Jee Advanced 2019 Paper 2

PHYSICS – JEE ADVANCED PAPER – 2

SECTION - 1

1. Consider two plane convex lens of same radius of curvature and refractive index n_1 and n_2 respectively. Now consider two cases:



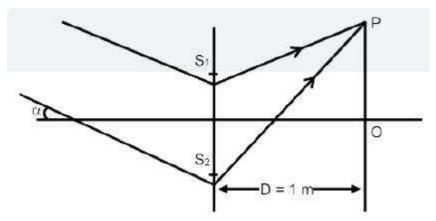
Case – I: When n_1 = n_2 = n, then equivalent focal length of lens is f_0

Case – II: When n_1 = n, n_2 = n + Δn , then equivalent focal length of lens is $f = f_0 + \Delta f_0$

Then correct options are:

- (a) If $\Delta n/n > 0$, then $\Delta f_0/f_0 < 0$
- (b) $|\Delta f_0/f_0| < |\Delta n/n|$
- (c) If n = 1.5, Δn = $10^{\text{-}3}$ and f_0 = 20 cm then $|\Delta f_0|$ = 0.02 cm

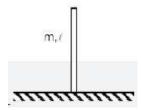
2. In YDSE monochromatic light of wavelength 600 nm incident of slits as shown in figure.



If $S_1S_2 = 3$ mm, OP = 11 mm then

- (a) If $\alpha = \frac{0.36}{\pi}$ degree then destructive interfaces at point P.
- (b) If $\alpha = \frac{0.36}{\pi}$ degree then constructive interfaces at point O.
- (c) If $\alpha = 0$ then constructive interfaces at O
- (d) Fringe width depends an $\boldsymbol{\alpha}$

3. A uniform rigid rod of mass m & length 1 is released from vertical position on rough surface with sufficient friction for lower end not to slip as shown in figure. When rod makes angle 60° with vertical then find correct alternative/s



(a)
$$\alpha = \frac{2g}{f}$$

(a)
$$\alpha = \frac{2g}{\ell}$$
 (b) $\omega = \sqrt{\frac{3g}{2\ell}}$

(d)
$$a_{radial} = \frac{3g}{4}$$

4. Monoatomic gas A having 5 mole is mixed with diatomic gas B having 1 mole in container of volume V_0 . Now the volume of mixture is compressed to $\frac{V_0}{4}$ by adiabatic process. Initial pressure and temperature of gas mixture is P_0 and T_0 . [given $2^{3.2} = 9.2$]

Choose correct option:

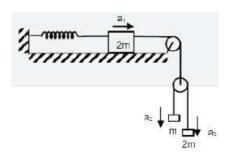
(a) $\gamma_{mix} = 1.6$

(b) Final pressure is between $9P_0$ and $10P_0$

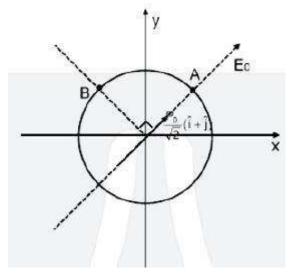
(c) $|W.D| = 13RT_0$

(d) Average Translational kinetic energy

5. The given arrangement is released from rest when spring is in natural length. Maximum extension in spring during the motion is x_0 . a_1 , a_2 and a_3 are accelerations of the blocks. Make the correct options



- (a) $a_2 a_1 = a_1 a_3$
- (b) $x_0 = \frac{4mg}{3k}$
- (c) Velocity of 2m connected to spring when elongation is $\frac{x_0}{2}$ is $v = \frac{x_0}{2} \sqrt{\frac{3k}{14m}}$
- (d) Acceleration a_1 at $\frac{x_0}{4}$ is $\frac{3kx_0}{42m}$
- 6. A dipole of Dipole moment $p = \frac{p_0}{\sqrt{2}}(\hat{i} + \hat{j})$. is placed at origin. Now a uniform external electric field at magnitude E_0 is applied along direction of dipole. Two points A and B are lying on a equipotential surface of radius R centered at origin. A is along axial position of dipole and B is along equatorial position. There correct option are:

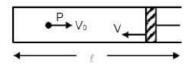


- (a) Net electric field at point A is $3E_0$
- (b) Net electric field at point B is Zero

(c) Radius of equatorial surface $R = \left(\frac{kp_0}{E_0}\right)^{1/3}$ (d) Radius of equatorial surface $R = \left(\frac{\sqrt{2}kp_0}{E_0}\right)^{1/3}$

- 7. A free hydrogen atom after absorbing a photon of wavelength λ_a gets excited from state n=1 to n=4. Immediately after electron jumps to n=m state by emitting a photon of wavelength λ_e . Let change in momentum of atom due to the absorption and the emission are ΔP_a and Δp_e respectively. If $\lambda_a / \lambda_e = 1/5$. Which of the following is correct
 - (a) m = 2
 - (b) $\Delta P_a/P_e = 1/2$
 - (c) $\lambda_e = 418 \text{ nm}$
 - (d) Ratio of K.E. of electron in the state n = m to n = 1 is $\frac{1}{4}$.

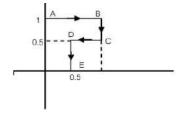
8. In a cylinder a heavy piston is moving with speed v as shown diagram and gas is filled inside it. A gas molecule is moving with speed v_0 towards moving piston. Then which of the following is correct (Assume v <<<< v_0 $\frac{\Delta \ell}{\ell}$) and collision is elastic)



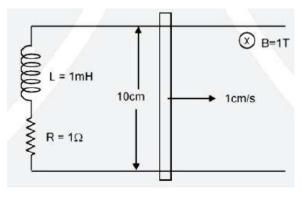
- (a) change in speed after collision is 2V
- (b) change is speed after collision is $2v_0 \frac{\Delta \ell}{\ell}$
- (c) rate of collision is $\frac{V}{\ell}$
- (d) When piston is at $\frac{\ell}{2}$ its kinetic energy will be four times

$\underline{SECTION-2}$

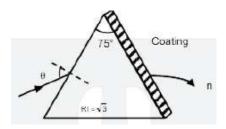
9. If $f = \alpha y \hat{i} + 2\alpha x \hat{j}$ calculate the work done if a particle moves along path as shown in diagram.



