

The Julia version 0.5 Express

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Introduction

The Purpose of this document is to introduce programmers to Julia programming by example. This is a simplified exposition of the language.

If some packages are missing on your system use `Pkg.add` to require installing them. There are many add-on packages which you can browse at <http://pkg.julialang.org/>.

Major stuff not covered (please see the documentation):

1. parametric types;
2. parallel and distributed processing;
3. advanced I/O operations;
4. package management; see `Pkg`;
5. interaction with system shell; see `run`;
6. exception handling; see `try`;
7. creation of coroutines; see `Task`;
8. two-way integration with C and Fortran.

You can find current Julia documentation at <http://julia.readthedocs.org/en/latest/manual/>.

The code was executed using the following Julia version:

```
In [2]: versioninfo()
```

```
Julia Version 1.7.1
Commit ac5cc99908 (2021-12-22 19:35 UTC)
Platform Info:
  OS: macOS (x86_64-apple-darwin19.5.0)
  CPU: Intel(R) Xeon(R) CPU E5-2697 v2 @ 2.70GHz
  WORD_SIZE: 64
  LIBM: libopenlibm
  LLVM: libLLVM-12.0.1 (ORCJIT, ivybridge)
```

Remember that you can expect every major version of Julia to introduce breaking changes.

Check <https://github.com/JuliaLang/julia/blob/master/NEWS.md> for release notes.

All suggestions how this guide can be improved are welcomed. Please contact me at bkamins@sgh.waw.pl.

Getting around

Running julia invokes interactive (REPL) mode. In this mode some useful commands are:

1. ^D (exits Julia, also calling `exit(c)` quits with exit code c);
2. ^C (interrupts computations);
3. ? (enters help mode)
4. ; (enters system shell mode)
5. putting ; after the expression will disable showing of its value.

Examples of some essential functions in REPL (they can be also invoked in scripts):

```
In [3]: apropos("apropos") # search documentation for "apropos" string
```

```
Base.Docs.apropos
Base.Docs.stripmd
```

```
In [4]: @less max(1,2) # show the definition of max function when invoked with arguments 1 and 2
```

```
min(x::T, y::T) where {T<:Real} = select_value(y < x, y, x)
minmax(x::T, y::T) where {T<:Real} = y < x ? (y, x) : (x, y)
```

```
In [5]: whos() # list of global variables and their types
```

Base		Module
Compat	21304 KB	Module
Core		Module
Julia	21506 KB	Module
JSON	21416 KB	Module
Main		Module
MbedTLS	21425 KB	Module
ZMQ	21366 KB	Module

```
In [6]: cd("D:/") # change working to D:/ (on Windows)
pwd() # get current working directory
```

```
Out [6]: "D:\\"
```

```
In [7]: include("file.jl") # execute source file, LoadError if execution fails
```

```
could not open file D:\file.jl
```

```
Stacktrace:
 [1] include_from_node1(::String) at .\loading.jl:552
 [2] include(::String) at .\sysimg.jl:14
```

```
In [8]: clipboard([1,2]) # copy data to system clipboard
clipboard() # load data from system clipboard as string
```

```
Out [8]: "[1, 2]"
```

```
In [9]: workspace() # clear workspace - create new Main module (only to be used interactively)
```

You can execute Julia script by running `julia script.jl`.

Try saving the following example script to a file and run it (more examples of all the constructs used are given in following sections):

```
In [10]: "Sieve of Eratosthenes function docstring"
function es(n::Int) # accepts one integer argument
    isprime = ones{Bool, n} # n-element vector of true-s
    isprime[1] = false # 1 is not a prime
    for i in 2:round{Int, sqrt(n)} # loop integers from 2 to sqrt(n)
        if isprime[i] # conditional evaluation
            for j in (i*i):i:n # sequence with step i
                isprime[j] = false
            end
        end
    end
    return filter(x -> isprime[x], 1:n) # filter using anonymous function
end
println(es(100)) # print all primes less or equal than 100
@time length(es(10^7)) # check function execution time and memory usage
```

```
[2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97]
0.136820 seconds (281 allocations: 24.162 MiB, 4.81% gc time)
```

```
Out [10]: 664579
```

Basic literals and types

Basic scalar literals (`x::Type` is a literal `x` with type `Type` assertion):

```
In [11]: 1::Int64 # 64-bit integer, no overflow warnings, fails on 32 bit Julia
```

```
Out [11]: 1
```

```
In [12]: 1.0::Float64 # 64-bit float, defines NaN, -Inf, Inf
```

```
Out [12]: 1.0
```

```
In [13]: true::Bool # boolean, allows "true" and "false"
```

```
Out [13]: true
```

```
In [14]: 'c'::Char # character, allows Unicode
```

```
Out [14]: 'c': ASCII/Unicode U+0063 (category Ll: Letter, lowercase)
```

```
In [15]: "s"::AbstractString # strings, allows Unicode, see also Strings
```

```
Out [15]: "s"
```

All basic types are immutable. Specifying type assertion is optional (and usually it is not needed, but I give it to show how you can do it). Type assertions for variables are made in the same way and may improve code performance.

If you do not specify type assertion Julia will choose a default. Note that defaults might be different on 32-bit and 64-bit versions of Julia. A most important difference is for integers which are `Int32` and `Int64` respectively. This means that `1::Int32` assertion will fail on 64-bit version. Notably `Int` is either `Int64` or `Int32` depending on version (the same with `UInt`). There is no automatic type conversion (especially important in function calls). Has to be explicit:

```
In [16]: Int64('a') # character to integer
```

```
Out [16]: 97
```

```
In [17]: Int64(2.0) # float to integer
```

```
Out [17]: 2
```

```
In [18]: Int64(1.3) # inexact error
```

```
InexactError()
```

```
Stacktrace:
```

```
[1] convert(::Type{Int64}, ::Float64) at .\float.jl:679  
[2] Int64(::Float64) at .\sysimg.jl:24
```

```
In [19]: Int64("a") # error no conversion possible
```

```
MethodError: Cannot `convert` an object of type String to an object of type Int64  
This may have arisen from a call to the constructor Int64(...),  
since type constructors fall back to convert methods.
```

```
Stacktrace:
```

```
[1] Int64(::String) at .\sysimg.jl:24
```

```
In [20]: Float64(1) # integer to float
```

```
Out [20]: 1.0
```

```
In [21]: Bool(1) # converts to boolean true
```

```
Out [21]: true
```

```
In [22]: Bool(0) # converts to boolean false
```

```
Out [22]: false
```

```
In [23]: Bool(2) # conversion error
```

