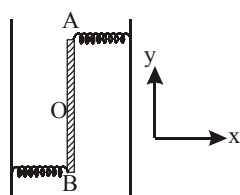


**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019****(Held On Saturday 12<sup>th</sup> JANUARY, 2019) TIME : 09 : 30 AM To 12 : 30 PM****PHYSICS**

1. Two light identical springs of spring constant  $k$  are attached horizontally at the two ends of a uniform horizontal rod AB of length  $\ell$  and mass  $m$ . The rod is pivoted at its centre 'O' and can rotate freely in horizontal plane. The other ends of the two springs are fixed to rigid supports as shown in figure. The rod is gently pushed through a small angle and released. The frequency of resulting oscillation is:

- (1)  $\frac{1}{2\pi}\sqrt{\frac{6k}{m}}$   
 (2)  $\frac{1}{2\pi}\sqrt{\frac{2k}{m}}$   
 (3)  $\frac{1}{2\pi}\sqrt{\frac{k}{m}}$   
 (4)  $\frac{1}{2\pi}\sqrt{\frac{3k}{m}}$



2. A cylinder of radius  $R$  is surrounded by a cylindrical shell of inner radius  $R$  and outer radius  $2R$ . The thermal conductivity of the material of the inner cylinder is  $K_1$  and that of the outer cylinder is  $K_2$ . Assuming no loss of heat, the effective thermal conductivity of the system for heat flowing along the length of the cylinder is:

- (1)  $K_1 + K_2$  (2)  $\frac{K_1 + K_2}{2}$   
 (3)  $\frac{2K_1 + 3K_2}{5}$  (4)  $\frac{K_1 + 3K_2}{4}$

3. A travelling harmonic wave is represented by the equation  $y(x, t) = 10^{-3} \sin(50t + 2x)$ , where  $x$  and  $y$  are in meter and  $t$  is in seconds. Which of the following is a correct statement about the wave?

The wave is propagating along the

- (1) negative  $x$ -axis with speed  $25\text{ms}^{-1}$   
 (2) The wave is propagating along the positive  $x$ -axis with speed  $25\text{ms}^{-1}$   
 (3) The wave is propagating along the positive  $x$ -axis with speed  $100\text{ms}^{-1}$   
 (4) The wave is propagating along the negative  $x$ -axis with speed  $100\text{ms}^{-1}$

- (1) 10 V/m (2) 24 V/m  
(3) 30 V/m (4) 6 V/m

4. A straight rod of length  $L$  extends from  $x = a$  to  $x = L + a$ . The gravitational force is exerts on a point mass ' $m$ ' at  $x = 0$ , if the mass per unit length of the rod is  $A + Bx^2$ , is given by:

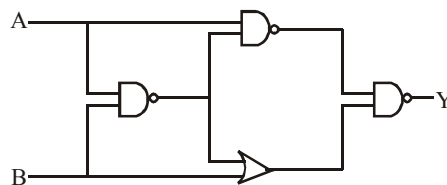
(1)  $Gm \left[ A \left( \frac{1}{a+L} - \frac{1}{a} \right) - BL \right]$

(2)  $Gm \left[ A \left( \frac{1}{a} - \frac{1}{a+L} \right) + BL \right]$

(3)  $Gm \left[ A \left( \frac{1}{a+L} - \frac{1}{a} \right) + BL \right]$

(4)  $Gm \left[ A \left( \frac{1}{a} - \frac{1}{a+L} \right) - BL \right]$

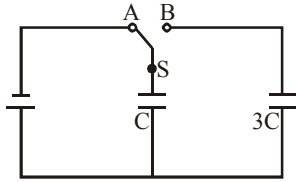
6. The output of the given logic circuit is :



- (1)  $\bar{A}B$   
(2)  $A\bar{B}$   
(3)  $AB + \bar{A}\bar{B}$   
(4)  $A\bar{B} + \bar{A}B$

5. A light wave is incident normally on a glass slab of refractive index 1.5. If 4% of light gets reflected and the amplitude of the electric field of the incident light is 30V/m, then the amplitude of the electric field for the wave propagating in the glass medium will be:

7. In the figure shown, after the switch 'S' is turned from position 'A' to position 'B', the energy dissipated in the circuit in terms of capacitance 'C' and total charge 'Q' is:



- (1)  $\frac{3Q^2}{8C}$     (2)  $\frac{3Q^2}{4C}$     (3)  $\frac{1Q^2}{8C}$     (4)  $\frac{5Q^2}{8C}$

8. A particle of mass  $m$  moves in a circular orbit in a central potential field  $U(r) = \frac{1}{2}kr^2$ . If Bohr's quantization conditions are applied, radii of possible orbitals and energy levels vary with quantum number  $n$  as:

- (1)  $r_n \propto n^2$ ,  $E_n \propto \frac{1}{n^2}$     (2)  $r_n \propto \sqrt{n}$ ,  $E_n \propto \frac{1}{n}$   
 (3)  $r \propto n$ ,  $E \propto n$     (4)  $r_n \propto \sqrt{n}$ ,  $E_n \propto n$

9. Two electric bulbs, rated at (25 W, 220 V) and (100 W, 220 V), are connected in series across a 220 V voltage source. If the 25 W and 100 W bulbs draw powers  $P_1$  and  $P_2$  respectively, then:

- (1)  $P_1 = 9 \text{ W}$ ,  $P_2 = 16 \text{ W}$   
 (2)  $P_1 = 4 \text{ W}$ ,  $P_2 = 16 \text{ W}$   
 (3)  $P_1 = 16 \text{ W}$ ,  $P_2 = 4 \text{ W}$   
 (4)  $P_1 = 16 \text{ W}$ ,  $P_2 = 9 \text{ W}$