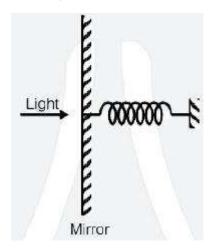
10. In a given circuit inductor of L = 1mH and resistance R = 1Ω are connected in series to ends of two parallel conducting rods as shown. Now a rod of length 10 cm is moved with constant velocity of 1 cm/s in magnetic field B = 1T. If rod starts moving at t = 0 then current in circuit after 1 millisecond is $x \times 10^{-3} A$. Then value of x is: (given $e^{-1} = 0.37$)



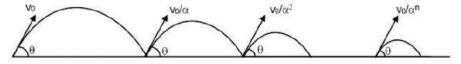
11. A prism is shown in the figure with prism angle 75° and refractive index $\sqrt{3}$. A light ray incidents on a surface at incident angle θ . Other face is coated with a medium of refractive index n. For $\theta \le 60^{\circ}$ ray suffers total internal reflection find value of n^2 .



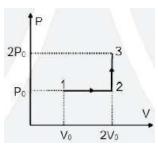
12. Perfectly reflecting mirror of mass M mounted on a spring constitute a spring mass system of angular frequency Ω such that $\frac{4\pi M\Omega}{h} = 10^{24} m^{-2}$ where h is plank constant. N photons of wavelength $\lambda = 8\pi \times 10^{-6}$ m strikes the mirror simultaneously at normal incidence such that the mirror gets displaced by 1 μ m. If the value of N is $x \times 10^{12}$, then find the value of x.



13. A particle is projected with speed v_0 at an angle θ ($\theta \neq 90^{\circ}$) with horizontal and it bounce at same angle with horizontal. If average velocity of journey is $0.8 v_0$ where v_0 is average velocity of first projectile then α is.



15. The sample of monoatomic gas undergoes a process as represented by P - V graph (if $P_0V_0 = 1/3 RT_0$) then



(P)
$$W_{1\to 2} = 1/3RT_0$$

(P)
$$W_{1\to2} = 1/3RT_0$$
 (Q) $Q_{1\to2\to3} = 11/6RT_0$ (R) $U_{1\to2} = RT_0/2$ (S) $W_{1\to2\to3} = 1/3RT_0$

(S)
$$W_{1\to 2\to 3} = 1/3RT_0$$

Which of the following options are correct

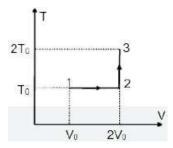
(a) P, Q, R, S are correct

(b) Only P, Q are correct

(c) Only R, S are correct

(d) Only P, R, S correct

16. A sample of monoatomic gas undergoes a process as represented by T - V graph (if $P_0V_0 = 1/3$ RT₀) then



(P) $W_{1\to 2} = \frac{1}{3} R T_0 \ell n 2$

(Q) $Q_{1\to 2\to 3} = \frac{RT_0}{6} (2\ell n(2) + 3)$

(R) $U_{1\to 2} = 0$

(S) $W_{1\to 2\to 3} = \frac{RT_0}{3} \ell n2$

Which of the following option are correct:

- (a) P, Q are incorrect
- (b) R, S are incorrect
- (c) P, Q, S are incorrect (d) none of these

- 17. Length of string of a musical instrument is varied from L_o to $2L_o$ in 4 different cases. Wire is made of different materials of mass per unit length μ , 2μ , 3μ , 4μ respectively. For first case (string 1) length is L_o , Tension is T_o then fundamental frequency is f_o , for second case length of the string is $\frac{3L_o}{2}$ (3rd Harmonic), for third case length of the string is $\frac{5L_o}{4}$ (5th Harmonic) and for the fourth case length of the string is $\frac{7L_o}{4}$ (14th harmonic). If frequency of all is same then tension in strings in terms of T_o will be:
 - (a) String 1

(P) T_o

(b) String – 2

(Q) $\frac{T_o}{\sqrt{2}}$

(c) String – 3

(R) $\frac{T_o}{2}$

(d) String – 4

- (S) $\frac{T_o}{16}$
- (T) $\frac{3T_o}{16}$

SECTION - 3

- 18. The free length of all four string is varied from L_0 to $2L_0$. Find the maximum fundamental frequency of 1, 2, 3, 4 in terms of f_0 (tension is same in all strings)
 - (a) String 1

