

09/04/2019  
Morning

# **JEE (MAIN)-2019 (Online) Phase-2**

## **(Physics, Chemistry and Mathematics)**

**Time : 3 hrs.**

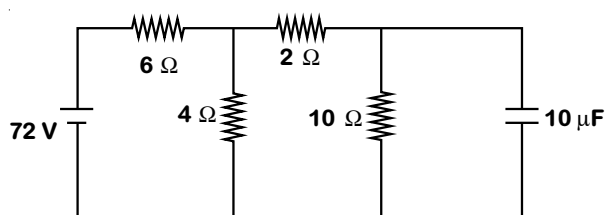
**M.M. : 360**

### **Important Instructions :**

1. The test is of **3 hours** duration.
2. The Test Booklet consists of **90** questions. The maximum marks are **360**.
3. There are **three** parts in the question paper A, B, C consisting of **Physics, Chemistry and Mathematics** having 30 questions in each part of equal weightage.
4. Each question is allotted 4 (**four**) marks for each correct response.  $\frac{1}{4}$  (*one-fourth*) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
5. There is only one correct response for each question.

## PART-A : PHYSICS

1. Determine the charge on the capacitor in the following circuit :



- (1)  $200 \mu\text{C}$                       (2)  $60 \mu\text{C}$   
 (3)  $10 \mu\text{C}$                       (4)  $2 \mu\text{C}$

2. The magnetic field of a plane electromagnetic wave is given by :

$$\vec{B} = B_0 \hat{i} [\cos(kz - \omega t) + B_1 \hat{j} \cos(kz + \omega t)]$$

where  $B_0 = 3 \times 10^{-5} \text{ T}$  and  $B_1 = 2 \times 10^{-6} \text{ T}$ .

The rms value of the force experienced by a stationary charge  $Q = 10^{-4} \text{ C}$  at  $z = 0$  is closest to:

- (1)  $0.6 \text{ N}$                       (2)  $0.9 \text{ N}$   
 (3)  $3 \times 10^{-2} \text{ N}$               (4)  $0.1 \text{ N}$

3. A stationary horizontal disc is free to rotate about its axis. When a torque is applied on it, its kinetic energy as a function of  $\theta$ , where  $\theta$  is the angle by which it has rotated, is given as  $k\theta^2$ . If its moment of inertia is  $I$  then the angular acceleration of the disc is:

- (1)  $\frac{2k}{I} \theta$                       (2)  $\frac{k}{I} \theta$   
 (3)  $\frac{k}{2I} \theta$                       (4)  $\frac{k}{4I} \theta$

4. The stream of a river is flowing with a speed of  $2 \text{ km/h}$ . A swimmer can swim at a speed of  $4 \text{ km/h}$ . What should be the direction of the swimmer with respect to the flow of the river to cross the river straight?

- (1)  $60^\circ$                       (2)  $90^\circ$   
 (3)  $150^\circ$                       (4)  $120^\circ$

5. A uniform cable of mass 'M' and length 'L' is placed on a horizontal surface such that its  $\left(\frac{1}{n}\right)^{\text{th}}$  part is hanging below the edge of the surface. To lift the hanging part of the cable upto the surface, the work done should be:

- (1)  $\frac{MgL}{n^2}$  (2)  $nMgL$   
 (3)  $\frac{MgL}{2n^2}$  (4)  $\frac{2MgL}{n^2}$

6. A signal  $A\cos\omega t$  is transmitted using  $v_0\sin\omega_0 t$  as carrier wave. The correct amplitude modulated (AM) signal is:

- (1)  $v_0\sin\omega_0 t + \frac{A}{2}\sin(\omega_0 - \omega)t + \frac{A}{2}\sin(\omega_0 + \omega)t$   
 (2)  $(v_0 + A)\cos\omega t \sin\omega_0 t$   
 (3)  $v_0\sin\omega_0 t + A\cos\omega t$   
 (4)  $v_0\sin[\omega_0(1 + 0.01 A\sin\omega t)t]$

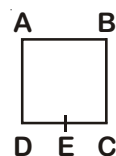
7. The following bodies are made to roll up (without slipping) the same inclined plane from a horizontal plane : (i) a ring of radius R, (ii) a solid cylinder of radius  $\frac{R}{2}$  and (iii) a solid

sphere of radius  $\frac{R}{4}$ . If, in each case, the speed of the center of mass at the bottom of the incline is same, the ratio of the maximum heights they climb is :

- (1) 14 : 15 : 20 (2) 10 : 15 : 7  
 (3) 4 : 3 : 2 (4) 2 : 3 : 4

8. A wire of resistance R is bent to form a square ABCD as shown in the figure. The effective resistance between E and C is

(E is mid-point of arm CD)



- (1)  $\frac{3}{4}R$  (2)  $R$   
 (3)  $\frac{1}{16}R$  (4)  $\frac{7}{64}R$

9. In the density measurement of a cube, the mass and edge length are measured as  $(10.00 \pm 0.10)$  kg and  $(0.10 \pm 0.01)$  m, respectively. The error in the measurement of density is

- (1)  $0.31 \text{ kg/m}^3$  (2)  $0.01 \text{ kg/m}^3$   
 (3)  $0.10 \text{ kg/m}^3$  (4)  $0.07 \text{ kg/m}^3$

Answer (Bonus)

10. A rectangular coil (Dimension 5 cm × 2.5 cm) with 100 turns, carrying a current of 3 A in the clock-wise direction, is kept centered at the origin and in the X-Z plane. A magnetic field of 1 T is applied along X-axis. If the coil is tilted through 45° about Z-axis, then the torque on the coil is

- (1) 0.55 Nm                      (2) 0.27 Nm  
(3) 0.42 Nm                      (4) 0.38 Nm

11. A simple pendulum oscillating in air has period T. The bob of the pendulum is completely immersed in a non-viscous liquid. The density

of the liquid is  $\frac{1}{16}$ th of the material of the bob.

