

# Decision tree learning example

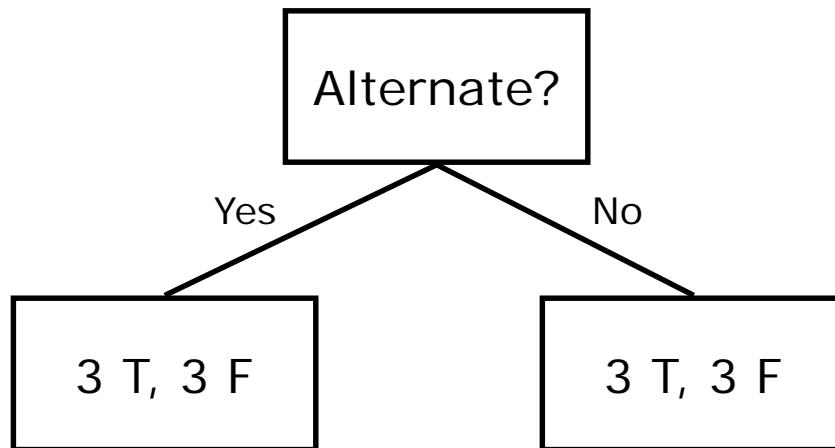
Example	Attributes										Target
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	<i>WillWait</i>
$X_1$	<i>T</i>	<i>F</i>	<i>F</i>	<i>T</i>	<i>Some</i>	<i>\$\$\$</i>	<i>F</i>	<i>T</i>	<i>French</i>	<i>0-10</i>	<i>T</i>
$X_2$	<i>T</i>	<i>F</i>	<i>F</i>	<i>T</i>	<i>Full</i>	<i>\$</i>	<i>F</i>	<i>F</i>	<i>Thai</i>	<i>30-60</i>	<i>F</i>
$X_3$	<i>F</i>	<i>T</i>	<i>F</i>	<i>F</i>	<i>Some</i>	<i>\$</i>	<i>F</i>	<i>F</i>	<i>Burger</i>	<i>0-10</i>	<i>T</i>
$X_4$	<i>T</i>	<i>F</i>	<i>T</i>	<i>T</i>	<i>Full</i>	<i>\$</i>	<i>F</i>	<i>F</i>	<i>Thai</i>	<i>10-30</i>	<i>T</i>
$X_5$	<i>T</i>	<i>F</i>	<i>T</i>	<i>F</i>	<i>Full</i>	<i>\$\$\$</i>	<i>F</i>	<i>T</i>	<i>French</i>	<i>&gt;60</i>	<i>F</i>
$X_6$	<i>F</i>	<i>T</i>	<i>F</i>	<i>T</i>	<i>Some</i>	<i>\$\$</i>	<i>T</i>	<i>T</i>	<i>Italian</i>	<i>0-10</i>	<i>T</i>
$X_7$	<i>F</i>	<i>T</i>	<i>F</i>	<i>F</i>	<i>None</i>	<i>\$</i>	<i>T</i>	<i>F</i>	<i>Burger</i>	<i>0-10</i>	<i>F</i>
$X_8$	<i>F</i>	<i>F</i>	<i>F</i>	<i>T</i>	<i>Some</i>	<i>\$\$</i>	<i>T</i>	<i>T</i>	<i>Thai</i>	<i>0-10</i>	<i>T</i>
$X_9$	<i>F</i>	<i>T</i>	<i>T</i>	<i>F</i>	<i>Full</i>	<i>\$</i>	<i>T</i>	<i>F</i>	<i>Burger</i>	<i>&gt;60</i>	<i>F</i>
$X_{10}$	<i>T</i>	<i>T</i>	<i>T</i>	<i>T</i>	<i>Full</i>	<i>\$\$\$</i>	<i>F</i>	<i>T</i>	<i>Italian</i>	<i>10-30</i>	<i>F</i>
$X_{11}$	<i>F</i>	<i>F</i>	<i>F</i>	<i>F</i>	<i>None</i>	<i>\$</i>	<i>F</i>	<i>F</i>	<i>Thai</i>	<i>0-10</i>	<i>F</i>
$X_{12}$	<i>T</i>	<i>T</i>	<i>T</i>	<i>T</i>	<i>Full</i>	<i>\$</i>	<i>F</i>	<i>F</i>	<i>Burger</i>	<i>30-60</i>	<i>T</i>

