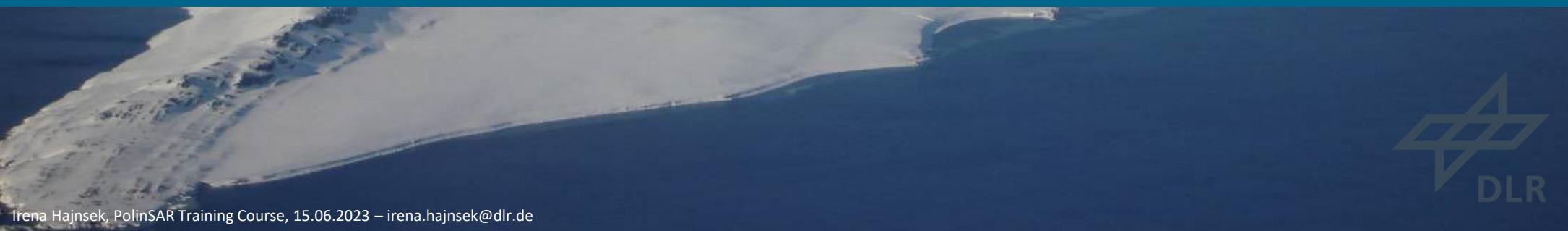


PolinSAR Training Course 2023

Application: Snow Height Estimation

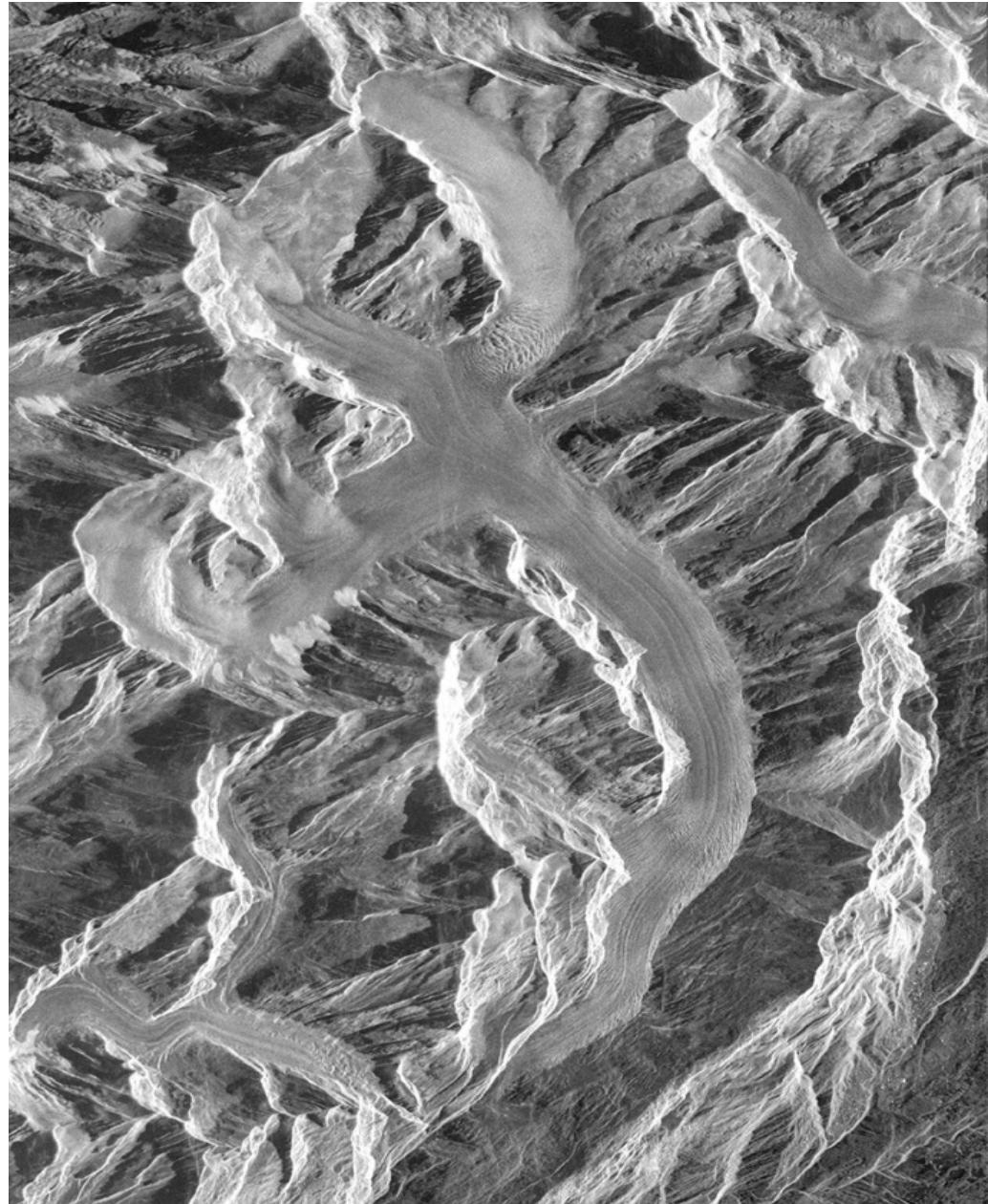
Irena Hajnsek

Microwaves and Radar Institute, DLR, Oberpfaffenhofen
Environmental Engineering, ETH, Zurich



Introduction

- Why is SAR good for snow parameter estimation?
- Introduction of the co-pol phase difference (CPD)
- TanDEM-X a co-pol system
- Testsite Great Aletschglacier
- Propagation model to estimate snow height



Why Radar Techniques for Snow?

- Optical methods sample only the snow surface
- Microwave penetrate into snow
- High frequency required to avoid total penetration: 5 - 50 GHz (note: stronger atmosphere influence)

Typical interactions of microwave and snow and ice:

- Total penetration ($T \ll 0^\circ\text{C}$, $n \ll 10 \text{ GHz}$)
- Total reflection at the surface ($T \geq 0^\circ\text{C}$)
- Volume scattering ($T < 0^\circ\text{C}$, $n > 5 \text{ GHz}$, depth > 2 m)

Interferometric applications for snow and ice:

- Multipass coherence decay: Snowfall / Melting
- Single pass: DEM-comparison based on surface reflection (deep firn, glacier mass balance)
- D-InSAR: freezing ground deformation, additional scatterers, complex path delays, atmosphere
- Polarimetric Phase differences (co-pol phase differences - CPD)

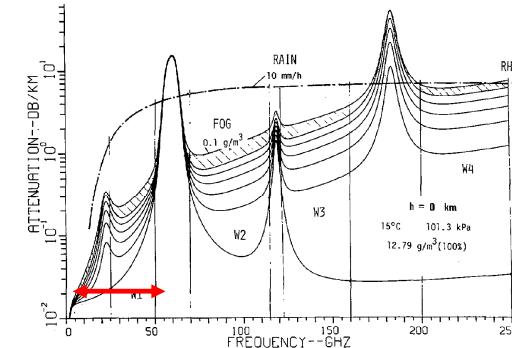
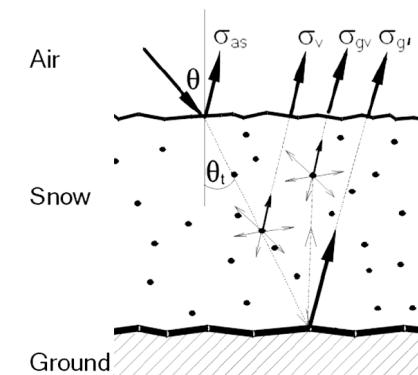
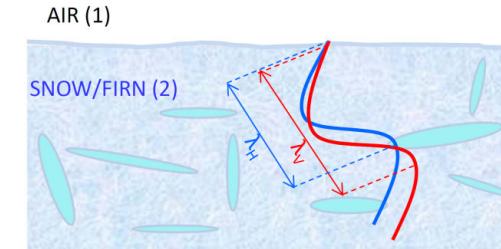


Fig. 1. Specific attenuation at sea level over the frequency range 1–250 GHz for various relative humidities (0 to 100 percent), including fog (0.1 g/m^3) and rain ($R = 10 \text{ mm/h}$).



Rott et al,
2010, IEEE
Proc.



Parrella,
PolInSAR
2013
Leinss et al. 2016,
The Cryosphere

Co-Polarimetric Phase Differences



$$[S] = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \rightarrow \vec{k}_{3L} = \begin{bmatrix} S_{HH} \\ \sqrt{2} \cdot S_{XX} \\ S_{VV} \end{bmatrix}$$

Lexicographic Scattering Vector

$$S_{HV} = S_{VH} = S_{XX}$$

Covariance Matrix: $[C_3] := \langle \vec{k}_{3L} \cdot \vec{k}_{3L}^* \rangle = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \sqrt{2} \langle S_{HH} S_{HV}^* \rangle & \langle S_{HH} S_{VV}^* \rangle \\ \sqrt{2} \langle S_{HV} S_{HH}^* \rangle & 2 \langle |S_{HV}|^2 \rangle & \sqrt{2} \langle S_{HV} S_{VV}^* \rangle \\ \langle S_{VV} S_{HH}^* \rangle & \sqrt{2} \langle S_{VV} S_{HV}^* \rangle & \langle |S_{VV}|^2 \rangle \end{bmatrix}$

Co-Pol Phase Difference:

$$\varphi_{CPD} = \arctan \frac{\text{Im}\{\langle S_{VV} S_{HH}^* \rangle\}}{\text{Re}\{\langle S_{VV} S_{HH}^* \rangle\}}$$

$[C]$ is by definition hermitian positive semi-definite matrices (i.e. have positive eigenvalues)

Types of Coherences



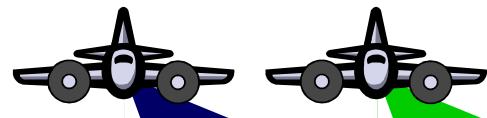
PolSAR

$$[S] = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}$$



Polarimetric Coherences

$$\tilde{\gamma}(S_{ij} S_{mn}) = \frac{< S_{ij} S_{mn}^* >}{\sqrt{< S_{ij} S_{ij}^* > < S_{mn} S_{mn}^* >}}$$



InSAR

$$[S_1 \quad S_2]$$



Interferometric Coherences

$$\tilde{\gamma}(S_1 S_2) = \frac{< S_1 S_2^* >}{\sqrt{< S_1 S_1^* > < S_2 S_2^* >}}$$



Pol-InSAR

$$[S_1] = \begin{bmatrix} S_{HH}^1 & S_{HV}^1 \\ S_{VH}^1 & S_{VV}^1 \end{bmatrix}$$

$$[S_2] = \begin{bmatrix} S_{HH}^2 & S_{HV}^2 \\ S_{VH}^2 & S_{VV}^2 \end{bmatrix}$$

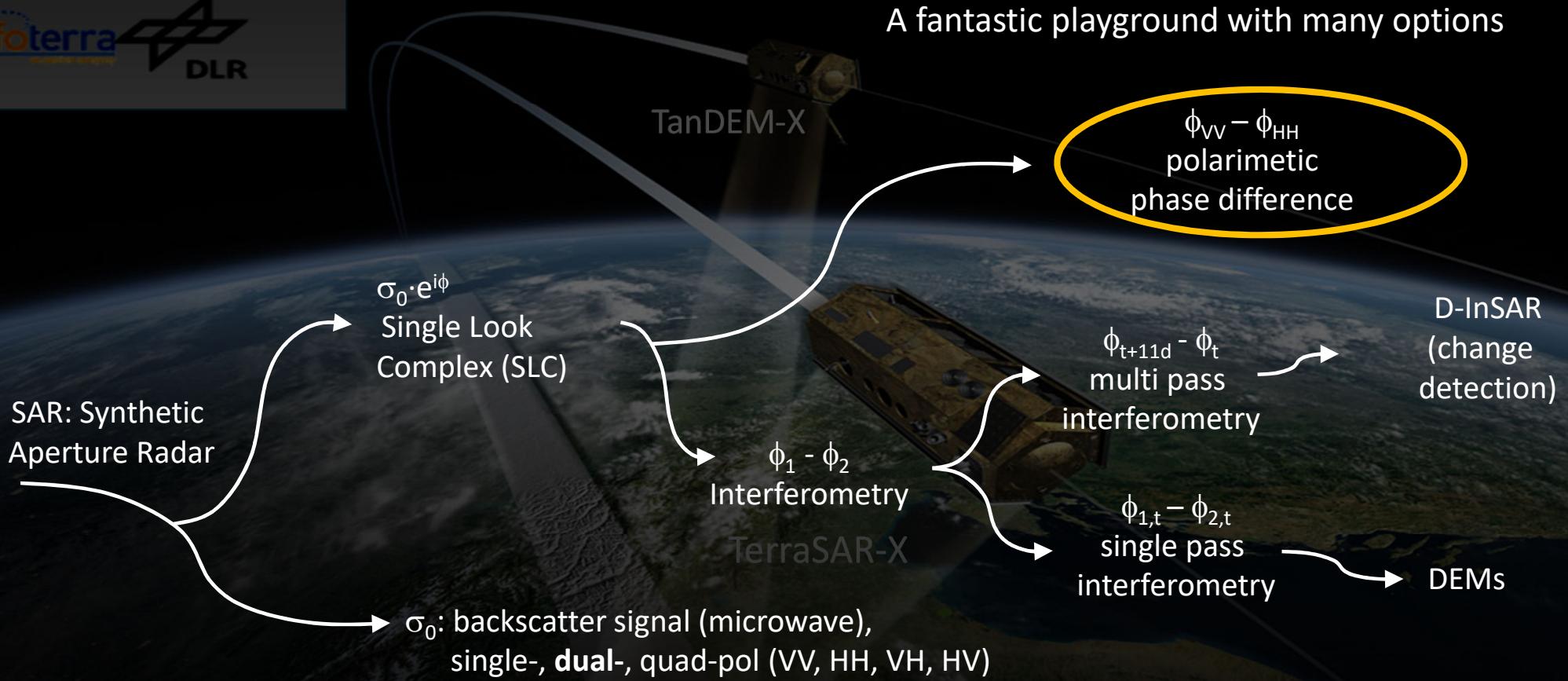


Polarimetric / Interferometric Coherences

$$\tilde{\gamma}(S_{ij}^1 S_{mn}^2) = \frac{< S_{ij}^1 S_{mn}^{2*} >}{\sqrt{< S_{ij}^1 S_{ij}^{1*} > < S_{mn}^2 S_{mn}^{2*} >}}$$

TerraSAR-X and TanDEM-X

A fantastic playground with many options



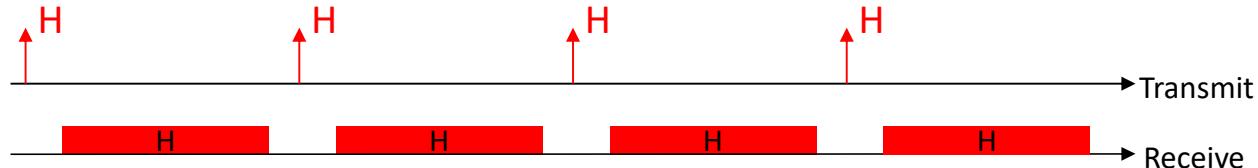
- X-Band: $n = 9.65$ GHz, $l = 3$ cm, Resolution: 3 m, Repeat cycle: 11 days
- Monostatic multi-pass Interferometry: $Dt = 11$ days
- Bistatic single-pass Interferometry: $Dt = 0$