10. A satellite of mass  $M$  is in a circular orbit of radius  $R$  about the centre of the earth. A meteorite of the same mass, falling towards the earth, collides with the satellite completely inelastically. The speeds of the satellite and the meteorite are the same, just before the collision. The subsequent motion of the combined body will be :

- (1) in a circular orbit of a different radius
- (2) in the same circular orbit of radius  $R$
- (3) in an elliptical orbit
- (4) such that it escapes to infinity

**11.** Let the moment of inertia of a hollow cylinder of length 30 cm (inner radius 10 cm and outer radius 20 cm), about its axis be  $I$ . The radius of a thin cylinder of the same mass such that its moment of inertia about its axis is also  $I$ , is:  
 (1) 12 cm (2) 18 cm (3) 16 cm (4) 14 cm

**12.** A passenger train of length 60m travels at a speed of 80 km/hr. Another freight train of length 120 m travels at a speed of 30 km/hr. The ratio of times taken by the passenger train to completely cross the freight train when : (i) they are moving in the same direction, and (ii) in the opposite directions is :

- (1)  $\frac{5}{2}$  (2)  $\frac{25}{11}$  (3)  $\frac{3}{2}$  (4)  $\frac{11}{5}$

**13.** An ideal gas occupies a volume of  $2\text{m}^3$  at a pressure of  $3 \times 10^6$  Pa. The energy of the gas is:

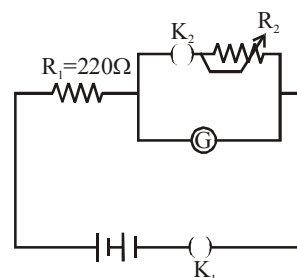
- (1)  $3 \times 10^2$  (2)  $10^8$  J  
 (3)  $6 \times 10^4$  J (4)  $9 \times 10^6$  J

**14.** A 100 V carrier wave is made to vary between 160 V and 40 V by a modulating signal. What is the modulation index?

- (1) 0.6 (2) 0.5 (3) 0.3 (4) 0.4

**15.** The galvanometer deflection, when key  $K_1$  is closed but  $K_2$  is open, equals  $\theta_0$  (see figure). On closing  $K_2$  also and adjusting  $R_2$  to  $5\Omega$ , the

deflection in galvanometer becomes  $\frac{\theta_0}{5}$ . The resistance of the galvanometer is, then, given by [Neglect the internal resistance of battery]:



- (1)  $12\Omega$  (2)  $25\Omega$  (3)  $5\Omega$  (4)  $22\Omega$

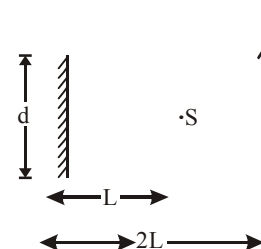
- 16.** A person standing on an open ground hears the sound of a jet aeroplane, coming from north at an angle  $60^\circ$  with ground level. But he finds the aeroplane right vertically above his position. If  $v$  is the speed of sound, speed of the plane is :

- (1)  $\frac{2v}{\sqrt{3}}$                       (2)  $v$   
 (3)  $\frac{v}{2}$                       (4)  $\frac{\sqrt{3}}{2}v$

- 17.** A proton and an  $\alpha$ -particle (with their masses in the ratio of 1:4 and charges in the ratio of 1:2) are accelerated from rest through a potential difference  $V$ . If a uniform magnetic field ( $B$ ) is set up perpendicular to their velocities, the ratio of the radii  $r_p : r_\alpha$  of the circular paths described by them will be :

- (1)  $1:\sqrt{2}$     (2)  $1 : 2$     (3)  $1 : 3$     (4)  $1:\sqrt{3}$

- 18.** A point source of light,  $S$  is placed at a distance  $L$  in front of the centre of plane mirror of width  $d$  which is hanging vertically on a wall. A man walks in front of the mirror along a line parallel to the mirror, at a distance  $2L$  as shown below. The distance over which the man can see the image of the light source in the mirror is :



- |          |                   |
|----------|-------------------|
| (1) $3d$ | (2) $\frac{d}{2}$ |
| (3) $d$  | (4) $2d$          |

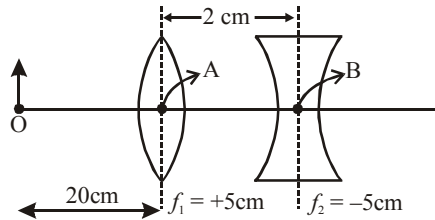
- 19.** The least count of the main scale of a screw gauge is 1 mm. The minimum number of divisions on its circular scale required to measure  $5\mu\text{m}$  diameter of wire is :

- |         |         |
|---------|---------|
| (1) 50  | (2) 100 |
| (3) 200 | (4) 500 |

- 20.** A simple pendulum, made of a string of length  $l$  and a bob of mass  $m$ , is released from a small angle  $\theta_0$ . It strikes a block of mass  $M$ , kept on a horizontal surface at its lowest point of oscillations, elastically. It bounces back and goes up to an angle  $\theta_1$ . Then  $M$  is given by :

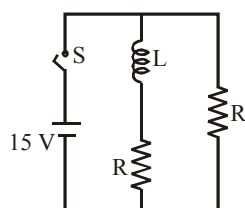
- |  |  |
|--|--|
| (1) $\frac{m}{2} \left( \frac{\theta_0 - \theta_1}{\theta_0 + \theta_1} \right)$ | (2) $\frac{m}{2} \left( \frac{\theta_0 + \theta_1}{\theta_0 - \theta_1} \right)$ |
| (3) $m \left( \frac{\theta_0 + \theta_1}{\theta_0 - \theta_1} \right)$           | (4) $m \left( \frac{\theta_0 - \theta_1}{\theta_0 + \theta_1} \right)$           |