T = True, F = False

$$\text{Entropy} = -\left(\frac{6}{12}\right)\log_2\left(\frac{6}{12}\right) - \left(\frac{6}{12}\right)\log_2\left(\frac{6}{12}\right) = 1$$

6 True,  
6 False

# Decision tree learning example

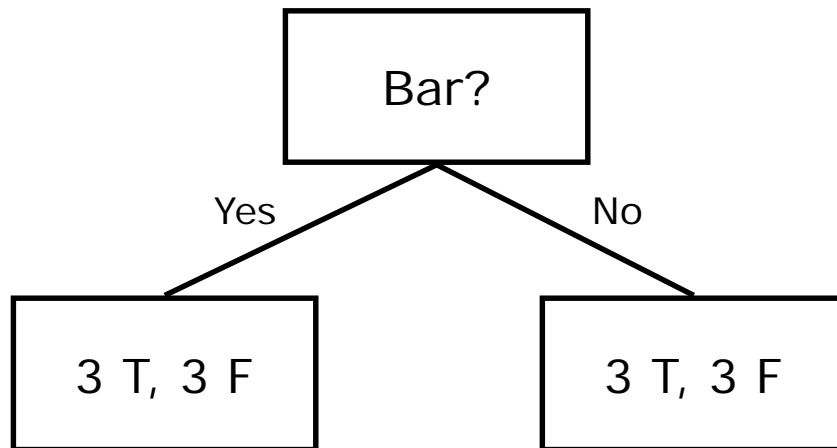


Example	Attributes										Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
X <sub>1</sub>	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
X <sub>2</sub>	T	F	F	T	Full	\$	F	F	Thai	30-60	F
X <sub>3</sub>	F	T	F	F	Some	\$	F	F	Burger	0-10	T
X <sub>4</sub>	T	F	T	T	Full	\$	F	F	Thai	10-30	T
X <sub>5</sub>	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
X <sub>6</sub>	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
X <sub>7</sub>	F	T	F	F	None	\$	T	F	Burger	0-10	F
X <sub>8</sub>	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
X <sub>9</sub>	F	T	T	F	Full	\$	T	F	Burger	>60	F
X <sub>10</sub>	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
X <sub>11</sub>	F	F	F	F	None	\$	F	F	Thai	0-10	F
X <sub>12</sub>	T	T	T	T	Full	\$	F	F	Burger	30-60	T

$$\begin{aligned}
 \text{Remainder}(\text{Alternate}) &= \frac{6}{12} \left[ -\left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) - \left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) \right] \\
 &\quad + \frac{6}{12} \left[ -\left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) - \left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) \right] = 1
 \end{aligned}$$

$$\text{Gain}(\text{Alternate}) = 1 - 1 = 0$$

# Decision tree learning example

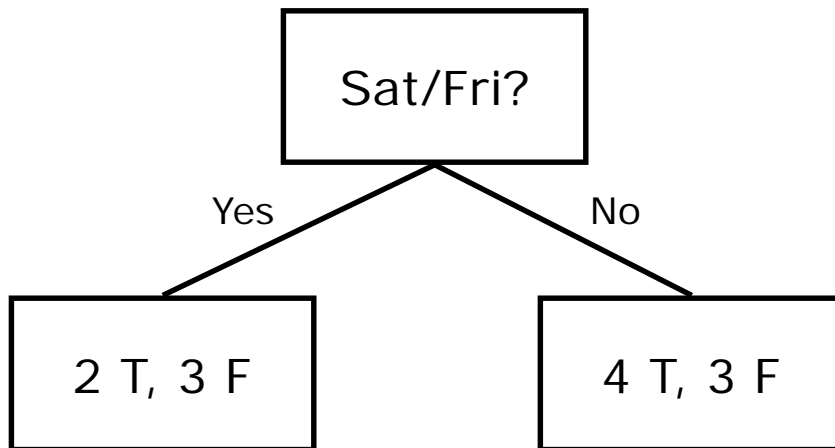


Example	Attributes										Target
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	<i>WillWait</i>
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T