InexactError()

```
Stacktrace:
 [1] convert(::Type{Bool}, ::Int64) at .\bool.jl:7
 [2] Bool(::Int64) at .\sysimg.jl:24
```

```
In [24]: Char(89) # integer to char
```

```
Out [24]: 'Y': ASCII/Unicode U+0059 (category Lu: Letter, uppercase)
```

```
In [25]: string(true) # cast bool to string (works with other types, note small caps)
```

```
Out [25]: "true"
```

```
In [26]: string(1,true) # string can take more than one argument and concatenate them
```

Out [26]: "1true"

```
In [27]: zero(10.0) # zero of type of 10.0
```

Out [27]: 0.0

```
In [28]: one(Int64) # one of type Int64
```

Out [28]: 1

General conversion can be done using `convert (Type, x)`:

```
In [29]: convert(Int64, 1.0) # convert float to integer
```

Out [29]: 1

Parsing strings can be done using `parse(Type, str)`:

```
In [30]: parse(Int64, "1") # parse "1" string as Int64
```

Out [30]: 1

Automatic promotion of many arguments to common type (if any) using promote:

```
In [31]: promote(true, BigInt(1)//3, 1.0) # tuple (see Tuples) of BigFloats, true promoted to 1.0
```

[illegible]

```
In [32]: promote("a", 1) # promotion to common type not possible
```

```
Out [32]: ("a", 1)
```

Many operations (arithmetic, assignment) are defined in a way that performs automatic type promotion. One can verify type of argument:

```
In [33]: typeof("abc") # String returned which is a AbstractString subtype
```

Out [33]: String

```
In [34]: isa("abc", AbstractString) # true
```

Out [34]: true

```
In [35]: isa(1, Float64) # false, integer is not a float
```

Out [35]: false

```
In [36]: isa(1.0, Float64) # true
```

Out [36]: true

```
In [37]: isa(1.0, Number) # true, Number is abstract type
```

```
In [48]: nothing # only instance of Void
```

Additionally #undef indicates an incompletely initialized instance.

Tuples

Tuples are immutable sequences indexed from 1:

```
In [49]: () # empty tuple
```

```
Out [49]: ()
```

```
In [50]: (1,) # one element tuple
```

```
Out [50]: (1,)
```

```
In [51]: ("a", 1) # two element tuple
```

```
Out [51]: ("a", 1)
```

```
In [52]: ('a', false)::Tuple{Char, Bool} # tuple type assertion
```

```
Out [52]: ('a', false)
```

```
In [53]: x = (1, 2, 3)
```

```
Out [53]: (1, 2, 3)
```

```
In [54]: x[1] # 1 (element)
```

```
Out [54]: 1
```

```
In [55]: x[1:2] # (1, 2) (tuple)
```

```
Out [55]: (1, 2)
```

```
In [56]: x[4] # bounds error
```

```
BoundsError: attempt to access (1, 2, 3)
at index [4]
```

```
Stacktrace:
 [1] getindex(::Tuple{Int64,Int64,Int64}, ::Int64) at .\tuple.jl:21
```

```
In [57]: x[1] = 1 # error - tuple is not mutable
```

```
MethodError: no method matching setindex!(::Tuple{Int64,Int64,Int64}, ::Int64, ::Int64)
```

```
In [58]: a, b = x # tuple unpacking a=1, b=2
println("$a $b")
```

```
1 2
```

Arrays

Arrays are mutable and passed by reference. Array creation:

```
In [59]: Array{Char}(2, 3, 4) # 2x3x4 array of Chars
```

```
Out [59]: 2×3×4 Array{Char,3}:
[:, :, 1] =
 '\U15fec730' '\U15fec770' '\U15fec7d0'
 '\0' '\0' '\0'

[:, :, 2] =
 '\U15fec810' '\U15fec850' '\U15fec890'
 '\0' '\0' '\0'

[:, :, 3] =
 '\U15feca90' '\U15fec610' '\U15fec9d0'
 '\0' '\0' '\0'

[:, :, 4] =
 '\U15fed1d0' '\U16105830' '\U161058f0'
```

```
'\0'      '\0'      '\0'

In [60]: Array{Int64}(0, 0) # degenerate 0x0 array of Int64

Out [60]: 0x0 Array{Int64,2}

In [61]: Array{Any}(2, 3) # 2x3 array of Any

Out [61]: 2x3 Array{Any,2}:
#undef #undef #undef
#undef #undef #undef

In [62]: zeros(5) # vector of Float64 zeros

Out [62]: 5-element Array{Float64,1}:
0.0
0.0
0.0
0.0
0.0

In [63]: ones(5) # vector of Float64 ones

Out [63]: 5-element Array{Float64,1}:
1.0
1.0
1.0
1.0
1.0

In [64]: ones{Int64, 2, 1} # 2x1 array of Int64 ones

Out [64]: 2x1 Array{Int64,2}:
1
1

In [65]: trues(3), falses(3) # tuple of vector of trues and of falses

Out [65]: (Bool{true, true, true}, Bool{false, false, false})

In [66]: eye(3) # 3x3 Float64 identity matrix

Out [66]: 3x3 Array{Float64,2}:
1.0 0.0 0.0
0.0 1.0 0.0
0.0 0.0 1.0

In [67]: x = linspace(1, 2, 5) # iterator having 5 equally spaced elements

Out [67]: 1.0:0.25:2.0

In [68]: collect(x) # converts iterator to vector

Out [68]: 5-element Array{Float64,1}:
1.0
1.25
1.5
1.75
2.0

In [69]: 1:10 # iterable from 1 to 10

Out [69]: 1:10

In [70]: 1:2:10 # iterable from 1 to 9 with 2 skip

Out [70]: 1:2:9

In [71]: reshape(1:12, 3, 4) # 3x4 array filled with 1:12 values

Out [71]: 3x4 Base.ReshapedArray{Int64,2,UnitRange{Int64},Tuple{}}:
 1  4  7 10
 2  5  8 11
 3  6  9 12

In [72]: fill("a", 2, 2) # 2x2 array filled with "a"
```

```
Out [72]: 2x2 Array{String,2}:  
  "a"  "a"  
  "a"  "a"
```

```
In [73]: repmat(eye(2), 3, 2) # 2x2 identity matrix repeated 3x2 times
```

```
Out [73]: 6x4 Array{Float64,2}:  
 1.0  0.0  1.0  0.0  
 0.0  1.0  0.0  1.0  
 1.0  0.0  1.0  0.0  
 0.0  1.0  0.0  1.0  
 1.0  0.0  1.0  0.0  
 0.0  1.0  0.0  1.0
```

```
In [74]: x = [1, 2] # two element vector !!!!!!! add x' here!
```

```
Out [74]: 2-element Array{Int64,1}:  
 1  
 2
```

```
In [75]: resize!(x, 5) # resize x in place to hold 5 values (filled with garbage)
```

```
Out [75]: 5-element Array{Int64,1}:  
 1  
 2  
569348  
 0  
 0
```

```
In [76]: [1] # vector with one element (not a scalar)
```

```
Out [76]: 1-element Array{Int64,1}:  
 1
```

```
In [77]: [x * y for x in 1:2, y in 1:3] # comprehension generating 2x3 array
```

```
Out [77]: 2x3 Array{Int64,2}:  
 1  2  3  
 2  4  6
```

```
In [78]: Float64[x^2 for x in 1:4] # casting comprehension result to Float64
```

```
Out [78]: 4-element Array{Float64,1}:  
 1.0  
 4.0  
 9.0  
16.0
```

```
In [79]: [1 2] # 1x2 matrix (hcat function)
```

```
Out [79]: 1x2 Array{Int64,2}:  
 1  2
```

```
In [80]: [1 2]' # 2x1 matrix (after transposing)
```

```
Out [80]: 2x1 Array{Int64,2}:  
 1  
 2
```

```
In [81]: [1, 2] # vector (concatenation)
```

```
Out [81]: 2-element Array{Int64,1}:  
 1  
 2
```

```
In [82]: [1; 2] # vector (vcat function)
```

```
Out [82]: 2-element Array{Int64,1}:  
 1  
 2
```

```
In [83]: [1 2 3; 1 2 3] # 2x3 matrix (hvcats function)
```

```
Out [83]: 2x3 Array{Int64,2}:  
 1  2  3  
 1  2  3
```



```
In [84]: [1; 2] == [1 2]' # false, different array dimensions
```