21. What is the position and nature of image formed by lens combination shown in figure? ( $f_1, f_2$  are focal lengths)



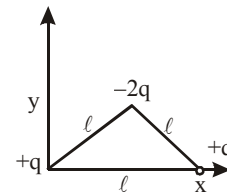
- (1) 70 cm from point B at left; virtual
- (2) 40 cm from point B at right; real
- (3)  $\frac{20}{3}$  cm from point B at right, real
- (4) 70 cm from point B at right, real

22. In the figure shown, a circuit contains two identical resistors with resistance  $R = 5\Omega$  and an inductance with  $L = 2\text{mH}$ . An ideal battery of 15 V is connected in the circuit. What will be the current through the battery long after the switch is closed?



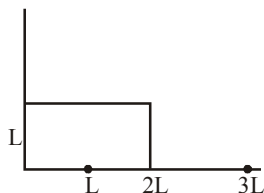
- (1) 6A
- (2) 7.5A
- (3) 5.5A
- (4) 3A

23. Determine the electric dipole moment of the system of three charges, placed on the vertices of an equilateral triangle, as shown in the figure:



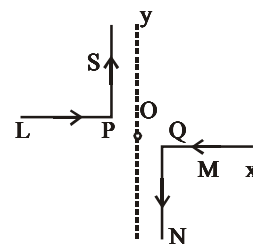
- (1)  $(q\ell)\frac{\hat{i}+\hat{j}}{\sqrt{2}}$
- (2)  $\sqrt{3}q\ell\frac{\hat{j}-\hat{i}}{\sqrt{2}}$
- (3)  $-\sqrt{3}q\ell\hat{j}$
- (4)  $2q\ell\hat{j}$

24. The position vector of the centre of mass  $\vec{r}_{cm}$  of an symmetric uniform bar of negligible area of cross-section as shown in figure is :



- (1)  $\vec{r}_{cm} = \frac{13}{8}L\hat{x} + \frac{5}{8}L\hat{y}$   
 (2)  $\vec{r}_{cm} = \frac{11}{8}L\hat{x} + \frac{3}{8}L\hat{y}$   
 (3)  $\vec{r}_{cm} = \frac{3}{8}L\hat{x} + \frac{11}{8}L\hat{y}$   
 (4)  $\vec{r}_{cm} = \frac{5}{8}L\hat{x} + \frac{13}{8}L\hat{y}$

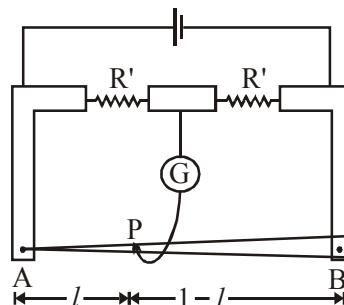
25. As shown in the figure, two infinitely long, identical wires are bent by  $90^\circ$  and placed in such a way that the segments LP and QM are along the x-axis, while segments PS and QN are parallel to the y-axis. If  $OP = OQ = 4\text{cm}$ , and the magnitude of the magnetic field at O is  $10^{-4}\text{ T}$ , and the two wires carry equal currents (see figure), the magnitude of the current in each wire and the direction of the magnetic field at O will be ( $\mu_0 = 4\pi \times 10^{-7}\text{ NA}^{-2}$ ) :



- (1) 40 A, perpendicular into the page  
 (2) 40 A, perpendicular out of the page  
 (3) 20 A, perpendicular out of the page  
 (4) 20 A, perpendicular into the page

26. In a meter bridge, the wire of length 1 m has a non-uniform cross-section such that, the variation  $\frac{dR}{d\ell}$  of its resistance R with length  $\ell$

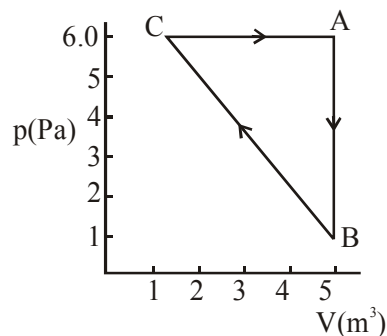
is  $\frac{dR}{d\ell} \propto \frac{1}{\sqrt{\ell}}$ . Two equal resistances are connected as shown in the figure. The galvanometer has zero deflection when the jockey is at point P. What is the length AP?



- (1) 0.25 m (2) 0.3m  
 (3) 0.35 m (4) 0.2 m



27. For the given cyclic process CAB as shown for a gas, the work done is :



- (1) 1 J                      (2) 5 J  
(3) 10 J                    (4) 30 J

28. An ideal battery of 4 V and resistance  $R$  are connected in series in the primary circuit of a potentiometer of length 1 m and resistance  $5\Omega$ . The value of  $R$ , to give a potential difference of 5 mV across 10 cm of potentiometer wire, is :

- (1) 490  $\Omega$                       (2) 480  $\Omega$   
(3) 395  $\Omega$                       (4) 495  $\Omega$

