

# A - Odd Position Sum

Time Limit: 2 sec / Memory Limit: 1024 MiB

Score : 100 points

## Problem Statement

You are given a sequence of positive integers of length  $N$ :  $A = (A_1, A_2, \dots, A_N)$ .

Find the sum of the odd-indexed elements of  $A$ . That is, find  $A_1 + A_3 + A_5 + \dots + A_m$ , where  $m$  is the largest odd number not exceeding  $N$ .

## Constraints

- $1 \leq N \leq 100$
- $1 \leq A_i \leq 100$
- All input values are integers.

## Input

The input is given from Standard Input in the following format:

```
N
A_1 A_2 ... A_N
```

## Output

Print the answer.

## Sample Input 1

```
7
3 1 4 1 5 9 2
```

## Sample Output 1

```
14
```

The sum of the odd-indexed elements of  $A$  is  $A_1 + A_3 + A_5 + A_7 = 3 + 4 + 5 + 2 = 14$ .

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## Sample Input 2

```
1
100
```

## Sample Output 2

```
100
```

## Sample Input 3

```
14
100 10 1 10 100 10 1 10 100 10 1 10 100 10
```

## Sample Output 3

```
403
```

# B - Four Hidden

Time Limit: 2 sec / Memory Limit: 1024 MiB

Score : 250 points

## Problem Statement

You are given a string  $T$  consisting of lowercase English letters and  $?$ , and a string  $U$  consisting of lowercase English letters.

The string  $T$  is obtained by taking some lowercase-only string  $S$  and replacing exactly four of its characters with  $?$ .

Determine whether it is possible that the original string  $S$  contained  $U$  as a contiguous substring.

## Constraints

- $T$  is a string of length between 4 and 10, inclusive, consisting of lowercase letters and  $?$ .
- $T$  contains exactly four occurrences of  $?$ .
- $U$  is a string of length between 1 and  $|T|$ , inclusive, consisting of lowercase letters.

## Input

The input is given from Standard Input in the following format:

```
 $T$   
 $U$ 
```

## Output

Print Yes if it is possible that the original string  $S$  contained  $U$  as a contiguous substring; otherwise, print No.

## Sample Input 1

```
tak??a?h?  
nashi
```

## Sample Output 1

Yes

For example, if  $S$  is takanashi, it contains nashi as a contiguous substring.

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## Sample Input 2

??e??e  
snuke

## Sample Output 2

No

No matter what characters replace the ?s in  $T$ ,  $S$  cannot contain snuke as a contiguous substring.

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## Sample Input 3

????  
aoki

## Sample Output 3

Yes

# C - 403 Forbidden

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Time Limit: 2 sec / Memory Limit: 1024 MiB

Score : 300 points

## Problem Statement

There are  $N$  users on WAtCoder, numbered from 1 to  $N$ , and  $M$  contest pages, numbered from 1 to  $M$ . Initially, no user has view permission for any contest page.

You are given  $Q$  queries to process in order. Each query is of one of the following three types:

- 1  $x$   $y$ : Grant user  $X$  view permission for contest page  $Y$ .
- 2  $x$ : Grant user  $X$  view permission for all contest pages.
- 3  $x$   $y$ : Answer whether user  $X$  can view contest page  $Y$ .

It is possible for a user to be granted permission for the same contest page multiple times.

## Constraints

- $1 \leq N \leq 2 \times 10^5$
  - $1 \leq M \leq 2 \times 10^5$
  - $1 \leq Q \leq 2 \times 10^5$
  - $1 \leq X \leq N$
  - $1 \leq Y \leq M$
  - All input values are integers.
-

## Input

The input is given from Standard Input in the following format:

```
 $N$   $M$   $Q$   
query1  
query2  
⋮  
query $Q$ 
```

Each query <sub>$i$</sub>  is in one of the following formats:

```
1  $X$   $Y$ 
```

```
2  $X$ 
```

```
3  $X$   $Y$ 
```

## Output

For each query of the third type, print Yes if user  $X$  can view contest page  $Y$ , otherwise print No, each on its own line.

### Sample Input 1

```
2 3 5  
1 1 2  
3 1 1  
3 1 2  
2 2  
3 2 3
```

## Sample Output 1

```
No  
Yes  
Yes
```

- In the first query, user 1 is granted permission to view contest page 2.
- At the second query, user 1 can view only page 2; they cannot view page 1, so print No.
- At the third query, user 1 can view page 2, so print Yes.
- In the fourth query, user 2 is granted permission to view all pages.
- At the fifth query, user 2 can view pages 1, 2, 3; they can view page 3, so print Yes.