If the bob is inside liquid all the time, its period of oscillation in this liquid is :

- (1)  $2T\sqrt{\frac{1}{14}}$                       (2)  $4T\sqrt{\frac{1}{15}}$   
(3)  $4T\sqrt{\frac{1}{14}}$                       (4)  $2T\sqrt{\frac{1}{10}}$

12. The total number of turns and cross-section area in a solenoid is fixed. However, its length L is varied by adjusting the separation between windings. The inductance of solenoid will be proportional to

- (1)  $1/L$                               (2) L  
(3)  $1/L^2$                               (4)  $L^2$

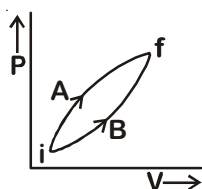
13. For a given gas at 1 atm pressure, rms speed of the molecules is 200 m/s at 127°C. At 2 atm pressure and at 227°C, the rms speed of the molecules will be:

- (1)  $100\sqrt{5}$  m/s                      (2) 100 m/s  
(3)  $80\sqrt{5}$  m/s                      (4) 80 m/s

14. A capacitor with capacitance 5 μF is charged to 5 μC. If the plates are pulled apart to reduce the capacitance to 2 μF, how much work is done?

- (1)  $2.55 \times 10^{-6}$  J                      (2)  $6.25 \times 10^{-6}$  J  
(3)  $3.75 \times 10^{-6}$  J                      (4)  $2.16 \times 10^{-6}$  J

15. Following figure shows two processes A and B for a gas. If  $\Delta Q_A$  and  $\Delta Q_B$  are the amount of heat absorbed by the system in two cases, and  $\Delta U_A$  and  $\Delta U_B$  are changes in internal energies, respectively, then:



- (1)  $\Delta Q_A > \Delta Q_B$ ;  $\Delta U_A = \Delta U_B$   
 (2)  $\Delta Q_A = \Delta Q_B$ ;  $\Delta U_A = \Delta U_B$   
 (3)  $\Delta Q_A > \Delta Q_B$ ;  $\Delta U_A > \Delta U_B$   
 (4)  $\Delta Q_A < \Delta Q_B$ ;  $\Delta U_A < \Delta U_B$
16. A concave mirror for face viewing has focal length of 0.4 m. The distance at which you hold the mirror from your face in order to see your image upright with a magnification of 5 is:  
 (1) 0.32 m (2) 0.24 m  
 (3) 1.60 m (4) 0.16 m

17. A solid sphere of mass 'M' and radius 'a' is surrounded by a uniform concentric spherical shell of thickness 2a and mass 2M. The gravitational field at distance '3a' from the centre will be:

- (1)  $\frac{GM}{9a^2}$  (2)  $\frac{2GM}{9a^2}$   
 (3)  $\frac{GM}{3a^2}$  (4)  $\frac{2GM}{3a^2}$

18. A moving coil galvanometer has resistance 50  $\Omega$  and it indicates full deflection at 4 mA current. A voltmeter is made using this galvanometer and a 5 k $\Omega$  resistance. The maximum voltage, that can be measured using this voltmeter, will be close to:

- (1) 10 V (2) 20 V  
 (3) 15 V (4) 40 V

19. The pressure wave,  $P = 0.01\sin[1000t - 3x]\text{Nm}^{-2}$ , corresponds to the sound produced by a vibrating blade on a day when atmospheric temperature is 0°C. On some other day when temperature is T, the speed of sound produced by the same blade and at the same frequency is found to be 336 ms<sup>-1</sup>. Approximate value of T is :

- (1) 4°C (2) 12°C  
 (3) 15°C (4) 11°C

20. Taking the wavelength of first Balmer line in hydrogen spectrum ( $n = 3$  to  $n = 2$ ) as 660 nm, the wavelength of the 2<sup>nd</sup> Balmer line ( $n = 4$  to  $n = 2$ ) will be :

- (1) 889.2 nm                      (2) 488.9 nm  
(3) 388.9 nm                      (4) 642.7 nm

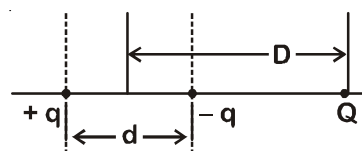
21. A body of mass 2 kg makes an elastic collision with a second body at rest and continues to move in the original direction but with one fourth of its original speed. What is the mass of the second body?