Polarization Modes @ TerraSAR-X/TanDEM-X



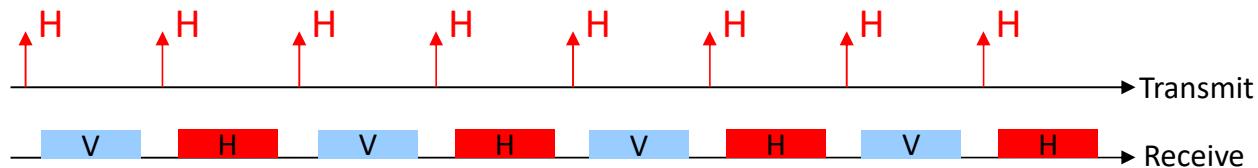
Single Polarization

- 1 polarization channel, {HH, VV}
- stripmap, spotlight, ScanSAR



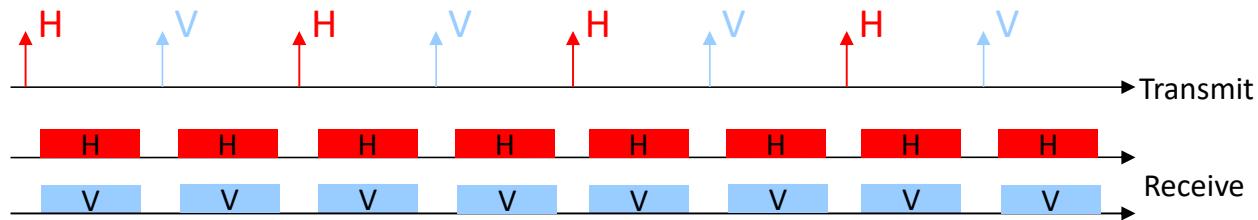
Dual Polarization

- 2 polarization channels, {HH/VV, HH/HV, VV/HV}
- stripmap, spotlight
- coherent pol. phase
- smaller elevation beam

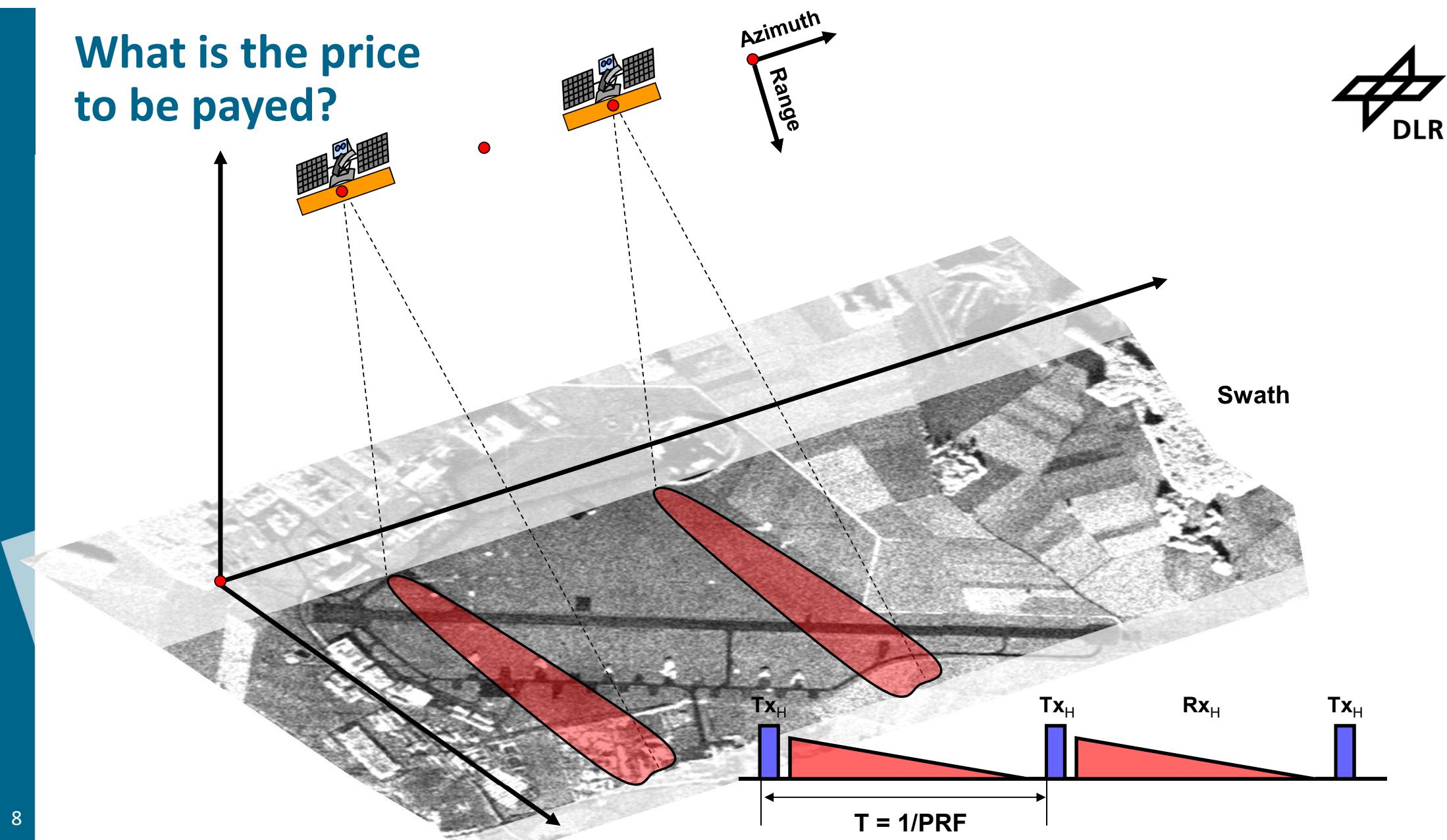


Quad Polarization

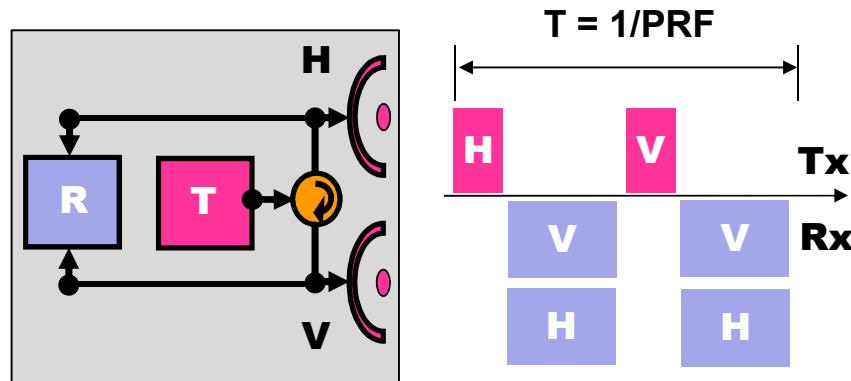
- All 4 pol. channels
- Stripmap
- coherent pol. Phase
- smaller elevation beam
- Experimental product



What is the price to be payed?



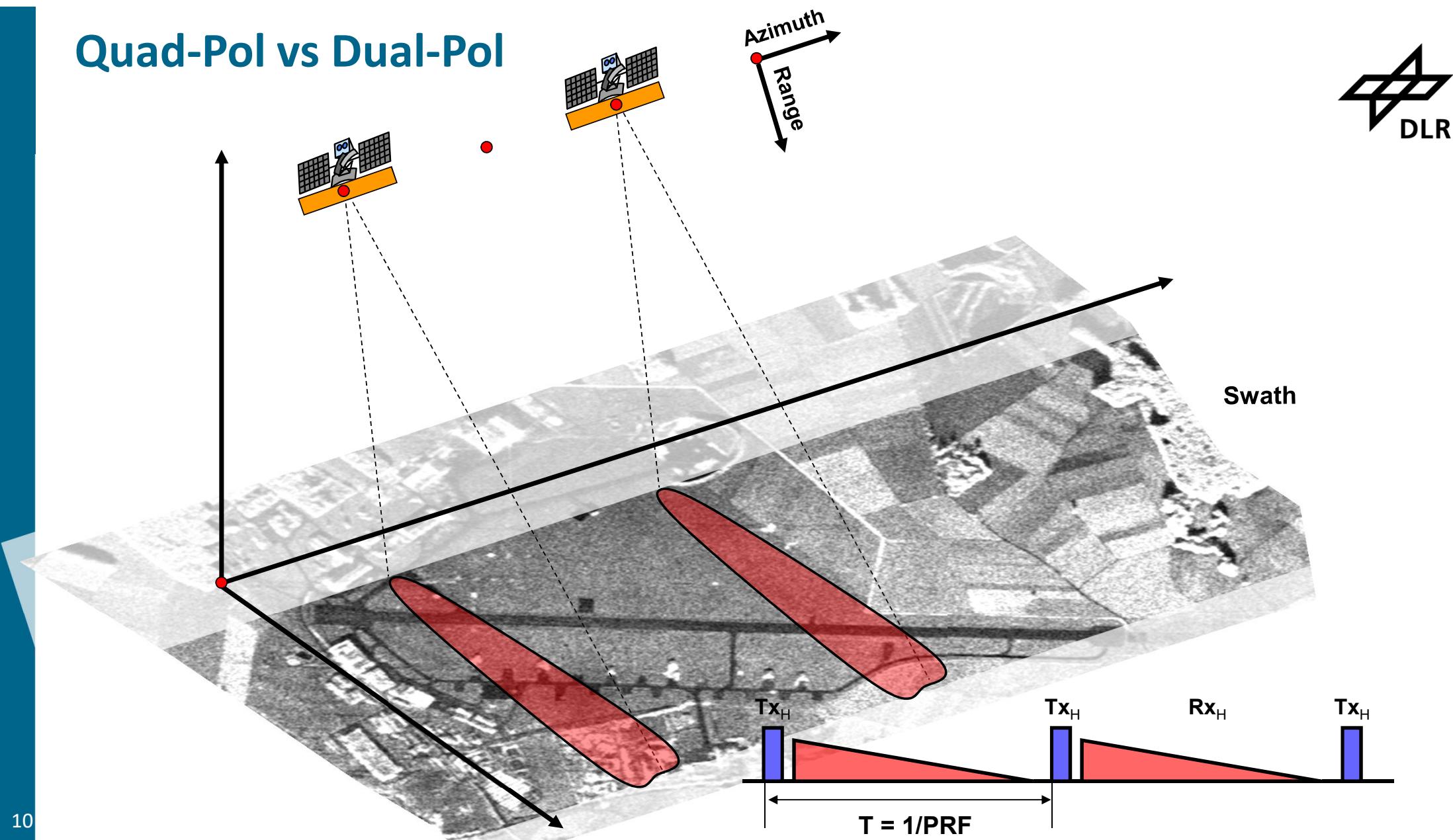
Quad Polarimetric Observation



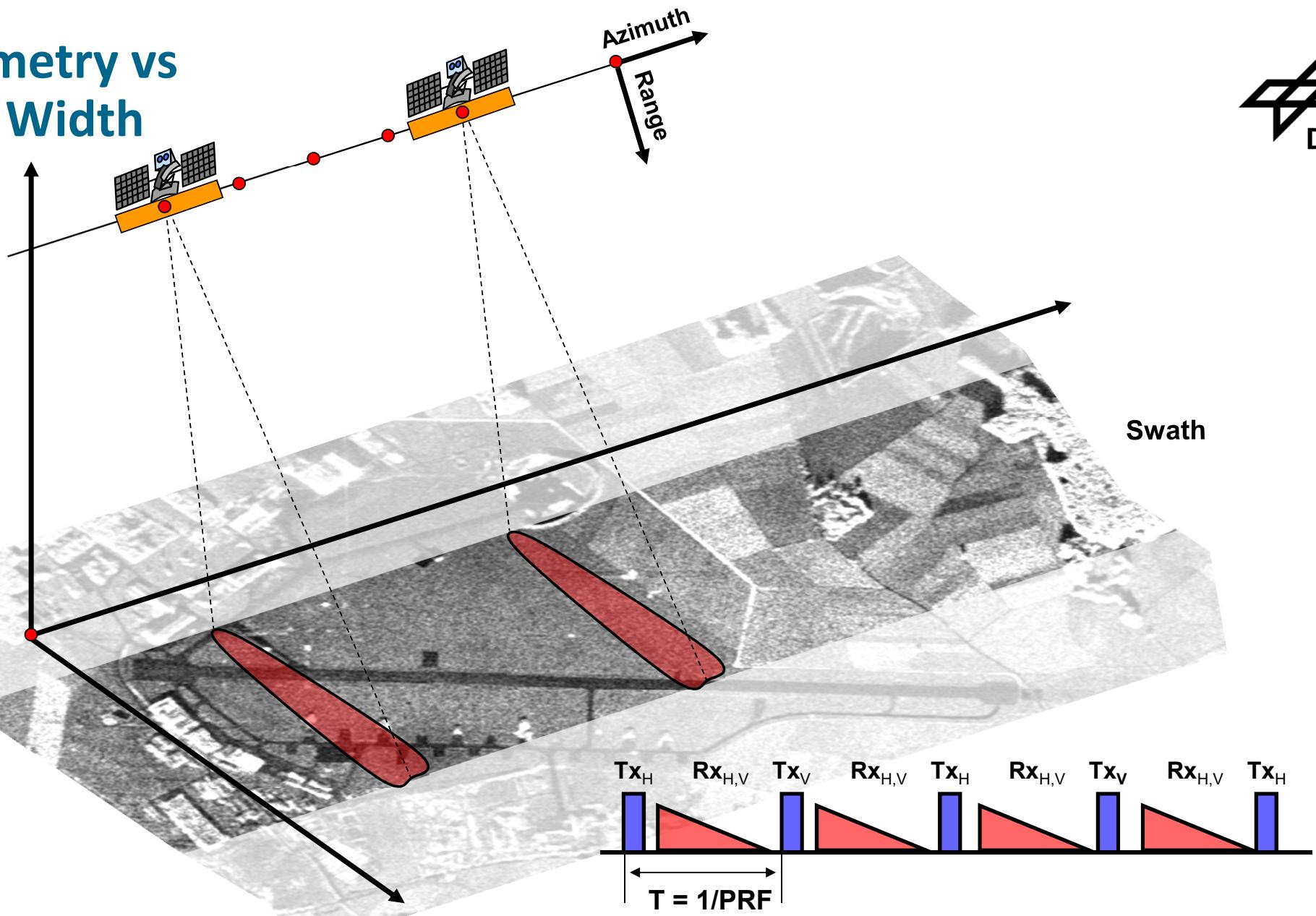
Quad Pol

$$\begin{array}{ll} \textbf{H} \quad \begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix} & \textbf{H} \quad \begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} S_{HH} \\ S_{VH} \end{bmatrix} \\ \textbf{V} \quad \begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} & \textbf{H} \quad \begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} S_{HV} \\ S_{VV} \end{bmatrix} \end{array}$$