## Sample Input 2

```
5 5 10  
2 2  
3 4 4  
1 1 1  
1 4 1  
1 4 2  
1 4 4  
1 2 4  
3 3 2  
3 5 4  
3 2 1
```

## Sample Output 2

```
No  
No  
No  
Yes
```

# D - Forbidden Difference

Time Limit: 2 sec / Memory Limit: 1024 MiB

Score : 425 points

## Problem Statement

You are given a length- $N$  integer sequence  $A = (A_1, A_2, \dots, A_N)$  and a non-negative integer  $D$ . We wish to delete as few elements as possible from  $A$  to obtain a sequence  $B$  that satisfies the following condition:

- $|B_i - B_j| \neq D$  for all  $i, j$  ( $1 \leq i < j \leq |B|$ ).

Find the minimum number of deletions required.

## Constraints

- $1 \leq N \leq 2 \times 10^5$
- $0 \leq D \leq 10^6$
- $0 \leq A_i \leq 10^6$
- All input values are integers.

## Input

The input is given from Standard Input in the following format:

```
N D
A_1 A_2 ... A_N
```

## Output

Print the answer.

## Sample Input 1

```
5 2
3 1 4 1 5
```



## Sample Output 1

```
1
```

Deleting  $A_1 = 3$  yields  $B = (1, 4, 1, 5)$ , which satisfies  $|B_i - B_j| \neq 2$  for all  $i < j$ .

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## Sample Input 2

```
4 3
1 6 1 8
```

## Sample Output 2

```
0
```

The sequence  $A$  may already satisfy the condition.

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## Sample Input 3

```
10 3
1 6 2 10 2 3 2 10 6 4
```

## Sample Output 3

```
2
```

# E - Forbidden Prefix

Time Limit: 2 sec / Memory Limit: 1024 MiB

Score : 500 points

## Problem Statement

There are two multisets of strings,  $X$  and  $Y$ , both initially empty.

You are given  $Q$  queries to process in order. In the  $i$ -th query, you receive an integer  $T_i$  and a string  $S_i$ . If  $T_i = 1$ , insert  $S_i$  into  $X$ ; if  $T_i = 2$ , insert  $S_i$  into  $Y$ .

After processing each query, print this value:

- the number of strings in  $Y$  that have no element of  $X$  as a prefix.

## Constraints

- $Q$  is an integer between 1 and  $2 \times 10^5$ , inclusive.
- $T_i \in \{1, 2\}$
- Each  $S_i$  is a string of length between 1 and  $5 \times 10^5$ , inclusive, consisting of lowercase English letters.
- $\sum_{i=1}^Q |S_i| \leq 5 \times 10^5$

## Input

The input is given from Standard Input in the following format:

```
Q
T1 S1
T2 S2
⋮
TQ SQ
```

## Output

Print  $Q$  lines. The  $i$ -th line ( $1 \leq i \leq Q$ ) should contain the count after processing the  $i$ -th query.

## Sample Input 1

```
4
1 at
2 watcoder
2 atcoder
1 wa
```

## Sample Output 1

```
0
1
1
0
```

The counts after processing the queries for  $i = 1, 2, 3, 4$  are as follows.

- $i = 1$ :  $Y$  is empty, so the count is 0.
- $i = 2$ : watcoder has no element of  $X$  as a prefix, so the count is 1.
- $i = 3$ : watcoder has no element of  $X$  as a prefix, while atcoder has at as a prefix, so the count is 1.
- $i = 4$ : watcoder has wa as a prefix, and atcoder has at as a prefix, so the count is 0.

## Sample Input 2

```
10
1 w
1 avko
2 atcoder
1 bzginn
2 beginner
1 atco
2 contest
1 ntxcdg
1 atc
1 contest
```

## Sample Output 2

```
0
0
1
1
2
1
2
2
2
1
```

# F - Shortest One Formula

Time Limit: 2 sec / Memory Limit: 1024 MiB

Score : 500 points

## Problem Statement

You are given a positive integer  $N$ .

Among all valid arithmetic expressions consisting of the characters  $1, +, *, (, \text{ and } )$ , find one of the minimum length whose value is  $N$ .

More formally, among the strings  $S$  satisfying all of the following conditions, find one of the minimum length:

- $S$  conforms to the symbol  $\langle \text{expr} \rangle$  in the BNF ([https://en.wikipedia.org/wiki/Backus%E2%80%93Naur\\_form](https://en.wikipedia.org/wiki/Backus%E2%80%93Naur_form)) below.
- The value of the expression represented by  $S$  is  $N$ .

```

<expr>    ::= <term> | <expr> "+" <term>
<term>    ::= <factor> | <term> "*" <factor>
<factor>  ::= <number> | "(" <expr> ")"
<number>  ::= "1" | "1" <number>
  
```

Strings that conform to  $\langle \text{expr} \rangle$  include:

- $1111+111$  representing  $1111 + 111$ .
- $(1+1)*(1+1)$  representing  $(1 + 1) \times (1 + 1)$ .
- $(11+(1+1)*(1+1))+1$  representing  $(11 + (1 + 1) \times (1 + 1)) + 1$ .