$$\begin{aligned}
 \text{Remainder}(\text{bar}) &= \frac{6}{12} \left[ -\left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) - \left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) \right] \\
 &\quad + \frac{6}{12} \left[ -\left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) - \left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) \right] = 1
 \end{aligned}$$

$$\text{Gain}(\text{Bar}) = 1 - 1 = 0$$

# Decision tree learning example

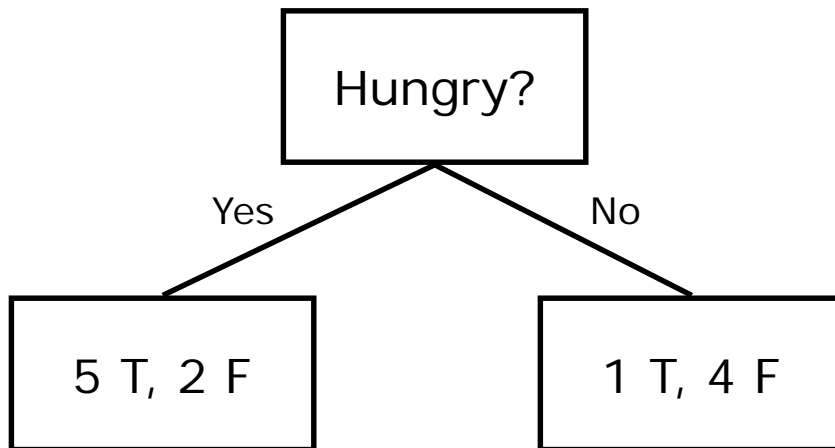


Example	Attributes										Target
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	<i>WillWait</i>
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T

$$\begin{aligned}
 \text{Remainder}(\text{Sat} / \text{Fri}) &= \frac{5}{12} \left[ -\left(\frac{2}{5}\right) \log_2 \left(\frac{2}{5}\right) - \left(\frac{3}{5}\right) \log_2 \left(\frac{3}{5}\right) \right] \\
 &\quad + \frac{7}{12} \left[ -\left(\frac{4}{7}\right) \log_2 \left(\frac{4}{7}\right) - \left(\frac{3}{7}\right) \log_2 \left(\frac{3}{7}\right) \right] = 0.9793
 \end{aligned}$$

$$\text{Gain}(\text{Sat/Fri}) = 1 - 0.9793 = 0.0207$$

# Decision tree learning example

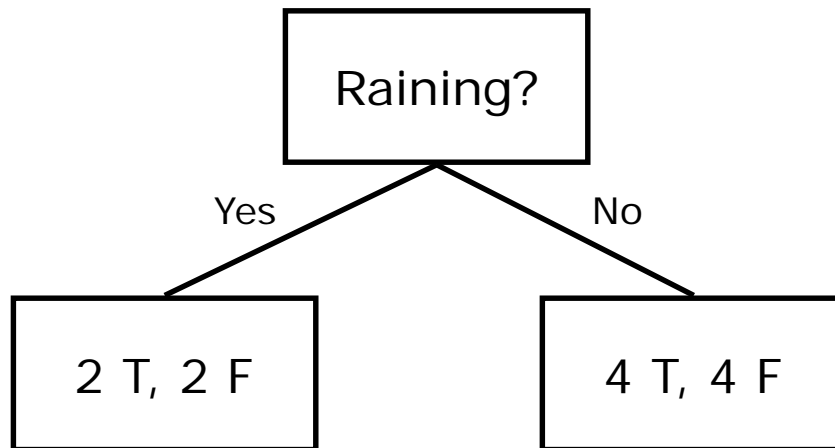


Example	Attributes										Target	
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	<i>Will</i>	<i>Wait</i>
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T	
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F	
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T	
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T	
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F	
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T	
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F	
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T	
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F	
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F	
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F	
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T	

$$\begin{aligned}
 \text{Remainder}(\text{Hungry}) &= \frac{7}{12} \left[ -\left(\frac{5}{7}\right) \log_2 \left(\frac{5}{7}\right) - \left(\frac{2}{7}\right) \log_2 \left(\frac{2}{7}\right) \right] \\
 &\quad + \frac{5}{12} \left[ -\left(\frac{1}{5}\right) \log_2 \left(\frac{1}{5}\right) - \left(\frac{4}{5}\right) \log_2 \left(\frac{4}{5}\right) \right] = 0.8043
 \end{aligned}$$