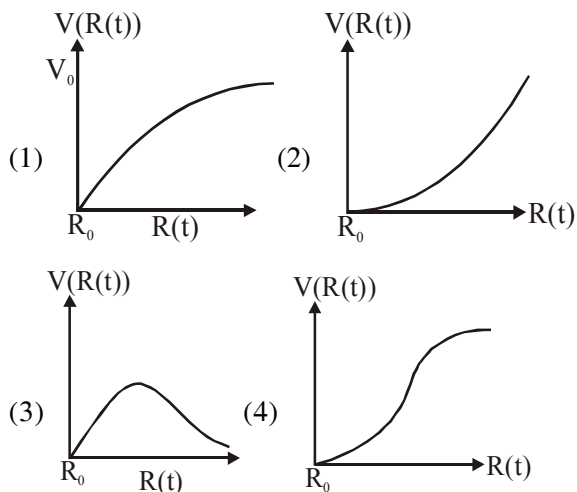
29. A particle A of mass ' $m$ ' and charge ' $q$ ' is accelerated by a potential difference of 50 V. Another particle B of mass ' $4m$ ' and charge ' $q$ ' is accelerated by a potential difference of 2500

V. The ratio of de-Broglie wavelengths  $\frac{\lambda_A}{\lambda_B}$  is

close to :

- (1) 10.00    (2) 14.14    (3) 4.47    (4) 0.07

30. There is a uniform spherically symmetric surface charge density at a distance  $R_0$  from the origin. The charge distribution is initially at rest and starts expanding because of mutual repulsion. The figure that represents best the speed  $V(R(t))$  of the distribution as a function of its instantaneous radius  $R(t)$  is :

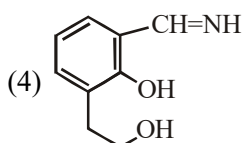
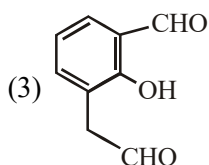
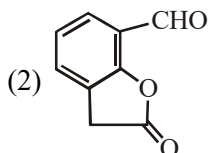
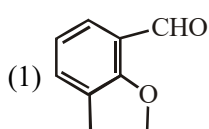
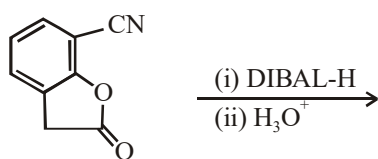


**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019****(Held On Saturday 12<sup>th</sup> JANUARY, 2019) TIME : 09 : 30 AM To 12 : 30 PM****CHEMISTRY**

1. Iodine reacts with concentrated  $\text{HNO}_3$  to yield Y along with other products. The oxidation state of iodine in Y, is :-

(1) 5      (2) 3      (3) 1      (4) 7

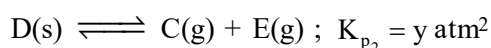
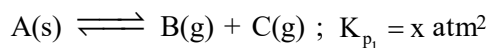
2. The major product of the following reaction is:



3. In a chemical reaction,  $\text{A} + 2\text{B} \xrightleftharpoons{K} 2\text{C} + \text{D}$ , the initial concentration of B was 1.5 times of the concentration of A, but the equilibrium concentrations of A and B were found to be equal. The equilibrium constant(K) for the aforesaid chemical reaction is :

(1) 16      (2) 4      (3) 1      (4)  $\frac{1}{4}$

4. Two solids dissociate as follows



The total pressure when both the solids dissociate simultaneously is :-

(1)  $x^2 + y^2 \text{ atm}$       (2)  $x^2 + y^2 \text{ atm}$   
 (3)  $2(\sqrt{x+y}) \text{ atm}$       (4)  $\sqrt{x+y} \text{ atm}$

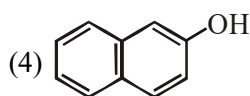
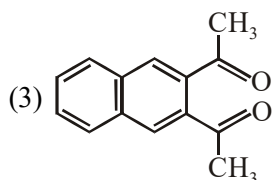
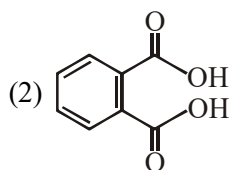
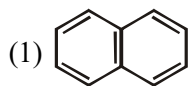
5. Freezing point of a 4% aqueous solution of X is equal to freezing point of 12% aqueous solution of Y. If molecular weight of X is A, then molecular weight of Y is :-

(1) A  
 (2) 3A  
 (3) 4A  
 (4) 2A

6. Poly- $\beta$ -hydroxybutyrate-co- $\beta$ -hydroxyvalerate(PHBV) is a copolymer of\_\_.

- (1) 3-hydroxybutanoic acid and 4-hydroxypentanoic acid
- (2) 2-hydroxybutanoic acid and 3-hydroxypentanoic acid
- (3) 3-hydroxybutanoic acid and 2-hydroxypentanoic acid
- (4) 3-hydroxybutanoic acid and 3-hydroxypentanoic acid

7. Among the following four aromatic compounds, which one will have the lowest melting point ?



8.  $\text{CH}_3\text{CH}_2-\overset{\text{OH}}{\underset{\text{Ph}}{\text{C}}}-\text{CH}_3$  cannot be prepared by :

- (1)  $\text{HCHO} + \text{PhCH}(\text{CH}_3)\text{CH}_2\text{MgX}$
- (2)  $\text{PhCOCH}_2\text{CH}_3 + \text{CH}_3\text{MgX}$
- (3)  $\text{PhCOCH}_3 + \text{CH}_3\text{CH}_2\text{MgX}$
- (4)  $\text{CH}_3\text{CH}_2\text{COCH}_3 + \text{PhMgX}$

9. The volume of gas A is twice than that of gas B. The compressibility factor of gas A is thrice than that of gas B at same temperature. The pressures of the gases for equal number of moles are :