- (1) 1.5 kg                      (2) 1.8 kg  
(3) 1.0 kg                      (4) 1.2 kg

22. An HCl molecule has rotational, translational and vibrational motions. If the rms velocity of HCl molecules in its gaseous phase is  $\bar{v}$ ,  $m$  is its mass and  $k_B$  is Boltzmann constant, then its temperature will be :

- (1)  $\frac{m\bar{v}^2}{5k_B}$   
(2)  $\frac{m\bar{v}^2}{6k_B}$   
(3)  $\frac{m\bar{v}^2}{7k_B}$   
(4)  $\frac{m\bar{v}^2}{3k_B}$

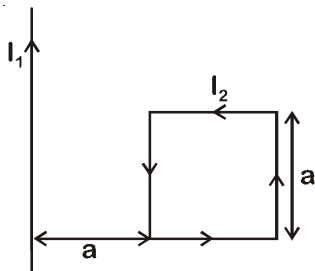
23. A system of three charges are placed as shown in the figure :



If  $D \gg d$ , the potential energy of the system is best given by :

- (1)  $\frac{1}{4\pi\epsilon_0} \left[ -\frac{q^2}{d} - \frac{qQd}{D^2} \right]$   
(2)  $\frac{1}{4\pi\epsilon_0} \left[ +\frac{q^2}{d} + \frac{qQd}{D^2} \right]$   
(3)  $\frac{1}{4\pi\epsilon_0} \left[ -\frac{q^2}{d} + \frac{2qQd}{D^2} \right]$   
(4)  $\frac{1}{4\pi\epsilon_0} \left[ -\frac{q^2}{d} - \frac{qQd}{2D^2} \right]$

24. A rigid square loop of side 'a' and carrying current  $I_2$  is lying on a horizontal surface near a long current  $I_1$  carrying wire in the same plane as shown in figure. The net force on the loop due to the wire will be :



- (1) Repulsive and equal to  $\frac{\mu_0 I_1 I_2}{4\pi}$
- (2) Repulsive and equal to  $\frac{\mu_0 I_1 I_2}{2\pi}$
- (3) Zero
- (4) Attractive and equal to  $\frac{\mu_0 I_1 I_2}{3\pi}$

25. A string is clamped at both the ends and it is vibrating in its 4<sup>th</sup> harmonic. The equation of the stationary wave is  $Y = 0.3 \sin (0.157x) \cos (200\pi t)$ . The length of the string is : (All quantities are in SI units)

- (1) 60 m
- (2) 20 m
- (3) 40 m
- (4) 80 m

26. An NPN transistor is used in common emitter configuration as an amplifier with 1 k $\Omega$  load resistance. Signal voltage of 10 mV is applied across the base-emitter. This produces a 3 mA change in the collector current and 15  $\mu$ A change in the base current of the amplifier. The input resistance and voltage gain are :

- (1) 0.33 k $\Omega$ , 1.5
- (2) 0.33 k $\Omega$ , 300
- (3) 0.67 k $\Omega$ , 200
- (4) 0.67 k $\Omega$ , 300

27. The electric field of light wave is given as

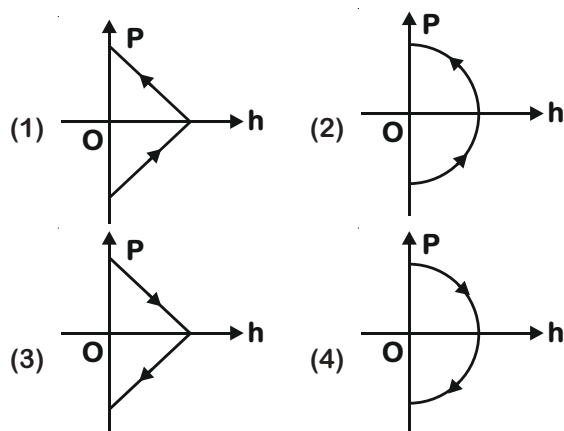
$$\vec{E} = 10^{-3} \cos\left(\frac{2\pi x}{5 \times 10^{-7}} - 2\pi \times 6 \times 10^{14} t\right) \hat{x} \frac{\text{N}}{\text{C}}.$$
 This

light falls on a metal plate of work function 2eV. The stopping potential of the photo-electrons is :

Given,  $E$  (in eV) =  $\frac{12375}{\lambda \text{ (in } \text{\AA})}$

- (1) 0.48 V
- (2) 2.48 V
- (3) 0.72 V
- (4) 2.0 V

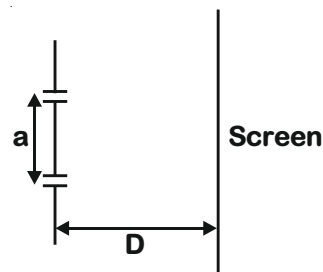
28. A ball is thrown vertically up (taken as + z-axis) from the ground. The correct momentum-height (p-h) diagram is:



29. If 'M' is the mass of water that rises in a capillary tube of radius 'r', then mass of water which will rise in a capillary tube of radius '2r' is

- (1) 2 M
- (2) M
- (3) 4 M
- (4)  $\frac{M}{2}$

30. The figure shows a Young's double slit experimental setup. It is observed that when a thin transparent sheet of thickness  $t$  and refractive index  $\mu$  is put in front of one of the slits, the central maximum gets shifted by a distance equal to  $n$  fringe widths. If the wavelength of light used is  $\lambda$ ,  $t$  will be

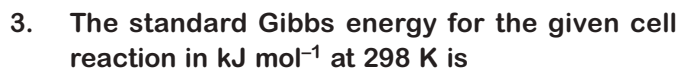


- (1)  $\frac{2nD\lambda}{a(\mu-1)}$
- (2)  $\frac{2D\lambda}{a(\mu-1)}$
- (3)  $\frac{nD\lambda}{a(\mu-1)}$
- (4)  $\frac{D\lambda}{a(\mu-1)}$