$$\text{Gain}(\text{Hungry}) = 1 - 0.8043 = 0.1957$$

# Decision tree learning example

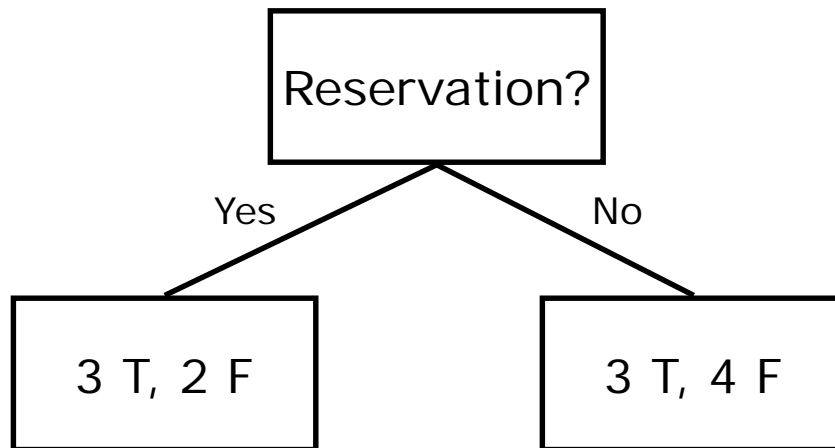


Example	Attributes										Target	
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	Will	Wait
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T	
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F	
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T	
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T	
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F	
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T	
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F	
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T	
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F	
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F	
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F	
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T	

$$\begin{aligned}
 \text{Remainder}(\text{Raining}) &= \frac{4}{12} \left[ -\left(\frac{2}{4}\right) \log_2 \left(\frac{2}{4}\right) - \left(\frac{2}{4}\right) \log_2 \left(\frac{2}{4}\right) \right] \\
 &\quad + \frac{8}{12} \left[ -\left(\frac{4}{8}\right) \log_2 \left(\frac{4}{8}\right) - \left(\frac{4}{8}\right) \log_2 \left(\frac{4}{8}\right) \right] = 1
 \end{aligned}$$

$$\text{Gain}(\text{Raining}) = 1 - 1 = 0$$

# Decision tree learning example

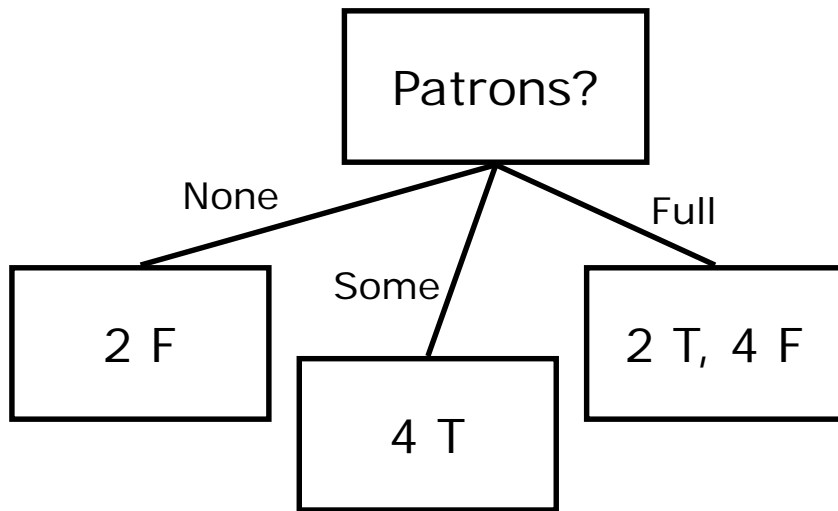


Example	Attributes										Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T

$$\begin{aligned}
 \text{Remainder(Reservation)} &= \frac{5}{12} \left[ -\left(\frac{3}{5}\right) \log_2 \left(\frac{3}{5}\right) - \left(\frac{2}{5}\right) \log_2 \left(\frac{2}{5}\right) \right] \\
 &\quad + \frac{7}{12} \left[ -\left(\frac{3}{7}\right) \log_2 \left(\frac{3}{7}\right) - \left(\frac{4}{7}\right) \log_2 \left(\frac{4}{7}\right) \right] = 0.9793
 \end{aligned}$$