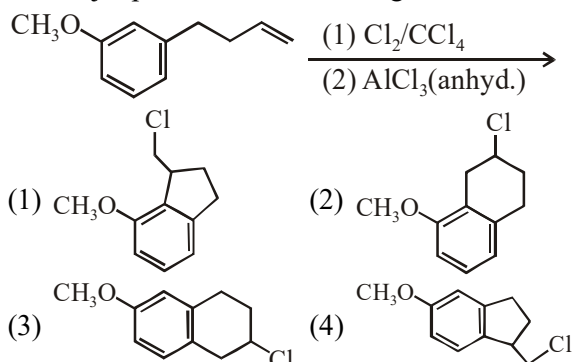
- (1)  $2P_A = 3P_B$
- (2)  $P_A = 3P_B$
- (3)  $P_A = 2P_B$
- (4)  $3P_A = 2P_B$

10. The element with  $Z = 120$  (not yet discovered) will be an/a :

- (1) transition metal
- (2) inner-transition metal
- (3) alkaline earth metal
- (4) alkali metal

11. Decomposition of X exhibits a rate constant of 0.05  $\mu\text{g}/\text{year}$ . How many years are required for the decomposition of 5  $\mu\text{g}$  of X into 2.5  $\mu\text{g}$  ?  
 (1) 50      (2) 25      (3) 20      (4) 40

12. The major product of the following reaction is :



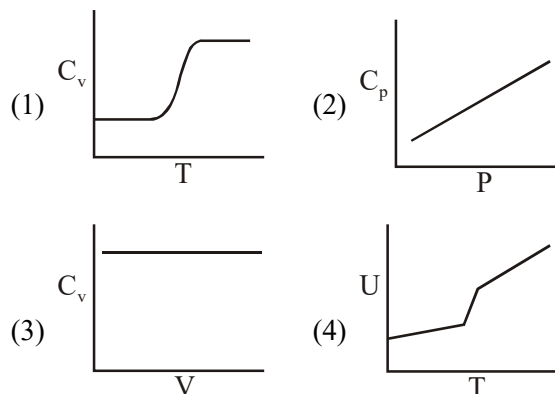
13. Given

Gas	H <sub>2</sub>	CH <sub>4</sub>	CO <sub>2</sub>	SO <sub>2</sub>
Critical Temperature/K	33	190	304	630

On the basis of data given above, predict which of the following gases shows least adsorption on a definite amount of charcoal ?

- (1) H<sub>2</sub>      (2) CH<sub>4</sub>      (3) SO<sub>2</sub>      (4) CO<sub>2</sub>

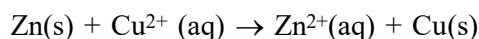
14. For diatomic ideal gas in a closed system, which of the following plots does not correctly describe the relation between various thermodynamic quantities ?



15. The standard electrode potential  $E^\ominus$  and its

temperature coefficient  $\left(\frac{dE^\ominus}{dT}\right)$  for a cell are 2V

and  $-5 \times 10^{-4} \text{ VK}^{-1}$  at 300 K respectively. The cell reaction is



The standard reaction enthalpy ( $\Delta_r H^\ominus$ ) at 300

K in  $\text{kJ mol}^{-1}$  is,

[Use  $R = 8 \text{ J K}^{-1} \text{ mol}^{-1}$  and  $F = 96,000 \text{ C mol}^{-1}$ ]

- (1) -412.8      (2) -384.0  
 (3) 206.4      (4) 192.0

16. The molecule that has minimum/no role in the formation of photochemical smog, is :

- (1)  $\text{CH}_2 = \text{O}$
- (2)  $\text{N}_2$
- (3)  $\text{O}_3$
- (4)  $\text{NO}$

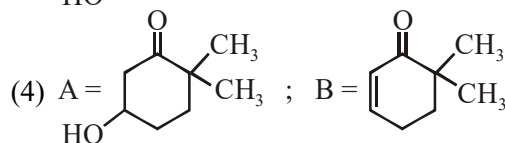
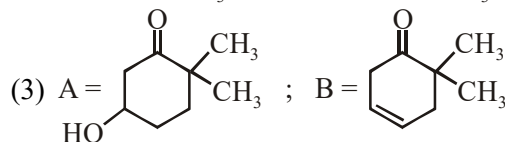
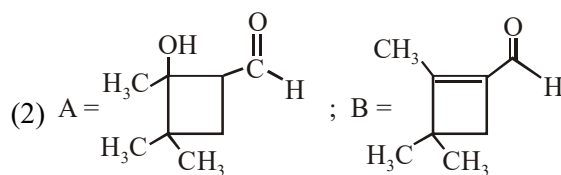
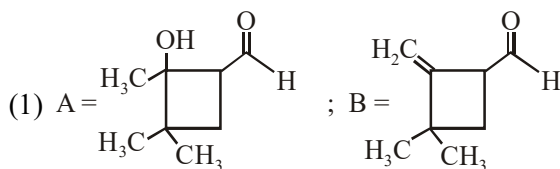
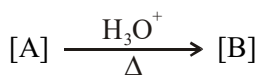
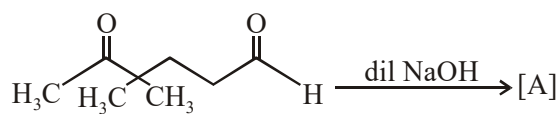
17. In the Hall-Heroult process, aluminium is formed at the cathode. The cathode is made out of :

- (1) Platinum
- (2) Carbon
- (3) Pure aluminium
- (4) Copper

18. Water samples with BOD values of 4 ppm and 18 ppm, respectively, are :

- (1) Highly polluted and Clean
- (2) Highly polluted and Highly polluted
- (3) Clean and Highly polluted
- (4) Clean and Clean

19. In the following reactions, products A and B are :



20. What is the work function of the metal if the light of wavelength  $4000 \text{ \AA}$  generates photoelectrons of velocity  $6 \times 10^5 \text{ ms}^{-1}$  from it ?