## PART-B : CHEMISTRY

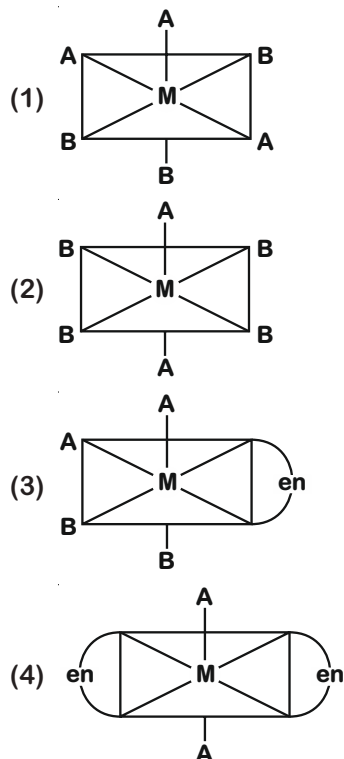
2. The major product of the following reaction is



(1) 192  
(2) 384  
(3) -384  
(4) -192

- (1)  $\text{Mg}(\text{NO}_3)_2$  and  $\text{Mg}_3\text{N}_2$
- (2)  $\text{MgO}$  and  $\text{Mg}(\text{NO}_3)_2$
- (3)  $\text{MgO}$  and  $\text{Mg}_3\text{N}_2$
- (4)  $\text{MgO}$  only

6. The one that will show optical activity is (en = ethane-1,2-diamine)



7. Liquid 'M' and liquid 'N' form an ideal solution. The vapour pressures of pure liquids 'M' and 'N' are 450 and 700 mmHg, respectively, at the same temperature. Then correct statement is

( $x_M$  = Mole fraction of 'M' in solution;

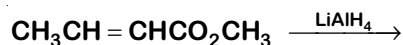
$x_N$  = Mole fraction of 'N' in solution;

$y_M$  = Mole fraction of 'M' in vapour phase;

$y_N$  = Mole fraction of 'N' in vapour phase)

- (1)  $\frac{x_M}{x_N} = \frac{y_M}{y_N}$                       (2)  $\frac{x_M}{x_N} > \frac{y_M}{y_N}$   
 (3)  $\frac{x_M}{x_N} < \frac{y_M}{y_N}$                       (4)  $(x_M - y_M) < (x_N - y_N)$

8. The major product of the following reaction is



- (1)  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{OH}$   
 (2)  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CHO}$   
 (3)  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CO}_2\text{CH}_3$   
 (4)  $\text{CH}_3\text{CH}=\text{CHCH}_2\text{OH}$

9. For any given series of spectral lines of atomic hydrogen, let  $\Delta\bar{\nu} = \bar{\nu}_{\text{max}} - \bar{\nu}_{\text{min}}$  be the difference in maximum and minimum frequencies in  $\text{cm}^{-1}$ .

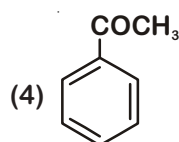
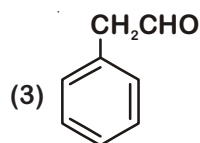
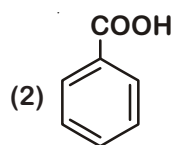
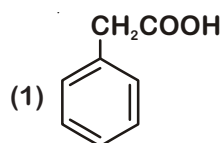
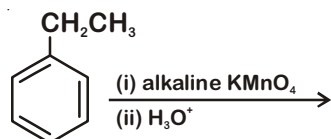
The ratio  $\Delta\bar{\nu}_{\text{Lyman}} / \Delta\bar{\nu}_{\text{Balmer}}$  is

- (1) 9 : 4                                      (2) 27 : 5  
 (3) 4 : 1                                      (4) 5 : 4

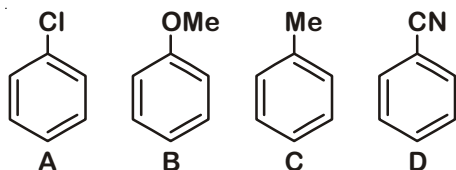
10. Among the following, the set of parameters that represents path functions, is

- (A)  $q + w$                                       (B)  $q$   
 (C)  $w$     (D)  $H - TS$   
 (1) (A), (B) and (C)                      (2) (B) and (C)  
 (3) (B), (C) and (D)                      (4) (A) and (D)

11. The major product of the following reaction is

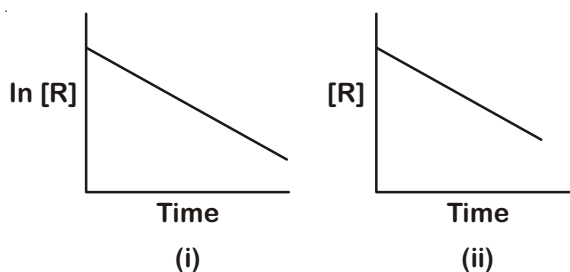


12. The increasing order of reactivity of the following compounds towards aromatic electrophilic substitution reaction is



- (1)  $\text{D} < \text{B} < \text{A} < \text{C}$
- (2)  $\text{D} < \text{A} < \text{C} < \text{B}$
- (3)  $\text{B} < \text{C} < \text{A} < \text{D}$
- (4)  $\text{A} < \text{B} < \text{C} < \text{D}$

13. The given plots represent the variation of the concentration of a reactant R with time for two different reactions (i) and (ii). The respective orders of the reactions are