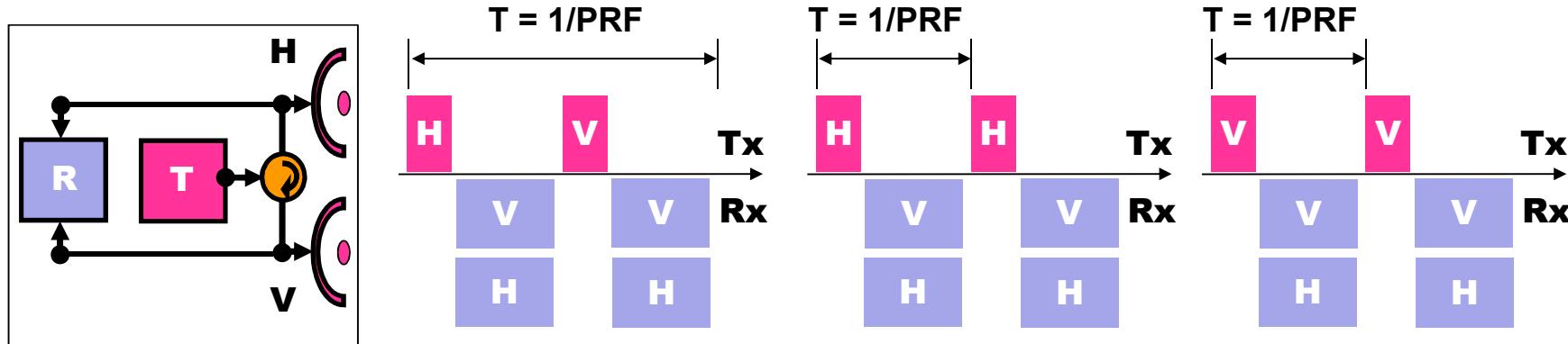
Quad-Pol vs Dual-Pol



Polarimetry vs Swath Width



Quad vs Dual Polarimetric Observations



Quad Pol

$$\begin{bmatrix} \text{H} \\ \text{V} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} \text{H} \\ \text{V} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^R \\ \mathbf{E}_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} S_{HH} \\ S_{VH} \end{bmatrix}$$

$$\begin{bmatrix} \text{V} \\ \text{H} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} \text{V} \\ \text{H} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^R \\ \mathbf{E}_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} S_{HV} \\ S_{VV} \end{bmatrix}$$

Dual Pol H

$$\begin{bmatrix} \text{H} \\ \text{V} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} \text{H} \\ \text{V} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^R \\ \mathbf{E}_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} S_{HH} \\ S_{VH} \end{bmatrix}$$

Dual Pol V

$$\begin{bmatrix} \text{V} \\ \text{H} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} \text{V} \\ \text{H} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^R \\ \mathbf{E}_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} \mathbf{E}_H^T \\ \mathbf{E}_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} S_{HV} \\ S_{VV} \end{bmatrix}$$

Dual Polarimetry – 2nd Order Descriptors

$$[C_3] = \langle \vec{k}_{3L} \cdot \vec{k}_{3L}^+ \rangle = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix}$$

3D Coherence (Covariance) Matrix
9 Parameters

$$[C_2] = \langle \vec{k}_{2D} \cdot \vec{k}_{2D}^+ \rangle = \left\langle \begin{bmatrix} S_A \\ S_B \end{bmatrix} \begin{bmatrix} S_A^* & S_B^* \end{bmatrix} \right\rangle = \begin{bmatrix} \langle |S_A|^2 \rangle & \langle S_A S_B^* \rangle \\ \langle S_B S_A^* \rangle & \langle |S_B|^2 \rangle \end{bmatrix}$$

2D Covariance (Coherence) Matrix

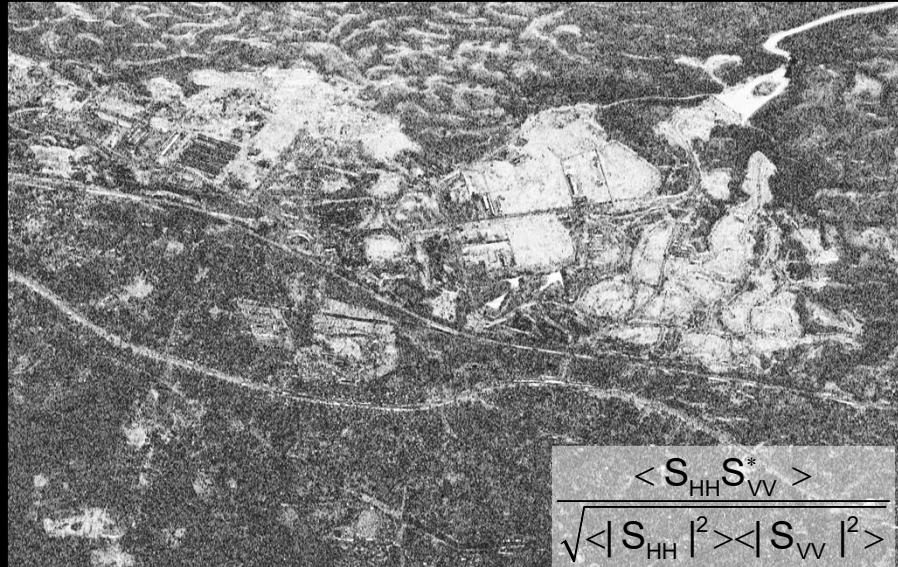
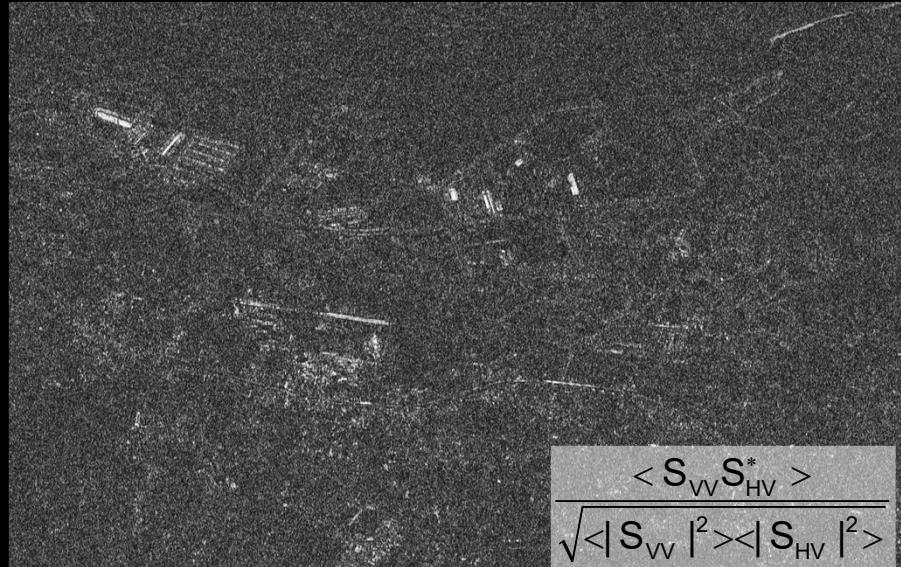
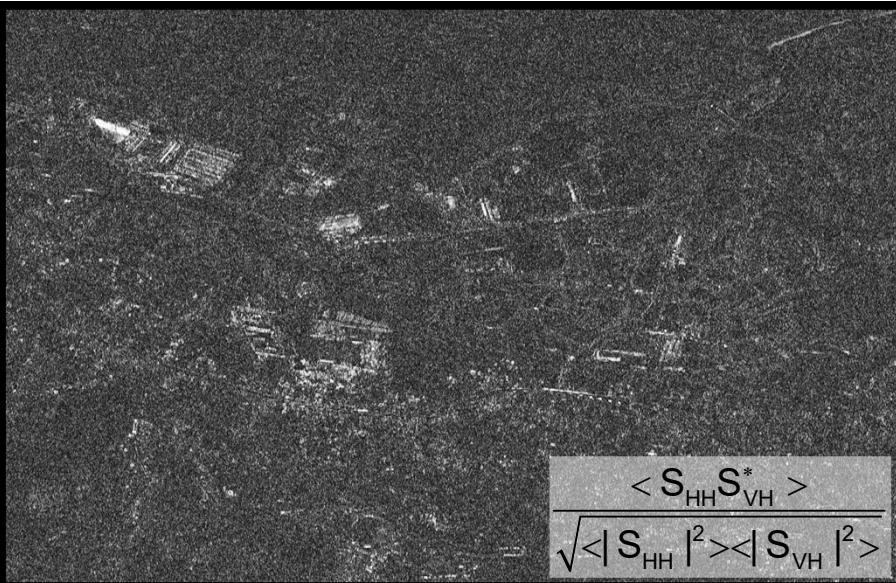
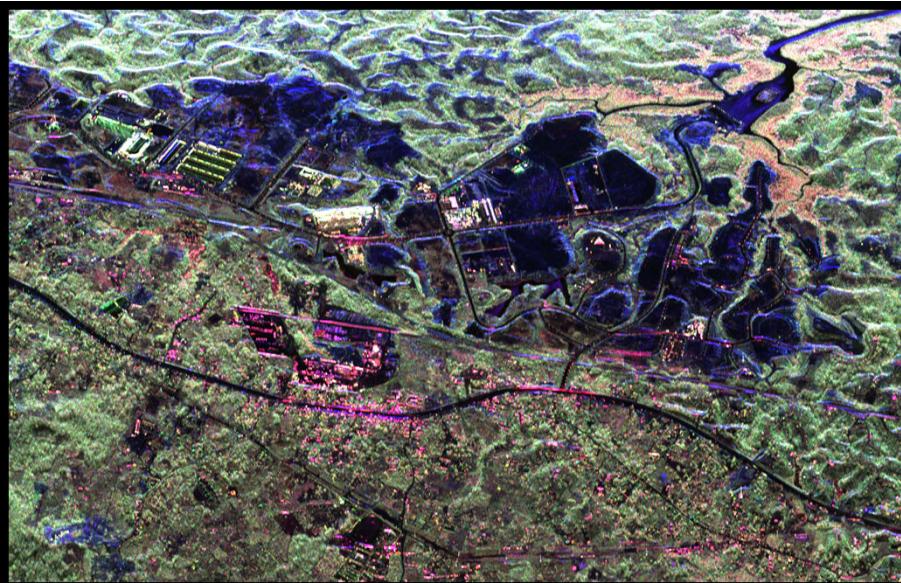
4 Parameters

$$[C_2] = [M][C_3][M]^T \quad \text{with} \quad [M] = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \end{bmatrix}$$

Case 1: HH-VH $[M] = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VH}^* \rangle \\ \langle S_{VH} S_{HH}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 2: VV-HV $[M] = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow [C_2] = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & \langle S_{VV} S_{HV}^* \rangle \\ \langle S_{HV} S_{VV}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 3: HH-VV $[M] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VV}^* \rangle \\ \langle S_{HH} S_{VV}^* \rangle & \langle |S_{VV}|^2 \rangle \end{bmatrix}$



Dual Polarimetry – 2nd Order Descriptors



$$[C_3] = \langle \vec{k}_{3L} \cdot \vec{k}_{3L}^+ \rangle = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix}$$

3D Coherence (Covariance) Matrix
9 Parameters

$$[C_2] = \langle \vec{k}_{2D} \cdot \vec{k}_{2D}^+ \rangle = \left\langle \begin{bmatrix} S_A \\ S_B \end{bmatrix} \begin{bmatrix} S_A^* & S_B^* \end{bmatrix} \right\rangle = \begin{bmatrix} \langle |S_A|^2 \rangle & \langle S_A S_B^* \rangle \\ \langle S_B S_A^* \rangle & \langle |S_B|^2 \rangle \end{bmatrix}$$

2D Covariance (Coherence) Matrix

4 Parameters

$$[C_2] = [M][C_3][M]^T \quad \text{with} \quad [M] = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \end{bmatrix}$$

Case 1: HH-VH $[M] = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VH}^* \rangle \\ \langle S_{VH} S_{HH}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix} = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & 0 \\ 0 & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 2: VV-HV $[M] = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow [C_2] = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & \langle S_{VV} S_{HV}^* \rangle \\ \langle S_{HV} S_{VV}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix} = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & 0 \\ 0 & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 3: HH-VV $[M] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VV}^* \rangle \\ \langle S_{HH} S_{VV}^* \rangle & \langle |S_{VV}|^2 \rangle \end{bmatrix}$

2-dim Polarimetry: 2nd Order Statistical Parameters

$$[T_3] := \langle \vec{k}_{3P} \cdot \vec{k}_{3P}^+ \rangle \quad \rightarrow \quad [T_3] = [U_3][\Lambda_3][U_3]^{-1}$$

$$[\Lambda_3] = \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \quad [U_3] = \begin{bmatrix} | & | & | \\ \vec{e}_1 & \vec{e}_2 & \vec{e}_3 \\ | & | & | \end{bmatrix}$$

$$P_i := \frac{\lambda_i}{\sum \lambda_i} \quad \vec{e}_i = \begin{bmatrix} \cos \alpha_i \exp(j\varphi_{i1}) \\ \sin \alpha_i \cos \beta \exp(j\varphi_{i2}) \\ \sin \alpha_i \sin \beta \exp(j\varphi_{i3}) \end{bmatrix}$$

$$H := \sum_{i=1}^3 P_i \log_3 P_i \quad A := \frac{P_2 - P_3}{P_2 + P_3} \quad \alpha := \sum_{i=1}^3 P_i \alpha_i$$

Entropy

Anisotropy

Alpha Angle

$$[T_2] := \langle \vec{k}_2 \cdot \vec{k}_2^+ \rangle \quad \rightarrow \quad [T_2] = [U_2][\Lambda_2][U_2]^{-1}$$

$$[\Lambda_2] = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} \quad [U_2] = \begin{bmatrix} | & | \\ \vec{e}_1 & \vec{e}_2 \\ | & | \end{bmatrix}$$

$$P_i := \frac{\lambda_i}{\sum \lambda_i} \quad \vec{e}_i = \begin{bmatrix} \cos \alpha_i \exp(j\varphi_{i1}) \\ \sin \alpha_i \exp(j\varphi_{i2}) \end{bmatrix}$$

$$\alpha_1 ; \alpha_2 = \frac{\pi}{2} - \alpha_1$$

$$H := \sum_{i=1}^2 P_i \log_2 P_i$$

Entropy
randomness

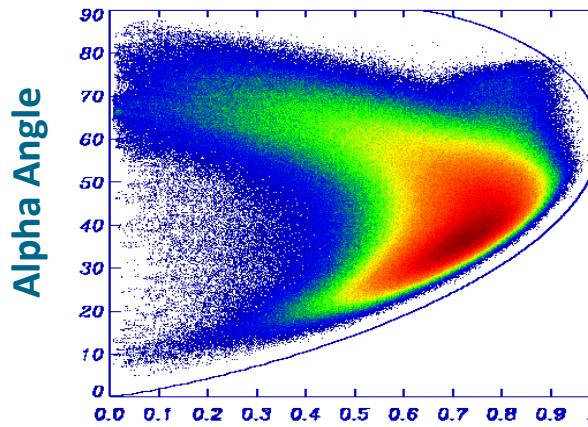
$$A := \frac{P_1 - P_2}{P_1 + P_2}$$

Anisotropy

$$\alpha := \sum_{i=1}^2 P_i \alpha_i$$

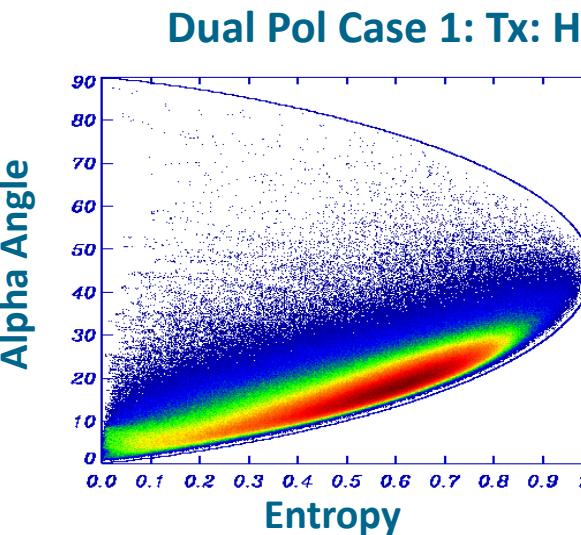
Alpha Angle
scat.mechan.