(Mass of electron =  $9 \times 10^{-31} \text{ kg}$ )

Velocity of light =  $3 \times 10^8 \text{ ms}^{-1}$

Planck's constant =  $6.626 \times 10^{-34} \text{ Js}$

Charge of electron =  $1.6 \times 10^{-19} \text{ JeV}^{-1}$ )

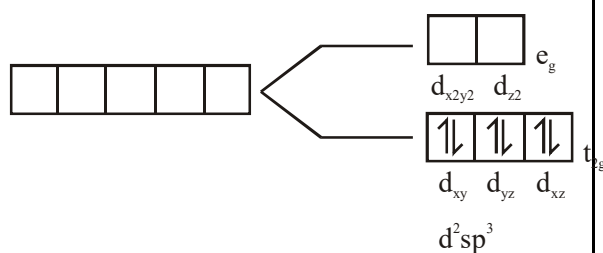
- (1) 0.9 eV
- (2) 4.0 eV
- (3) 2.1 eV
- (4) 3.1 eV

**21.** Among the following compounds most basic amino acid is :

- (1) Lysine
- (2) Asparagine
- (3) Serine
- (4) Histidine

**22.** The metal d-orbitals that are directly facing the ligands in  $K_3[Co(CN)_6]$  are :

- (1)  $d_{xz}$ ,  $d_{yz}$  and  $d_{z^2}$
- (2)  $d_{xy}$ ,  $d_{xz}$  and  $d_{yz}$
- (3)  $d_{xy}$  and  $d_{x^2-y^2}$
- (4)  $d_{x^2-y^2}$  and  $d_{z^2}$



**23.** The hardness of a water sample (in terms of equivalents of  $CaCO_3$ ) containing  $10^{-3}$  M  $CaSO_4$  is :

(molar mass of  $CaSO_4 = 136 \text{ g mol}^{-1}$ )

- (1) 100 ppm
- (2) 50 ppm
- (3) 10 ppm
- (4) 90 ppm

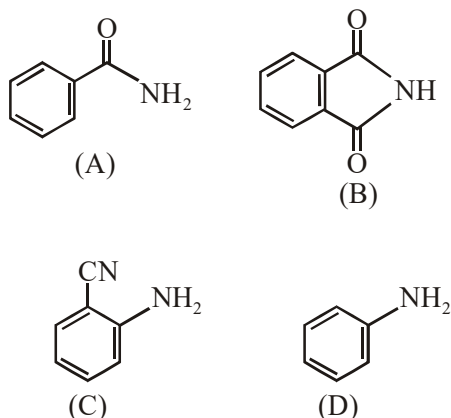
**24.** The correct order for acid strength of compounds  $CH \equiv CH$ ,  $CH_3-C \equiv CH$  and  $CH_2=CH_2$  is as follows :

- (1)  $CH \equiv CH > CH_2 = CH_2 > CH_3-C \equiv CH$
- (2)  $HC \equiv CH > CH_3-C \equiv CH > CH_2 = CH_2$
- (3)  $CH_3-C \equiv CH > CH_2 = CH_2 > HC \equiv CH$
- (4)  $CH_3-C \equiv CH > CH \equiv CH > CH_2 = CH_2$

**25.**  $Mn_2(CO)_{10}$  is an organometallic compound due to the presence of :

- (1) Mn – Mn bond
- (2) Mn – C bond
- (3) Mn – O bond
- (4) C – O bond

**26.** The increasing order of reactivity of the following compounds towards reaction with alkyl halides directly is :

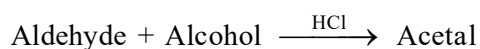


- (1) (B) < (A) < (D) < (C)
- (2) (B) < (A) < (C) < (D)
- (3) (A) < (C) < (D) < (B)
- (4) (A) < (B) < (C) < (D)

27. The pair of metal ions that can give a spinonly magnetic moment of 3.9 BM for the complex  $[M(H_2O)_6]Cl_2$ , is :

- (1)  $Cr^{2+}$  and  $Mn^{2+}$       (2)  $V^{2+}$  and  $Co^{2+}$   
 (3)  $V^{2+}$  and  $Fe^{2+}$       (4)  $Co^{2+}$  and  $Fe^{2+}$

28. In the following reaction



Aldehyde                      Alcohol

HCHO                           $tBuOH$

$CH_3CHO$                       MeOH

The best combinations is :

- (1) HCHO and MeOH  
 (2) HCHO and  $tBuOH$   
 (3)  $CH_3CHO$  and MeOH  
 (4)  $CH_3CHO$  and  $tBuOH$

29. 50 mL of 0.5 M oxalic acid is needed to neutralize 25 mL of sodium hydroxide solution. The amount of NaOH in 50 mL of the given sodium hydroxide solution is :

- (1) 40 g    (2) 20 g    (3) 80 g    (4) 10 g

30. A metal on combustion in excess air forms X, X upon hydrolysis with water yields  $H_2O_2$  and  $O_2$  along with another product. The metal is :

- (1) Rb      (2) Na      (3) Mg      (4) Li



# TEST PAPER OF JEE(MAIN) EXAMINATION – 2019

**(Held On SATURDAY 12<sup>th</sup> JANUARY., 2019) TIME : 09 : 30 AM To 12 : 30 PM**  
**MATHEMATICS**

1. For  $x > 1$ , if  $(2x)^{2y} = 4e^{2x-2y}$ , then  
 $(1 + \log_e 2x)^2 \frac{dy}{dx}$  is equal to :  
 (1)  $\log_e 2x$   
 (2)  $\frac{x \log_e 2x + \log_e 2}{x}$   
 (3)  $x \log_e 2x$   
 (4)  $\frac{x \log_e 2x - \log_e 2}{x}$
  