Strings that do not conform to  $\langle \text{expr} \rangle$  include:

- $(1+1)(1+1)$
- $1+2$
- $1-1$
- $1/1$
- $)1($
- $1++1$
- $+1$
- $(+1)$
- $1*+1$

## Constraints

- $1 \leq N \leq 2000$
- All input values are integers.

## Input

The input is given from Standard Input in the following format:

$N$

## Output

Print a solution.

### Sample Input 1

9

### Sample Output 1

$(1+1+1)*(1+1+1)$

Expressions whose value is 9 include:

- $(1+1+1)*(1+1+1)$
- $1+1+1+1+1+1+1+1+1$
- $(1+1)*(1+1)*(1+1)+1$

Among them, a shortest is  $(1+1+1)*(1+1+1)$ .

### Sample Input 2

11

### Sample Output 2

11

## Sample Input 3

```
403
```

## Sample Output 3

```
1+(1+1+1)*(1+11+11+111)
```

# G - Odd Position Sum Query

Time Limit: 4 sec / Memory Limit: 1024 MiB

Score : 600 points

## Problem Statement

There is an initially empty sequence  $A$ .

You are given  $Q$  queries to process in order. The  $i$ -th query is explained below:

You are given an integer  $y_i$ . If  $i = 1$ , let  $z$  be 0; otherwise, let  $z$  be the answer to the  $(i - 1)$ -th query. Define  $x_i = ((y_i + z) \bmod 10^9) + 1$ . Append  $x_i$  to the end of  $A$ . Then, let  $B = (B_1, B_2, \dots, B_i)$  be the sequence  $A$  sorted in ascending order, and find the sum of the odd-indexed elements of  $B$ . That is, find  $B_1 + B_3 + B_5 + \dots + B_m$ , where  $m$  is the largest odd number not exceeding  $i$ .

## Constraints

- $1 \leq Q \leq 3 \times 10^5$
- $0 \leq y_i < 10^9$
- $1 \leq x_i \leq 10^9$
- All input values are integers.

## Input

The input is given from Standard Input in the following format:

```
Q
y1
y2
⋮
yQ
```

## Output

Print  $Q$  lines. The  $i$ -th line should contain the answer to the  $i$ -th query.



## Sample Input 1

```
5
1
3
1
999999994
999999993
```

## Sample Output 1

```
2
2
8
6
1000000006
```

- For the 1st query,  $y_1 = 1, z = 0$ , so  $x_1 = ((1 + 0) \bmod 10^9) + 1 = 2$ . Appending this to the end of  $A$  gives  $A = (2)$ . Sorting  $A$  in ascending order yields  $B = (2)$ , and the sought value is  $B_1 = 2$ .
- For the 2nd query,  $y_2 = 3, z = 2$ , so  $x_2 = ((3 + 2) \bmod 10^9) + 1 = 6$ . Appending gives  $A = (2, 6)$ , so  $B = (2, 6)$  and the sought value is  $B_1 = 2$ .
- For the 3rd query,  $y_3 = 1, z = 2$ , so  $x_3 = ((1 + 2) \bmod 10^9) + 1 = 4$ . Appending gives  $A = (2, 6, 4)$ , so  $B = (2, 4, 6)$  and the sought value is  $B_1 + B_3 = 8$ .
- For the 4th query,  $y_4 = 999999994, z = 8$ , so  $x_4 = ((999999994 + 8) \bmod 10^9) + 1 = 3$ . Appending gives  $A = (2, 6, 4, 3)$ , so  $B = (2, 3, 4, 6)$  and the sought value is  $B_1 + B_3 = 6$ .
- For the 5th query,  $y_5 = 999999993, z = 6$ , so  $x_5 = ((999999993 + 6) \bmod 10^9) + 1 = 1000000000$ . Appending gives  $A = (2, 6, 4, 3, 1000000000)$ , so  $B = (2, 3, 4, 6, 1000000000)$  and the sought value is  $B_1 + B_3 + B_5 = 1000000006$ .

## Sample Input 2

```
8
105282053
695234822
468007124
120710491
568831200
700753895
765188109
262666319
```

## Sample Output 2

```
105282054
105282054
905798931
599798602
995656103
891549225
1652393438
1652393438
```

Below are the values of  $x_1, x_2, \dots, x_8$  in order:

```
105282054
800516877
573289179
26509423
168629803
696409999
656737335
915059758
```