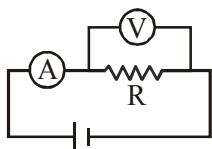


TEST PAPER OF JEE(MAIN) EXAMINATION – 2019**(Held On Thursday 10th JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM****PHYSICS**

1. Two forces P and Q of magnitude $2F$ and $3F$, respectively, are at an angle θ with each other. If the force Q is doubled, then their resultant also gets doubled. Then, the angle is :
- (1) 30° (2) 60° (3) 90° (4) 120°

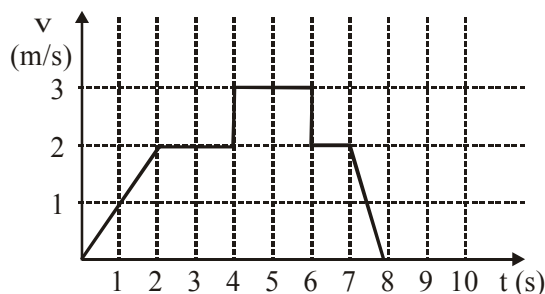
2. The actual value of resistance R, shown in the figure is 30Ω . This is measured in an experiment as shown using the standard formula $R = \frac{V}{I}$, where V and I are the readings of the voltmeter and ammeter, respectively. If the measured value of R is 5% less, then the internal resistance of the voltmeter is :



- (1) 350Ω (2) 570Ω (3) 35Ω (4) 600Ω

3. An unknown metal of mass 192 g heated to a temperature of 100°C was immersed into a brass calorimeter of mass 128 g containing 240 g of water a temperature of 8.4°C . Calculate the specific heat of the unknown metal if water temperature stabilizes at 21.5°C (Specific heat of brass is $394\text{ J kg}^{-1}\text{ K}^{-1}$)
- (1) $1232\text{ J kg}^{-1}\text{ K}^{-1}$ (2) $458\text{ J kg}^{-1}\text{ K}^{-1}$
 (3) $654\text{ J kg}^{-1}\text{ K}^{-1}$ (4) $916\text{ J kg}^{-1}\text{ K}^{-1}$

4. A particle starts from the origin at time $t = 0$ and moves along the positive x-axis. The graph of velocity with respect to time is shown in figure. What is the position of the particle at time $t = 5\text{ s}$?



- (1) 6 m (2) 9 m (3) 3 m (4) 10 m

5. The self induced emf of a coil is 25 volts . When the current in it is changed at uniform rate from 10 A to 25 A in 1 s , the change in the energy of the inductance is :

- (1) 437.5 J (2) 637.5 J
 (3) 740 J (4) 540 J

6. A current of 2 mA was passed through an unknown resistor which dissipated a power of 4.4 W . Dissipated power when an ideal power supply of 11 V is connected across it is :

- (1) $11 \times 10^{-5}\text{ W}$ (2) $11 \times 10^{-4}\text{ W}$
 (3) $11 \times 10^5\text{ W}$ (4) $11 \times 10^{-3}\text{ W}$

7. The diameter and height of a cylinder are measured by a meter scale to be 12.6 ± 0.1 cm and 34.2 ± 0.1 cm, respectively. What will be the value of its volume in appropriate significant figures ?
 (1) 4260 ± 80 cm³ (2) 4300 ± 80 cm³
 (3) 4264.4 ± 81.0 cm³ (4) 4264 ± 81 cm³
8. At some location on earth the horizontal component of earth's magnetic field is 18×10^{-6} T. At this location, magnetic needle of length 0.12 m and pole strength 1.8 Am is suspended from its mid-point using a thread, it makes 45° angle with horizontal in equilibrium. To keep this needle horizontal, the vertical force that should be applied at one of its ends is :
 (1) 3.6×10^{-5} N (2) 6.5×10^{-5} N
 (3) 1.3×10^{-5} N (4) 1.8×10^{-5} N
9. The modulation frequency of an AM radio station is 250 kHz, which is 10% of the carrier wave. If another AM station approaches you for license what broadcast frequency will you allot ?
 (1) 2750 kHz (2) 2000 kHz
 (3) 2250 kHz (4) 2900 kHz
10. A hoop and a solid cylinder of same mass and radius are made of a permanent magnetic material with their magnetic moment parallel to their respective axes. But the magnetic moment of hoop is twice of solid cylinder. They are placed in a uniform magnetic field in such a manner that their magnetic moments make a small angle with the field. If the oscillation periods of hoop and cylinder are T_h and T_c respectively, then :
 (1) $T_h = 0.5 T_c$ (2) $T_h = 2 T_c$
 (3) $T_h = 1.5 T_c$ (4) $T_h = T_c$
11. The electric field of a plane polarized electromagnetic wave in free space at time $t = 0$ is given by an expression

$$\vec{E}(x, y) = 10\hat{j} \cos [(6x + 8z)]$$
 The magnetic field \vec{B} (x, z, t) is given by : (c is the velocity of light)
 (1) $\frac{1}{c}(6\hat{k} + 8\hat{i})\cos[(6x - 8z + 10ct)]$
 (2) $\frac{1}{c}(6\hat{k} - 8\hat{i})\cos[(6x + 8z - 10ct)]$
 (3) $\frac{1}{c}(6\hat{k} + 8\hat{i})\cos[(6x + 8z - 10ct)]$
 (4) $\frac{1}{c}(6\hat{k} - 8\hat{i})\cos[(6x + 8z + 10ct)]$