- (1) 0, 1
- (2) 1, 1
- (3) 1, 0
- (4) 0, 2

14. The osmotic pressure of a dilute solution of an ionic compound XY in water is four times that of a solution of 0.01 M  $\text{BaCl}_2$  in water. Assuming complete dissociation of the given ionic compounds in water, the concentration of XY (in  $\text{mol L}^{-1}$ ) in solution is

- (1)  $16 \times 10^{-4}$
- (2)  $4 \times 10^{-4}$
- (3)  $6 \times 10^{-2}$
- (4)  $4 \times 10^{-2}$

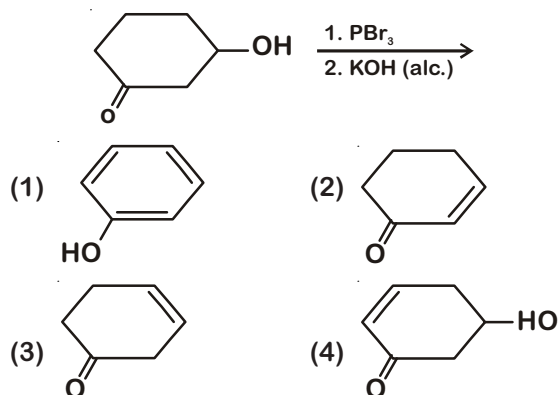
15. Consider the van der Waals constants, a and b, for the following gases.

Gas	Ar	Ne	Kr	Xe
$a/(\text{atm dm}^6 \text{ mol}^{-2})$	1.3	0.2	5.1	4.1
$b/(10^{-2} \text{ dm}^3 \text{ mol}^{-1})$	3.2	1.7	1.0	5.0

Which gas is expected to have the highest critical temperature?

- (1) Ne
- (2) Kr
- (3) Xe
- (4) Ar

16. The major product of the following reaction is



17. Among the following, the molecule expected to be stabilized by anion formation is

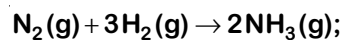
$C_2$ ,  $O_2$ , NO,  $F_2$

- |           |           |
|-----------|-----------|
| (1) $F_2$ | (2) NO    |
| (3) $C_2$ | (4) $O_2$ |

18. Excessive release of  $CO_2$  into the atmosphere results in

- (1) Depletion of ozone
- (2) Polar vortex
- (3) Formation of smog
- (4) Global warming

19. For a reaction,



Identify dihydrogen ( $H_2$ ) as a limiting reagent in the following reaction mixtures.

- (1) 35 g of  $N_2$  + 8 g of  $H_2$
- (2) 28 g of  $N_2$  + 6 g of  $H_2$
- (3) 56 g of  $N_2$  + 10 g of  $H_2$
- (4) 14 g of  $N_2$  + 4 g of  $H_2$

20. Match the catalysts (Column I) with products (Column II).

Column I	Column II
Catalyst	Product
(A) $V_2O_5$	(i) Polyethylene
(B) $TiCl_4/Al(Me)_3$	(ii) Ethanal
(C) $PdCl_2$	(iii) $H_2SO_4$
(D) Iron Oxide	(iv) $NH_3$
(1) (A)-(iv); (B)-(iii); (C)-(ii); (D)-(i)	
(2) (A)-(iii); (B)-(iv); (C)-(i); (D)-(ii)	
(3) (A)-(iii); (B)-(i); (C)-(ii); (D)-(iv)	
(4) (A)-(ii); (B)-(iii); (C)-(i); (D)-(iv)	

21. The element having greatest difference between its first and second ionization energies, is

- |        |        |
|--------|--------|
| (1) K  | (2) Sc |
| (3) Ca | (4) Ba |

22. The correct order of the oxidation states of nitrogen in NO, N<sub>2</sub>O, NO<sub>2</sub>, and N<sub>2</sub>O<sub>3</sub> is

- (1) NO<sub>2</sub> < NO < N<sub>2</sub>O<sub>3</sub> < N<sub>2</sub>O
- (2) N<sub>2</sub>O < NO < N<sub>2</sub>O<sub>3</sub> < NO<sub>2</sub>
- (3) NO<sub>2</sub> < N<sub>2</sub>O<sub>3</sub> < NO < N<sub>2</sub>O
- (4) N<sub>2</sub>O < N<sub>2</sub>O<sub>3</sub> < NO < NO<sub>2</sub>

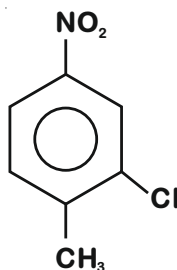
23. Which of the following statements is not true about sucrose?

- (1) The glycosidic linkage is present between C<sub>1</sub> of α-glucose and C<sub>1</sub> of β-fructose
- (2) On hydrolysis, it produces glucose and fructose
- (3) It is a non-reducing sugar
- (4) It is also named as invert sugar

24. The ore that contains the metal in the form of fluoride is

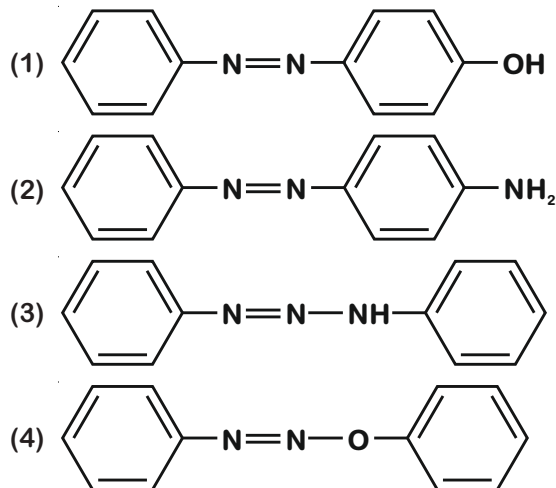
- |               |                |
|---------------|----------------|
| (1) malachite | (2) sphalerite |
| (3) magnetite | (4) cryolite   |