$$\text{Gain(Reservation)} = 1 - 0.9793 = 0.0207$$

# Decision tree learning example



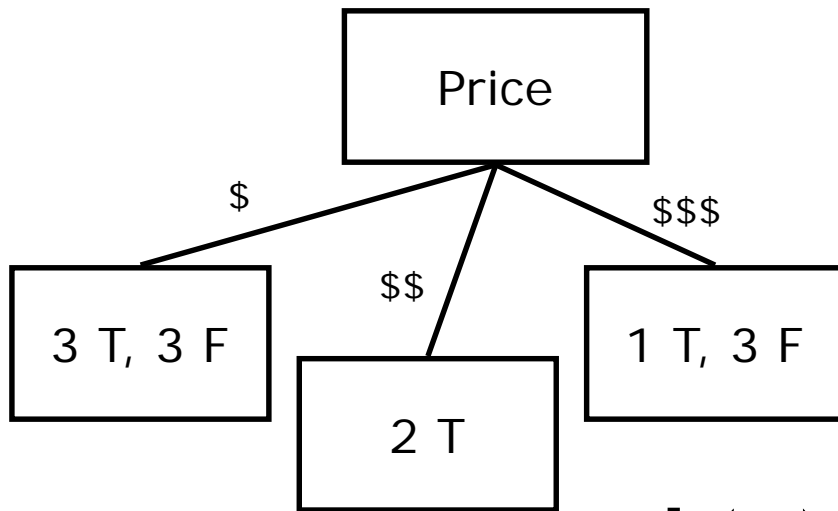
Example	Attributes										Target	
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	Will	Wait
X <sub>1</sub>	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T	
X <sub>2</sub>	T	F	F	T	Full	\$	F	F	Thai	30-60	F	
X <sub>3</sub>	F	T	F	F	Some	\$	F	F	Burger	0-10	T	
X <sub>4</sub>	T	F	T	T	Full	\$	F	F	Thai	10-30	T	
X <sub>5</sub>	T	F	T	F	Full	\$\$\$	F	T	French	>60	F	
X <sub>6</sub>	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T	
X <sub>7</sub>	F	T	F	F	None	\$	T	F	Burger	0-10	F	
X <sub>8</sub>	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T	
X <sub>9</sub>	F	T	T	F	Full	\$	T	F	Burger	>60	F	
X <sub>10</sub>	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F	
X <sub>11</sub>	F	F	F	F	None	\$	F	F	Thai	0-10	F	
X <sub>12</sub>	T	T	T	T	Full	\$	F	F	Burger	30-60	T	

$$\begin{aligned}
 \text{Remainder}(\text{Patron}) &= \frac{2}{12} \left[ -\left(\frac{0}{2}\right) \log_2 \left(\frac{0}{2}\right) - \left(\frac{2}{2}\right) \log_2 \left(\frac{2}{2}\right) \right] \\
 &+ \frac{4}{12} \left[ -\left(\frac{4}{4}\right) \log_2 \left(\frac{4}{4}\right) - \left(\frac{0}{4}\right) \log_2 \left(\frac{0}{4}\right) \right] + \frac{6}{12} \left[ -\left(\frac{2}{6}\right) \log_2 \left(\frac{2}{6}\right) - \left(\frac{4}{6}\right) \log_2 \left(\frac{4}{6}\right) \right] \\
 &= 0.459
 \end{aligned}$$

$$\text{Gain}(\text{Patron}) = 1 - 0.459 = 0.541$$



# Decision tree learning example



Example	Attributes										Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T