12. Consider the nuclear fission

Given that the binding energy/nucleon of Ne^{20} , He^4 and C^{12} are, respectively, 8.03 MeV, 7.07 MeV and 7.86 MeV, identify the correct statement :

- (1) 8.3 MeV energy will be released
- (2) energy of 12.4 MeV will be supplied
- (3) energy of 11.9 MeV has to be supplied
- (4) energy of 3.6 MeV will be released

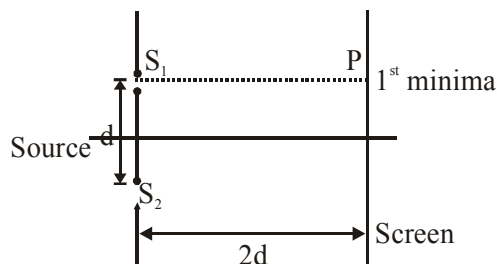
- 13.** Two vectors \vec{A} and \vec{B} have equal magnitudes. The magnitude of $(\vec{A} + \vec{B})$ is 'n' times the magnitude of $(\vec{A} - \vec{B})$. The angle between \vec{A} and \vec{B} is :

- (1) $\sin^{-1} \left[\frac{n^2 - 1}{n^2 + 1} \right]$ (2) $\cos^{-1} \left[\frac{n - 1}{n + 1} \right]$
(3) $\cos^{-1} \left[\frac{n^2 - 1}{n^2 + 1} \right]$ (4) $\sin^{-1} \left[\frac{n - 1}{n + 1} \right]$

- 14.** A particle executes simple harmonic motion with an amplitude of 5 cm. When the particle is at 4 cm from the mean position, the magnitude of its velocity in SI units is equal to that of its acceleration. Then, its periodic time in seconds is :

- (1) $\frac{7}{3}\pi$ (2) $\frac{3}{8}\pi$
(3) $\frac{4\pi}{3}$ (4) $\frac{8\pi}{3}$

15. Consider a Young's double slit experiment as shown in figure. What should be the slit separation d in terms of wavelength λ such that the first minima occurs directly in front of the slit (S_1) ?



- (1) $\frac{\lambda}{2(5-\sqrt{2})}$ (2) $\frac{\lambda}{(5-\sqrt{2})}$
 (3) $\frac{\lambda}{(\sqrt{5}-2)}$ (4) $\frac{\lambda}{2(\sqrt{5}-2)}$

16. The eye can be regarded as a single refracting surface. The radius of curvature of this surface is equal to that of cornea (7.8 mm). This surface separates two media of refractive indices 1 and 1.34. Calculate the distance from the refracting surface at which a parallel beam of light will come to focus.

- (1) 2 cm (2) 1 cm
 (3) 3.1 cm (4) 4.0 cm

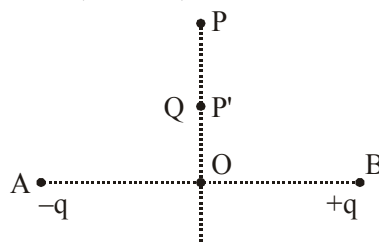
17. Half mole of an ideal monoatomic gas is heated at constant pressure of 1 atm from 20 °C to 90°C. Work done by gas is close to : (Gas constant $R = 8.31 \text{ J/mol.K}$)
 (1) 73 J (2) 291 J (3) 581 J (4) 146 J

18. A metal plate of area $1 \times 10^{-4} \text{ m}^2$ is illuminated by a radiation of intensity 16 mW/m^2 . The work function of the metal is 5 eV. The energy of the incident photons is 10 eV and only 10% of it produces photo electrons. The number of emitted photo electrons per second and their maximum energy, respectively, will be : [$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$]

- (1) 10^{10} and 5 eV (2) 10^{14} and 10 eV
 (3) 10^{12} and 5 eV (4) 10^{11} and 5 eV

19. Charges $-q$ and $+q$ located at A and B, respectively, constitute an electric dipole. Distance $AB = 2a$, O is the mid point of the dipole and OP is perpendicular to AB. A charge Q is placed at P where $OP = y$ and $y \gg 2a$. The charge Q experiences an electrostatic force F. If Q is now moved along the equatorial line

to P' such that $OP' = \left(\frac{y}{3}\right)$, the force on Q will be close to : $\left(\frac{y}{3} \gg 2a\right)$