(P) 1

(b) String – 2

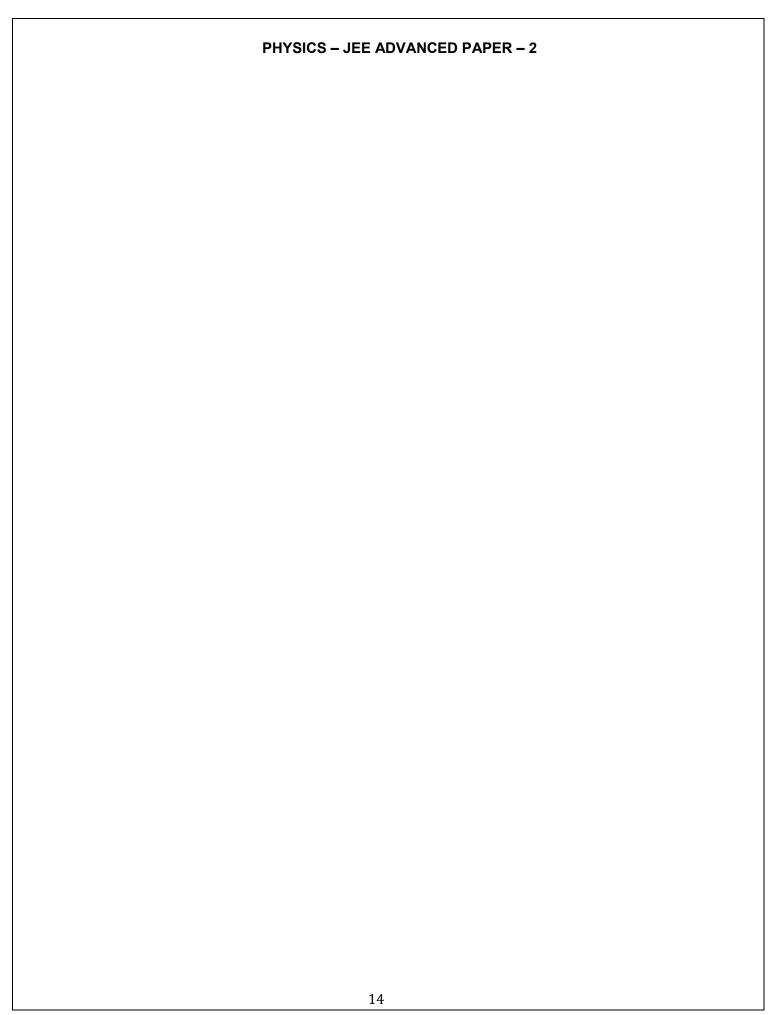
(Q) $\frac{1}{2}$

(c) String – 3

 $(R) \ \frac{1}{\sqrt{2}}$

(d) String – 4

- (S) $\frac{1}{\sqrt{3}}$
- (T) $\frac{1}{16}$
- (U) $\frac{3}{16}$



SECTION - 1

1. With reference to aqua regia, choose the correct option(s):

(a) Aqua regia is prepared by mixing conc. HCl and conc. HNO₃ in 3: 1 molar ratio.

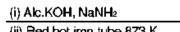
(b) Reaction of gold with aqua regia produces an anion having Au in +3 oxidation state.

(c) Reaction of gold with aqua regia produces NO2 in the absence of air

(d) The yellow colour of aqua regia is due to the presence of NOCl & Cl₂.

2. Choose the correct option that gives aromatic compound as major product:

$$CH_3$$
 Br
 Br



3. Which of the following reaction produce propane as major product?

$$(c) \ \ \text{H}_3C \xrightarrow{\qquad CI \qquad \underline{\text{Zn. dil}} \text{HCl.}} \ \ \underline{\text{Zn. trig. HCl.}}$$

$$(d) \begin{picture}(20,0) \put(0,0){\line(1,0){100}} \put(0,0){\line(1,0)$$

- 4. Which of the following is/are correct
 - (a) Teflon is formed by polymerization of tetrafluoroethene.
 - (b) Natural rubber is the trans from of polyisoprene.
 - (c) Cellulose contains only $\alpha\text{-D-glucose}$ linkage
 - (d) Nylon-6 contains amide linkage.

5.

$$\begin{array}{c} C \equiv C - CH_2 - CH = O \\ \hline \\ O \\ O \\ O \\ \end{array}$$

$$\begin{array}{c} (1) \ HgSO_4 / dilH_2SO_4 \\ \hline \\ (2) \ AgNO_3 \ NH_4OH \\ \hline \\ (3) \ ZnHg/HCI \\ \end{array}$$

$$\begin{array}{c} (1) \ SOCI_2 / Py \\ \hline \\ (2) \ AlCI_3 \\ \hline \\ (2) \ AlCI_3 \\ \end{array}$$

$$\begin{array}{c} ZnHg/HCI \\ \hline \\ SOMe \\ \end{array}$$

$$\begin{array}{c} C \\ O \\ O \\ \end{array}$$

$$R = \underbrace{\text{MeO}}_{\text{(b)}}, \quad S = \underbrace{\text{MeO}}_{\text{MeO}}, \quad S = \underbrace{\text{MeO}}_{\text{(c)}}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}, \quad S = \underbrace{\text{MeO}}_{\text{(d)}}, \quad S = \underbrace{\text{MeO}}_{\text{(d$$

6. Consider the following reaction (unbalanced)

Zn + Hot conc.
$$H_2SO_4 \rightarrow G + R + X$$

$$Zn + conc.$$
 $NaOH \rightarrow T + Q$

$$G + H_2S + NH_3$$
 $(aq) \rightarrow Z$ (precipitate) + X + Y

Choose the correct option(s)

(a) R is a V-shaped molecule

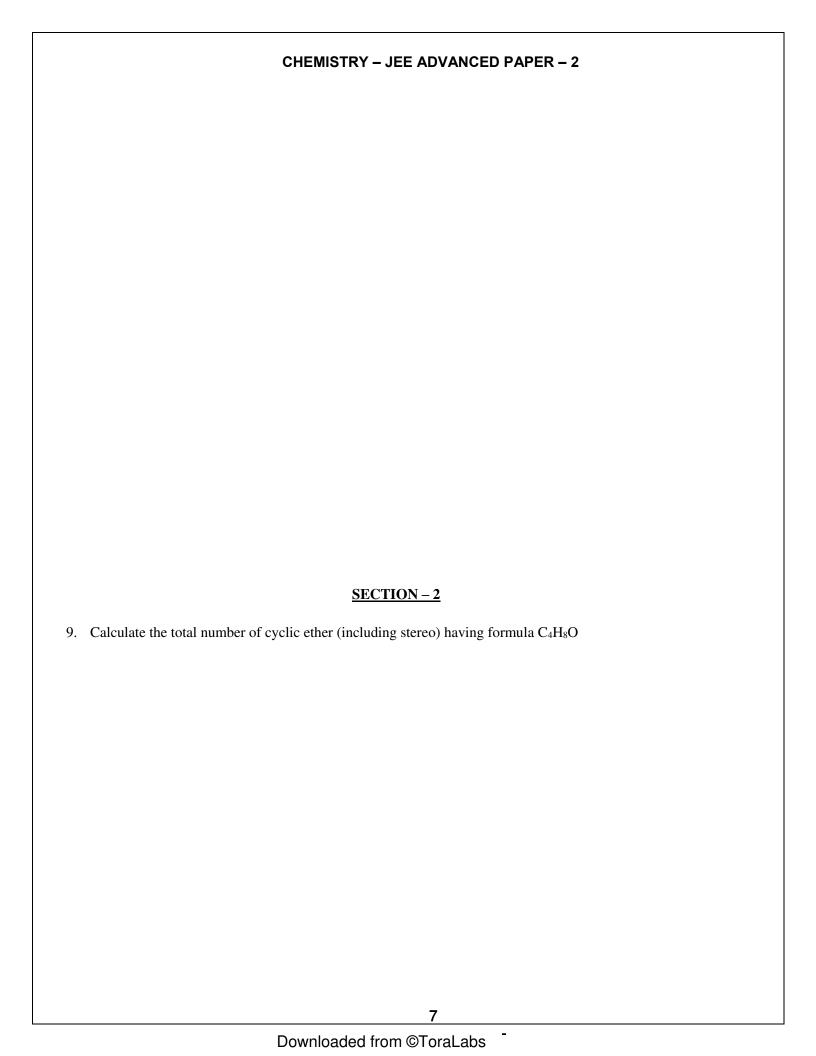
(b) Z is dirty white in colour

- (c) Bond order of Q is 1 in its ground state
- (d) The oxidation state of Zn in T is +1.

7. In the Mac. Arthur process of extraction

$$Au \xrightarrow{NaCN+Q} R \xrightarrow{extracted} Z$$

- (a) R is $[Au(CN_4)]^{(-)}$ (b) Z is $[Zn(CN)_4]^{2-}$
- (c) Q is O_2
- (d) Y is Zn
- 8. For He⁺ the electron is in orbit with energy equal to 3.4eV. The azimuthal quantum number for that orbit is 2 and magnetic quantum number is 0. Then which of the following is/are correct.
 - (a) The subshell is 4d.
 - (b) The number of angular nodes in it is 2.
 - (c) The numbers of radial nodes in it is 3.
 - (d) The nuclear charge experienced in n = 4 is 2e less than that in n = 1, where e is electric charge.



10. 1 mole of Rhombic sulphur is treated with conc. HNO₃. Find the mass of H₂O formed.

11. Mole fraction of urea in 900 gram water is 0.05. Density of Solution is 1.2 g/cm³. Find molarity of Solution.

12. Number of hydroxyl group in compound 'Y' is:

$$\begin{array}{c|c}
& \xrightarrow{\text{H}_2/\text{Pd BaSo}_4} \text{'X'} \xrightarrow{\text{dil.KMnO}_4} \text{Y'}
\end{array}$$

CHEMISTRY - JEE ADVANCED PAPER - 2 13. In following reaction the value of K is 5×10^{-4} S⁻¹. $2N_2O_5 \xrightarrow{\Delta} 2N_2O_4 + O_2$ Initial pressure was 1 atm, while the final pressure was 1.45 atm at time $y \times 10^3$ sec calculate 'y'. 9 Downloaded from ©ToraLabs

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14. Number of N-Mn-Cl bonds [N-Mn bonds is cis to Mn-Cl bond] in cis [Mn(en) ₂ Cl ₂] are
<u>SECTION – 3</u>
Match the column
List 1
Q Angular momentum II II ∝ n-2
R Kinetic energy III III ∞ n ⁻⁰ S Potential energy IV IV ∞ n ¹
V α n²
, '_
15. Which of the following is correct (a) P.U. (b) P.U. (c) P.V. (d) P.U.
(a) P I (b) P II (c) P V (d) P III

- 16. Which of following is correct.
 - (a) S IV
- (b) R I
- (c) R II
- (d) S III

Answer the question no. 17 & 18 on the basis of information given in Column – I & Column – II. Match the reactant in column - I with the possible intermediates and products of Column – II.

- 17. Which of the following is correct?
 - (a) P II, III; S II, III (b) P II, IV; S II, III (c) P III, VI; S II, III (d) P I, III; S IV, V

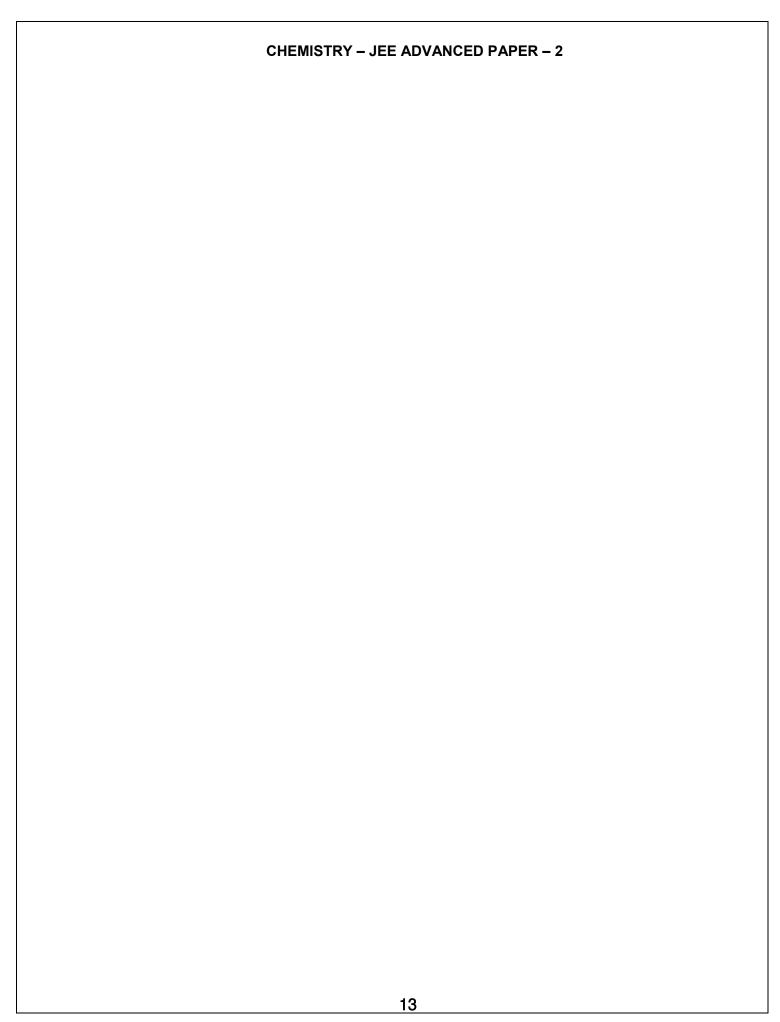
18. Which of the following is correct?

$$(a)\;Q-I,\,IV,\,VI;\,R-II,\,III,\,V$$

$$(b)\;Q-I,\,III,\,VI;\,R-II,\,IV,\,V$$

(c)
$$Q - I$$
, II , VI ; $R - II$, III , VI

(d)
$$Q - I$$
, IV , V ; $R - III$, I , V



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SECTION - 1

1. Let f: R \rightarrow R be given by f(x) = (x - 1)(x - 2)(x - 5). Define $F(x) = \int_{0}^{x} f(t) dt$, x > 0. Then which of the

following options is/are correct?

- (a) F has a local minimum at x = 1
- (b) F has a local maximum at x = 2

(c) $F(x) \neq 0$ for all $x \in (0, 5)$

(d) F has two local maxima and one local minimum in $(0, \infty)$

2. For $a \in \mathbb{R}$, |a| > 1, let $\lim_{n \to \infty} \left(\frac{1 + \sqrt[3]{2} +\sqrt[3]{n}}{n^{7/3} \left(\frac{1}{(an+1)^2} + \frac{1}{(an+2)^2} + + \frac{1}{(an+n)^2} \right)} \right) = 54$. Then the possible value(s) of a

is/are:

(a) 8

- (b) 9 (c) 6
- (d) 7

3. Three lines

$$L_1: \vec{r} = \lambda \hat{i}, \lambda \in R,$$

$$L_2: \vec{r} = \vec{k} + \mu \hat{j}, \mu \in R$$
 and

$$L_3: \vec{r} = \hat{i} + \hat{j} + v\hat{k}, v \in R$$

are given. For which point(s) Q and L2 can we find a point P on L1 and a point R on L3 so that P, Q and R are collinear?

- (a) $\hat{k} + \hat{j}$
- (b) \hat{k}
- (c) $\hat{k} + \frac{1}{2}\hat{j}$ (d) $\hat{k} \frac{1}{2}\hat{j}$

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4. Let $F: R \rightarrow R$ be a function. We say that f has

PROPERTY 1 $if \lim_{h\to 0} \frac{f(h)-f(0)}{\sqrt{|h|}}$ exists and is finite and

PROPERTY 2 $f \lim_{h\to 0} \frac{f(h) - f(0)}{h^2}$ exists and is finite

Then which of the following options is/are correct?

- (a) f(x) = x|x| has PROPERTY 2
- (b) $F(x) = x^{2/3}$ has PROPERTY 1
- (c) $f(x) = \sin x$ has PROPERTY 2
- (d) f(x) = |x| has PROPERTY 1

5. For non-negative integers n, let

$$f(n) = \frac{\sum_{k=0}^{n} \sin\left(\frac{k+1}{x+2}\pi\right) \sin\left(\frac{k+2}{n+2}\pi\right)}{\sum_{k=0}^{n} \sin^{2}\left(\frac{k+1}{n+2}\pi\right)}$$

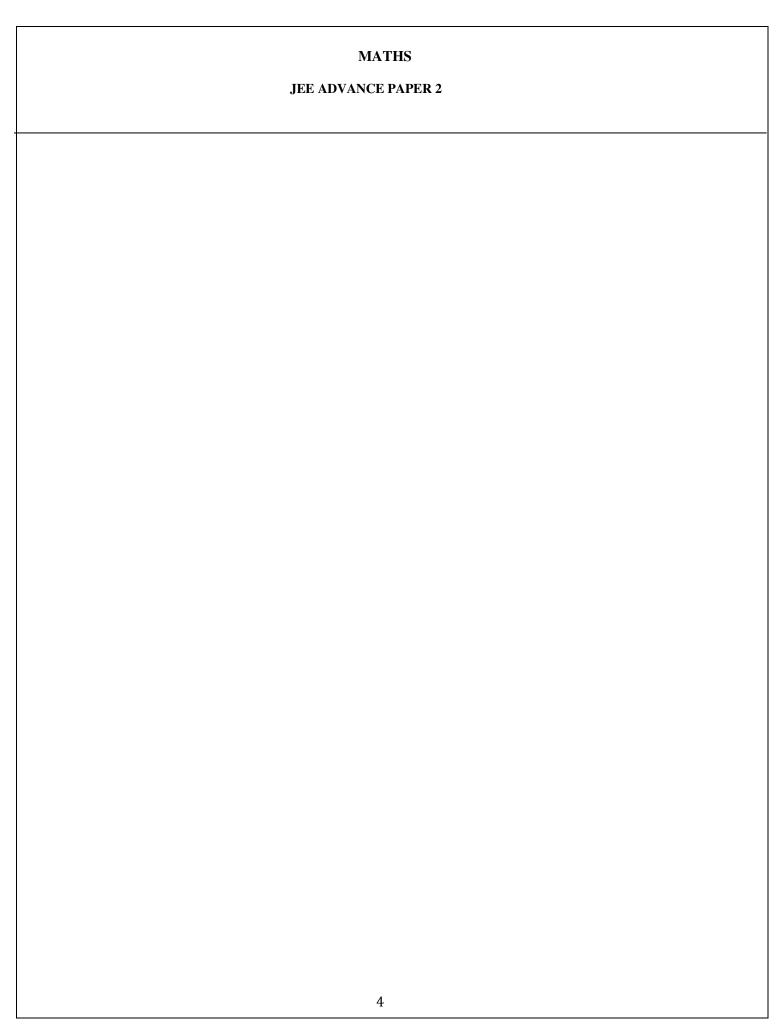
Assuming $\cos^{-1} x$ takes value in $[0, \pi]$, which of the following options is/are correct?

(a) $\sin (7 \cos^{-1} f(5)) = 0$

(b) $f(4) = \frac{\sqrt{3}}{2}$

(c) $\lim_{n\to\infty} f(n) = \frac{1}{2}$

(d) If $\alpha = \tan(\cos^{-1} f(6))$, then $\alpha^2 + 2\alpha - 1 = 0$



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6. Let $P_1 = I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, P_2 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}, P_3 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}, P_4 = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}, P_5 = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}, P_6 = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$

$$P_6 = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \text{ and } X = \sum_{k=1}^{6} P_K \begin{bmatrix} 2 & 1 & 3 \\ 1 & 0 & 2 \\ 3 & 2 & 1 \end{bmatrix} P_K^T$$

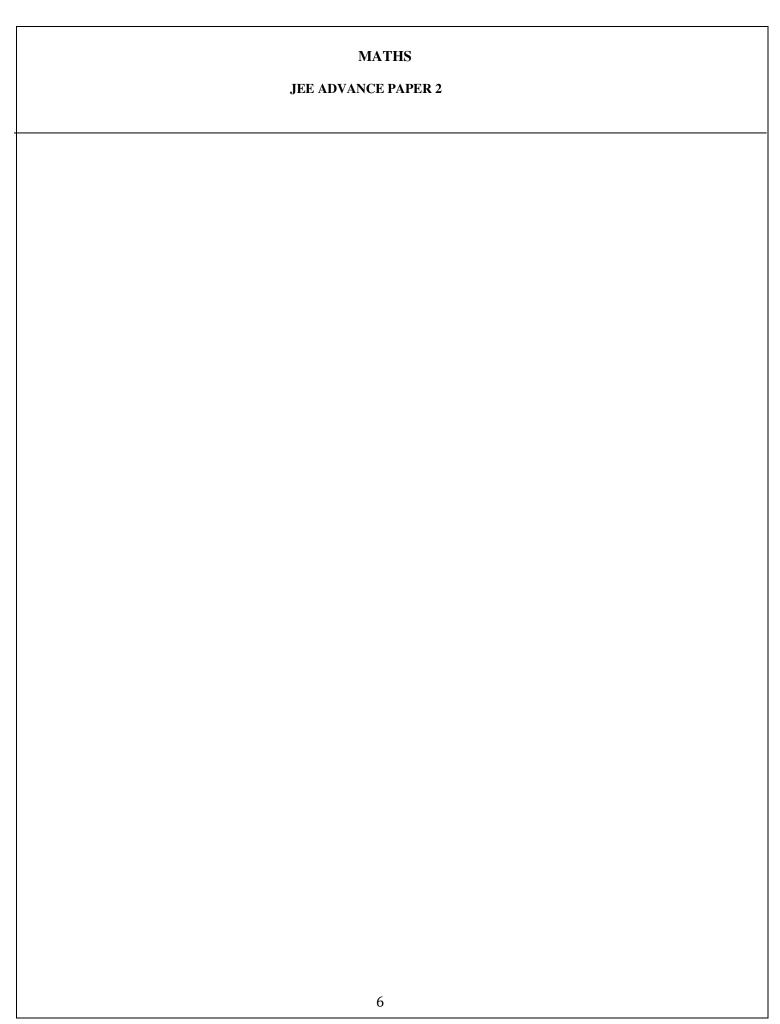
Where P_K^T denotes the transpose of the matrix P_K . Then which of the following options is/are correct?

(a) X - 30I is an invertible matrix

(b) The sum of diagonal entries of X is 18

(c) If $X \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \alpha \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$, then $\alpha = 30$

(d) X is a symmetric matrix



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7. Let $x \in R$ and let $P = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 2 & 2 \\ 0 & 0 & 3 \end{bmatrix}$, $Q = \begin{bmatrix} 2 & x & x \\ 0 & 4 & 0 \\ x & x & 6 \end{bmatrix}$ and $R = PQP^{-1}$

Then which of the following options is/are correct?

