```
cd ::= class C extends D \{ \overline{fd}; kd \overline{md} \}
                                                                                        class
fd := q C f
                                                                                         field
kd ::= q C ( t C g, t C f ) { super(g); this.f = f; }
                                                                                    constructor
md ::= t C m (t C this, t C x) {\overline{t} C y \overline{s}; return z}
                                                                                  instance method
                                                                                     expression
e := x | x.f
s := x = e \mid x.f = y \mid x = y.m(z) \mid super(g) \mid this(g) \mid x = new C() \mid s;s
                                                                                      statement
                                                                                   qualifier type
k ::= initialized | underinitialized | unknowninitialized | fbcbottom
                                                                             initializatioin qualifier
q ::= readonly | mutable | polymutable | substitutablepolymutable |
receiverdependantmutable | immutable | bottom
                                                                              immutability qualifier
```

Qualifier Hierarchy

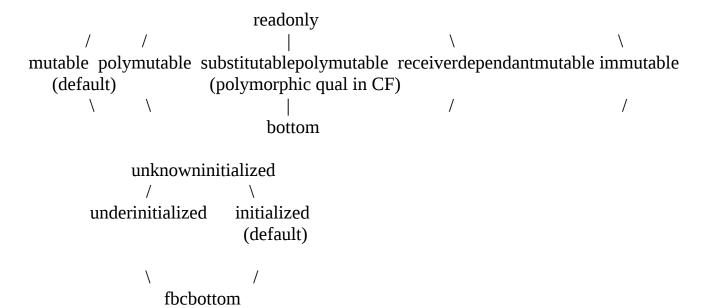


Figure 1 Combination of qualifiers. Two qualifier hierarchies are orthogonal. If an object is under initialization, its immutability guarantee is not satisfied. So even immutable and receiverdependantmutable objects can also be modified when under initialization.

Subtype relations

$$k_1 q_1 <: k_2 q_2 <=> k_1 <: k_2 \land q_1 <: q_2$$

Helper Functions

$$q C f$$

$$fType(f) = q$$

Note:

1) No initialization modifier on field declarations. In actual implementation, to have circular initialization, *@NotOnlyInitialized* can be used on field declaration. However, it doesn't belong to initialization qualifier hierarchy.

2) The field is unique within the whole type hierarchy

fields(C) returns all fields directly declared in C. cBody(kd) returns constructor body of kd. mBody(md) returns method body of md.

Viewpoint Adaptation Rules

- _ ⊳ mutable = mutable
- $_$ \triangleright readonly = readonly
- _ ⊳ immutable = immutable
- \triangleright bottom = bottom
- _ ⊳ polymutable = substitutablepolymutable
- $q \triangleright receiver dependant mutable = q$

Note: substitutable polymutable only exists shortly after viewpoint adaptation is done, but will must be substituted by another qualifier immediately by Qualifier Polymorphism. So, substitutable polymutable should not appear on left or right side of viewpoint adaptation triangle.

Special Rules

- Forbid polymutable fields; readonly or polymutable constructor return type and readonly instantiation of objects
- In constructor, $q_{this} = q_{ret}$
- Forbid initialization modifier on fields, constructor return type and new statement
- Forbid bottom except on (implicit/explicit) lower bounds and null literal.
- Forbid explicit use of substitutable polymutable everywhere.

TODO: Should we allow polymutable constructor return type?

Typing Rules

$$\begin{array}{c}
x \in \Gamma \\
\hline
\Gamma \vdash x : \Gamma(x)
\end{array} (T-VAR)$$

$$\Gamma(x) = k_x q_x \quad \text{fType}(f) = q_f \quad q = q_x \triangleright q_f$$

$$\downarrow \text{initialized} \quad if \ k_x = initialized$$

$$\downarrow \text{unknowninitialized} \quad otherwise$$

$$\Gamma \vdash x.f : k \neq 0$$

$$(T-FLD)$$

Figure 2 Expression typing

$$\Gamma \vdash e = t_e \quad t_e <: \Gamma(x)$$

$$\Gamma \vdash x = e$$
(T-VARASS)

$$\begin{split} \Gamma(x) &= k_x \, q_x \quad \Gamma(y) = k_y \, q_y \quad typeof(f) = q_f \\ q_x &= \text{mutable } V \\ q_f &= \text{mutable } V \\ q_f &= \text{readonly } V \\ (k_x &= \text{underinitialized } \Lambda \, q_x = \text{immutable) } V \\ (k_x &= \text{underinitialized } \Lambda \, q_x = \text{polyimmutable)} \\ q_y &<: q_x \, \triangleright \, q_f \\ k_x &= \text{underinitialized } V \, k_y = \text{initialized} \end{split}$$