- (1) $\frac{F}{3}$ (2) $3F$ (3) $9F$ (4) $27F$

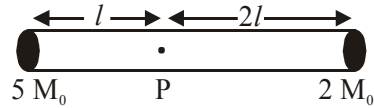
- 20.** Two stars of masses 3×10^{31} kg each, and at distance 2×10^{11} m rotate in a plane about their common centre of mass O. A meteorite passes through O moving perpendicular to the star's rotation plane. In order to escape from the gravitational field of this double star, the minimum speed that meteorite should have at O is : (Take Gravitational constant $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$)

- (1) $1.4 \times 10^5 \text{ m/s}$ (2) $24 \times 10^4 \text{ m/s}$
 (3) $3.8 \times 10^4 \text{ m/s}$ (4) $2.8 \times 10^5 \text{ m/s}$

- 21.** A closed organ pipe has a fundamental frequency of 1.5 kHz. The number of overtones that can be distinctly heard by a person with this organ pipe will be : (Assume that the highest frequency a person can hear is 20,000 Hz)

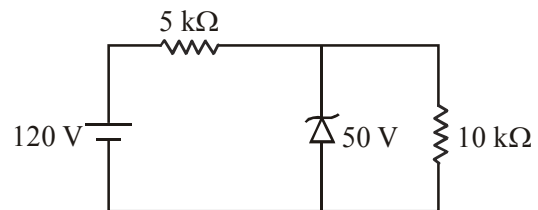
- (1) 7 (2) 5 (3) 6 (4) 4

- 22.** A rigid massless rod of length $3l$ has two masses attached at each end as shown in the figure. The rod is pivoted at point P on the horizontal axis (see figure). When released from initial horizontal position, its instantaneous angular acceleration will be :



- (1) $\frac{g}{2l}$ (2) $\frac{7g}{3l}$ (3) $\frac{g}{13l}$ (4) $\frac{g}{3l}$

- 23.** For the circuit shown below, the current through the Zener diode is :



- (1) 5 mA (2) Zero (3) 14 mA (4) 9 mA

- 24.** Four equal point charges Q each are placed in the xy plane at $(0, 2)$, $(4, 2)$, $(4, -2)$ and $(0, -2)$. The work required to put a fifth charge Q at the origin of the coordinate system will be :

(1) $\frac{Q^2}{2\sqrt{2}\pi\epsilon_0}$ (2) $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{5}}\right)$
 (3) $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{3}}\right)$ (4) $\frac{Q^2}{4\pi\epsilon_0}$

- 25.** A cylindrical plastic bottle of negligible mass is filled with 310 ml of water and left floating in a pond with still water. If pressed downward slightly and released, it starts performing simple harmonic motion at angular frequency ω . If the radius of the bottle is 2.5 cm then ω close to : (density of water = 10^3 kg / m^3)

(1) 5.00 rad s^{-1} (2) 1.25 rad s^{-1}
 (3) 3.75 rad s^{-1} (4) 2.50 rad s^{-1}

- 26.** A parallel plate capacitor having capacitance 12 pF is charged by a battery to a potential difference of 10 V between its plates. The charging battery is now disconnected and a porcelain slab of dielectric constant 6.5 is slipped between the plates the work done by the capacitor on the slab is :

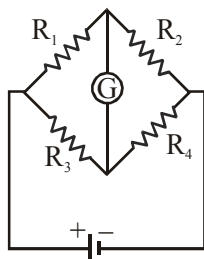
(1) 692 pJ (2) 60 pJ
 (3) 508 pJ (4) 560 pJ

- 27.** Two kg of a monoatomic gas is at a pressure of $4 \times 10^4 \text{ N/m}^2$. The density of the gas is 8 kg / m^3 . What is the order of energy of the gas due to its thermal motion ?

(1) 10^3 J (2) 10^5 J
 (3) 10^6 J (4) 10^4 J

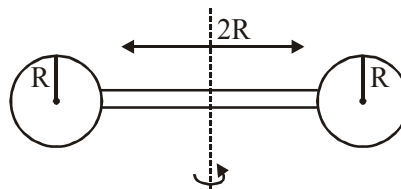
28. A particle which is experiencing a force, given by $\vec{F} = 3\vec{i} - 12\vec{j}$, undergoes a displacement of $\vec{d} = 4\vec{i}$. If the particle had a kinetic energy of 3 J at the beginning of the displacement, what is its kinetic energy at the end of the displacement ?
 (1) 15 J (2) 10 J (3) 12 J (4) 9 J

29. The Wheatstone bridge shown in Fig. here, gets balanced when the carbon resistor used as R_1 has the colour code (Orange, Red, Brown). The resistors R_2 and R_4 are 80Ω and 40Ω , respectively. Assuming that the colour code for the carbon resistors gives their accurate values, the colour code for the carbon resistor, used as R_3 , would be :



- (1) Red, Green, Brown
 (2) Brown, Blue, Brown
 (3) Grey, Black, Brown
 (4) Brown, Blue, Black

30. Two identical spherical balls of mass M and radius R each are stuck on two ends of a rod of length $2R$ and mass M (see figure). The moment of inertia of the system about the axis passing perpendicularly through the centre of the rod is :