- (a) For x = 1, there exists a unit vector $\alpha \hat{i} + \beta \hat{j} + \gamma \hat{k}$ for which R $\begin{bmatrix} \alpha \\ \beta \\ \gamma \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$
- (b) There exists a real number x such that PQ = QP
- (c) det R = det $\begin{bmatrix} 2 & x & x \\ 0 & 4 & 0 \\ x & x & 5 \end{bmatrix} + 8, \text{ for all } x \in R$ (d) for x = 0, if $R \begin{bmatrix} 1 \\ a \\ b \end{bmatrix} = 6 \begin{bmatrix} 1 \\ a \\ b \end{bmatrix}, \text{ then } a + b = 5$

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8. Let
$$f(x) = \frac{\sin \pi x}{x^2}, x > 0$$

Let $x_1 \le x_2 \le x_3 \le \ldots \le x_n \le \ldots$ be all the points of local maximum of f and $y_1 \le y_2 \le y_3 \le \ldots \le y_n \le \ldots$ be all the points of local minimum of f.

Then which of the following options is/are correct?

(a)
$$|x_n - y_n| > 1$$
 for every n

(b)
$$x_1 < y_1$$

(c)
$$x_n \in \left(2n, 2n + \frac{1}{2}\right)$$
 for every n

(d)
$$x_{n+1} - x_n > 2$$
 for every n

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SECTION - 2

1. The value of $\sec^{-1}\left(\frac{1}{4}\sum_{k=0}^{10}\sec\left(\frac{7\pi}{12} + \frac{k\pi}{2}\right)\sec\left(\frac{7\pi}{12} + \frac{(k+1)\pi}{2}\right)\right)$ in the interval $\left[-\frac{\pi}{4}, \frac{3\pi}{4}\right]$ equals

2. Let |X| denote the number of elements in set X. Let $S = \{1,2,3,4,5,6\}$ be a sample space, where each element is equally likely to occur. If A and B are independent events associated with S, then the number of ordered pairs (A,B) such that $1 \le |B| \le |A|$, equals.

3. Five person A, B, C, D and E are seated in a circular arrangement. If each of them is given a hat of one of the three colours red, blue and green, then the number of ways of distributing the hats such that the persons seated in adjacent seats get different coloured hats is

4. Suppose

$$\det\begin{bmatrix} \sum_{k=0}^{n} k & \sum_{k=0}^{n} {}^{n}C_{k}k^{2} \\ \sum_{k=0}^{n} {}^{n}C_{k}k & \sum_{k=0}^{n} {}^{n}C_{k}3^{k} \end{bmatrix} = 0, \text{ holds for some positive integer n. Then } \sum_{k=0}^{n} \frac{{}^{n}C_{k}}{k+1} \text{ equals}$$

5. The value of the integral $\int_{0}^{\pi/2} \frac{3\sqrt{\cos\theta}}{\left(\sqrt{\cos\theta} + \sqrt{\sin\theta}\right)^{5}} d\theta \text{ equals}$

6. Let $\vec{a} = 2\hat{i} + \hat{j} - \hat{k}$ and $\vec{b} = \hat{i} + 2\hat{j} + \hat{k}$ be two vectors. Consider a vector $\vec{c} = \alpha \vec{a} + \beta \vec{b} + \alpha$, $\beta \varepsilon \Box$. If the projection of \vec{c} on the vector $(\vec{a} + \vec{b})$ is $3\sqrt{2}$, then the minimum value of $(\vec{c} - (\vec{a} \times \vec{b}))$. \vec{c} equals

SECTION - 3

1. Answer the following by appropriately matching the lists based on the information given in the paragraph Let $f(x) = \sin(\pi \cos x)$ and $g(x) = \cos(2\pi \sin x)$ be two functions defined for x > 0. Define the following sets whose element are written in the increasing order:

$$X = \{x : f(x) = 0\}, Y = \{x : f'(x) = 0\}$$

 $Z = \{x : g(x) = 0\}, W = \{x : g'(x) = 0\}$

List –I contains the sets X,Y,Z and W. List – II contains some information regarding these sets.

List I

$$(P) \supseteq \left\{ \frac{\pi}{2}, \frac{3\pi}{2}, 4\pi, 7\pi \right\}$$

(II) Y

(Q) an arithmetic progression

(III)Z

(R) Not an arithmetic progression

$$(S) \supseteq \left\{ \frac{\pi}{6}, \frac{7\pi}{6}, \frac{13\pi}{6} \right\}$$

$$(T) \supseteq \left\{ \frac{\pi}{3}, \frac{2\pi}{3}, \pi \right\}$$

$$(\mathsf{U})\supseteq\left\{\frac{\pi}{6},\frac{3\pi}{4}\right\}$$

Which of the following is the only correct combination?

- (a) (II), (R), (S)
- (b) (I), (P), (R)
- (c) (II), (Q), (T)
- (d)(I),(Q),(U)
- 2. Answer the following by appropriately matching the lists based on the information given in the paragraph Let $f(x) = \sin(\pi \cos x)$ and $g(x) = \cos(2\pi \sin x)$ be two functions defined for x > 0. Define the following sets whose element are written in the increasing order:

$$X = \{x: f(x) = 0\}, Y = \{x: f'(x) = 0\}$$

$$Z = \{x : g(x) = 0\}, W = \{x : g'(x) = 0\}$$

List –I contains the sets X,Y,Z and W. List – II contains some information regarding these sets.

List I

$$(P) \supseteq \left\{ \frac{\pi}{2}, \frac{3\pi}{2}, 4\pi, 7\pi \right\}$$

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$$(T) \supseteq \left\{ \frac{\pi}{3}, \frac{2\pi}{3}, \pi \right\}$$

$$(U) \supseteq \left\{ \frac{\pi}{6}, \frac{3\pi}{4} \right\}$$

Which of the following is the only correct combination?