Out [84]: false

```
In [85]: [(1, 2)] # 1-element vector
```

Out [85]: 1-element Array{Tuple{Int64,Int64},1}:
(1, 2)

```
In [86]: collect((1, 2)) # 2-element vector by tuple unpacking
```

Out [86]: 2-element Array{Int64,1}:
1
2

```
In [87]: [[1 2] 3] # append to a row vector (hcat)
```

Out [87]: 1×3 Array{Int64,2}:
1 2 3

```
In [88]: [[1; 2]; 3] # append to a column vector (vcat)
```

Out [88]: 3-element Array{Int64,1}:
1
2
3

Vectors (1D arrays) are treated as column vectors.

Julia offers sparse and distributed matrices (see documentation for details).

Commonly needed array utility functions:

```
In [89]: a = [x * y for x in 1:2, y in 1, z in 1:3] # 2x3 array of Int64; singleton dimension is dropped
```

Out [89]: 2×3 Array{Int64,2}:
1 1 1
2 2 2

```
In [90]: a = [x * y for x in 1:2, y in 1:1, z in 1:3] # 2x1x3 array of Int64; singleton dimension is not dropped
```

Out [90]: 2×1×3 Array{Int64,3}:
[:, :, 1] =
1
2

[:, :, 2] =
1
2

[:, :, 3] =
1
2

```
In [91]: ndims(a) # number of dimensions in a
```

Out [91]: 3

```
In [92]: eltype(a) # type of elements in a
```

Out [92]: Int64

```
In [93]: length(a) # number of elements in a
```

Out [93]: 6

```
In [94]: size(a) # tuple containing dimension sizes of a
```

Out [94]: (2, 1, 3)

```
In [95]: vec(a) # cast array to vector (single dimension)
```

Out [95]: 6-element Array{Int64,1}:
1
2
1

```
2
1
2
```

```
In [96]: squeeze(a, 2) # remove 2nd dimension as it has size 1
```

```
Out [96]: 2×3 Array{Int64,2}:
 1  1  1
 2  2  2
```

```
In [97]: sum(a, 3) # calculate sums for 3rd dimensions, similarly: mean, std, prod, minimum, maximum, any,
```

```
Out [97]: 2×1×1 Array{Int64,3}:
[:, :, 1] =
 3
 6
```

```
In [98]: count(x -> x > 0, a) # count number of times a predicate is true, similar: all, any
```

```
Out [98]: 6
```

Array access functions:

```
In [99]: a = linspace(0, 1) # LinSpace{Float64} of length 50
```

```
Out [99]: 0.0:0.02040816326530612:1.0
```

```
In [100]: a[1] # get scalar 0.0
```

```
Out [100]: 0.0
```

```
In [101]: a[end] # get scalar 1.0 (last position)
```

```
Out [101]: 1.0
```

```
In [102]: a[1:2:end] # every second element from range, LinSpace{Float64}
```

```
Out [102]: 0.0:0.04081632653061224:0.9795918367346939
```

```
In [103]: a[repmat([true, false], 25)] # select every second element, Array{Float64,1}
```

```
Out [103]: 25-element Array{Float64,1}:
 0.0
 0.0408163
 0.0816327
 0.122449
 0.163265
 0.204082
 0.244898
 0.285714
 0.326531
 0.367347
 0.408163
 0.44898
 0.489796
 0.530612
 0.571429
 0.612245
 0.653061
 0.693878
 0.734694
 0.77551
 0.816327
 0.857143
 0.897959
 0.938776
 0.979592
```

```
In [104]: a[[1, 3, 6]] # 1st, 3rd and 6th element of a, Array{Float64,1}
```

```
Out [104]: 3-element Array{Float64,1}:
 0.0
 0.0408163
 0.102041
```

```
In [105]: view(a, 1:2:50) # view into subsarray of a
```

```

Out [105]: 25-element
SubArray{Float64,1,StepRangeLen{Float64,Base.TwicePrecision{Float64},Base.TwicePrecision{Float64}},T
0.0
0.0408163
0.0816327
0.122449
0.163265
0.204082
0.244898
0.285714
0.326531
0.367347
0.408163
0.44898
0.489796
0.530612
0.571429
0.612245
0.653061
0.693878
0.734694
0.77551
0.816327
0.857143
0.897959
0.938776
0.979592