- (1) $\frac{152}{15}MR^2$ (2) $\frac{17}{15}MR^2$
 (3) $\frac{137}{15}MR^2$ (4) $\frac{209}{15}MR^2$

TEST PAPER OF JEE(MAIN) EXAMINATION – 2019**(Held On Thursday 10th JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM****CHEMISTRY**

1. An ideal gas undergoes isothermal compression from 5 m³ against a constant external pressure of 4 Nm⁻². Heat released in this process is used to increase the temperature of 1 mole of Al. If molar heat capacity of Al is 24 J mol⁻¹ K⁻¹, the temperature of Al increases by :

(1) $\frac{3}{2}$ K (2) $\frac{2}{3}$ K (3) 1 K (4) 2 K

2. The 71st electron of an element X with an atomic number of 71 enters into the orbital :
(1) 4f (2) 6p (3) 6s (4) 5d

3. The number of 2-centre-2-electron and 3-centre-2-electron bonds in B₂H₆, respectively, are :
(1) 2 and 4 (2) 2 and 1
(3) 2 and 2 (4) 4 and 2

4. The amount of sugar (C₁₂H₂₂O₁₁) required to prepare 2 L of its 0.1 M aqueous solution is :
(1) 68.4 g (2) 17.1 g (3) 34.2 g (4) 136.8 g

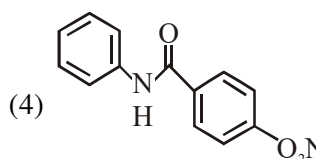
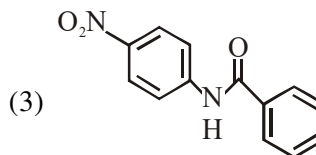
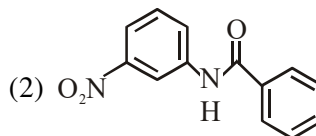
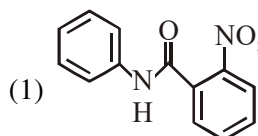
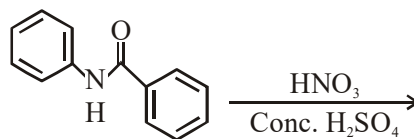
5. Among the following reactions of hydrogen with halogens, the one that requires a catalyst is :

(1) $\text{H}_2 + \text{I}_2 \rightarrow 2\text{HI}$ (2) $\text{H}_2 + \text{F}_2 \rightarrow 2\text{HF}$
(3) $\text{H}_2 + \text{Cl}_2 \rightarrow 2\text{HCl}$ (4) $\text{H}_2 + \text{Br}_2 \rightarrow 2\text{HBr}$

6. Sodium metal on dissolution in liquid ammonia gives a deep blue solution due to the formation of:

(1) sodium ion-ammonia complex
(2) sodamide
(3) sodium-ammonia complex
(4) ammoniated electrons

7. What will be the major product in the following mononitration reaction ?

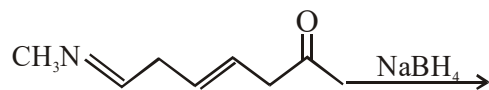


8. In the cell $\text{Pt(s)}|\text{H}_2(\text{g}, 1\text{bar})|\text{HCl(aq)}|\text{Ag(s)}|\text{Pt(s)}$ the cell potential is 0.92 when a 10^{-6} molal HCl solution is used. The standard electrode potential of $(\text{AgCl}/\text{Ag}, \text{Cl}^-)$ electrode is :

$$\left\{ \text{given, } \frac{2.303RT}{F} = 0.06\text{V at } 298\text{K} \right\}$$

- (1) 0.20 V (2) 0.76 V (3) 0.40 V (4) 0.94 V

9. The major product of the following reaction is:

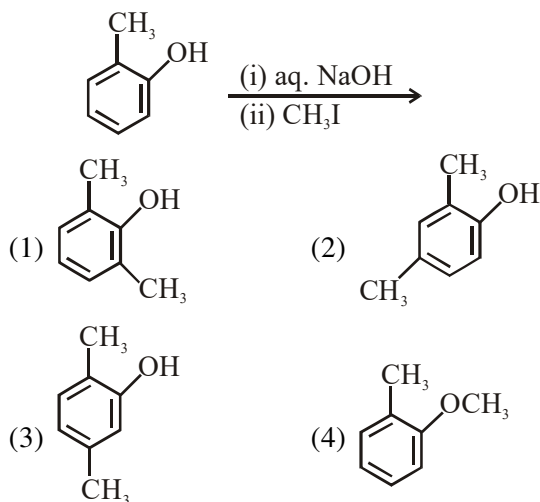


- (1) $\text{CH}_3\text{N}=\text{CH}-\text{CH}_2-\text{CH}=\text{CH}-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$
 (2) $\text{CH}_3\text{N}=\text{CH}-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$
 (3) $\text{CH}_3\text{N}-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}=\text{CH}-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$
 (4) $\text{CH}_3\text{N}-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$