(T-FLDASS)

$$\begin{split} \Gamma(x) &= k_x \ q_x \quad \underline{\Gamma}(y) = k_y \ q_y \quad \Gamma(\overline{z}) = \overline{k_z} \, \overline{q_z} \quad typeof(m) = k_{this} \ q_{this}, \ \overline{k_p} \, \overline{q_p} \rightarrow k_{ret} \ q_{ret} \\ k_y &<: k_{this} \quad \overline{k_z} <: \overline{k_p} \quad k_{ret} <: k_x \end{split}$$

$$q_{this-vp} = q_y . \triangleright q_{this} \quad \overline{q_{p-vp}} = q_y \triangleright \overline{q_p} \quad q_{ret-vp} = q_y \triangleright q_{ret}$$

 $q_{this-vp}$ = substitutablepolymutable \mathbf{V} q_{p-vp} = substitutablepolymutable \mathbf{V} q_{ret-vp} = substitutablepolymutable \Rightarrow s exists

$$\begin{array}{lll} q_{y} <: & \begin{cases} q_{\text{this-vp}} & \textit{if } q_{\textit{this-vp}} \neq \textit{substitutablepolymutable} \\ s & \textit{else} \end{cases} \\ \hline q_{z} <: & \begin{cases} \overline{q}_{p\text{-vp}} & \textit{if } \overline{q}_{p\text{-vp}} \neq \textit{substitutablepolymutable} \\ s & \textit{else} \end{cases} \\ \\ q_{x} :> & \begin{cases} q_{\text{ret-vp}} & \textit{if } q_{\textit{ret-vp}} \neq \textit{substitutablepolymutable} \\ s & \textit{else} \end{cases} \\ \hline \Gamma \vdash x = y.[s]m(\overline{z}) & \text{(T-CALL)} \end{cases}$$

Note: inference of s is another subproblem. It is disussed in the last two pages.

$$kd \ in \ C \qquad C <: D \qquad typeof(D) = \overline{k}_{p\text{-D}} \ \overline{q}_{p\text{-D}} \rightarrow q_{ret\text{-D}} \qquad typeof(kd) = \overline{} \rightarrow q_{ret\text{-C}}$$

$$if \quad q_{ret\text{-D}} = receiver dependant mutable$$

$$q_{ret\text{-C}} = \begin{cases} immutable & \text{if } q_{ret\text{-D}} = immutable \\ if \quad q_{ret\text{-D}} = mutable \end{cases}$$

$$r(z) = k_z \ q_z \qquad \qquad \overline{k}_z <: \overline{k}_{p\text{-D}} \qquad \qquad \overline{q}_z <: q_{ret\text{-C}} \rhd \overline{q}_{p\text{-D}}$$

$$\Gamma \vdash super(\overline{z}) \ in \ kd \qquad \qquad (T\text{-SUPER})$$

^{*} Previously, when $q_{\text{ret-D}}$ = mutable, $q_{\text{ret-C}}$ can still be immutable. Because at that time, immutable constructors only have immutable or polyimmutable(does not exist anymore), thus any mutable objet created locally cannot escape and be captured by outside objects; Neither outside mutable objects will be captured by the

receiverdependantmutable field when invoking mutable super constructor in immutable constructor. But now, immutable and receiverdependantmutable constructors don't have such restrictions(mutable parameters are allowed in both cases) any more, so outside mutable objects can be captured by receiverdependantmutable field. If we allow calling mutable super() in immutable subclass constructor, when we use this_{sub}.rdmf to access the field, the result is not guarantee to be immutable(may be the mutable object assigned in super mutable constructor). Therefore, we don't allow this kinds of flexibility and require subclass and superclass constructors should have the exact same qualifier if $q_{ret-D} \neq receiverdependantmutable$

(T-THIS) (omitted)

* *Note:* In real Java code, one class can have multiple overloaded consturctors. One constructor can invoke the other by "this(..., ...)". The type rule T-THIS is very much the same as T-SUPER except that the constructor invoked by "this(..., ...)" comes from the same class.

$$\begin{split} &\Gamma(x) = k_x \ \underline{q_x} & \Gamma(\overline{y}) = \overline{k_y} \ \overline{q_y} & typeof(C) = \overline{k_p} \ \overline{q_p} \to q_{ret} \\ &\overline{q_y} <: q \rhd \overline{q_p} & q <: q \rhd q_{ret} & q \neq readonly \\ &\overline{k_y} <: \overline{k_p} \\ &q <: q_x \quad k <: k_x & k = \begin{cases} & initialized & if \ \overline{k_p} = initialized \\ & underinitialized & otherwise \end{cases} \\ &\Gamma \vdash x = new \ q \ C(\overline{y}) \end{split}$$

$$\begin{array}{cccc}
\Gamma \vdash s_1 & \Gamma \vdash s_2 \\
\hline
\Gamma \vdash s_1; s_2
\end{array} (T-SEQ)$$