```

```

In [106]: endof(a) # last index of the collection a

```

```

Out [106]: 50

```

Observe the treatment of trailing singleton dimensions:

```

In [107]: a = reshape(1:12, 3, 4)

```

```

Out [107]: 3×4 Base.ReshapedArray{Int64,2,UnitRange{Int64},Tuple{}}:
 1  4  7 10
 2  5  8 11
 3  6  9 12

```

```

In [108]: a[:, 1:2] # 3x2 matrix

```

```

Out [108]: 3×2 Array{Int64,2}:
 1  4
 2  5
 3  6

```

```

In [109]: a[:, 1] # 3 element vector

```

```

Out [109]: 3-element Array{Int64,1}:
 1
 2
 3

```

```

In [110]: a[1, :] # 4 element vector

```

```

Out [110]: 4-element Array{Int64,1}:
 1
 4
 7
10

```

```

In [111]: a[1:1, :] # 1x4 matrix

```

```

Out [111]: 1×4 Array{Int64,2}:
 1  4  7 10

```

```

In [112]: a[:, :, 1, 1] # works 3x4 matrix

```

```

Out [112]: 3×4 Array{Int64,2}:
 1  4  7 10
 2  5  8 11
 3  6  9 12

```

```

In [113]: a[:, :, :, [true]] # wroks 3x4x1 matrix

```

```

Out [113]: 3×4×1×1 Array{Int64,4}:

```

```
[:, :, 1, 1] =  
1  4  7 10  
2  5  8 11  
3  6  9 12
```

```
In [114]: a[1, 1, [false]] # works 0-element Array{Int64,1}
```

```
Out [114]: 0-element Array{Int64,1}
```

```
In [115]: a[] # first element of an array
```

```
Out [115]: 1
```

Array assignment:

```
In [116]: x = collect(reshape(1:8, 2, 4))
```

```
Out [116]: 2×4 Array{Int64,2}:  
1  3  5  7  
2  4  6  8
```

```
In [117]: x[:, 2:3] = [1 2] # error; size mismatch
```

DimensionMismatch("tried to assign 1×2 array to 2×2 destination")

Stacktrace:

```
[1] throw_setindex_mismatch(::Array{Int64,2}, ::Tuple{Int64,Int64}) at .\indices.jl:94  
[2] setindex_shape_check(::Array{Int64,2}, ::Int64, ::Int64) at .\indices.jl:151  
[3] macro expansion at .\multidimensional.jl:501 [inlined]  
[4] _unsafe_setindex!(::IndexLinear, ::Array{Int64,2}, ::Array{Int64,2}, ::Base.Slice{Base.OneTo{Int64}}) at .\multidimensional.jl:488 [inlined]  
[5] macro expansion at .\multidimensional.jl:488 [inlined]  
[6] _setindex! at .\multidimensional.jl:484 [inlined]  
[7] setindex!(::Array{Int64,2}, ::Array{Int64,2}, ::Colon, ::UnitRange{Int64}) at .\abstractarray.jl:101
```

```
In [118]: x[:, 2:3] = repmat([1 2], 2) # OK
```

```
Out [118]: 2×2 Array{Int64,2}:  
1  2  
1  2
```

```
In [119]: x[:, 2:3] = 3 # OK
```

```
Out [119]: 3
```

Arrays are assigned and passed by reference. Therefore copying is provided:

```
In [120]: x = Array{Any}(2)  
x[1] = ones(2)  
x[2] = trues(3)  
a = x  
b = copy(x) # shallow copy  
c = deepcopy(x) # deep copy  
x[1] = "Bang"  
x[2][1] = false  
x
```

```
Out [120]: 2-element Array{Any,1}:  
"Bang"  
Bool{false, true, true}
```

```
In [121]: a # identical as x
```

```
Out [121]: 2-element Array{Any,1}:  
"Bang"  
Bool{false, true, true}
```

```
In [122]: b # only x[2][1] changed from original x
```

```
Out [122]: 2-element Array{Any,1}:  
[1.0, 1.0]  
Bool{false, true, true}
```

```
In [123]: c # contents to original x
```

```
Out [123]: 2-element Array{Any,1}:  
  [1.0, 1.0]  
  Bool{true, true, true}
```

Array types syntax examples:

```
In [124]: [1 2]::Array{Int64, 2} # 2 dimensional array of Int64
```

```
Out [124]: 1×2 Array{Int64,2}:  
  1  2
```

```
In [125]: [true; false]::Vector{Bool} # vector of Bool
```

```
Out [125]: 2-element Array{Bool,1}:  
  true  
  false
```

```
In [126]: [1 2; 3 4]::Matrix{Int64} # matrix of Int64
```

```
Out [126]: 2×2 Array{Int64,2}:  
  1  2  
  3  4
```

Composite types

Composite types are mutable and passed by reference. You can define and access composite types:

```
In [127]: mutable struct Point  
           x::Int64  
           y::Float64  
           meta  
         end  
p = Point(0, 0.0, "Origin")
```

```
Out [127]: Point{0, 0.0, "Origin"}
```

```
In [128]: p.x # access field
```

```
Out [128]: 0
```

```
In [129]: p.meta = 2 # change field value
```

```
Out [129]: 2
```

```
In [130]: p.x = 1.5 # error, wrong data type
```

```
InexactError()
```

```
Stacktrace:  
 [1] convert(::Type{Int64}, ::Float64) at .\float.jl:679
```

```
In [131]: p.z = 1 # error - no such field
```

```
type Point has no field z
```

```
In [132]: fieldnames(p) # get names of instance fields
```

```
Out [132]: 3-element Array{Symbol,1}:  
 :x  
 :y  
 :meta
```

```
In [133]: fieldnames(Point) # get names of type fields
```

```
Out [133]: 3-element Array{Symbol,1}:  
 :x  
 :y  
 :meta
```

You can define type to be immutable by removing word `mutable`. There are also union types (see documentation for details).