2-dim Polarimetry – 2nd Order Example X-band from PI-SAR Test Site: Gifu



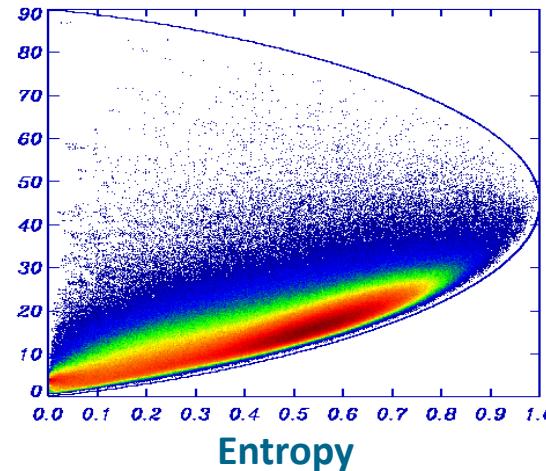
Quad Pol

Entropy

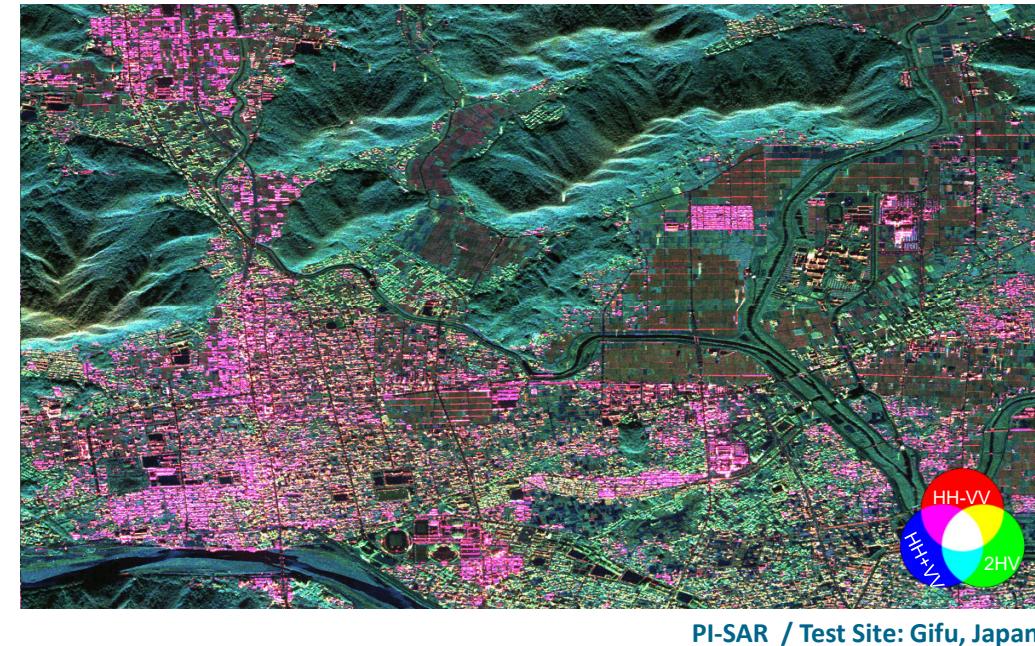
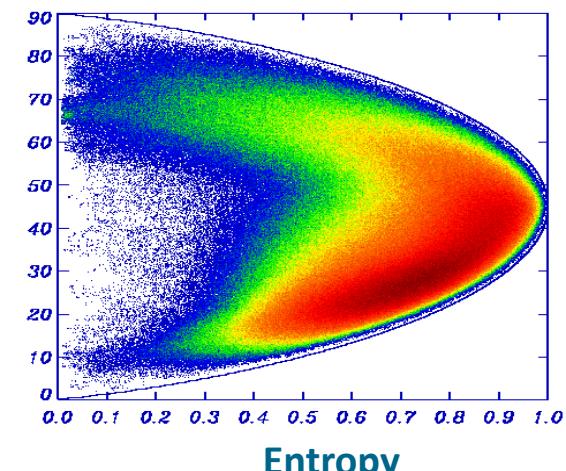


Dual Pol Case 1: Tx: H

Dual Pol Case 2: Tx: V



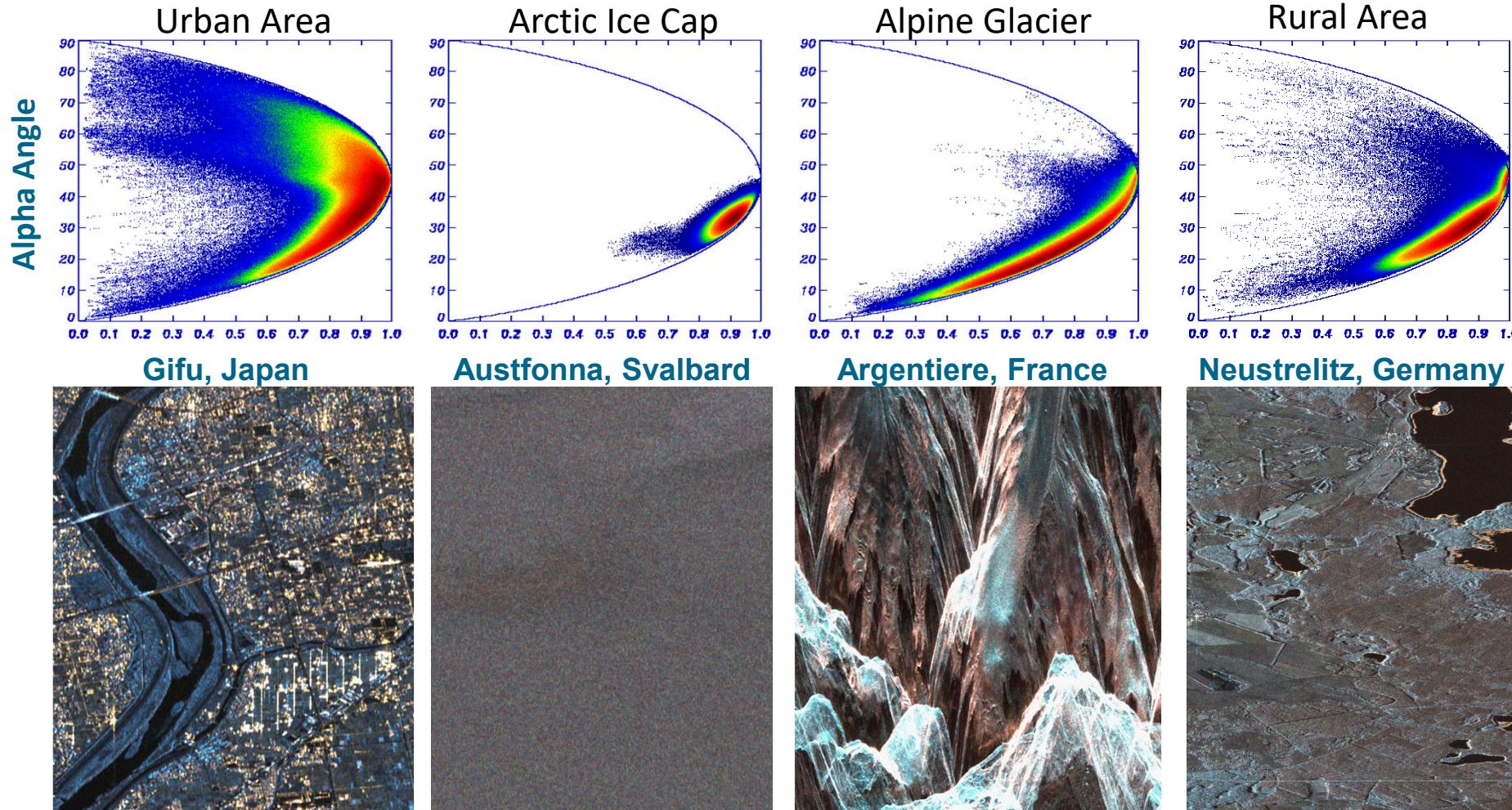
Dual Pol Case 3: Tx: H & V



PI-SAR / Test Site: Gifu, Japan

2-dim Polarimetry – 2nd Order

Example from TerraSAR-X for different surface types



TanDEM-X: The Great Aletsch Glacier and Available Data



The Great Aletsch Glacier

- ✓ Length 23 km
- ✓ Surface 86 km^3
- ✓ From $\sim 1800 \text{ m}$ to $\sim 3500 \text{ m}$ altitude
- ✓ Negative mass balance since 1881
- ✓ Front reatreats up to 4 m/year
- ✓ Equilibrium Line at 3000 m

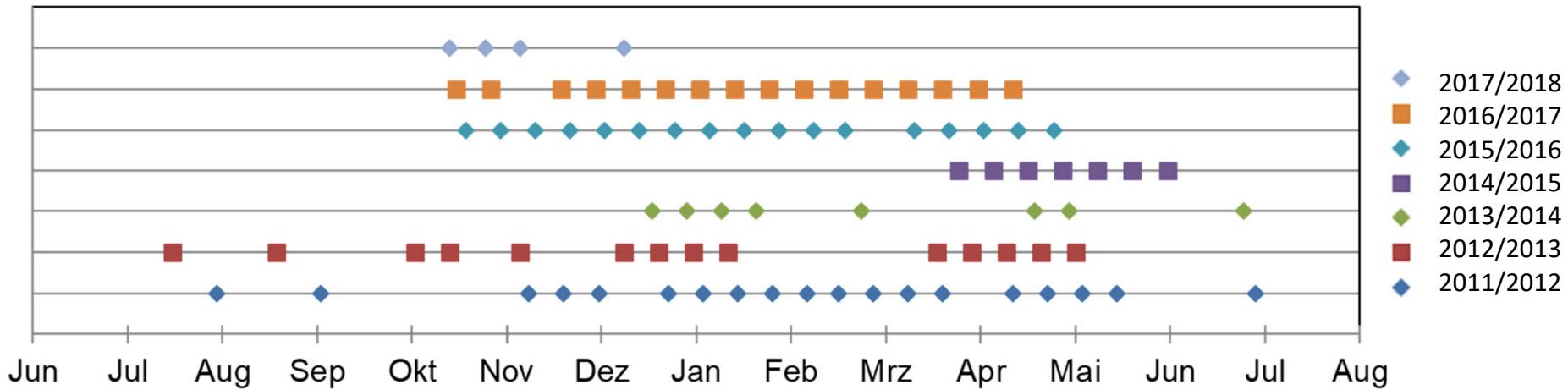


Map of Switzerland, Aletsch is marked

Source: Map.geo.admin.ch (Schweizerische Eidgenossenschaft), Date: 25.06.18

SAR Data

- ✓ TanDEM-X time series
- ✓ Dual-Pol (HH and VV)
- ✓ 7-year time period (2011-2018)
- ✓ 86 acquisitions from same orbit
- ✓ $\text{rg} \times \text{az} = 1,76 \times 6,6 \text{ m}$ resolution
- ✓ Incidence angle $\theta_{inc} = 31,6^\circ$



Great Aletsch Glacier / Grosser Aletschgletscher



- 23 km long
- Covers 80 square kilometers
- over 800 meters thick ice
- 15 cubic kilometers of ice
- 20% of the entire Swiss Ice mass
- expected to lose 90% of it's mass until 2100.

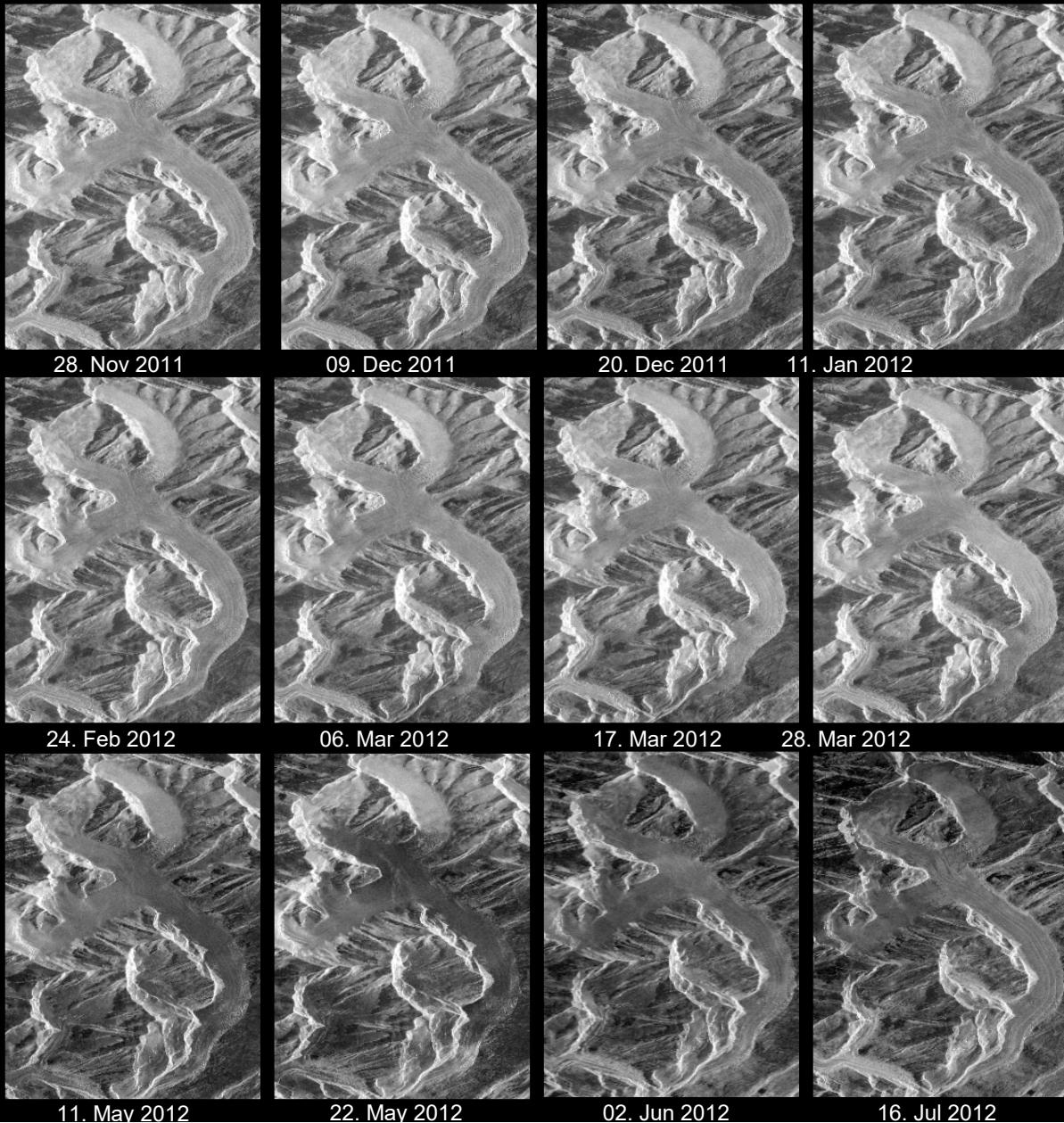
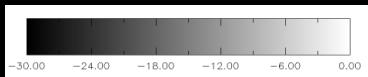
Jouvet et al. J. Glac. (2011)