25. The correct IUPAC name of the following compound is



- (1) 3-chloro-4-methyl-1-nitrobenzene
- (2) 5-chloro-4-methyl-1-nitrobenzene
- (3) 2-methyl-5-nitro-1-chlorobenzene
- (4) 2-chloro-1-methyl-4-nitrobenzene

26. Aniline dissolved in dilute HCl is reacted with sodium nitrite at 0°C. This solution was added dropwise to a solution containing equimolar mixture of aniline and phenol in dil. HCl. The structure of the major product is



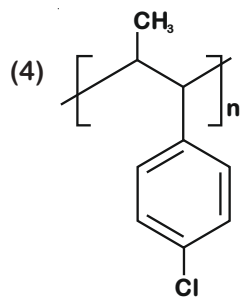
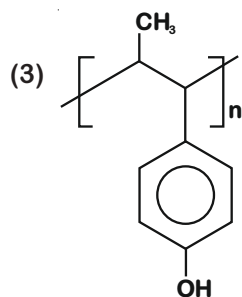
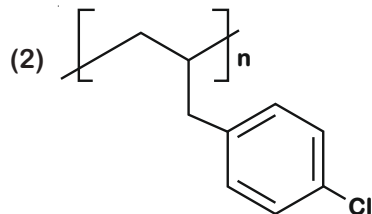
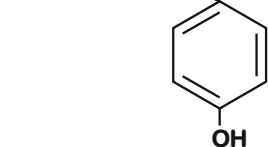
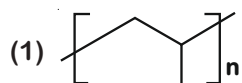
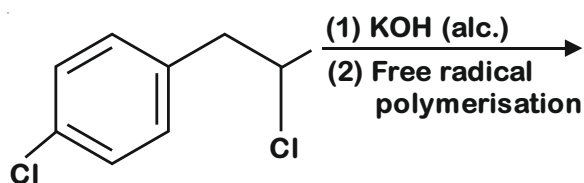
27. The aerosol is a kind of colloid in which

- (1) solid is dispersed in gas
- (2) gas is dispersed in solid
- (3) liquid is dispersed in water
- (4) gas is dispersed in liquid

28. The degenerate orbitals of  $[\text{Cr}(\text{H}_2\text{O})_6]^{3+}$  are

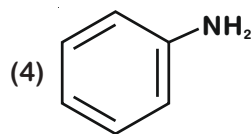
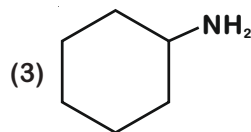
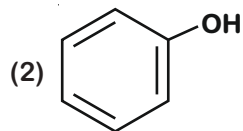
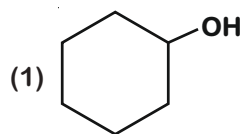
- (1)  $d_{xz}$  and  $d_{yz}$
- (2)  $d_{x^2-y^2}$  and  $d_{xy}$
- (3)  $d_{z^2}$  and  $d_{xz}$
- (4)  $d_{yz}$  and  $d_{z^2}$

29. The major product of the following reaction is



30. The organic compound that gives following qualitative analysis is

Test	Inference
(a) Dil. HCl	Insoluble
(b) NaOH solution	Soluble
(c) $\text{Br}_2/\text{water}$	Decolourization



## PART-C : MATHEMATICS

1. Let  $p, q \in \mathbb{R}$ . If  $2 - \sqrt{3}$  is a root of the quadratic equation,  $x^2 + px + q = 0$ , then :

(1)  $q^2 - 4p - 16 = 0$       (2)  $p^2 - 4q + 12 = 0$   
(3)  $p^2 - 4q - 12 = 0$       (4)  $q^2 + 4p + 14 = 0$

2. If the line,  $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-2}{4}$  meets the plane,  $x + 2y + 3z = 15$  at a point P, then the distance of P from the origin is :

(1)  $2\sqrt{5}$                       (2)  $\frac{9}{2}$   
(3)  $\frac{7}{2}$                           (4)  $\frac{\sqrt{5}}{2}$

3. If a tangent to the circle  $x^2 + y^2 = 1$  intersects the coordinate axes at distinct points P and Q, then the locus of the mid-point of PQ is :

(1)  $x^2 + y^2 - 16x^2y^2 = 0$   
(2)  $x^2 + y^2 - 2x^2y^2 = 0$   
(3)  $x^2 + y^2 - 4x^2y^2 = 0$   
(4)  $x^2 + y^2 - 2xy = 0$

4. If  $f(x)$  is a non-zero polynomial of degree four, having local extreme points at  $x = -1, 0, 1$ ; then the set

$$S = \{x \in \mathbb{R} : f(x) = f(0)\}$$

contains exactly :

- (1) Four irrational numbers  
(2) Four rational numbers  
(3) Two irrational and one rational number  
(4) Two irrational and two rational numbers

5. If the standard deviation of the numbers  $-1, 0, 1$ ,  $k$  is  $\sqrt{5}$  where  $k > 0$ , then  $k$  is equal to :

