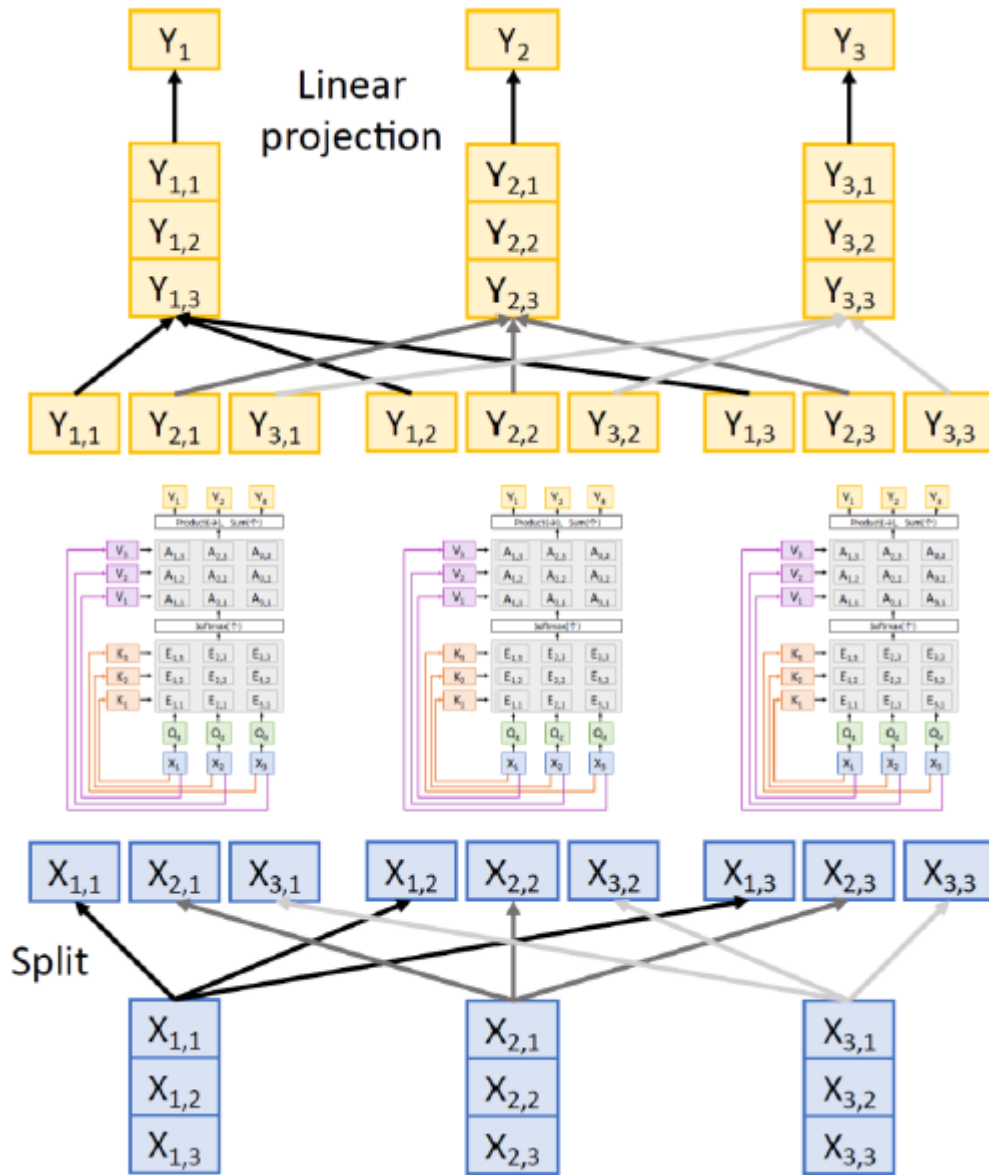
(g) Sum weighted values to get output

$$Y_i = \sum_j A_{i,j} V_j$$

2. Masked self-attention



3. Multihead self-attention



4. Transformer