L. Leinss



Aletschgletscher, Switzerland

2011 - 2012 Time series σ_{HH}^0

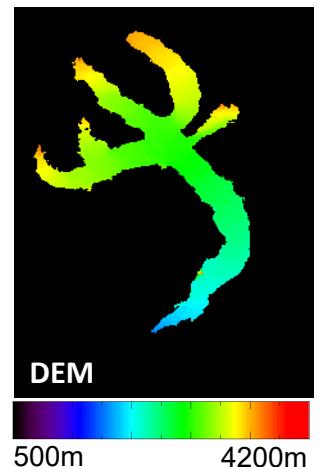
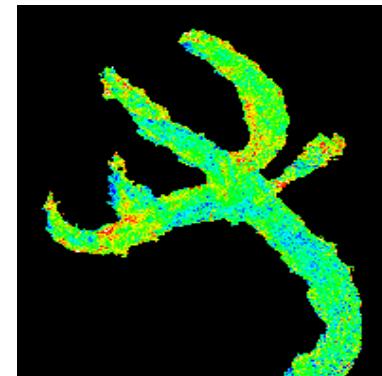
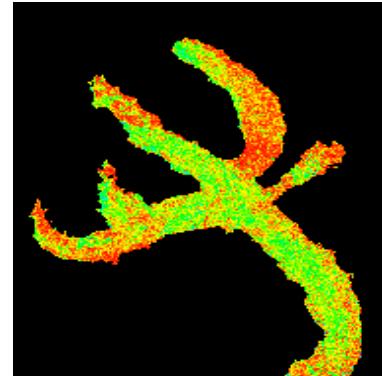
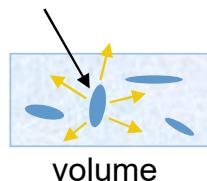


Polarimetric Analysis: Sensitivity to Seasonal Dynamics

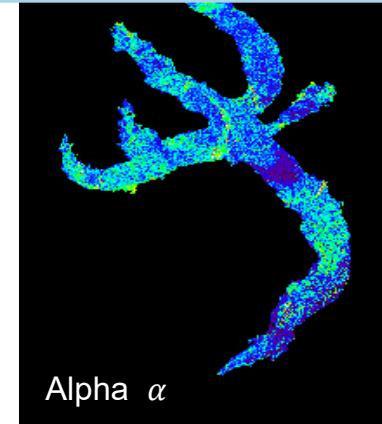
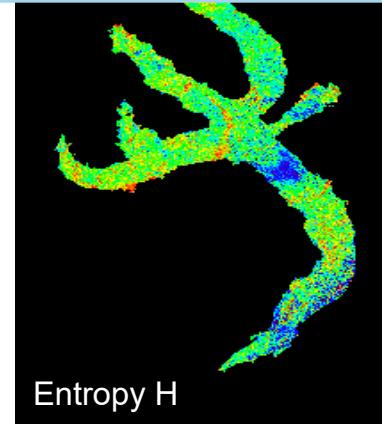
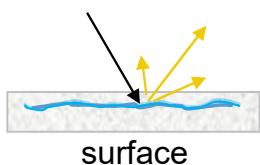