- (1)  $\sqrt{6}$  (2)  $2\sqrt{6}$   
(3)  $2\sqrt{\frac{10}{3}}$  (4)  $4\sqrt{\frac{5}{3}}$

6. If the fourth term in the Binomial expansion of

$$\left(\frac{2}{x} + x^{\log_8 x}\right)^6 \quad (x > 0) \text{ is } 20 \times 8^7, \text{ then a value of } x$$

is :

- (1)  $8^3$  (2)  $8$   
(3)  $8^{-2}$  (4)  $8^2$

7. The integral  $\int \sec^{2/3} x \operatorname{cosec}^{4/3} x \, dx$  is equal to :

(Here  $C$  is a constant of integration)

- (1)  $-3\cot^{-1/3} x + C$   
(2)  $-3\tan^{-1/3} x + C$   
(3)  $-\frac{3}{4} \tan^{-4/3} x + C$   
(4)  $3\tan^{-1/3} x + C$

8. If one end of a focal chord of the parabola,  $y^2 = 16x$  is at  $(1, 4)$ , then the length of this focal chord is :

- (1) 24  
(2) 20  
(3) 22  
(4) 25



9. If the function  $f$  defined on  $\left(\frac{\pi}{6}, \frac{\pi}{3}\right)$  by

$$f(x) = \begin{cases} \frac{\sqrt{2} \cos x - 1}{\cot x - 1}, & x \neq \frac{\pi}{4} \\ k, & x = \frac{\pi}{4} \end{cases}$$

is continuous, then  $k$  is equal to :

- (1) 1 (2)  $\frac{1}{2}$   
(3)  $\frac{1}{\sqrt{2}}$  (4) 2

10. All the points in the set

$$S = \left\{ \frac{\alpha + i}{\alpha - i} : \alpha \in \mathbf{R} \right\} (i = \sqrt{-1})$$

lie on a :

- (1) Straight line whose slope is 1  
(2) Circle whose radius is  $\sqrt{2}$   
(3) Circle whose radius is 1  
(4) Straight line whose slope is -1

11. Let  $\vec{\alpha} = 3\hat{i} + \hat{j}$  and  $\vec{\beta} = 2\hat{i} - \hat{j} + 3\hat{k}$ . If  $\vec{\beta} = \vec{\beta}_1 - \vec{\beta}_2$ , where  $\vec{\beta}_1$  is parallel to  $\vec{\alpha}$  and  $\vec{\beta}_2$  is perpendicular to  $\vec{\alpha}$ , then  $\vec{\beta}_1 \times \vec{\beta}_2$  is equal to :

- (1)  $\frac{1}{2}(3\hat{i} - 9\hat{j} + 5\hat{k})$  (2)  $\frac{1}{2}(-3\hat{i} + 9\hat{j} + 5\hat{k})$   
(3)  $-3\hat{i} + 9\hat{j} + 5\hat{k}$  (4)  $3\hat{i} - 9\hat{j} - 5\hat{k}$

12. Let  $\sum_{k=1}^{10} f(a+k) = 16(2^{10} - 1)$ , where the function  $f$  satisfies  $f(x+y) = f(x)f(y)$  for all natural numbers  $x, y$  and  $f(1) = 2$ . Then the natural number 'a' is :

- (1) 2  
(2) 3  
(3) 16  
(4) 4

13. If  $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix} \cdots \begin{bmatrix} 1 & n-1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 78 \\ 0 & 1 \end{bmatrix}$ ,

then the inverse of  $\begin{bmatrix} 1 & n \\ 0 & 1 \end{bmatrix}$  is :

(1)  $\begin{bmatrix} 1 & 0 \\ 13 & 1 \end{bmatrix}$

(2)  $\begin{bmatrix} 1 & -13 \\ 0 & 1 \end{bmatrix}$

(3)  $\begin{bmatrix} 1 & -12 \\ 0 & 1 \end{bmatrix}$

(4)  $\begin{bmatrix} 1 & 0 \\ 12 & 1 \end{bmatrix}$

14. Let  $S = \{\theta \in [-2\pi, 2\pi] ; 2\cos^2\theta + 3\sin\theta = 0\}$ . Then the sum of the elements of S is :

(1)  $\pi$

(2)  $2\pi$

(3)  $\frac{13\pi}{6}$

(4)  $\frac{5\pi}{3}$

15. Let  $f(x) = 15 - |x - 10|$ ;  $x \in \mathbb{R}$ . Then the set of all values of x, at which the function,  $g(x) = f(f(x))$  is not differentiable, is :

(1) (10, 15)

(2) {5, 10, 15, 20}

(3) {10}

(4) {5, 10, 15}

16. The area (in sq. units) of the region

$A = \{(x, y) : x^2 \leq y \leq x + 2\}$  is :

(1)  $\frac{31}{6}$

(2)  $\frac{10}{3}$

(3)  $\frac{9}{2}$

(4)  $\frac{13}{6}$

17. If the line  $y = mx + 7\sqrt{3}$  is normal to the hyperbola  $\frac{x^2}{24} - \frac{y^2}{18} = 1$ , then a value of  $m$  is :

(1)  $\frac{2}{\sqrt{5}}$

(2)  $\frac{3}{\sqrt{5}}$

(3)  $\frac{\sqrt{15}}{2}$

(4)  $\frac{\sqrt{5}}{2}$

18. Let  $\alpha$  and  $\beta$  be the roots of the equation  $x^2 + x + 1 = 0$ . Then for  $y \neq 0$  in  $\mathbb{R}$ ,