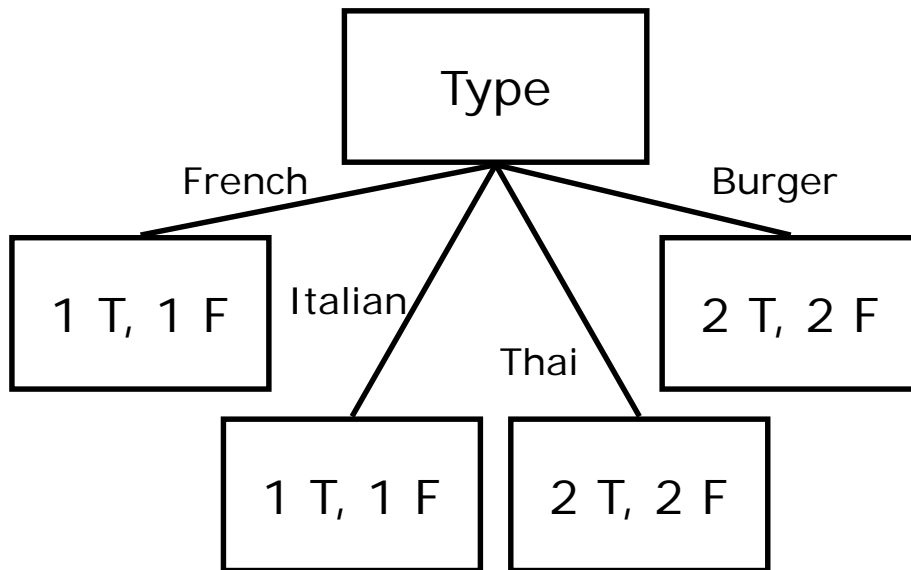
$$\text{Remainder}(\text{Price}) = \frac{6}{12} \left[ -\left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) - \left(\frac{3}{6}\right) \log_2 \left(\frac{3}{6}\right) \right]$$

$$+ \frac{2}{12} \left[ -\left(\frac{2}{2}\right) \log_2 \left(\frac{2}{2}\right) - \left(\frac{0}{2}\right) \log_2 \left(\frac{0}{2}\right) \right]$$

$$+ \frac{4}{12} \left[ -\left(\frac{1}{4}\right) \log_2 \left(\frac{1}{4}\right) - \left(\frac{3}{4}\right) \log_2 \left(\frac{3}{4}\right) \right] = 0.7704$$

