

The Fast Fourier Transform on GPUs

Some images in this part by Mario Garrido



The Fast Fourier Transform (FFT)

Fast implementation of the Fourier Transform

Converts a signal to frequency space

Very important algorithm in signal processing



FFT

Computes the Discrete Fourier Transform (DFT) of a signal of N samples in NlogN time

Many variants. Cooley-Tukey (1965) most common.



DFT

The Discrete Fourier Transform

Converts a signal to frequency space

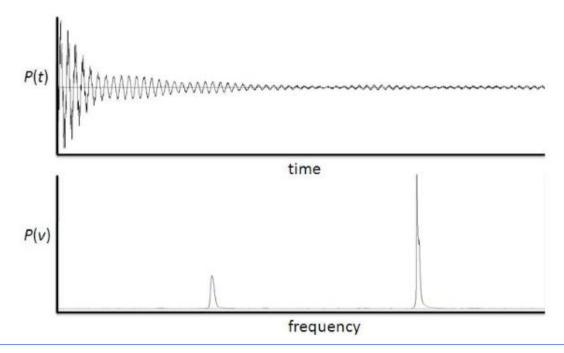
Essentially a series of convolutions with harmonic functions of varying frequency

$$X_k = \sum_{n=0}^{N-1} x_n e^{-i2\pi k \frac{n}{N}}$$
 $k = 0, \dots, N-1.$



DFT example

1D signal to frequency space (e.g. sound)





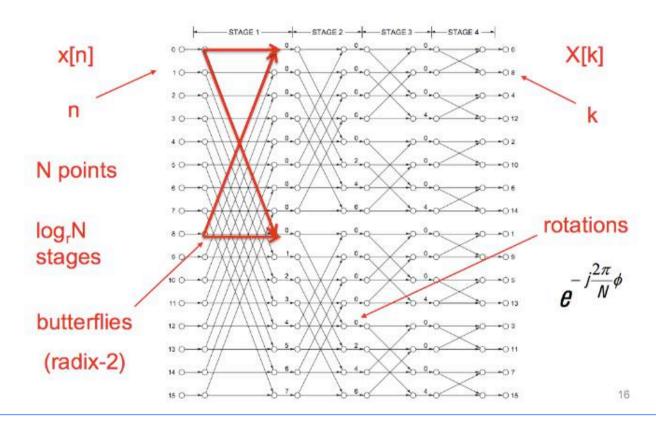
DFT example

2D signal to frequency space (e.g. images)





FFT flow graph (Radix-2)



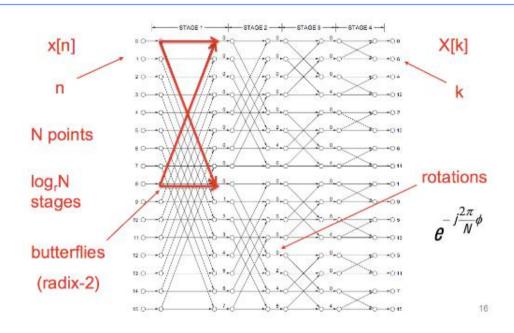


FFT in parallel

Pretty parallel from the start!

BUT very large jumps in memory for some stages!





"Large" stages: Can not be performed within shared memory! "Small" stages: Can be performed within shared memory!



Possible approach

Perform all "small" stages in a single run, using shared memory. Very fast!

Perform all "large" stages as separate kernel runs.



NVidia "made your bed" for FFT

cufft, CUDA FFT, included in all CUDA distributions

A well optimized CUDA implementation



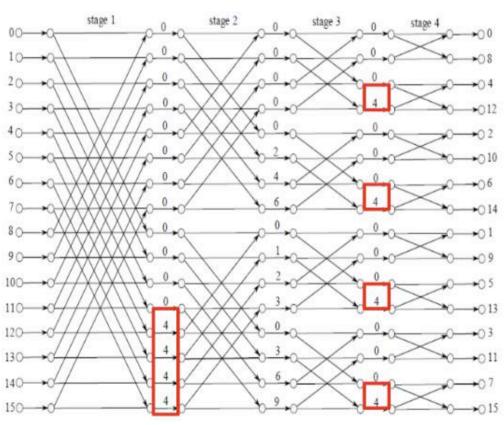
But there are alternatives!