  2. The sum of the distinct real values of  $\mu$ , for which the vectors,  $\hat{i}\hat{\mu} + \hat{j} + \hat{k}$ ,  $\hat{i} + \hat{\mu}\hat{j} + \hat{k}$ ,  $\hat{i} + \hat{j} + \mu\hat{k}$  are co-planer, is :  
 (1) 2                  (2) 0                  (3) -1                  (4) 1
  
  3. Let S be the set of all points in  $(-\pi, \pi)$  at which the function,  $f(x) = \min \{\sin x, \cos x\}$  is not differentiable. Then S is a subset of which of the following?  
 (1)  $\left\{-\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{3\pi}{4}, \frac{\pi}{4}\right\}$   
 (2)  $\left\{-\frac{3\pi}{4}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{4}\right\}$   
 (3)  $\left\{-\frac{\pi}{2}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{\pi}{2}\right\}$   
 (4)  $\left\{-\frac{\pi}{4}, 0, \frac{\pi}{4}\right\}$
  
  4. The product of three consecutive terms of a G.P. is 512. If 4 is added to each of the first and the second of these terms, the three terms now form an A.P. Then the sum of the original three terms of the given G.P. is  
 (1) 36                                  (2) 24  
 (3) 32                                  (4) 28

5. The integral  $\int \cos(\log_e x) dx$  is equal to :  
(where C is a constant of integration)

- (1)  $\frac{x}{2}[\sin(\log_e x) - \cos(\log_e x)] + C$   
(2)  $\frac{x}{2}[\cos(\log_e x) + \sin(\log_e x)] + C$   
(3)  $x[\cos(\log_e x) + \sin(\log_e x)] + C$   
(4)  $x[\cos(\log_e x) - \sin(\log_e x)] + C$

6. Let  $S_k = \frac{1+2+3+\dots+k}{k}$ . If

$$S_1^2 + S_2^2 + \dots + S_{10}^2 = \frac{5}{12}A, \text{ then } A \text{ is equal to :}$$

- (1) 303      (2) 283      (3) 156      (4) 301

=

7. Let  $S = \{1, 2, 3, \dots, 100\}$ . The number of non-empty subsets A of S such that the product of elements in A is even is :-

- (1)  $2^{50}(2^{50}-1)$       (2)  $2^{100}-1$   
(3)  $2^{50}-1$       (4)  $2^{50}+1$

8. If the sum of the deviations of 50 observations from 30 is 50, then the mean of these observation is :

- (1) 50      (2) 51      (3) 30      (4) 31

9. If a variable line,  $3x+4y-\lambda=0$  is such that the two circles  $x^2 + y^2 - 2x - 2y + 1 = 0$  and  $x^2+y^2-18x-2y+78 = 0$  are on its opposite sides, then the set of all values of  $\lambda$  is the interval :-

- (1) [12, 21]      (2) (2, 17)  
(3) (23, 31)      (4) [13, 23]

10. A ratio of the 5<sup>th</sup> term from the beginning to the 5<sup>th</sup> term from the end in the binomial

expansion of  $\left(2^{\frac{1}{3}} + \frac{1}{2(3)^{\frac{1}{3}}}\right)^{10}$  is :

- (1)  $1 : 4(16)^{\frac{1}{3}}$                       (2)  $1 : 2(6)^{\frac{1}{3}}$   
 (3)  $2(36)^{\frac{1}{3}} : 1$                       (4)  $4(36)^{\frac{1}{3}} : 1$

11. let  $C_1$  and  $C_2$  be the centres of the circles  $x^2+y^2-2x-2y-2=0$  and  $x^2+y^2-6x-6y+14=0$  respectively. If P and Q are the points of intersection of these circles, then the area (in sq. units) of the quadrilateral  $PC_1QC_2$  is :  
 (1) 8                      (2) 6                      (3) 9                      (4) 4

12. In a random experiment, a fair die is rolled until two fours are obtained in succession. The probability that the experiment will end in the fifth throw of the die is equal to :

- (1)  $\frac{150}{6^5}$                       (2)  $\frac{175}{6^5}$                       (3)  $\frac{200}{6^5}$                       (4)  $\frac{225}{6^5}$

13. If the straight line,  $2x-3y+17=0$  is perpendicular to the line passing through the points (7, 17) and (15,  $\beta$ ), then  $\beta$  equals :-

- (1) -5                                      (2)  $-\frac{35}{3}$   
 (3)  $\frac{35}{3}$                                       (4) 5

14. Let f and g be continuous functions on  $[0, a]$  such that  $f(x) = f(a-x)$  and  $g(x)+g(a-x)=4$ ,

then  $\int_0^a f(x)g(x)dx$  is equal to :-

- (1)  $4\int_0^a f(x)dx$                       (2)  $2\int_0^a f(x)dx$   
 (3)  $-3\int_0^a f(x)dx$                       (4)  $\int_0^a f(x)dx$

15. The maximum area (in sq. units) of a rectangle having its base on the x-axis and its other two vertices on the parabola,  $y = 12-x^2$  such that the rectangle lies inside the parabola, is :-

- (1)  $20\sqrt{2}$                       (2)  $18\sqrt{3}$                       (3) 32                      (4) 36

16. The Boolean expression

$((p \wedge q) \vee (p \vee \sim q)) \wedge (\sim p \wedge \sim q)$  is equivalent to:

- (1)  $p \wedge (\sim q)$                       (2)  $p \vee (\sim q)$   
 (3)  $(\sim p) \wedge (\sim q)$               (4)  $p \wedge q$