$$\text{Gain}(\text{Remainder}) = 1 - 0.7704 = 0.2296$$

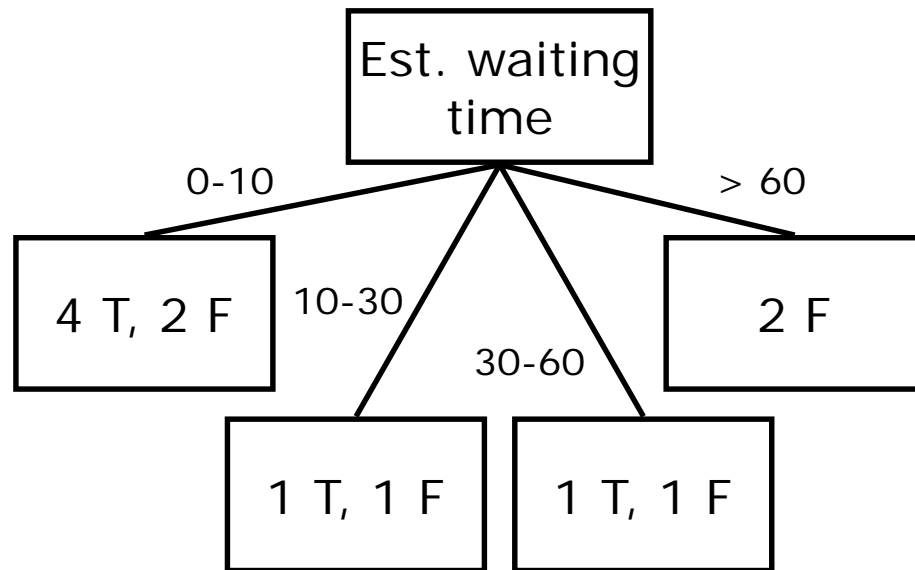
# Decision tree learning example



Example	Attributes										Target	
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait	
X <sub>1</sub>	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T	
X <sub>2</sub>	T	F	F	T	Full	\$	F	F	Thai	30-60	F	
X <sub>3</sub>	F	T	F	F	Some	\$	F	F	Burger	0-10	T	
X <sub>4</sub>	T	F	T	T	Full	\$	F	F	Thai	10-30	T	
X <sub>5</sub>	T	F	T	F	Full	\$\$\$	F	T	French	>60	F	
X <sub>6</sub>	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T	
X <sub>7</sub>	F	T	F	F	None	\$	T	F	Burger	0-10	F	
X <sub>8</sub>	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T	
X <sub>9</sub>	F	T	T	F	Full	\$	T	F	Burger	>60	F	
X <sub>10</sub>	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F	
X <sub>11</sub>	F	F	F	F	None	\$	F	F	Thai	0-10	F	
X <sub>12</sub>	T	T	T	T	Full	\$	F	F	Burger	30-60	T	

$$\begin{aligned}
 \text{Remainder}(\text{Type}) &= \frac{2}{12} \left[ -\left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) \right] \\
 &+ \frac{2}{12} \left[ -\left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) \right] \\
 &+ \frac{4}{12} \left[ -\left(\frac{2}{4}\right) \log_2 \left(\frac{2}{4}\right) - \left(\frac{2}{4}\right) \log_2 \left(\frac{2}{4}\right) \right] + \frac{4}{12} \left[ -\left(\frac{2}{4}\right) \log_2 \left(\frac{2}{4}\right) - \left(\frac{2}{4}\right) \log_2 \left(\frac{2}{4}\right) \right] = 1 \\
 \text{Gain}(\text{Type}) &= 1 - 1 = 0
 \end{aligned}$$