10. The pair that contains two P-H bonds in each of the oxoacids is :

- (1) H_3PO_2 and $\text{H}_4\text{P}_2\text{O}_5$
 (2) $\text{H}_4\text{P}_2\text{O}_5$ and $\text{H}_4\text{P}_2\text{O}_6$
 (3) H_3PO_3 and H_3PO_2
 (4) $\text{H}_4\text{P}_2\text{O}_5$ and H_3PO_3

11. The major product of the following reaction is:



12. The difference in the number of unpaired electrons of a metal ion in its high-spin and low-spin octahedral complexes is two. The metal ion is :

- (1) Fe^{2+} (2) Co^{2+} (3) Mn^{2+} (4) Ni^{2+}

13. A compound of formula A_2B_3 has the hcp lattice. Which atom forms the hcp lattice and what fraction of tetrahedral voids is occupied by the other atoms :

- (1) hcp lattice-A, $\frac{2}{3}$ Tetrahedral voids-B
 (2) hcp lattice-B, $\frac{1}{3}$ Tetrahedral voids-A
 (3) hcp lattice-B, $\frac{2}{3}$ Tetrahedral voids-A
 (4) hcp lattice-A $\frac{1}{3}$ Tetrahedral voids-B

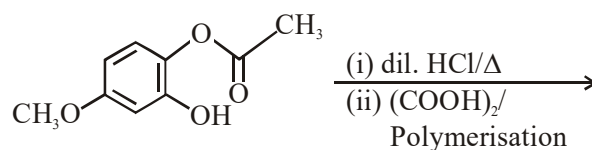
- 14.** The reaction that is NOT involved in the ozone layer depletion mechanism in the stratosphere is:

- (1) $\text{HOCl(g)} \xrightarrow{h\nu} \dot{\text{O}}\text{H(g)} + \dot{\text{Cl}}\text{(g)}$
- (2) $\text{CF}_2\text{Cl}_2\text{(g)} \xrightarrow{uv} \dot{\text{Cl}}\text{(g)} + \dot{\text{CF}}_2\text{Cl(g)}$
- (3) $\text{CH}_4 + 2\text{O}_3 \rightarrow 3\text{CH}_2=\text{O} + 3\text{H}_2\text{O}$
- (4) $\text{Cl}\dot{\text{O}}\text{(g)} + \text{O(g)} \rightarrow \dot{\text{Cl}}\text{(g)} + \text{O}_2\text{(g)}$

- 15.** The process with negative entropy change is :

- (1) Dissolution of iodine in water
- (2) Synthesis of ammonia from N_2 and H_2
- (3) Dissolution of $\text{CaSO}_4\text{(s)}$ to CaO(s) and $\text{SO}_3\text{(g)}$
- (4) Sublimation of dry ice

- 16.** The major product of the following reaction is:

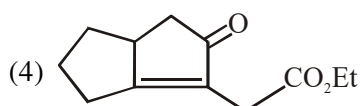
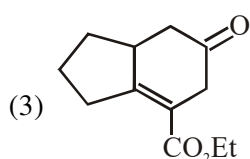
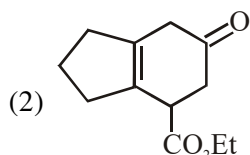
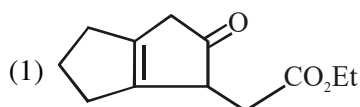
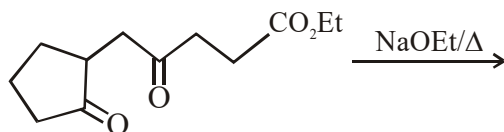


- (1)
- (2)
- (3)
- (4)

- 17.** A reaction of cobalt(III) chloride and ethylenediamine in a 1 : 2 mole ratio generates two isomeric products A (violet coloured) B (green coloured). A can show optical activity, B is optically inactive. What type of isomers does A and B represent ?

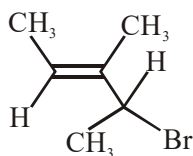
- (1) Geometrical isomers
- (2) Ionisation isomers]
- (3) Coordination isomers
- (4) Linkage isomers

18. The major product obtained in the following reaction is :



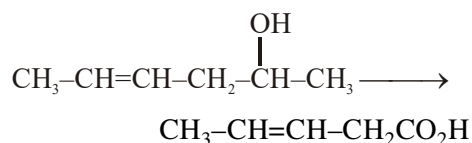
19. Which of the following tests cannot be used for identifying amino acids ?
 (1) Biuret test (2) Xanthoproteic test
 (3) Barfoed test (4) Ninhydrin test

20. What is the IUPAC name of the following compound ?



- (1) 3-Bromo-1, 2-dimethylbut-1-ene]
 (2) 4-Bromo-3-methylpent-2-ene
 (3) 2-Bromo-3-methylpent-3-ene
 (4) 3-Bromo-3-methyl-1, 2-dimethylprop-1-ene