17.  $\lim_{x \rightarrow \pi/4} \frac{\cot^3 x - \tan x}{\cos(x + \pi/4)}$  is :

- (1) 4              (2)  $8\sqrt{2}$               (3) 8              (4)  $4\sqrt{2}$

18. Considering only the principal values of inverse functions, the set

$$A = \left\{ x \geq 0 : \tan^{-1}(2x) + \tan^{-1}(3x) = \frac{\pi}{4} \right\}$$

- (1) is an empty set  
 (2) Contains more than two elements  
 (3) Contains two elements  
 (4) is a singleton

19. An ordered pair  $(\alpha, \beta)$  for which the system of linear equations

$$(1+\alpha)x + \beta y + z = 2$$

$$\alpha x + (1+\beta)y + z = 3$$

$\alpha x + \beta y + 2z = 2$  has a unique solution is

- (1) (1, -3)                      (2) (-3, 1)  
 (3) (2, 4)                      (4) (-4, 2)

20. The area (in sq. units) of the region bounded by the parabola,  $y = x^2 + 2$  and the lines,  $y = x + 1$ ,  $x = 0$  and  $x = 3$ , is :

- (1)  $\frac{15}{4}$               (2)  $\frac{15}{2}$               (3)  $\frac{21}{2}$               (4)  $\frac{17}{4}$

21. If  $\lambda$  be the ratio of the roots of the quadratic equation in  $x$ ,  $3m^2x^2+m(m-4)x+2=0$ , then the least value of  $m$  for which  $\lambda+\frac{1}{\lambda}=1$ , is :
- (1)  $2-\sqrt{3}$                       (2)  $4-3\sqrt{2}$   
 (3)  $-2+\sqrt{2}$                       (4)  $4-2\sqrt{3}$
22. If the vertices of a hyperbola be at  $(-2, 0)$  and  $(2, 0)$  and one of its foci be at  $(-3, 0)$ , then which one of the following points does not lie on this hyperbola?
- (1)  $(4, \sqrt{15})$                       (2)  $(-6, 2\sqrt{10})$   
 (3)  $(6, 5\sqrt{2})$                       (4)  $(2\sqrt{6}, 5)$
23. If  $\frac{z-\alpha}{z+\alpha}$  ( $\alpha \in \mathbb{R}$ ) is a purely imaginary number and  $|z|=2$ , then a value of  $\alpha$  is :
- (1) 1                      (2) 2                      (3)  $\sqrt{2}$                       (4)  $\frac{1}{2}$
24. Let  $P(4, -4)$  and  $Q(9, 6)$  be two points on the parabola,  $y^2=4x$  and let  $X$  be any point on the arc  $POQ$  of this parabola, where  $O$  is the vertex of this parabola, such that the area of  $\Delta PXQ$  is maximum. Then this maximum area (in sq. units) is :
- (1)  $\frac{125}{4}$                       (2)  $\frac{125}{2}$                       (3)  $\frac{625}{4}$                       (4)  $\frac{75}{2}$
25. the perpendicular distance from the origin to the plane containing the two lines,  $\frac{x+2}{3}=\frac{y-2}{5}=\frac{z+5}{7}$  and  $\frac{x-1}{1}=\frac{y-4}{4}=\frac{z+4}{7}$ , is:
- (1)  $\frac{11}{\sqrt{6}}$                       (2)  $6\sqrt{11}$                       (3) 11                      (4)  $11\sqrt{6}$

26. The maximum value of  $3\cos\theta + 5\sin\left(\theta - \frac{\pi}{6}\right)$  for any real value of  $\theta$  is :

(1)  $\sqrt{19}$     (2)  $\frac{\sqrt{79}}{2}$     (3)  $\sqrt{31}$     (4)  $\sqrt{34}$

27. A tetrahedron has vertices  $P(1, 2, 1)$ ,  $Q(2, 1, 3)$ ,  $R(-1, 1, 2)$  and  $O(0, 0, 0)$ . The angle between the faces  $OPQ$  and  $PQR$  is :

(1)  $\cos^{-1}\left(\frac{9}{35}\right)$     (2)  $\cos^{-1}\left(\frac{19}{35}\right)$   
 (3)  $\cos^{-1}\left(\frac{17}{31}\right)$     (4)  $\cos^{-1}\left(\frac{7}{31}\right)$

29. Let  $P = \begin{bmatrix} 1 & 0 & 0 \\ 3 & 1 & 0 \\ 9 & 3 & 1 \end{bmatrix}$  and  $Q = [q_{ij}]$  be two  $3 \times 3$

matrices such that  $Q - P^5 = I_3$ . Then  $\frac{q_{21} + q_{31}}{q_{32}}$  is

equal to:

(1) 15    (2) 9    (3) 135    (4) 10

28. Let  $y = y(x)$  be the solution of the differential equation,  $x \frac{dy}{dx} + y = x \log_e x$ , ( $x > 1$ ). If  $2y(2) = \log_e 4 - 1$ , then  $y(e)$  is equal to :-

(1)  $\frac{e^2}{4}$     (2)  $\frac{e}{4}$     (3)  $-\frac{e}{2}$     (4)  $-\frac{e^2}{2}$

30. Consider three boxes, each containing 10 balls labelled 1,2,...,10. Suppose one ball is randomly drawn from each of the boxes. Denote by  $n_i$ , the label of the ball drawn from the  $i^{\text{th}}$  box, ( $i = 1, 2, 3$ ). Then, the number of ways in which the balls can be chosen such that  $n_1 < n_2 < n_3$  is :
- (1) 82      (2) 240      (3) 164      (4) 120