Appendix A.
Two long proofs