✓ Wet and dry glacier conditions

Winter image
08.02.2013



Summer
09.05.2013

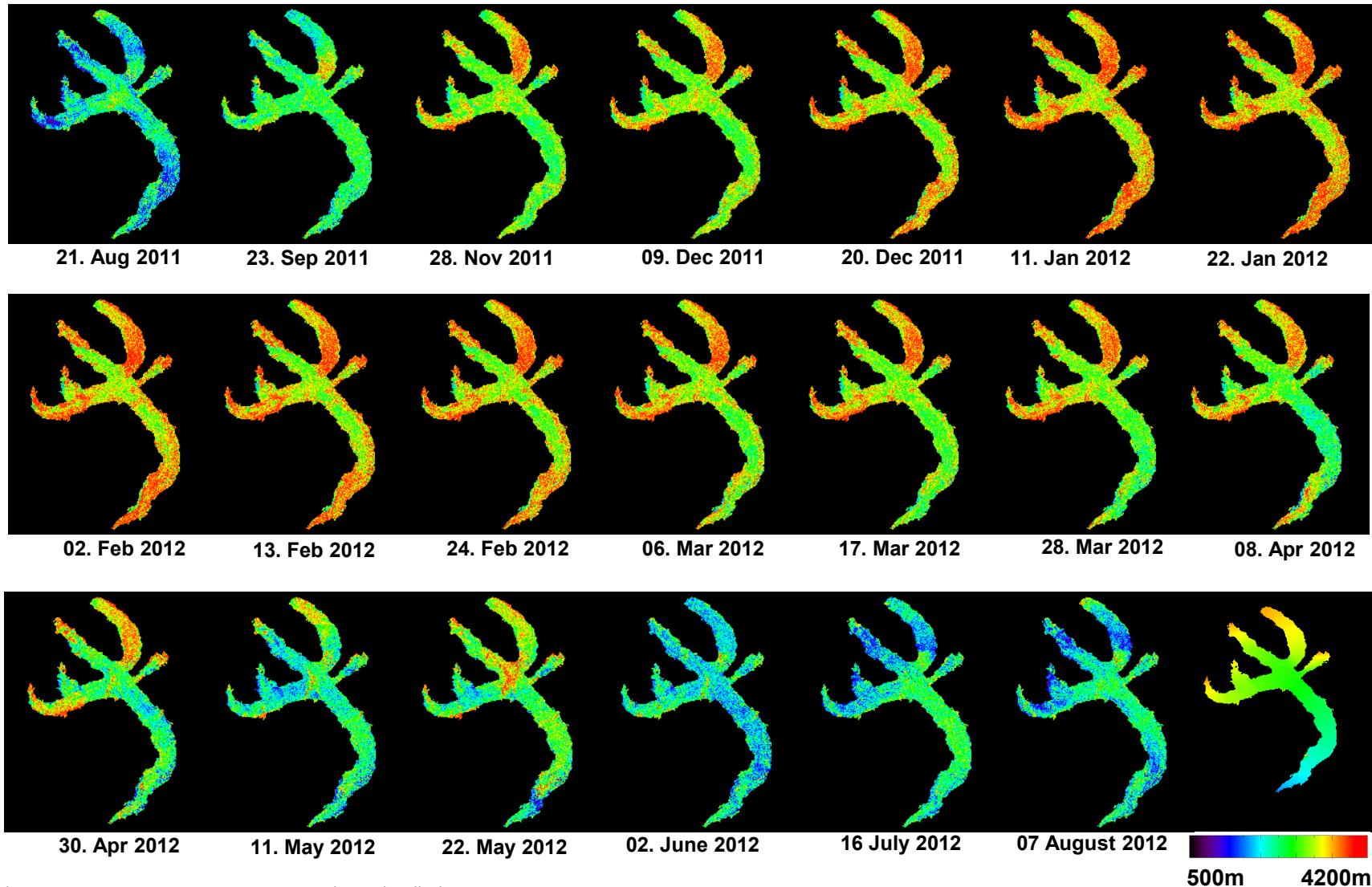


-30 dB 0 dB

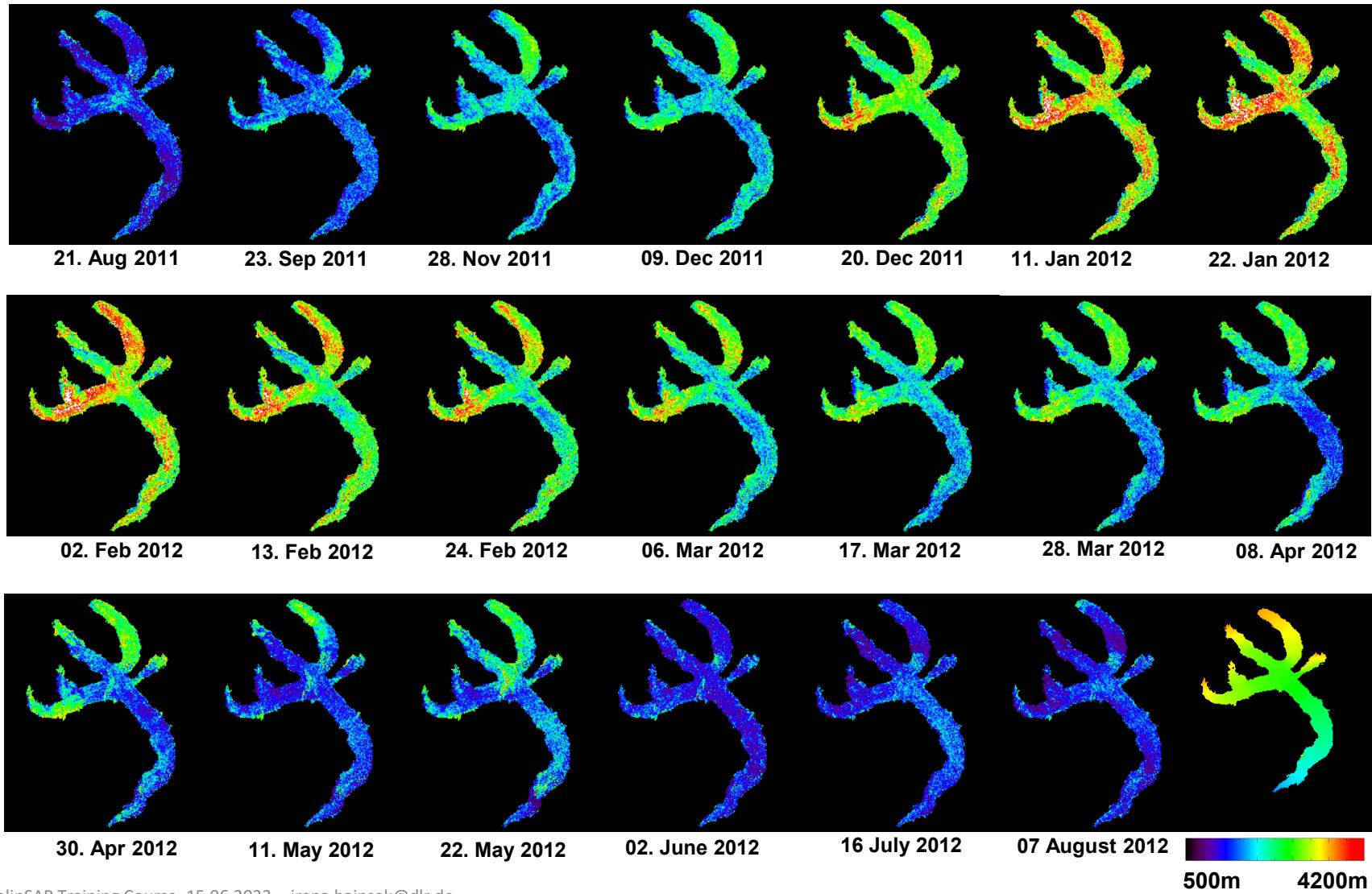
0 1

0 ° 60 °

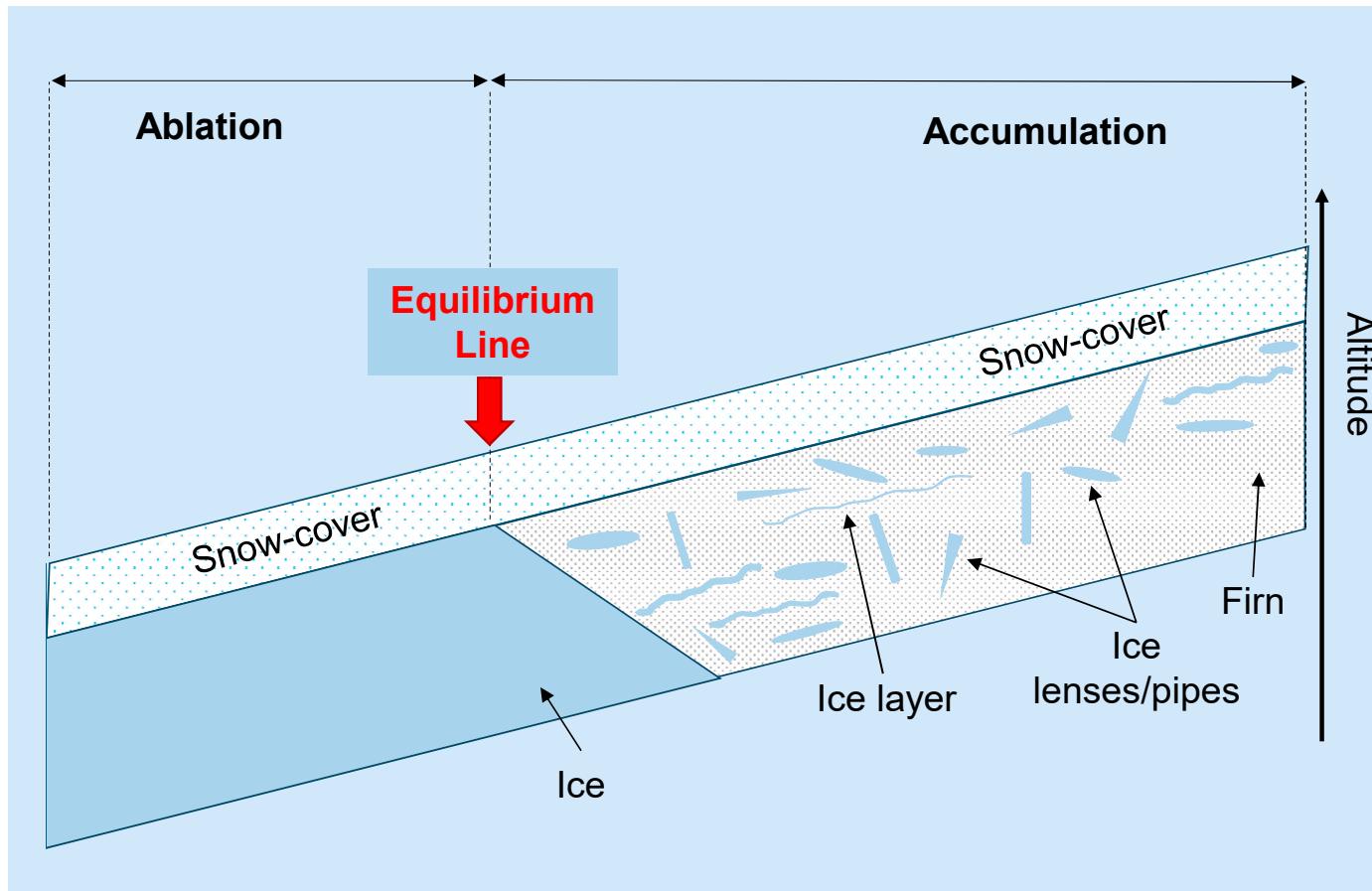
Entropy Time Series 2011/012



Alpha Angle Time Series 2011/012

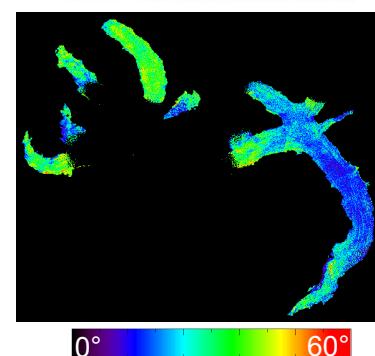
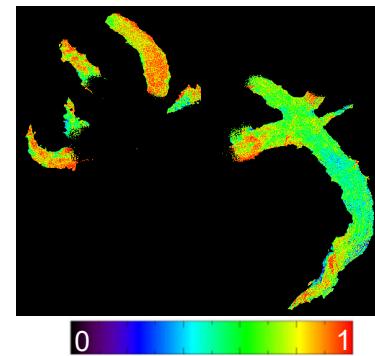
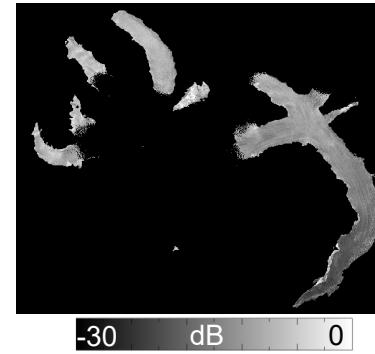
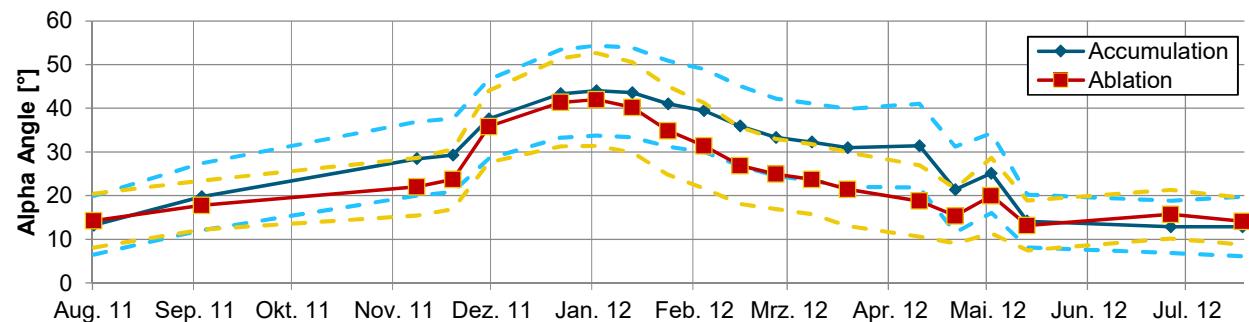
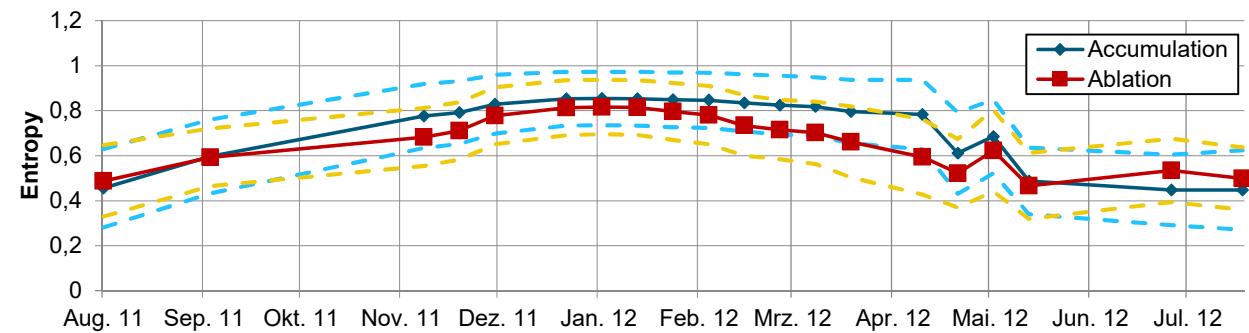
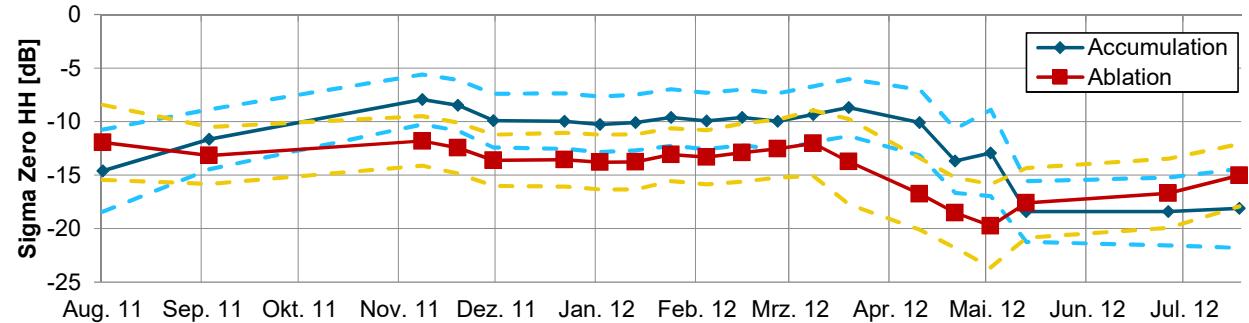


Basics of Glaciology

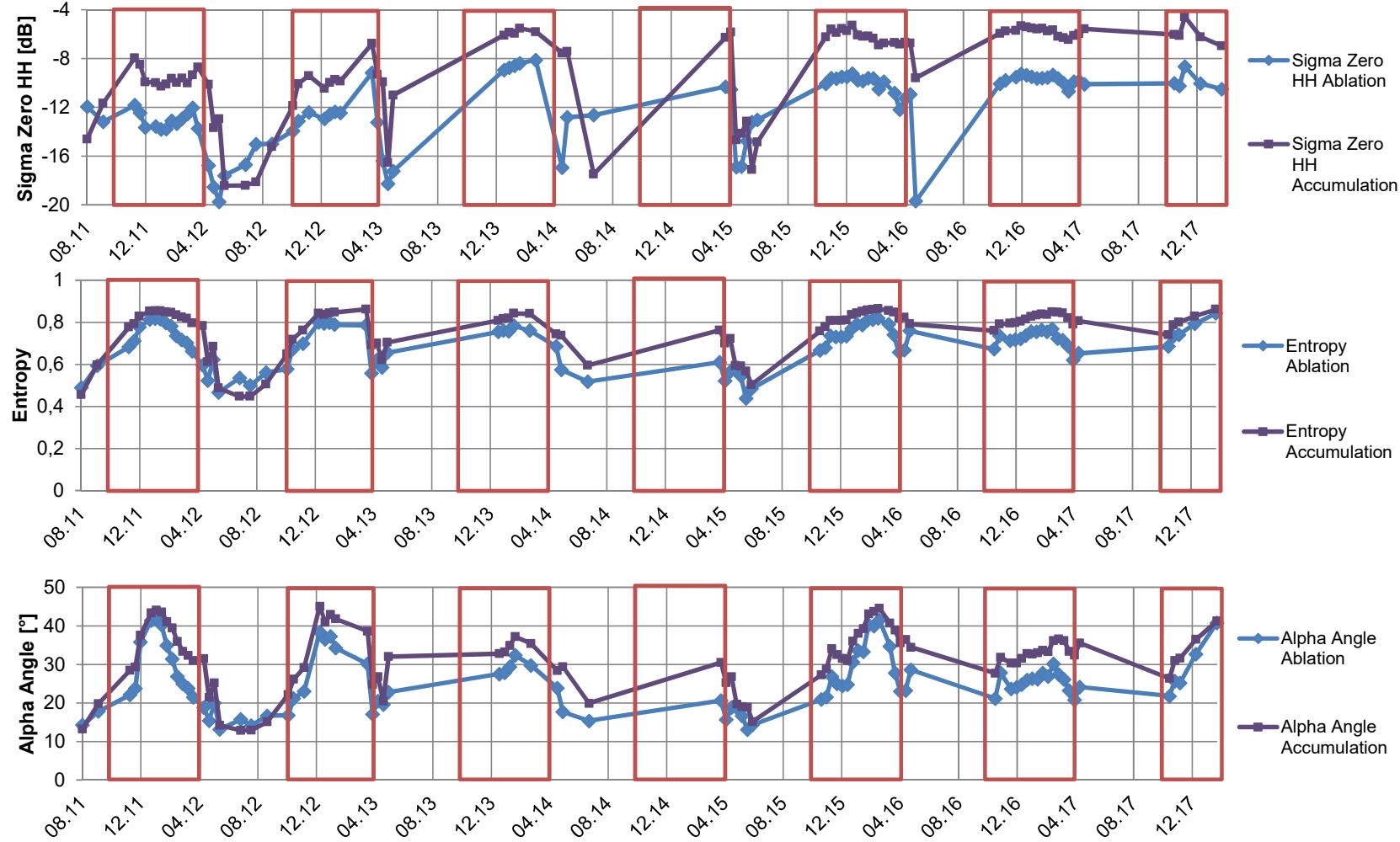


The equilibrium-line (ELA) altitude is a line on the glacier where accumulation equals ablation

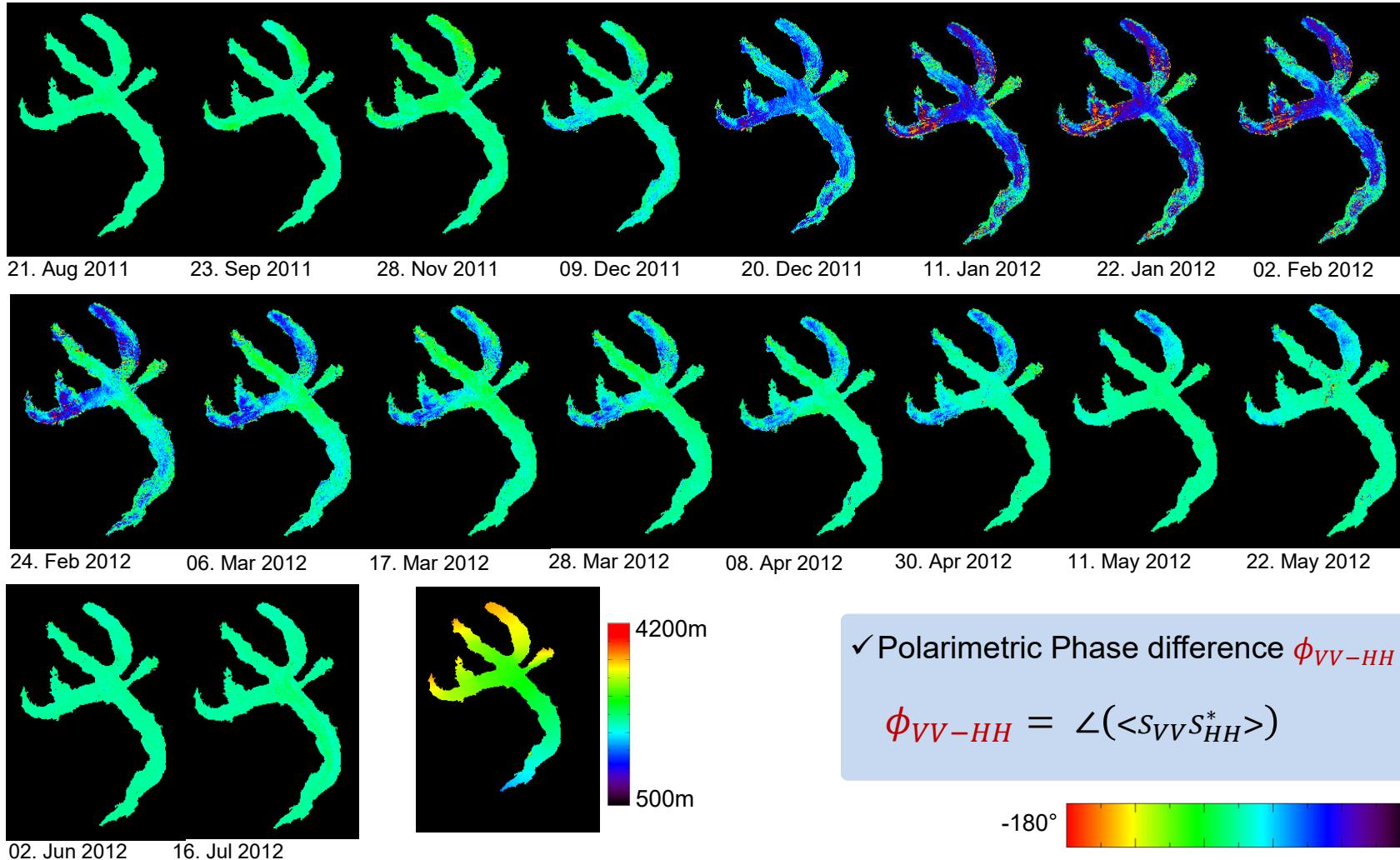
Polarimetric Analysis: Seasonal Dynamics of Glacier Zones



Polarimetric Analysis: Interannual Dynamics of Glacier Zones



Polarimetric Phase Diff. and Snow Accumulation

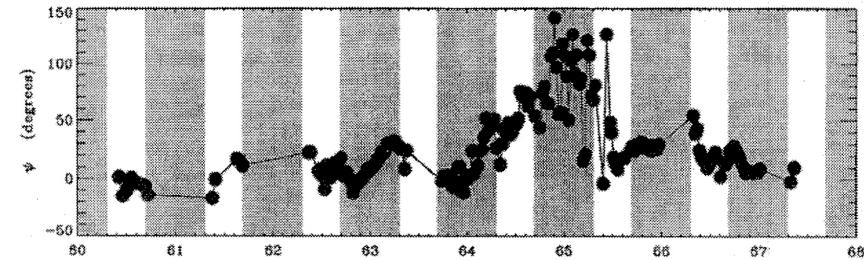


Why is snow depth proportional to $(\phi_{VV} - \phi_{HH})$?



- Fresh snow causes the highest phase differences
-> Also observed by [Chang, 1993] at 95 GHz.

Chang, P. et al. «Polarimetric backscatter from fresh and metamorphic snowcover at millimeter wavelengths», *IEEE Transactions on Antennas and Propagation*, , **1996**, 44



- Oriented particles within a volume cause polarization dependent propagation speeds [Cloude, 2000], [Parrella, 2013] & [Leinss, 2016].

Cloude et al. «The Remote Sensing of Oriented Volume Scattering Using Polarimetric Radar Interferometry.», *Proceedings of ISAP*, Fukuoka, Japan, **2000**.