Dictionaries

Associative collections (key-value dictionaries):

```
In [134]: x = Dict{Float64, Int64}() # empty dictionary mapping floats to integers
```

```
Out [134]: Dict{Float64,Int64} with 0 entries
```

```
In [135]: y = Dict("a"=>1, "b"=>2) # filled dictionary
```

```
Out [135]: Dict{String,Int64} with 2 entries:
  "b" => 2
  "a" => 1
```

```
In [136]: y["a"] # element retrieval
```

```
Out [136]: 1
```

```
In [137]: y["c"] # error
```

```
KeyError: key "c" not found
```

```
Stacktrace:
 [1] getindex(::Dict{String,Int64}, ::String) at .\dict.jl:474
```

```
In [138]: y["c"] = 3 # added element
```

```
Out [138]: 3
```

```
In [139]: haskey(y, "b") # check if y contains key "b"
```

```
Out [139]: true
```

```
In [140]: keys(y), values(y) # tuple of iterators returning keys and values in y
```

```
Out [140]: (String["c", "b", "a"], [3, 2, 1])
```

```
In [141]: delete!(y, "b") # delete key from a collection, see also: pop!
```

```
Out [141]: Dict{String,Int64} with 2 entries:
  "c" => 3
  "a" => 1
```

```
In [142]: get(y, "c", "default") # return y["c"] or "default" if not haskey(y, "c")
```

```
Out [142]: 3
```

Julia also supports operations on sets and dequeues, priority queues and heaps (please refer to documentation).

Strings

String operations:

```
In [143]: "Hi " * "there!" # string concatenation
```

```
Out [143]: "Hi there!"
```

```
In [144]: "Ho " ^ 3 # repeat string
```

```
Out [144]: "Ho Ho Ho "
```

```
In [145]: string("a= ", 123.3) # create using print function
```

```
Out [145]: "a= 123.3"
```

```
In [146]: repr(123.3) # fetch value of show function to a string
```

```
Out [146]: "123.3"
```

```
In [147]: contains("ABCD", "CD") # check if first string contains second
```

Out [147]: true

In [148]: `"\\n\\t\\$" # C-like escaping in strings, new \\$ escape`

Out [148]: `"\\n\\t\\"`

In [149]: `x = 123
"$x + 3 = $(x+3)" # unescaped $ is used for interpolation`

Out [149]: `"123 + 3 = 126"`

In [150]: `"\\$199" # to get a $ symbol you must escape it`

Out [150]: `"\\$199"`

PCRE regular expressions handling:

In [151]: `r = r"A|B" # create new regexp`

Out [151]: `r"A|B"`

In [152]: `ismatch(r, "CD") # false, no match found`

Out [152]: `false`

In [153]: `m = match(r, "ACBD") # find first regexp match, see documentation for details`

Out [153]: `RegexMatch("A")`

There is a vast number of string functions—please refer to documentation.

Programming constructs

The simplest way to create new variable is by assignment:

In [154]: `x = 1.0 # x is Float64`

Out [154]: `1.0`

In [155]: `x = 1 # now x is Int32 on 32 bit machine and Int64 on 64 bit machine`

Out [155]: `1`

Expressions can be compound using ; or begin end block:

In [156]: `x = (a = 1; 2 * a) # after: x = 2; a = 1
(x, a)`

Out [156]: `(2, 1)`

In [157]: `y = begin
 b = 3
 3 * b
end # after: y = 9; b = 3
(y, b)`

Out [157]: `(9, 3)`

There are standard programming constructs:

```
In [158]: if false # if clause requires Bool test
          z = 1
        elseif 1==2
          z = 2
        else
          a = 3
        end # after this a = 3 and z is undefined
        (a, isdefined(:z))
```

Out [158]: (3, false)

```
In [159]: 1==2 ? "A" : "B" # standard ternary operator
```

Out [159]: "B"

```
In [160]: i = 1
          while true
            i += 1
            if i > 10
              break
            end
          end
          end
          i
```

Out [160]: 11

```
In [161]: for x in 1:10 # x in collection, can also use = here instead of in
          if 3 < x < 6
            continue # skip one iteration
          end
          println(x)
        end # x is introduced in loop outer scope
        x
```

```
1
2
3
6
7
8
9
10
```

Out [161]: 10

You can define your own functions:

```
In [162]: f(x, y = 10) = x + y # new function f with y defaulting to 10; last result returned
          f(3, 2) # simple call, 5 returned
```

Out [162]: 5

```
In [163]: f(3) # 13 returned
```

Out [163]: 13

```
In [164]: function g(x::Int, y::Int) # type restriction
          return y, x # explicit return of a tuple
        end
          g(x::Int, y::Bool) = x * y # add multiple dispatch
          g(2, true) # second definition is invoked
```

Out [164]: 2

```
In [165]: methods(g) # list all methods defined for g
```

Out [165]: 2 methods for generic function **g**:

- **g(x::Int64, y::Bool)** at In[164]:4
- **g(x::Int64, y::Int64)** at In[164]:2


```

In [166]: (x -> x^2)(3) # anonymous function with a call
Out [166]: 9

In [167]: () -> 0 # anonymous function with no arguments
Out [167]: (::#13) (generic function with 1 method)

In [168]: h(x...) = sum(x)/length(x) - mean(x) # vararg function; x is a tuple
           h(1, 2, 3) # result is 0
Out [168]: 0.0

In [169]: x = (2, 3) # tuple
           f(x) # error

MethodError: no method matching +(::Tuple{Int64,Int64}, ::Int64)
Closest candidates are:
  +(::Any, ::Any, ::Any, ::Any...) at operators.jl:424
  +(::Complex{Bool}, ::Real) at complex.jl:239
  +(::Char, ::Integer) at char.jl:40
  ...

Stacktrace:
 [1] f(::Tuple{Int64,Int64}) at .\In[162]:1

In [170]: f(x...) # OK - tuple unpacking
Out [170]: 5

In [171]: s(x; a = 1, b = 1) = x * a / b # function with keyword arguments a and b
           s(3, b = 2) # call with keyword argument
Out [171]: 1.5

In [172]: x1(x; x::Int64 = 2) = x # single keyword argument
           x1() # 2 returned
Out [172]: 2

In [173]: x2(x; x::Bool = true) = x # no multiple dispatch for keyword arguments; function overwritten
           x2() # true; old function was overwritten
Out [173]: true

In [174]: q(f::Function, x) = 2 * f(x) # simple function wrapper
           q(x -> 2x, 10) # 40 returned, no need to use * in 2x (means 2*x)
Out [174]: 40

In [175]: q(10) do x # creation of anonymous function by do construct, useful eg. in IO
           2 * x
           end
Out [175]: 40

In [176]: m = reshape(1:12, 3, 4)
           map(x -> x ^ 2, m) # 3x4 array returned with transformed data
Out [176]: 3×4 Array{Int64,2}:
 1  16  49  100
 4  25  64  121
 9  36  81  144

In [177]: filter(x -> bits(x)[end] == '0', 1:12) # a fancy way to choose even integers from the range
Out [177]: 6-element Array{Int64,1}:
 2
 4
 6
 8
10
12