21. Which is the most suitable reagent for the following transformation ?



- (1) alkaline KMnO₄ (2) I₂/NaOH
 (3) Tollen's reagent (4) CrO₂/CS₂

22. The correct match between item 'I' and item 'II' is :

Item 'I' (compound)	Item 'II' (reagent)
(A) Lysine	(P) 1-naphthol
(B) Furfural	(Q) ninhydrin
(C) Benzyl alcohol	(R) KMnO ₄
(D) Styrene	(S) Ceric ammonium nitrate

- (1) (A)→(Q), (B)→(P), (C)→(S), (D)→(R)
 (2) (A)→(Q), (B)→(R), (C)→(S), (D)→(P)
 (3) (A)→(Q), (B)→(P), (C)→(R), (D)→(S)
 (4) (A)→(R), (B)→(P), (C)→(Q), (D)→(S)

23. In the reaction of oxalate with permanganate in acidic medium, the number of electrons involved in producing one molecule of CO₂ is :

- (1) 10 (2) 2 (3) 1 (4) 5

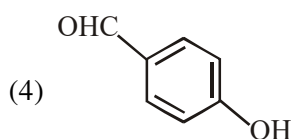
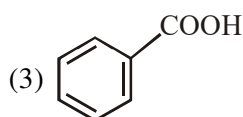
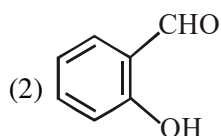
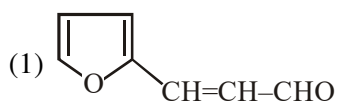
24. 5.1g NH₄SH is introduced in 3.0 L evacuated flask at 327°C. 30% of the solid NH₄SH decomposed to NH₃ and H₂S as gases. The K_p of the reaction at 327°C is (R = 0.082 L atm mol⁻¹K⁻¹, Molar mass of S = 32 g mol⁻¹, molar mass of N = 14g mol⁻¹)

- (1) 1 × 10⁻⁴ atm² (2) 4.9 × 10⁻³ atm²
 (3) 0.242 atm² (4) 0.242 × 10⁻⁴ atm²

25. The electrolytes usually used in the electroplating of gold and silver, respectively, are :
 (1) $[\text{Au}(\text{OH})_4]^-$ and $[\text{Ag}(\text{OH})_2]^-$
 (2) $[\text{Au}(\text{CN})_2]^-$ and $[\text{Ag} \text{Cl}_2]^-$
 (3) $[\text{Au}(\text{NH}_3)_2]^+$ and $[\text{Ag}(\text{CN})_2]^-$
 (4) $[\text{Au}(\text{CN})_2]^-$ and $[\text{Ag}(\text{CN})_2]^-$

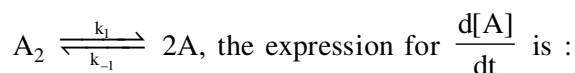
26. Elevation in the boiling point for 1 molal solution of glucose is 2 K. The depression in the freezing point of 2 molal solutions of glucose in the same solvent is 2 K. The relation between K_b and K_f is:
 (1) $K_b = 0.5 K_f$ (2) $K_b = 2 K_f$
 (3) $K_b = 1.5 K_f$ (4) $K_b = K_f$

27. An aromatic compound 'A' having molecular formula $\text{C}_7\text{H}_6\text{O}_2$ on treating with aqueous ammonia and heating forms compound 'B'. The compound 'B' on reaction with molecular bromine and potassium hydroxide provides compound 'C' having molecular formula $\text{C}_6\text{H}_7\text{N}$. The structure of 'A' is :



28. The ground state energy of hydrogen atom is -13.6 eV . The energy of second excited state He^+ ion in eV is :
 (1) -6.04 (2) -27.2 (3) -54.4 (4) -3.4

29. For an elementary chemical reaction,



- (1) $2k_1[\text{A}_2] - k_{-1}[\text{A}]^2$ (2) $k_1[\text{A}_2] - k_{-1}[\text{A}]^2$
 (3) $2k_1[\text{A}_2] - 2k_{-1}[\text{A}]^2$ (4) $k_1[\text{A}_2] + k_{-1}[\text{A}]^2$

30. Haemoglobin and gold sol are examples of :
 (1) negatively charged sols
 (2) positively charged sols
 (3) negatively and positively charged sols, respectively
 (4) positively and negatively charged sols, respectively

TEST PAPER OF JEE(MAIN) EXAMINATION – 2019**(Held On Thursday 10th JANUARY, 2019) TIME : 2 : 30 PM To 5 : 30 PM****MATHEMATICS**

1. Let $z = \left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^5 + \left(\frac{\sqrt{3}}{2} - \frac{i}{2}\right)^5$. If $R(z)$ and $I[z]$

respectively denote the real and imaginary parts of z , then :

- (1) $R(z) > 0$ and $I(z) > 0$
 (2) $R(z) < 0$ and $I(z) > 0$
 (3) $R(z) = -3$
 (4) $I(z) = 0$