Optimization approaches made in a specific implementation

2013 publication: "New Radix-2 and Radix-2 Constant Geometry Fast Fourier Transform Lagorithms for GPUs", Ambuluri, Garrido, Ogniewski, Ragnemalm, Caffarena

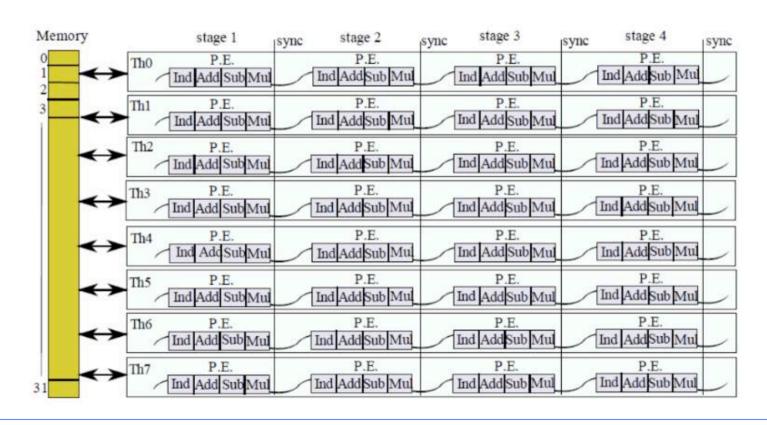


Simplify - use Radix-2²



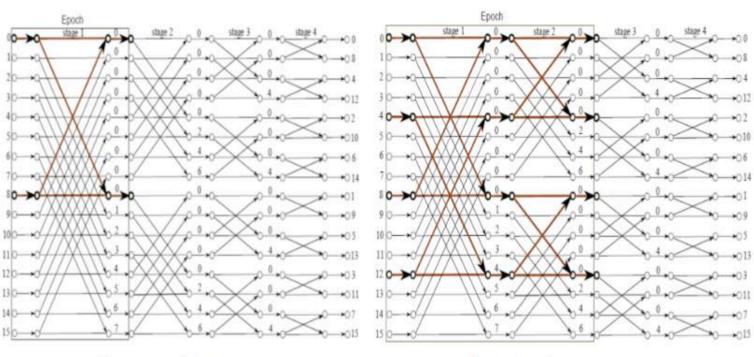


Use shared memory





Reduce synch. points

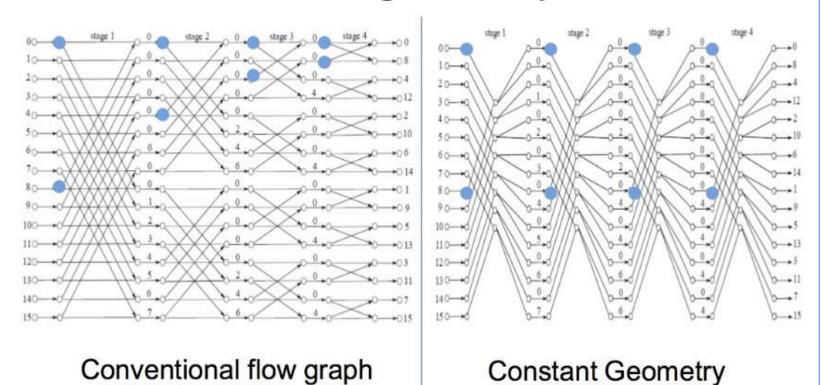


2-word group

4-word group



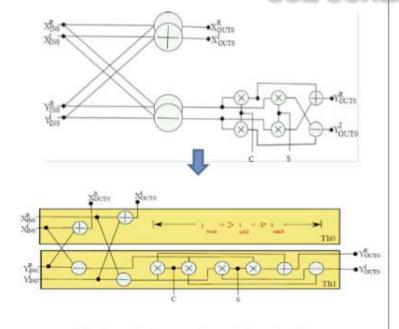
Reduce index calculations: Constant geometry FFT



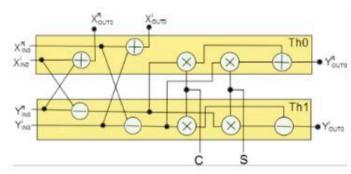


Balance load between threads

USE SCHEDULING



Unbalanced scheduling



Balanced scheduling



Result:

Our implementation was significantly faster that NVidia's cufft - that is, for the sizes we tried

Best paper award at the conference

Algorithms can often be modified more than it seems