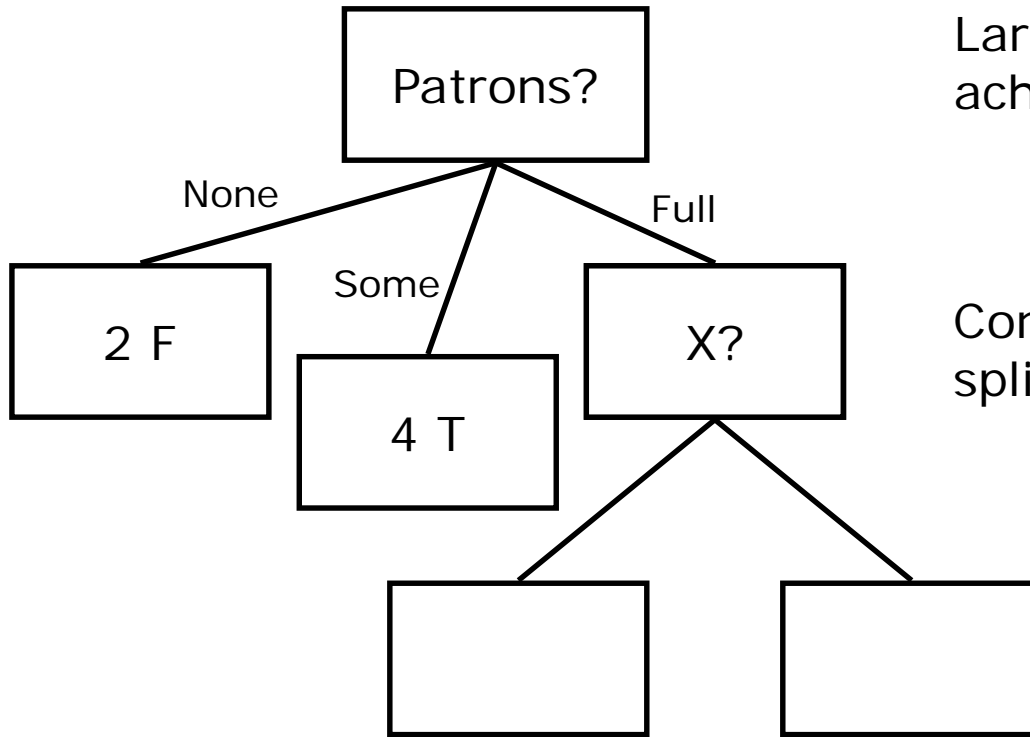
# Decision tree learning example



Example	Attributes										Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
X <sub>1</sub>	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
X <sub>2</sub>	T	F	F	T	Full	\$	F	F	Thai	30-60	F
X <sub>3</sub>	F	T	F	F	Some	\$	F	F	Burger	0-10	T
X <sub>4</sub>	T	F	T	T	Full	\$	F	F	Thai	10-30	T
X <sub>5</sub>	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
X <sub>6</sub>	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
X <sub>7</sub>	F	T	F	F	None	\$	T	F	Burger	0-10	F
X <sub>8</sub>	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
X <sub>9</sub>	F	T	T	F	Full	\$	T	F	Burger	>60	F
X <sub>10</sub>	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
X <sub>11</sub>	F	F	F	F	None	\$	F	F	Thai	0-10	F
X <sub>12</sub>	T	T	T	T	Full	\$	F	F	Burger	30-60	T

$$\begin{aligned}
 \text{Remainder}(\text{Wait}) &= \frac{6}{12} \left[ -\left(\frac{4}{6}\right) \log_2 \left(\frac{4}{6}\right) - \left(\frac{2}{6}\right) \log_2 \left(\frac{2}{6}\right) \right] \\
 &+ \frac{2}{12} \left[ -\left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) \right] \\
 &+ \frac{2}{12} \left[ -\left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) \log_2 \left(\frac{1}{2}\right) \right] + \frac{2}{12} \left[ -\left(\frac{0}{2}\right) \log_2 \left(\frac{0}{2}\right) - \left(\frac{2}{2}\right) \log_2 \left(\frac{2}{2}\right) \right] = 0.7925 \\
 \text{Gain}(\text{Wait}) &= 1 - 0.7925 = 0.2075
 \end{aligned}$$

# Decision tree learning example

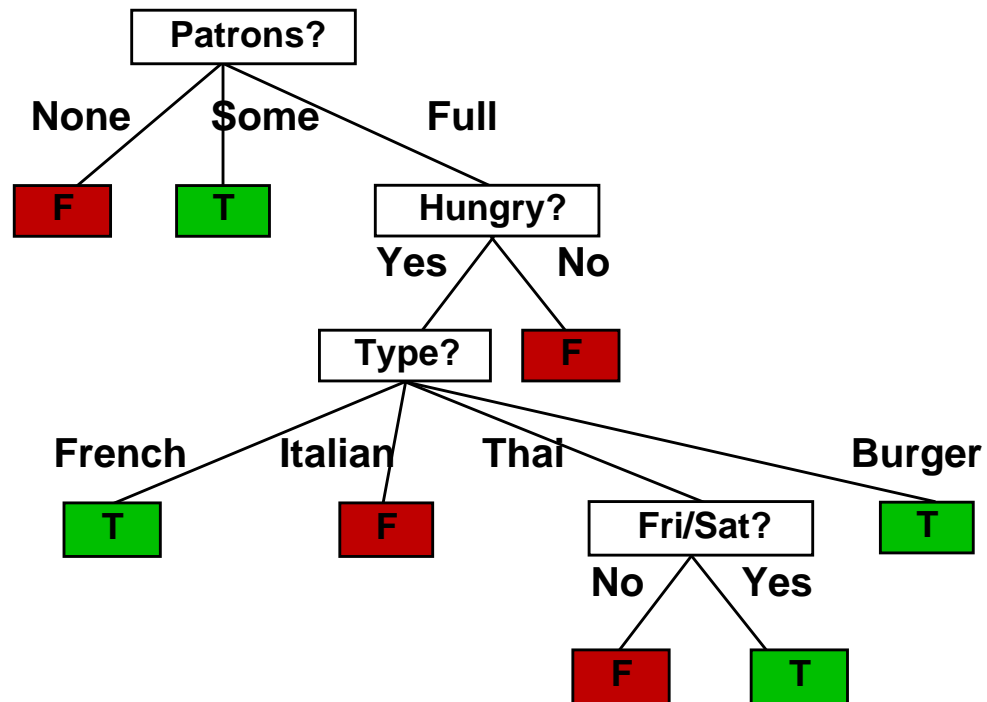


Largest entropy decrease (0.541)  
achieved by splitting on Patrons.

Continue like this, making new  
splits, always purifying nodes.

## Example contd.

Decision tree learned from the 12 examples:



Substantially simpler than “true” tree—a more complex hypothesis isn’t justified by small amount of data