2. Let $a_1, a_2, a_3, \dots, a_{10}$ be in G.P. with $a_i > 0$ for $i = 1, 2, \dots, 10$ and S be the set of pairs (r, k) , $r, k \in \mathbb{N}$ (the set of natural numbers) for which

$$\begin{vmatrix} \log_e a_1^r a_2^k & \log_e a_2^r a_3^k & \log_e a_3^r a_4^k \\ \log_e a_4^r a_5^k & \log_e a_5^r a_6^k & \log_e a_6^r a_7^k \\ \log_e a_7^r a_8^k & \log_e a_8^r a_9^k & \log_e a_9^r a_{10}^k \end{vmatrix} = 0$$

Then the number of elements in S , is :

- (1) Infinitely many (2) 4
 (3) 10 (4) 2

3. The positive value of λ for which the co-efficient of x^2 in the expression

$$x^2 \left(\sqrt{x} + \frac{\lambda}{x^2} \right)^{10} \text{ is } 720, \text{ is :}$$

- (1) $\sqrt{5}$ (2) 4
 (3) $2\sqrt{2}$ (4) 3

4. The value of $\cos \frac{\pi}{2^2} \cdot \cos \frac{\pi}{2^3} \cdot \dots \cdot \cos \frac{\pi}{2^{10}} \cdot \sin \frac{\pi}{2^{10}}$ is :

- (1) $\frac{1}{256}$ (2) $\frac{1}{2}$
 (3) $\frac{1}{512}$ (4) $\frac{1}{1024}$

5. The value of $\int_{-\pi/2}^{\pi/2} \frac{dx}{[x] + [\sin x] + 4}$, where $[t]$

denotes the greatest integer less than or equal to t , is :

(1) $\frac{1}{12}(7\pi + 5)$ (2) $\frac{3}{10}(4\pi - 3)$

(3) $\frac{1}{12}(7\pi - 5)$ (4) $\frac{3}{20}(4\pi - 3)$

6. If the probability of hitting a target by a shooter, in any shot, is $1/3$, then the minimum number of independent shots at the target required by him so that the probability of hitting the target

at least once is greater than $\frac{5}{6}$, is :

- (1) 6 (2) 5
(3) 4 (4) 3

7. If mean and standard deviation of 5 observations x_1, x_2, x_3, x_4, x_5 are 10 and 3, respectively, then the variance of 6 observations x_1, x_2, \dots, x_5 and -50 is equal to :

- (1) 582.5 (2) 507.5
(3) 586.5 (4) 509.5

8. The length of the chord of the parabola $x^2 = 4y$ having equation $x - \sqrt{2}y + 4\sqrt{2} = 0$ is :

- (1) $2\sqrt{11}$ (2) $3\sqrt{2}$
(3) $6\sqrt{3}$ (4) $8\sqrt{2}$

9. Let $A = \begin{bmatrix} 2 & b & 1 \\ b & b^2 + 1 & b \\ 1 & b & 2 \end{bmatrix}$ where $b > 0$. Then the

minimum value of $\frac{\det(A)}{b}$ is :

- (1) $\sqrt{3}$ (2) $-\sqrt{3}$
 (3) $-2\sqrt{3}$ (4) $2\sqrt{3}$

10. The tangent to the curve, $y = xe^{x^2}$ passing through the point (1,e) also passes through the point :

- (1) $\left(\frac{4}{3}, 2e\right)$ (2) (2,3e)
 (3) $\left(\frac{5}{3}, 2e\right)$ (4) (3,6e)

11. The number of values of $\theta \in (0, \pi)$ for which the system of linear equations

$$x + 3y + 7z = 0$$

$$-x + 4y + 7z = 0$$

$$(\sin 3\theta)x + (\cos 2\theta)y + 2z = 0$$

has a non-trivial solution, is :

- (1) One (2) Three
 (3) Four (4) Two

12. If $\int_0^x f(t)dt = x^2 + \int_x^1 t^2 f(t)dt$, then $f'(1/2)$ is :

- (1) $\frac{6}{25}$ (2) $\frac{24}{25}$
 (3) $\frac{18}{25}$ (4) $\frac{4}{5}$

13. Let $f : (-1,1) \rightarrow \mathbb{R}$ be a function defined by $f(x) = \max\{-|x|, -\sqrt{1-x^2}\}$. If K be the set of all points at which f is not differentiable, then K has exactly :

- (1) Three elements (2) One element
 (3) Five elements (4) Two elements

14. Let $S = \left\{ (x,y) \in \mathbb{R}^2 : \frac{y^2}{1+r} - \frac{x^2}{1-r} = 1 \right\}$, where $r \neq \pm 1$. Then S represents :

- (1) A hyperbola whose eccentricity is $\frac{2}{\sqrt{r+1}}$,
 where $0 < r < 1$.
 (2) An ellipse whose eccentricity is $\frac{1}{\sqrt{r+1}}$,
 where $r > 1$
 (3) A hyperbola whose eccentricity is $\frac{2}{\sqrt{1-r}}$,
 when $0 < r < 1$.
 (4) An ellipse whose eccentricity is $\sqrt{\frac{2}{r+1}}$,
 when $r > 1$