```

Default function argument beasts:

```
In [178]: y = 10
          f1(x=y) = x; f1() # 10
```

Out [178]: 10

```
In [179]: f2(x=y,y=1) = x; f2() # 10
```

Out [179]: 10

```
In [180]: f3(y=1,x=y) = x; f3() # 1
```

Out [180]: 1

```
In [181]: f4(;x=y) = x; f4() # 10
```

Out [181]: 10

```
In [182]: f5(;x=y,y=1) = x; f5() # error - y not defined yet :(
```

UndefVarError: y not defined

Stacktrace:
[1] f5() at .\In[182]:1

```
In [183]: f6(;y=1,x=y) = x; f6() # 1
```

Out [183]: 1

Variable scoping

The following constructs introduce new variable scope: `function`, `while`, `for`, `try/catch`, `let`, `type`.

You can define variables as:

- `global`: use variable from global scope;
- `local`: define new variable in current scope;
- `const`: ensure variable type is constant (global only).

Special cases:

```
In [184]: w # error, variable does not exist
```

UndefVarError: w not defined

```
In [185]: f() = global w = 1
          f() # after the call w is defined globally
          w
```

Out [185]: 1

```
In [186]: function fn(n)
          x = 0
          for i = 1:n
              x = i
          end
          x
        end
          fn(10) # 10; inside loop we use outer local variable
```

Out [186]: 10

```
In [187]: function fn2(n)
           x = 0
           for i = 1:n
               local x
               x = i
           end
           x
       end
       fn2(10) # 0; inside loop we use new local variable
```

Out [187]: 0

```
In [188]: function fn3(n)
           for i = 1:n
               local x # this local can be omitted; for introduces new scope
               x = i
           end
           x
       end
       fn3(10) # x fetched from global scope as it was already defined
```

Out [188]: (2, 3)

```
In [189]: const n = 2
           n = 3 # warning, value changed
```

WARNING: redefining constant n

Out [189]: 3

```
In [190]: n = 3.0 # error, wrong type
```

invalid redefinition of constant n

```
In [191]: function fun() # no warning
           const x = 2
           x = true
       end
       fun() # true, no warning
```

Out [191]: true

Global constants speed up execution.

The let rebinds the variable:

```
In [192]: Fs = Array{Any}(2)
           i = 1
           while i <= 2
               j = i
               Fs[i] = () -> j
               i += 1
           end
           Fs[1](), Fs[2]() # (2, 2); the same binding for j
```

Out [192]: (2, 2)

```
In [193]: Fs = Array{Any}(2)
           i = 1
           while i <= 2
               let j = i
                   Fs[i] = () -> j
               end
               i += 1
           end
           Fs[1](), Fs[2]() # (1, 2); new binding for j
```

Out [193]: (1, 2)

```
In [194]: Fs = Array{Any}(2)
          i = 1
          for i in 1:2
              j = i
              Fs[i] = () -> j
          end
          Fs[1](), Fs[2]() # (1, 2); for loops and comprehensions rebind variables

Out [194]: (1, 2)
```

Modules

Modules encapsulate code. Can be reloaded, which is useful to redefine functions and types, as top level functions and types are defined as constants.

```
In [195]: module M # module name; can be replaced in one session
          export xx # what module exposes for the world
          xx = 1
          y = 2 # hidden variable
          end

          whos(M) # list exported variables

          M      996 bytes  Module
          xx      8 bytes  Int64
```

```
In [196]: xx # not found in global scope

UndefVarError: xx not defined
```

```
In [197]: M.y # direct variable access possible

Out [197]: 2
```

```
In [198]: # import all exported variables
          # load standard packages this way
          using M

          #import variable y to global scope (even if not exported)
          import M.y

          WARNING: import of M.y into Main conflicts with an existing identifier; ignored.
```

Operators

Julia follows standard operators with the following quirks:

```
In [199]: true || false # binary or operator (singeltons only), || and && use short-circuit evaluation

Out [199]: true

In [ ]: [1 2] .& [2 1] # bitwise and operator

In [201]: 1 < 2 < 3 # chaining conditions is OK (singeltons only)

Out [201]: true

In [202]: [1 2] .< [2 1] # for vectorized operators need to add '.' in front

Out [202]: 1×2 BitArray{2}:
           true  false

In [203]: x = [1 2 3]
           2x + 2(x+1) # multiplication can be omitted between a literal and a variable or a left parenthesis

Out [203]: 1×3 Array{Int64,2}:
           6  10  14
```

```

In [204]: y = [1, 2, 3]

Out [204]: 3-element Array{Int64,1}:
 1
 2
 3

In [205]: x + y # error

DimensionMismatch("dimensions must match")

Stacktrace:
 [1] promote_shape(::Tuple{Base.OneTo{Int64},Base.OneTo{Int64}}, ::Tuple{Base.OneTo{Int64}}) at .\ir
 [2] +(::Array{Int64,2}, ::Array{Int64,1}) at .\arraymath.jl:37

In [206]: x .+ y # 3x3 matrix, dimension broadcasting

Out [206]: 3x3 Array{Int64,2}:
 2  3  4
 3  4  5
 4  5  6

In [207]: x + y' # 1x3 matrix

Out [207]: 1x3 Array{Int64,2}:
 2  4  6

In [208]: x * y # array multiplication, 1-element vector (not scalar)

Out [208]: 1-element Array{Int64,1}:
 14

In [209]: x .* y # element-wise multiplication, 3x3 array

Out [209]: 3x3 Array{Int64,2}:
 1  2  3
 2  4  6
 3  6  9

In [210]: x == [1 2 3] # true, object looks the same

Out [210]: true

In [211]: x === [1 2 3] # false, objects not identical

Out [211]: false

In [212]: z = reshape(1:9, 3, 3)

Out [212]: 3x3 Base.ReshapedArray{Int64,2,UnitRange{Int64},Tuple{}}:
 1  4  7
 2  5  8
 3  6  9

In [213]: z + x # error

DimensionMismatch("dimensions must match")

Stacktrace:
 [1] promote_shape(::Tuple{Base.OneTo{Int64},Base.OneTo{Int64}}, ::Tuple{Base.OneTo{Int64},Base.OneTo{Int64}}) at .\ir
 [2] promote_shape(::Base.ReshapedArray{Int64,2,UnitRange{Int64},Tuple{}}, ::Array{Int64,2}) at .\ir
 [3] +(::Base.ReshapedArray{Int64,2,UnitRange{Int64},Tuple{}}, ::Array{Int64,2}) at .\arraymath.jl:37

In [214]: z .+ x # x broadcasted vertically

Out [214]: 3x3 Array{Int64,2}:
 2  6  10
 3  7  11
 4  8  12

In [215]: z .+ y # y broadcasted horizontally

Out [215]: 3x3 Array{Int64,2}:
 2  5  8
 4  7  10