- (a) (IV), (Q), (T)
- (b) (IV), (P), (R), (S)
- (c) (III), (R), (U)
- (d) (III), (P), (Q), (U)

MATHS	
JEE ADVANCE PAPER 2	
2. Answer the following by engropristely metaling the lists based on the information given in the new value	
3. Answer the following by appropriately matching the lists based on the information given in the paragraph	
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JEE ADVANCE PAPER 2

Let the circles $C_1: x^2 + y^2 = 9$ and $C_2: (x - 3)^2 + (y - 4)^2 = 16$, intersect at the points X and Y. Suppose that another circle $C_3: (x - h)^2 + (y - k)^2 = r^2$ satisfies the following conditions:

- (i) centre of C₃ is collinear with the centres of C₁ and C₂
- (ii) C₁ and C₂ both lie inside C₃, and
- (iii) C₃ touches C₁ at M and C₂ at N

Let the line through X and Y intersect C_3 at Z and W, and let a common tangent of C_1 and C_3 be a tangent to the parabola $x_2 = 8\alpha y$.

There are some expression given in the List - I whose values are given in List - II below:

(I) 2h + k

(II) $\frac{Length \, of \, ZW}{Length \, of \, XY}$

(Q)
$$\sqrt{6}$$

(III) $\frac{Area \, of \, triangle \, MZN}{Area \, of \, triangle \, ZMW}$

$$(R) \ \frac{5}{4}$$

(IV) α

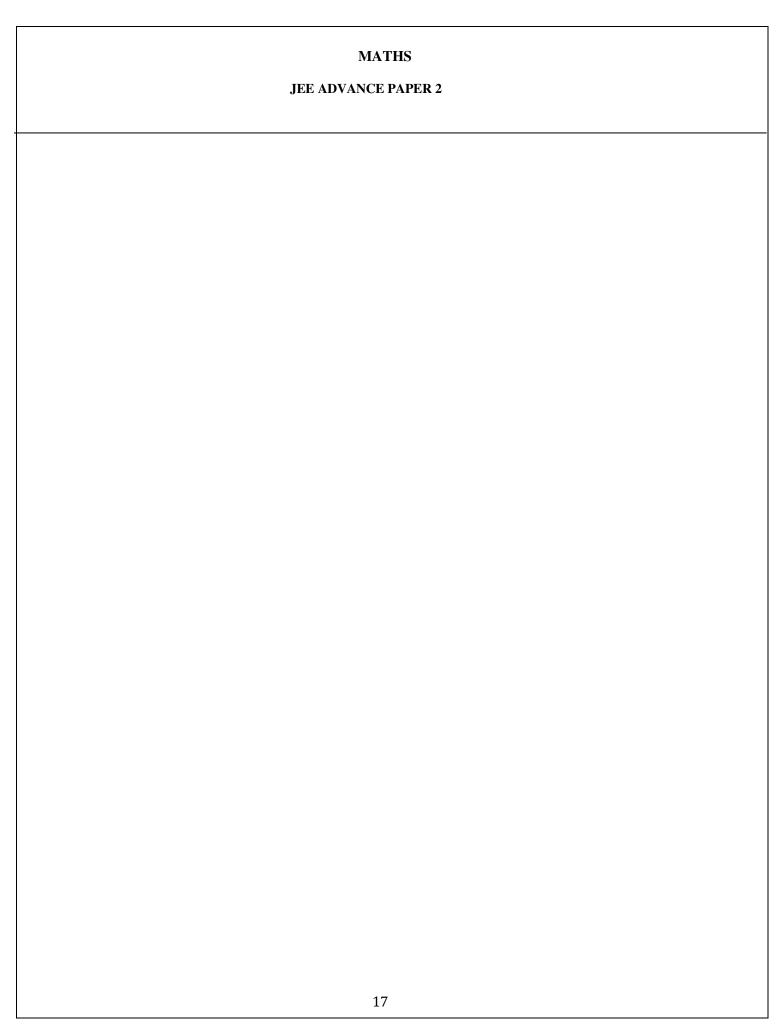
(S)
$$\frac{21}{5}$$

(T)
$$2\sqrt{6}$$

(U)
$$\frac{10}{3}$$

Which of the following is the only INCORRECT combination?

(a) (IV), (S)



- 4. Answer the following by appropriately matching the lists based on the information given in the paragraph Let the circles $C_1: x^2 + y^2 = 9$ and $C_2: (x-3)^2 + (y-4)^2 = 16$, intersect at the points X and Y. Suppose that another circle $C_3: (x-h)^2 + (y-k)^2 = r^2$ satisfies the following conditions:
 - (i) centre of C_3 is collinear with the centres of C_1 and C_2
 - (ii) C₁ and C₂ both lie inside C₃, and
 - (iii) C₃ touches C₁ at M and C₂ at N

Let the line through X and Y intersect C_3 at Z and W, and let a common tangent of C_1 and C_3 be a tangent to the parabola $x_2 = 8\alpha y$.

There are some expression given in the List – I whose values are given in List – II below:

List – II

(I) 2h + k

(P) 6

(II) $\frac{Length \, of \, ZW}{Length \, of \, XY}$

- (Q) $\sqrt{6}$
- (III) $\frac{Area of triangle MZN}{Area of triangle ZMW}$
- $(R) \ \frac{5}{4}$

(IV) α

- (S) $\frac{21}{5}$
- (T) $2\sqrt{6}$
- (U) $\frac{10}{3}$

Which of the following is the only INCORRECT combination?

- (a) (II), (T)
- (b) (I), (S)
- (c) (I), (U)
- (d) (II), (Q)