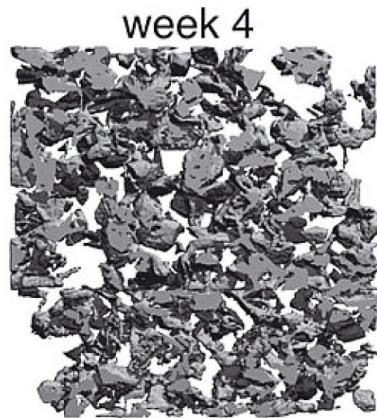
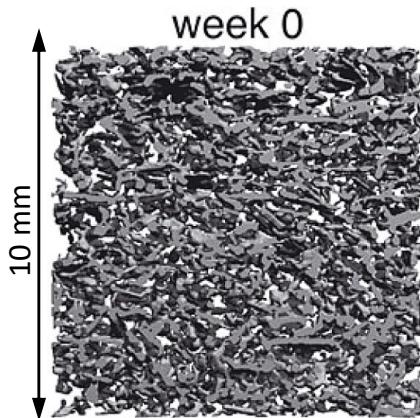
Parrella, G. "On the Interpretation of L- and P-band PolSAR Signatures of Polothermal Glaciers", *POLInSAR*, **2013**

Leinss, S. "Anisotropy of seasonal snow measured by polarimetric phase differences in radar time series. *The Cryosphere* **2016**"

- Recrystallization of snow changes the shape and orientation of ice grains in a snow cover driven by a vertical temperature gradient. [Riche, 2013]

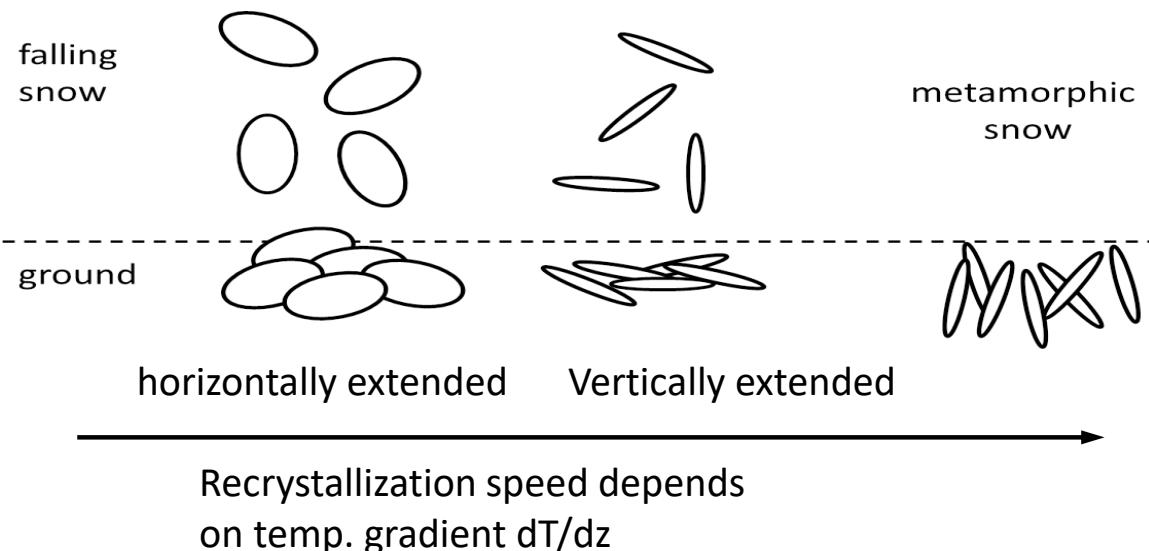
Riche, F. et al. "Evolution of crystal orientation in snow during temperature gradient metamorphism", *Journal of Glaciology*, **2013**, 59, 47-55

Why is snow depth proportional to $(\phi_{VV} - \phi_{HH})$?

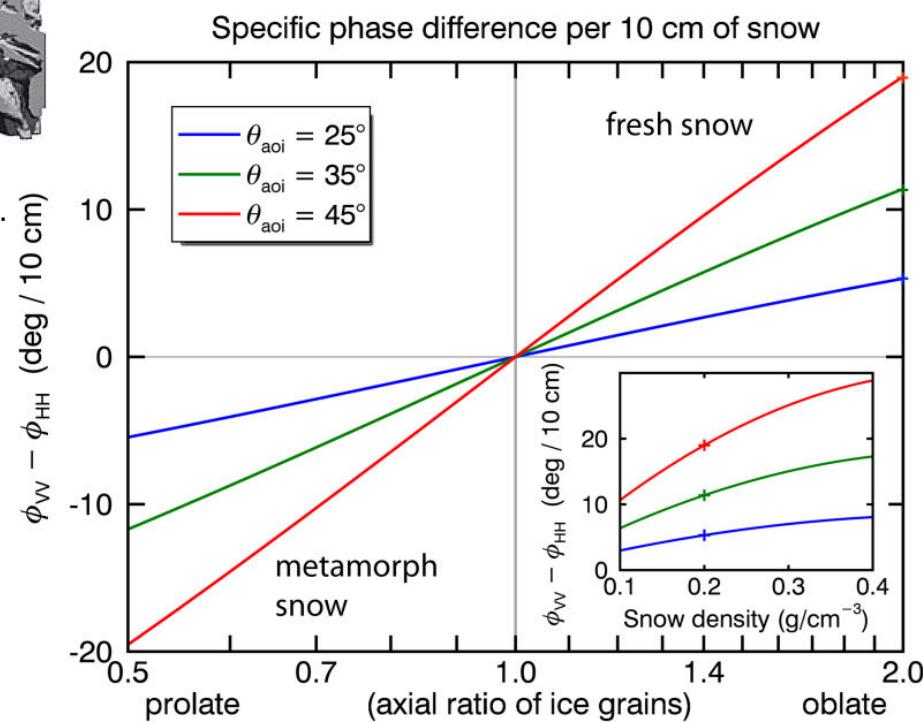


Riche, F. et al. "Evolution of crystal orientation in snow during temperature gradient metamorphism", *Journal of Glaciology*, 2013, 59, 47-55

Simplification for model:

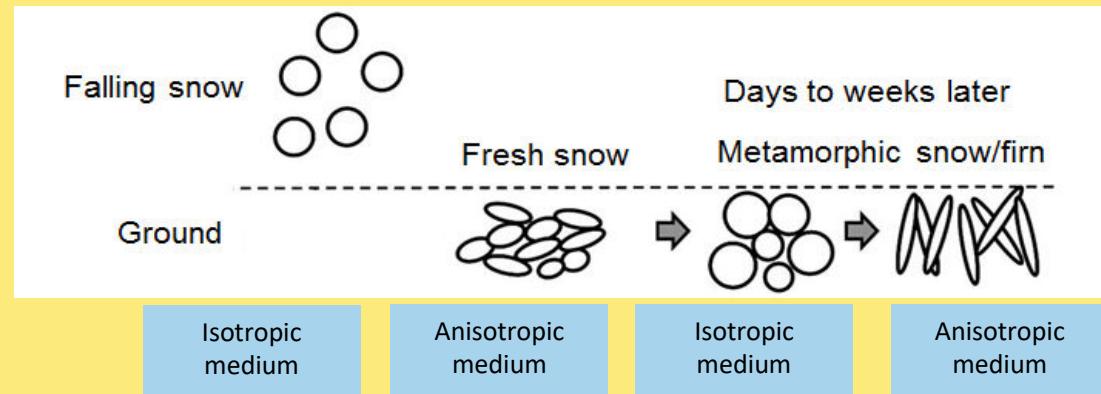


> 11 recrystallization cycles after 12 weeks.



Parrella, G. "On the Interpretation of L- and P-band PolSAR Signatures of Polothermal Glaciers", *POLInSAR 2013*

Propagation Model to Invert Snow Accumulation

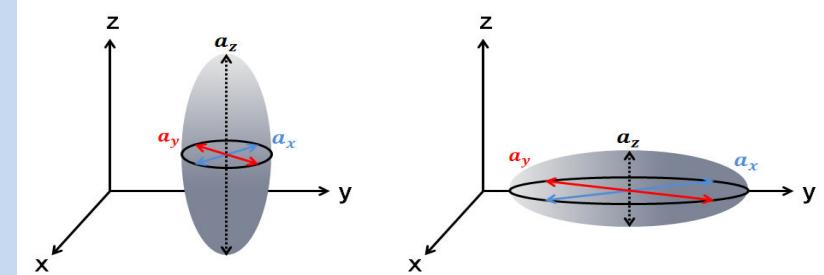


Modelling anisotropic snow

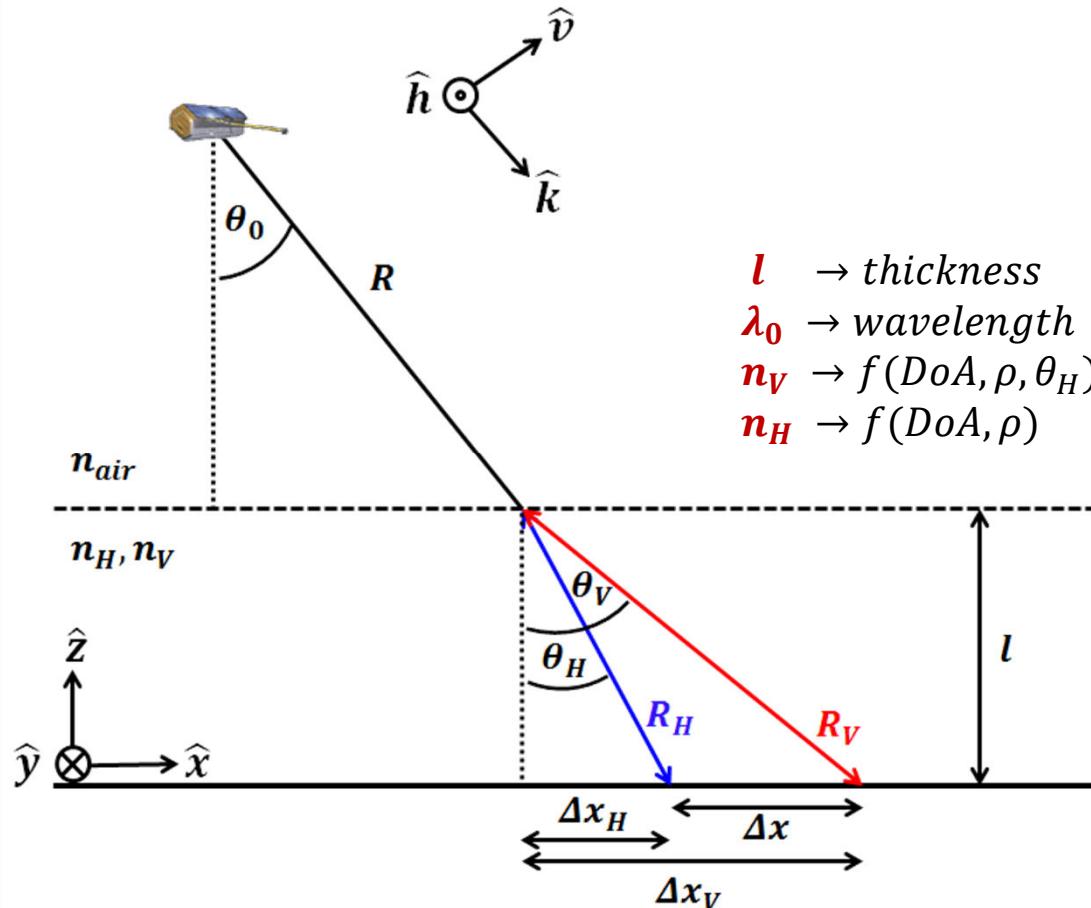
- ✓ Two phase mixture of air and ice inclusions
- ✓ Spheroidal grains described by degree of anisotropy $DoA = \frac{a_z}{a_x}$
- ✓ Effective permittivity components depend on DoA and volume fraction (density)

$$\epsilon_{eff,x,y,z} = \epsilon_{air} + \varphi_{vol}\epsilon_{air}\frac{\epsilon_{ice}-\epsilon_{air}}{\epsilon_{air}+(1-\varphi_{vol})N_{x,y,z}(\epsilon_{ice}-\epsilon_{air})}$$

- ✓ Refractive indices $n_{x,y}$ and n_z ($n^2 = \epsilon_r$)



Propagation Model to Invert Snow Accumulation



- ✓ Transformation from $(x,y,z) \rightarrow (H,V)$ coordinate system
- ✓ H component $n_H = n_{x,y}$
- ✓ V component $n_V = \sqrt{n_x^2 \cos^2 \theta_H + n_z^2 \sin^2 \theta_H}$

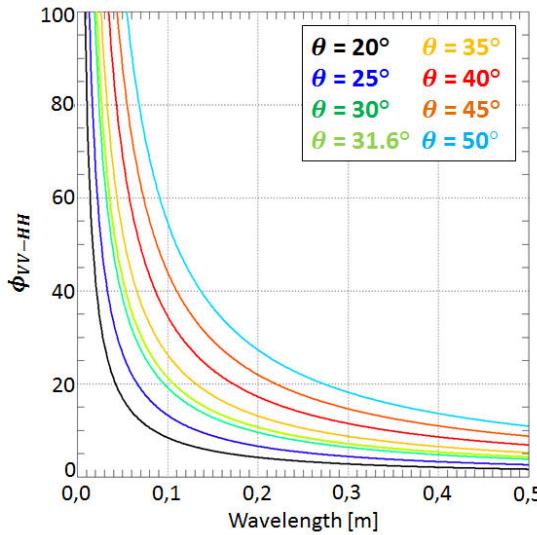
$$\phi_{VV-HH} = 2 \frac{2\pi}{\lambda_0} (n_V R_V - n_H R_H)$$

$$R_V = \frac{\cos \theta_V}{l}$$

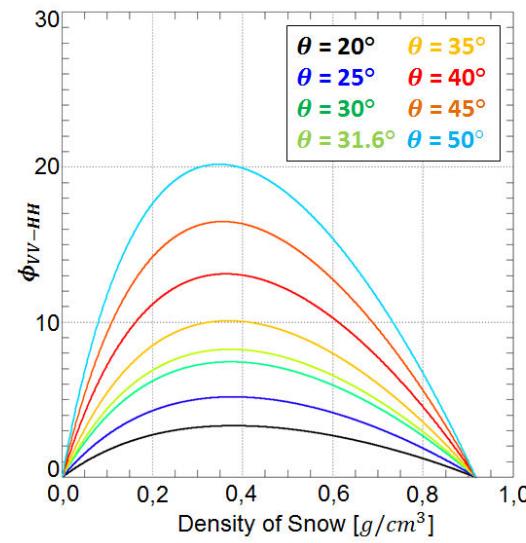
$$R_H = \frac{\cos \theta_H}{l}$$

$$\boxed{\phi_{VV-HH} = 2 \frac{2\pi \cdot l}{\lambda_0} \left(\frac{n_V}{\cos \theta_V} - \frac{n_H}{\cos \theta_H} \right)}$$