```

```
6 9 12
```

```
In [216]: # explicit broadcast of singleton dimensions
# function + is called for each array element
broadcast(+, [1 2], [1; 2])
```

```
Out [216]: 2×2 Array{Int64,2}:
 2  3
 3  4
```

Many typical matrix transformation functions are available (see documentation).

Essential general usage functions

```
In [217]: show(collect(1:100)) # show text representation of an object
```

```
[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27,
```

```
In [218]: eps() # distance from 1.0 to next representable Float64
```

```
Out [218]: 2.220446049250313e-16
```

```
In [219]: nextfloat(2.0) # next float representable, similarly provided prevfloat
```

```
Out [219]: 2.0000000000000004
```

```
In [220]: isequal(NaN, NaN) # true
```

```
Out [220]: true
```

```
In [221]: NaN == NaN # false
```

```
Out [221]: false
```

```
In [222]: NaN === NaN # true
```

```
Out [222]: true
```

```
In [223]: isequal(1, 1.0) # true
```

```
Out [223]: true
```

```
In [224]: 1 == 1.0 # true
```

```
Out [224]: true
```

```
In [225]: 1 === 1.0 # false
```

```
Out [225]: false
```

```
In [226]: isfinite(Inf) # false, similarly provided: isinf, isnan
```

```
Out [226]: false
```

```
In [227]: fld(-5, 3), mod(-5, 3) # (-2, 1), division towards minus infinity
```

```
Out [227]: (-2, 1)
```

```
In [228]: div(-5, 3), rem(-5, 3) # (-1, -2), division towards zero
```

```
Out [228]: (-1, -2)
```

```
In [229]: find(x -> mod(x, 2) == 0, 1:8) # find indices for which function returns true
```

```
Out [229]: 4-element Array{Int64,1}:
 2
 4
 6
 8
```

```

In [230]: x = [1 2]; identity(x) == x # true, identity function

Out [230]: true

In [231]: info("Info") # print information, similarly warn and error (raises error)

␣[1m␣[36mINFO: ␣[39m␣[22m␣[36mInfo
␣[39m

In [232]: ntuple(x->2x, 3) # create tuple by calling x->2x with values 1, 2 and 3

Out [232]: (2, 4, 6)

In [233]: isdefined(:x) # if variable x is defined (:x is a symbol)

Out [233]: true

In [234]: y = Array{Any}(2); isassigned(y, 3) # if position 3 in array is assigned (not out of bounds or #un

Out [234]: false

In [235]: fieldtype(typeof(1:2),:start) # get type of the field in composite type (passed as symbol)

Out [235]: Int64

In [236]: fieldnames(typeof(1:2))

Out [236]: 2-element Array{Symbol,1}:
 :start
 :stop

In [237]: 1:5 |> exp |> sum # function application chaining

␣[1m␣[33mWARNING: ␣[39m␣[22m␣[33mexp{T <: Number}(x::AbstractArray{T}) is deprecated, use exp.(x)
instead.␣[39m
Stacktrace:
 [1] ␣[1mdepwarn␣[22m␣[22m␣[1m(␣[22m␣[22m::String, ::Symbol␣[1m]␣[22m␣[22m at
␣[1m.\deprecated.jl:64␣[22m␣[22m
 [2] ␣[1mexp␣[22m␣[22m␣[1m(␣[22m␣[22m::UnitRange{Int64}␣[1m]␣[22m␣[22m at
␣[1m.\deprecated.jl:51␣[22m␣[22m
 [3] ␣[1m]>␣[22m␣[22m␣[1m(␣[22m␣[22m::UnitRange{Int64}, ::Base.#exp␣[1m]␣[22m␣[22m at
␣[1m.\operators.jl:857␣[22m␣[22m
 [4] ␣[1minclude_string␣[22m␣[22m␣[1m(␣[22m␣[22m::String, ::String␣[1m]␣[22m␣[22m at
␣[1m.\loading.jl:498␣[22m␣[22m
 [5] ␣[1mexecute_request␣[22m␣[22m␣[1m(␣[22m␣[22m::LastMain.ZMQ.Socket,
::LastMain.IJulia.Msg␣[1m]␣[22m␣[22m at
␣[1mD:\Software\JULIA_PKG\v0.6\IJulia\src\execute_request.jl:156␣[22m␣[22m
 [6] ␣[1meventloop␣[22m␣[22m␣[1m(␣[22m␣[22m::LastMain.ZMQ.Socket␣[1m]␣[22m␣[22m at
␣[1mD:\Software\JULIA_PKG\v0.6\IJulia\src\eventloop.jl:8␣[22m␣[22m
 [7] ␣[1m(:::LastMain.IJulia.##9#12)␣[22m␣[22m␣[1m(␣[22m␣[22m␣[1m]␣[22m␣[22m at
␣[1m.\task.jl:335␣[22m␣[22m
while loading In[237], in expression starting on line 1

Out [237]: 233.2041839862982

In [238]: zip(1:3, 1:3) |> collect # convert iterables to iterable tuple and pass it to collect

Out [238]: 3-element Array{Tuple{Int64,Int64},1}:
 (1, 1)
 (2, 2)
 (3, 3)

In [239]: enumerate("abc") # create iterator of tuples (index, collection element)

Out [239]: Enumerate{String}("abc")

In [240]: collect(enumerate("abc"))

Out [240]: 3-element Array{Tuple{Int64,Char},1}:
 (1, 'a')
 (2, 'b')
 (3, 'c')

In [241]: isempty("abc") # check if collection is empty

```

```

Out [241]: false

In [242]: 'b' in "abc" # check if element is in a collection

Out [242]: true

In [243]: indexin(collect("abc"), collect("abrakadabra")) # [11, 9, 0] ('c' not found), needs arrays

Out [243]: 3-element Array{Int64,1}:
 11
  9
  0

In [244]: findin("abc", "abrakadabra") # [1, 2] ('c' was not found)

Out [244]: 2-element Array{Int64,1}:
 1
 2

In [245]: unique("abrakadabra") # return unique elements

Out [245]: 5-element Array{Char,1}:
 'a'
 'b'
 'r'
 'k'
 'd'

In [246]: issubset("abc", "abcd") # check if every element in fist collection is in the second

Out [246]: true

In [247]: indmax("abrakadabra") # index of maximal element (3 - 'r' in this case)

Out [247]: 3

In [248]: findmax("abrakadabra") # tuple: maximal element and its index

Out [248]: ('r', 3)

In [249]: filter(x->mod(x,2)==0, 1:10) # retain elements of collection that meet predicate

Out [249]: 5-element Array{Int64,1}:
 2
 4
 6
 8
10

In [250]: dump(1:2:5) # show all user-visible structure of an object

StepRange{Int64,Int64}
 start: Int64 1
 step: Int64 2
 stop: Int64 5

In [251]: sort(rand(10)) # sort 10 uniform random variables

Out [251]: 10-element Array{Float64,1}:
 0.0146516
 0.305749
 0.408407
 0.524122
 0.608936
 0.685384
 0.777021
 0.826193
 0.855542
 0.993751

```

Reading and writing data

For I/O details refer documentation. Basic operations:

- `readdlm`, `readcsv`: read from file
- `writedlm`, `writcsv`: write to a file

Random numbers

Basic random numbers:

```
In [252]: srand(1) # set random number generator seed to 1
          rand() # generate random number from U[0,1)
```

```
Out [252]: 0.23603334566204692
```

```
In [253]: rand(3, 4) # generate 3x4 matrix of random numbers from U[0,1]
```

```
Out [253]: 3×4 Array{Float64,2}:
 0.346517  0.488613  0.999905  0.555751
 0.312707  0.210968  0.251662  0.437108
 0.00790928 0.951916  0.986666  0.424718
```

```
In [254]: rand(2:5, 10) # generate vector of 10 random integer numbers in range form 2 to 5
```

```
Out [254]: 10-element Array{Int64,1}:
 4
 2
 3
 4
 5
 5
 3
 4
 3
 5
```

```
In [255]: randn(10) # generate vector of 10 random numbers from standard normal distribution
```

```
Out [255]: 10-element Array{Float64,1}:
 0.795949
 0.670062
 0.550852
-0.0633746
 1.33694
-0.0731486
-0.745464
-1.22006
-0.0531773
-0.165136
```

Advanced randomness form Distributions package:

```
In [ ]: using Distributions # load package
        sample(1:10, 10) # single bootstrap sample from set 1-10
```

```
␣[1m␣[36mINFO: ␣[39m␣[22m␣[36mRecompiling stale cache file
D:\Software\JULIA_PKG\lib\v0.6\Distributions.ji for module Distributions.
␣[39m
```

```
In [ ]: b = Beta(0.4, 0.8) # Beta distribution with parameters 0.4 and 0.8
        # see documentation for supported distributions
```

```
In [ ]: mean(b) # expected value of distribution b
        # see documentation for other supported statistics
```

```
In [ ]: rand(b, 100) # 100 independent random samples from distribution b
```

Statistics and machine learning

Visit <http://juliastats.github.io/> for the details (in particular R-like data frames).

Starting with Julia version 0.4 there is a core language construct `Nullable` that allows to represent missing value (similar to Haskell's `Maybe`).

```
In [ ]: u1 = Nullable{1} # contains value
        u2 = Nullable{Int64}{} # missing value
        get(u1) # OK
```

```
In [ ]: get(u2) # error - missing
```

```
In [ ]: isnull(u1) # false
```

```
In [ ]: isnull(u2) # true
```

Plotting

There are several plotting packages for Julia: PyPlot, Gadfly, Plots,

```
In [ ]: using PyPlot
        srand(1) # second plot
        x, y = randn(100), randn(100)
        plot(x, y)
```

Macros

You can define macros (see documentation for details). Useful standard macros.

Assertions:

```
In [ ]: @assert 1 == 2 "ERROR" # 2 macro arguments; error raised
```

```
In [ ]: using Base.Test # load Base.Test module
        @test 1 == 2 # similar to assert; error
```

```
In [ ]: @test_approx_eq 1 1.1 # error
```

```
In [ ]: @test_approx_eq_eps 1 1.1 0.2 # no error
```

Function vectorization:

```
In [ ]: t(x::Float64, y::Float64 = 1.0) = x * y
```

```
In [ ]: t(1.0, 2.0) # OK
```

```
In [ ]: t([1.0 2.0]) # error
```

```
In [ ]: t.([1.0 2.0]) # OK
```

```
In [ ]: t([1.0 2.0], 2.0) # error
```

```
In [ ]: t.([1.0 2.0], 2.0) # OK
```

```
In [ ]: t.(2.0, [1.0 2.0]) # OK
```

Benchmarking:

```
In [ ]: @time [x for x in 1:10^6].' # print time and memory
```

```
In [ ]: @timed [x for x in 1:10^6].' # return value, time and memory
```

```
In [ ]: @elapsed [x for x in 1:10^6] # return time
```

```
In [ ]: @allocated [x for x in 1:10^6] # return memory
```

```
In [ ]: tic() # start timer
```

```
In [ ]: toc() # stop timer and print time
```

```
In [ ]: tic()  
toq()
```