- # E

- 19.** Two sides of a parallelogram are along the lines, $x + y = 3$ and $x - y + 3 = 0$. If its diagonals intersect at (2,4), then one of its vertex is :
- (1) (2,6) (2) (2,1)
 (3) (3,5) (4) (3,6)

- 20.** Let $\vec{\alpha} = (\lambda - 2)\vec{a} + \vec{b}$ and $\vec{\beta} = (4\lambda - 2)\vec{a} + 3\vec{b}$ be two given vectors where vectors \vec{a} and \vec{b} are non-collinear. The value of λ for which vectors $\vec{\alpha}$ and $\vec{\beta}$ are collinear, is :

- (1) -3 (2) 4
 (3) 3 (4) -4

- 21.** The value of $\cot\left(\sum_{n=1}^{19} \cot^{-1}\left(1 + \sum_{p=1}^n 2p\right)\right)$ is :

- (1) $\frac{22}{23}$ (2) $\frac{23}{22}$ (3) $\frac{21}{19}$ (4) $\frac{19}{21}$

- 22.** With the usual notation, in ΔABC , if $\angle A + \angle B = 120^\circ$, $a = \sqrt{3} + 1$ and $b = \sqrt{3} - 1$, then the ratio $\angle A : \angle B$, is :
- (1) 7 : 1 (2) 5 : 3
 (3) 9 : 7 (4) 3 : 1

- 23.** The plane which bisects the line segment joining the points $(-3, -3, 4)$ and $(3, 7, 6)$ at right angles, passes through which one of the following points ?
- (1) $(4, -1, 7)$ (2) $(4, 1, -2)$
 (3) $(-2, 3, 5)$ (4) $(2, 1, 3)$

- 24.** Consider the following three statements :
 P : 5 is a prime number.
 Q : 7 is a factor of 192.
 R : L.C.M. of 5 and 7 is 35.
 Then the truth value of which one of the following statements is true ?
- (1) $(P \wedge Q) \vee (\sim R)$
 (2) $(\sim P) \wedge (\sim Q \wedge R)$
 (3) $(\sim P) \vee (Q \wedge R)$
 (4) $P \vee (\sim Q \wedge R)$
- 25.** On which of the following lines lies the point of intersection of the line, $\frac{x-4}{2} = \frac{y-5}{2} = \frac{z-3}{1}$ and the plane, $x + y + z = 2$?
- (1) $\frac{x-2}{2} = \frac{y-3}{2} = \frac{z+3}{3}$
 (2) $\frac{x-4}{1} = \frac{y-5}{1} = \frac{z-5}{-1}$
 (3) $\frac{x-1}{1} = \frac{y-3}{2} = \frac{z+4}{-5}$
 (4) $\frac{x+3}{3} = \frac{4-y}{3} = \frac{z+1}{-2}$

26. Let f be a differentiable function such that

$$f'(x) = 7 - \frac{3f(x)}{4x}, (x > 0) \text{ and } f(1) \neq 4.$$

Then $\lim_{x \rightarrow 0^+} xf\left(\frac{1}{x}\right)$:

- (1) Exists and equals 4
- (2) Does not exist
- (3) Exist and equals 0
- (4) Exists and equals $\frac{4}{7}$

27. A helicopter is flying along the curve given by $y - x^{3/2} = 7$, ($x \geq 0$). A soldier positioned at the

point $\left(\frac{1}{2}, 7\right)$ wants to shoot down the helicopter

when it is nearest to him. Then this nearest distance is :

- (1) $\frac{1}{2}$
- (2) $\frac{1}{3}\sqrt{\frac{7}{3}}$
- (3) $\frac{1}{6}\sqrt{\frac{7}{3}}$
- (4) $\frac{\sqrt{5}}{6}$

28. If $\int x^5 e^{-4x^3} dx = \frac{1}{48} e^{-4x^3} f(x) + C$, where C is a constant of integration, then $f(x)$ is equal to :

- | | |
|-----------------|-----------------|
| (1) $-4x^3 - 1$ | (2) $4x^3 + 1$ |
| (3) $-2x^3 - 1$ | (4) $-2x^3 + 1$ |

29. The curve amongst the family of curves, represented by the differential equation, $(x^2 - y^2)dx + 2xy dy = 0$ which passes through $(1,1)$ is :

- (1) A circle with centre on the y-axis
- (2) A circle with centre on the x-axis
- (3) An ellipse with major axis along the y-axis
- (4) A hyperbola with transverse axis along the x-axis

30. If the area of an equilateral triangle inscribed in the circle, $x^2 + y^2 + 10x + 12y + c = 0$ is $27\sqrt{3}$ sq. units then c is equal to :

(1) 20

(2) 25

(3) 13

(4) -25