$\begin{vmatrix} y+1 & \alpha & \beta \\ \alpha & y+\beta & 1 \\ \beta & 1 & y+\alpha \end{vmatrix}$  is equal to :

(1)  $y(y^2 - 1)$

(2)  $y^3 - 1$

(3)  $y(y^2 - 3)$

(4)  $y^3$

19. The value of  $\cos^2 10^\circ - \cos 10^\circ \cos 50^\circ + \cos^2 50^\circ$  is :

(1)  $\frac{3}{4}$

(2)  $\frac{3}{2}(1 + \cos 20^\circ)$

(3)  $\frac{3}{2}$

(4)  $\frac{3}{4} + \cos 20^\circ$

20. A committee of 11 members is to be formed from 8 males and 5 females. If  $m$  is the number of ways the committee is formed with at least 6 males and  $n$  is the number of ways the committee is formed with at least 3 females, then :

(1)  $m = n = 68$

(2)  $m + n = 68$

(3)  $m = n = 78$

(4)  $n = m - 8$

21. Slope of a line passing through P(2, 3) and intersecting the line,  $x + y = 7$  at a distance of 4 units from P, is :

- (1)  $\frac{\sqrt{7}-1}{\sqrt{7}+1}$  (2)  $\frac{1-\sqrt{7}}{1+\sqrt{7}}$   
 (3)  $\frac{\sqrt{5}-1}{\sqrt{5}+1}$  (4)  $\frac{1-\sqrt{5}}{1+\sqrt{5}}$

22. The value of  $\int_0^{\pi/2} \frac{\sin^3 x}{\sin x + \cos x} dx$  is :

- (1)  $\frac{\pi-2}{4}$  (2)  $\frac{\pi-2}{8}$   
 (3)  $\frac{\pi-1}{4}$  (4)  $\frac{\pi-1}{2}$

23. Let S be the set of all values of x for which the tangent to the curve  $y = f(x) = x^3 - x^2 - 2x$  at (x, y) is parallel to the line segment joining the points (1, f(1)) and (-1, f(-1)), then S is equal to :

- (1)  $\left\{\frac{1}{3}, -1\right\}$  (2)  $\left\{-\frac{1}{3}, 1\right\}$   
 (3)  $\left\{-\frac{1}{3}, -1\right\}$  (4)  $\left\{\frac{1}{3}, 1\right\}$

24. A plane passing through the points (0, -1, 0) and (0, 0, 1) and making an angle  $\frac{\pi}{4}$  with the plane  $y - z + 5 = 0$ , also passes through the point :

- (1)  $(\sqrt{2}, 1, 4)$  (2)  $(\sqrt{2}, -1, 4)$   
 (3)  $(-\sqrt{2}, -1, -4)$  (4)  $(-\sqrt{2}, 1, -4)$

25. The solution of the differential equation

$x \frac{dy}{dx} + 2y = x^2 (x \neq 0)$  with  $y(1) = 1$ , is :

(1)  $y = \frac{4}{5}x^3 + \frac{1}{5x^2}$

(2)  $y = \frac{x^3}{5} + \frac{1}{5x^2}$

(3)  $y = \frac{x^2}{4} + \frac{3}{4x^2}$

(4)  $y = \frac{3}{4}x^2 + \frac{1}{4x^2}$

26. Let the sum of the first  $n$  terms of a non-constant A.P.,  $a_1, a_2, a_3, \dots$  be  $50n + \frac{n(n-7)}{2}A$ , where  $A$  is a constant. If  $d$  is the common difference of this A.P., then the ordered pair  $(d, a_{50})$  is equal to :

(1)  $(50, 50 + 46A)$       (2)  $(A, 50 + 45A)$

(3)  $(A, 50 + 46A)$       (4)  $(50, 50 + 45A)$

27. For any two statements  $p$  and  $q$ , the negation of the expression  $p \vee (\sim p \wedge q)$  is :

(1)  $\sim p \wedge \sim q$

(2)  $\sim p \vee \sim q$

(3)  $p \wedge q$

(4)  $p \leftrightarrow q$

28. If the tangent to the curve,  $y = x^3 + ax - b$  at the point  $(1, -5)$  is perpendicular to the line,  $-x + y + 4 = 0$ , then which one of the following points lies on curve?

(1)  $(-2, 1)$

(2)  $(2, -2)$

(3)  $(2, -1)$

(4)  $(-2, 2)$

29. If the function  $f : \mathbb{R} - \{1, -1\} \rightarrow A$  defined by

$f(x) = \frac{x^2}{1-x^2}$ , is surjective, then A is equal to :

- |                            |                            |
|----------------------------|----------------------------|
| (1) $[0, \infty)$          | (2) $\mathbb{R} - \{-1\}$  |
| (3) $\mathbb{R} - (-1, 0)$ | (4) $\mathbb{R} - [-1, 0)$ |

30. Four persons can hit a target correctly with probabilities  $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$  and  $\frac{1}{8}$  respectively. If all hit at the target independently, then the probability that the target would be hit, is :

- |                     |                      |
|---------------------|----------------------|
| (1) $\frac{7}{32}$  | (2) $\frac{25}{192}$ |
| (3) $\frac{1}{192}$ | (4) $\frac{25}{32}$  |