Figure 3 Statement typing

Well-formdness Rules

$$\begin{split} cBody(kd) &= super(g); \ this.f = f \qquad typeof(kd) = \overline{k_p} \ \overline{q_p} \to q_{ret} \\ q_{ret} \neq readonly \ \ & \Lambda \ q_{ret} \neq polymutable \\ \Gamma &= (this: underinitialized \ q_{ret}, \ \overline{p}: \overline{k_p} \ \overline{q_p}, \ \overline{y}: \overline{k_{local}} \ \overline{q_{local}}) \\ \Gamma &\vdash super(\overline{y}) \ in \ kd \quad \Gamma \vdash this.f = f \end{split}$$

(WF-CONS)

 $\vdash_{\mathsf{C}} \mathsf{kd} \mathsf{ is } \mathsf{OK}$

Note: $\vdash_{C \text{ kd}}$ reads "constructor kd in class C is well-formed".

 $\begin{array}{ll} mBody(md) = \stackrel{-}{s}; return \ \underline{z} \quad \underline{typeof(md)} = k_{this} \ q_{this}, \ \overline{k_p} \ \overline{q_p} \rightarrow t_{ret} \\ \Gamma = (this: k_{this} \ q_{this}, \ \overline{p}: \overline{k_p} \ \overline{q_p}, \ \overline{y}: \overline{k_{local}} \ \overline{q_{local}}) \quad \Gamma \vdash \overline{s} \quad \Gamma(z) <: t_{ret} \\ Standard \ method \ overriding \ rule \end{array}$

(WF-METH)

 $\vdash_{\mathsf{C}} \mathsf{md} \mathsf{ is } \mathsf{OK}$

Figure 4 Well-formdness typing

Extension to real Java

In real Java, there are static fields, static methods, initialization blocks.

Helper Method

usedQualifiers(s) returns all immutability qualifiers used in s recursively

fType(sfd) ≠ polymutable ∧ fType(sfd) ≠ receiverdependantmutable

(WF-STATIC-FLD)

F sfd is OK

 $\begin{array}{ll} mBody(smd) = \bar{s}; return \ z & typeof(smd) = \bar{k}_p \ \bar{q}_p \to t_{ret} \\ \bar{\Gamma} = (\bar{p}: \bar{k}_p \ \bar{q}_p, \ \bar{y}: \bar{k}_{local} \ \bar{q}_{local}) & \bar{\Gamma} \vdash \bar{s} & \bar{\Gamma}(z) <: t_{ret} \\ \bar{q}_p \neq receiver depend ant mutable \ \Lambda \ q_{ret} \neq receiver depend ant mutable \\ receiver depend ant mutable \ \notin \ used Qualifiers(\bar{s}; return \ z) \end{array}$

 \vdash smd is OK

 $\Gamma \vdash s$ receiverdependantmutable ∉ usedQualifiers(s) $\vdash sib is OK$ $\Gamma \vdash s$ $\vdash_{C} ib is OK$ $\vdash_{C} ib is OK$ $\vdash_{C} ib is OK \vdash_{C} kd is OK \vdash_{Smd} is OK \vdash_{C} md is OK$ $\vdash_{C} md is OK$

Inference of immutability qualifier for polymutable methods

After viewpoint adapting m() at the invocation site, if $q_{this-vp}$, \overline{q}_{p-vp} , q_{ret-vp} are NOT substitutable polymutable, standard subtyping rules apply:

$$q_{y} <: \ q_{\text{this-vp}} \qquad \qquad q_{z} <: \ q_{\text{p-vp}} \qquad \qquad q_{\text{ret-vp}} <: \ q_{x}$$

But if any of them is substitutable polymutable, we use a variable \mathbf{s} to replace corresponding $q_{\text{this-vp}}$, $q_{\text{p-vp}}$, $q_{\text{ret-vp}}$ and add it/them to constraints set. After collecting all the constraints, we try to find a solution \mathbf{s} that satisfies all the subtype constraints. If there is such a solution, then method invocation typechecks; Otherwise, it doesn't typecheck.

For example, assuming we have a method after viewpoint adaptation with signature: substitutable polymutable Object m(substitutable polymutable A this, substitutable polymutable Object p);

If we invoke it as:

immutable A a:

readonly Object ro = a.m(new immutable Object());

Constraints are collected in this way:

immutable <: s immutable <: s s <: readonly

We'll have a solution:

s = immutable(or readonly), so this method invocation typechecks.

But if we invoke the method as: