

Числено диференциране

Като се използват формули за числено диференциране с грешка $O(h^2)$ да се попълнят празните полета в таблицата

$$\alpha \quad \begin{matrix} i=0 \\ 0 \end{matrix} \quad \begin{matrix} i=1 \\ 0.1 \end{matrix} \quad \begin{matrix} i=2 \\ 0.2 \end{matrix} \quad \begin{matrix} i=3 \\ 0.3 \end{matrix} \quad \begin{matrix} i=4 \\ 0.4 \end{matrix} \quad \begin{matrix} i=5 \\ 0.5 \end{matrix} \quad \Rightarrow h = 0.1$$

$$y(\alpha) \quad -0.2 \quad 0.2 \quad 0.5 \quad 0.7 \quad 0.87 \quad 1$$

$$y'(\alpha) \quad 4.5 \quad 3.5 \quad 2.5 \quad 1.85 \quad 1.5 \quad 5.9$$

$$y''(\alpha) \quad X \quad -10 \quad 10 \quad -3 \quad -4 \quad X$$

$$y_2'' = \frac{y_1 - 2y_2 + y_3}{h^2}$$

$$10 = \frac{0.2 - 2 \cdot 0.5 + y_3}{0.1^2}$$

$$10 = \frac{0.2 - 1 + y_3}{0.01} \quad | \cdot 0.01$$

$$0.1 = 0.2 - 1 + y_3$$

$$-y_3 = 0.2 - 1 - 0.1$$

$$y_3 = 0.7$$

$$y_2' = \frac{y_3 - y_1}{2h}$$

$$y_2' = \frac{0.7 - 0.2}{2 \cdot 0.1}$$

$$y_2' = \frac{0.5}{0.2}$$

$$y_2' = 2.5$$

$$y_4' = \frac{y_5 - y_3}{2h}$$

$$y_4' = \frac{1 - 0.7}{2 \cdot 0.1}$$

$$y_4' = \frac{0.3}{0.2}$$

$$y_4' = 1.5$$

$$y_4' = \frac{y_2 - 4y_3 + 3y_4}{2h}$$

$$1.5 = \frac{0.5 - 4 \cdot 0.7 + 3y_4}{2 \cdot 0.1}$$

$$1.5 = \frac{0.5 - 2.8 + 3y_4}{0.2}$$

$$0.3 = 0.5 - 2.8 + 3y_4$$

$$-3y_4 = 0.5 - 2.8 - 0.3$$

$$-3y_4 = -2.6 / (-3)$$

$$y_4 = 0.87$$

$$y_2' = \frac{y_0 - 4y_1 + 3y_2}{2h}$$

$$2.5 = \frac{y_0 - 4 \cdot 0.2 + 3 \cdot 0.5}{0.2}$$

$$0.5 = y_0 - 0.8 + 1.5$$

$$-y_0 = -0.8 + 1.5 - 0.5$$

$$-y_0 = 0.2$$

$$y_0 = -0.2$$

$$y_0' = \frac{-3 y_0 + 4 y_1 - y_2}{2 h}$$

$$y_0' = \frac{-3 * (-0.2) + 4 * 0.2 - 0.5}{0.2}$$

$$y_0' = \frac{0.6 + 0.8 - 0.5}{0.2}$$

$$y_0' = \frac{0.9}{0.2}$$

$$y_0' = 4.5$$

$$y_1' = \frac{y_2 - y_0}{2 h}$$

$$y_1' = \frac{0.5 - (-0.2)}{0.2}$$

$$y_1' = \frac{0.7}{0.2}$$

$$y_1' = 3.5$$

$$y_3' = \frac{y_4 - y_2}{2 h}$$

$$y_3' = \frac{0.87 - 0.5}{0.2}$$

$$y_3' = \frac{0.37}{0.2}$$

$$y_3' = 1.85$$

$$y_5' = \frac{y_3 - 4 y_4 + 3 y_5}{2 h}$$

$$y_5' = \frac{0.7 - 4 * 0.87 + 3 * 1}{0.2}$$

$$y_5' = \frac{0.7 - 4 * 0.87 + 3 * 1}{0.2}$$

$$y_5' = \frac{0.7 - 3.48 + 3}{0.2}$$

$$y_5' = \frac{1.18}{0.2}$$

$$y_5' = 5.9$$

$$y_1'' = \frac{y_0 - 2 y_1 + y_2}{h^2}$$

$$y_1'' = \frac{-0.2 - 2 * 0.2 + 0.5}{0.01}$$

$$y_1'' = \frac{-0.2 - 0.4 + 0.5}{0.01}$$

$$y_1'' = \frac{-0.1}{0.01}$$

$$y_1'' = -10$$

$$y_3'' = \frac{y_2 - 2 y_3 + y_4}{h^2}$$

$$y_3'' = \frac{0.5 - 2 * 0.7 + 0.87}{0.01}$$

$$y_3'' = \frac{0.5 - 2 * 0.7 + 0.87}{0.01}$$

$$y_3'' = \frac{0.5 - 1.4 + 0.87}{0.01}$$

$$y_3'' = \frac{-0.03}{0.01}$$

$$y_3'' = -3$$

$$y_4'' = \frac{y_3 - 2 y_4 + y_5}{h^2}$$

$$y_4'' = \frac{0.7 - 2 * 0.87 + 1}{0.01}$$

$$y_4'' = \frac{0.7 - 1.74 + 1}{0.01}$$

$$y_4'' = \frac{-0.04}{0.01}$$

$$y_4'' = -4$$