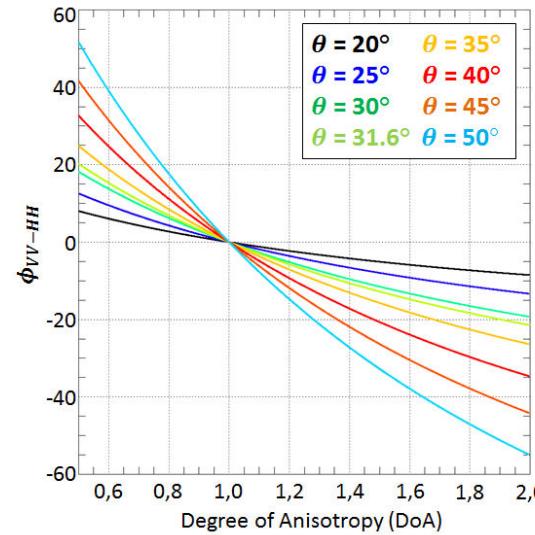
Propagation Model: Sensitivity Analysis



- ✓ Sensitivity increases with frequency

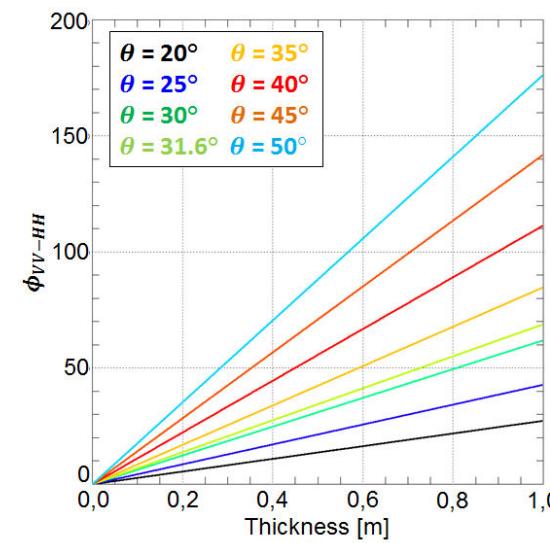


- ✓ Increasing until medium is too dense

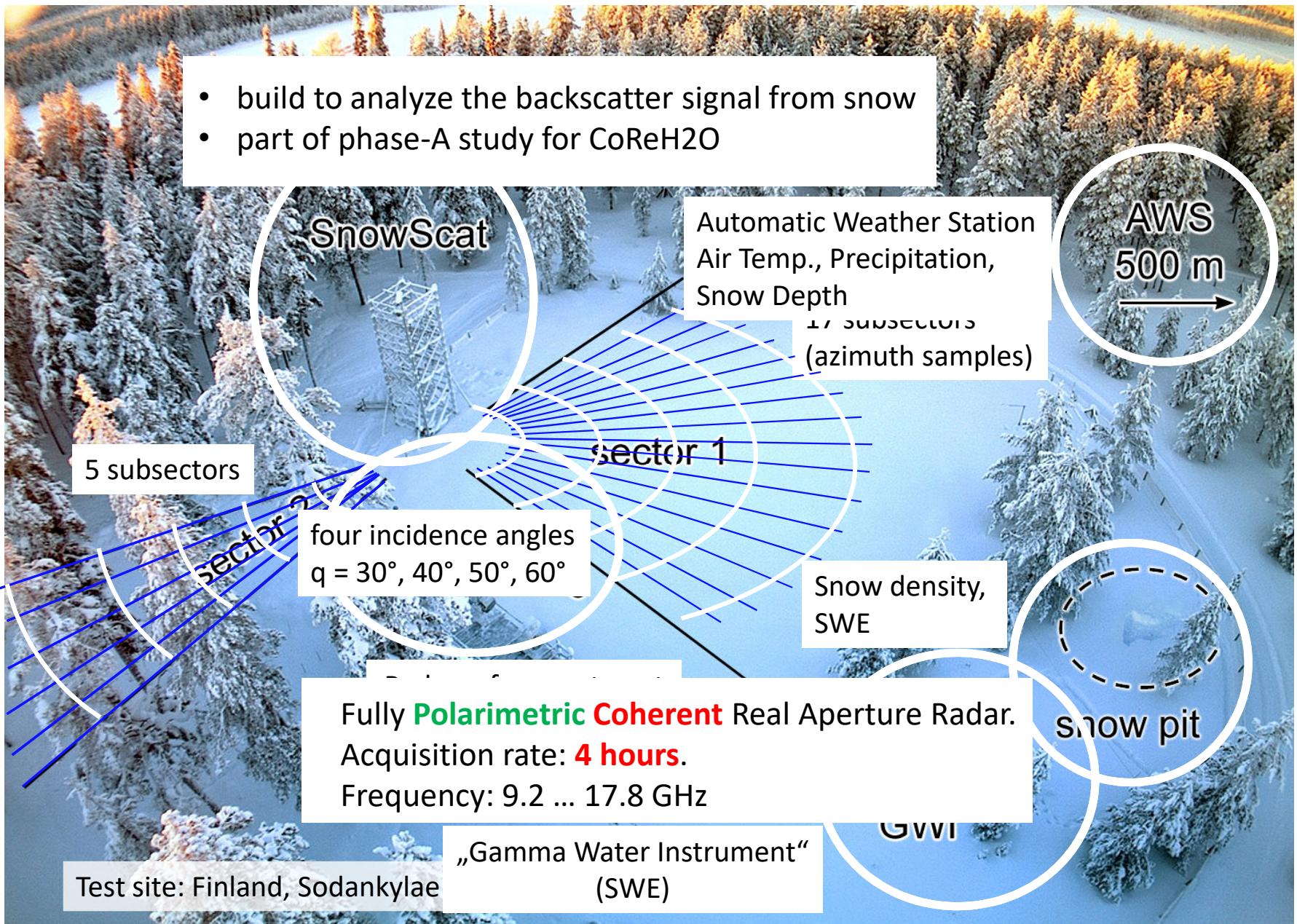


$\rho = 0,2 \text{ g/cm}^3$
$DoA = 0,8$
$l = 0,1\text{m}$
$\lambda = 0,031\text{m}$

- ✓ More sensitive for higher anisotropy

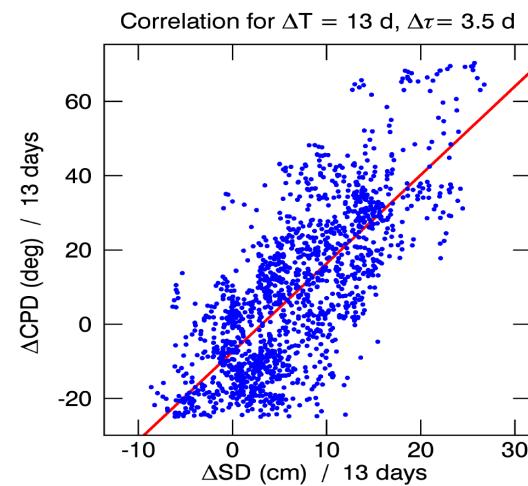
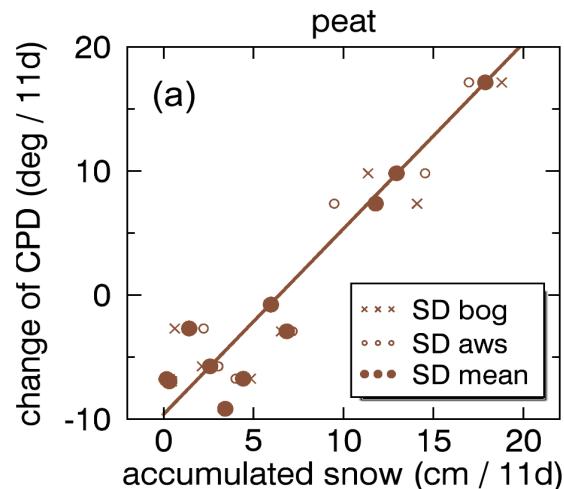
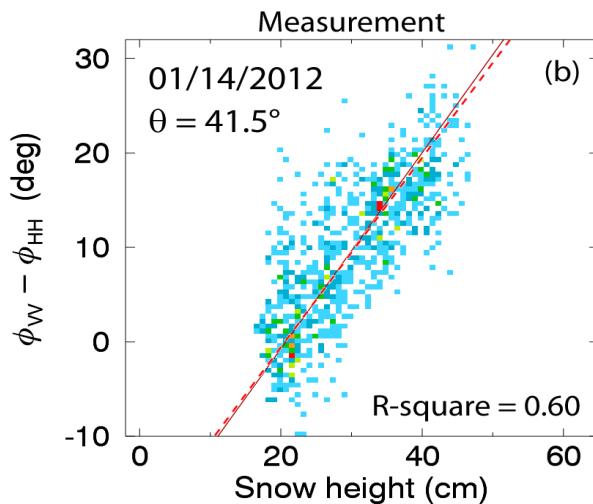


- ✓ Linear dependency on thickness



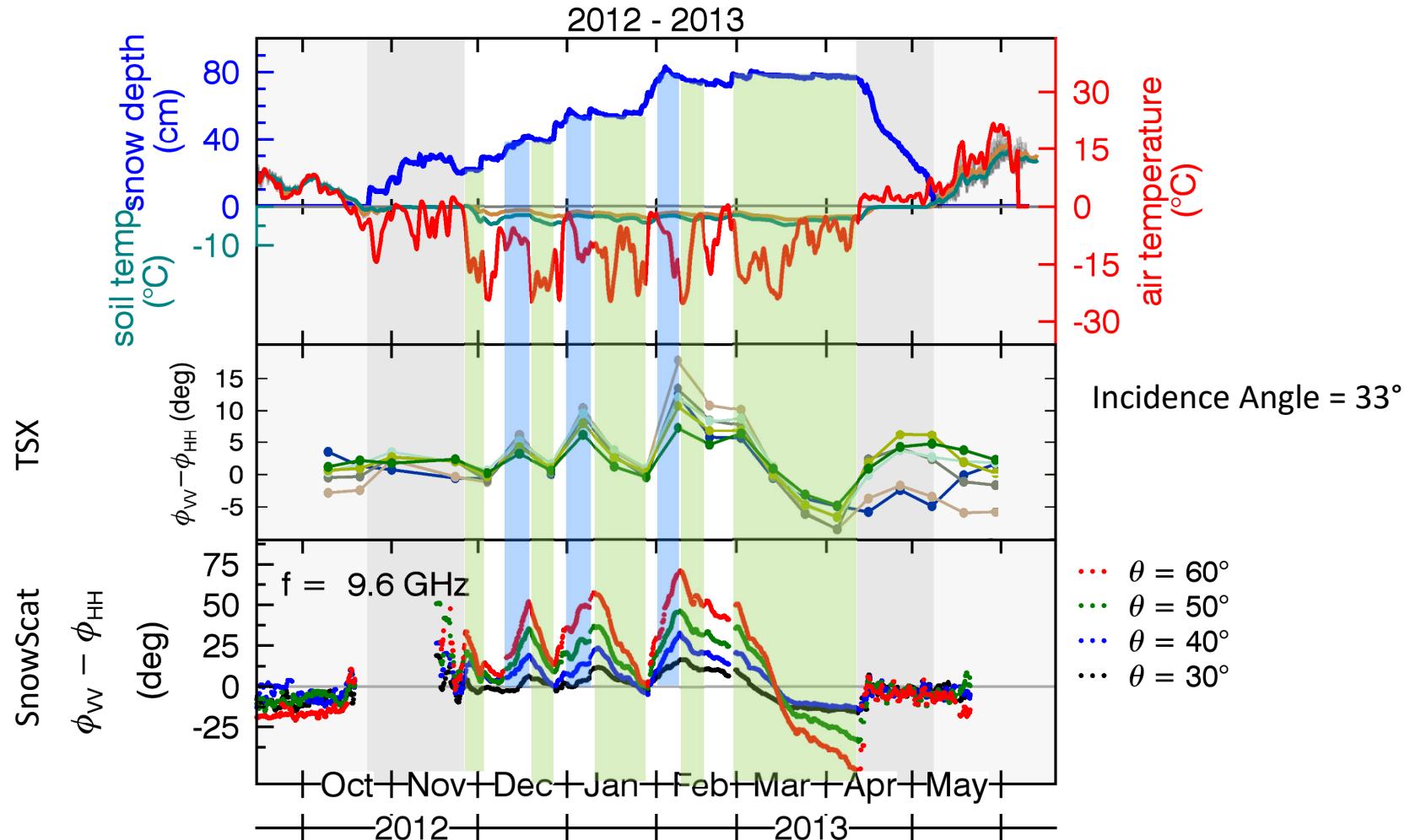
Detection of Fresh Snow

The anisotropic character of fresh snow can be used to determine the amount of fresh snow within the last few days.



- TerraSAR-X:
Total snow height after
30 days of snowfall
(spatial correlation)
- TerraSAR-X:
Change of snow height
within 11 days
(temporal correlation)
- SnowScat:
Change of snow height
within 13 days.
(temporal correlation)

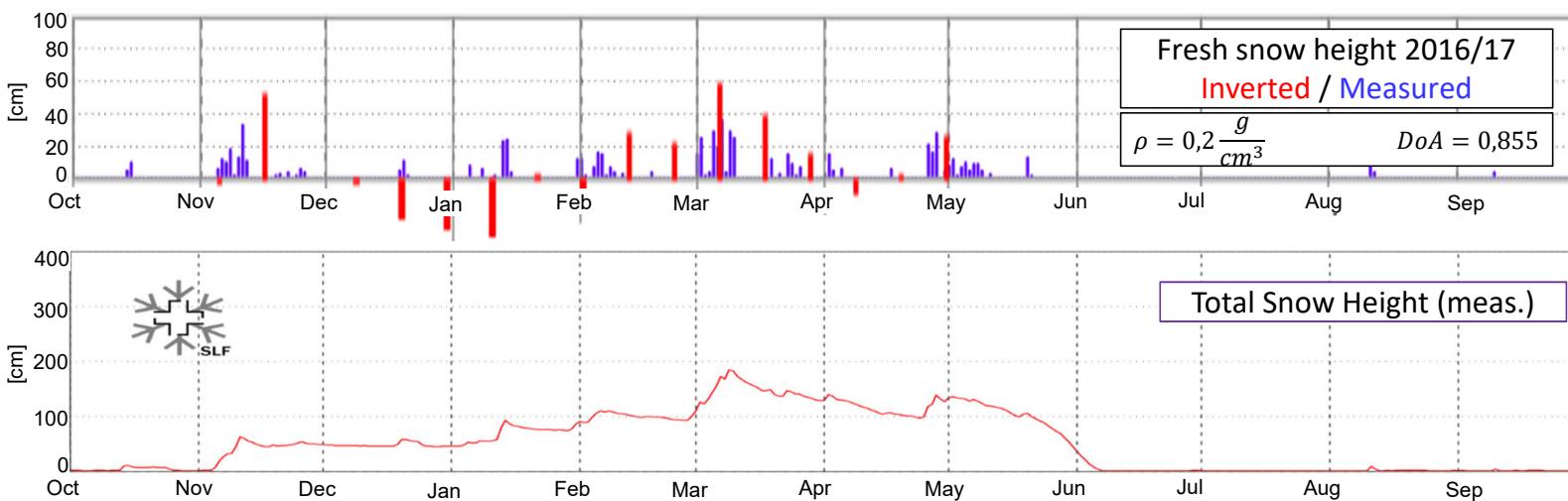
Time series: TSX and SnowScat



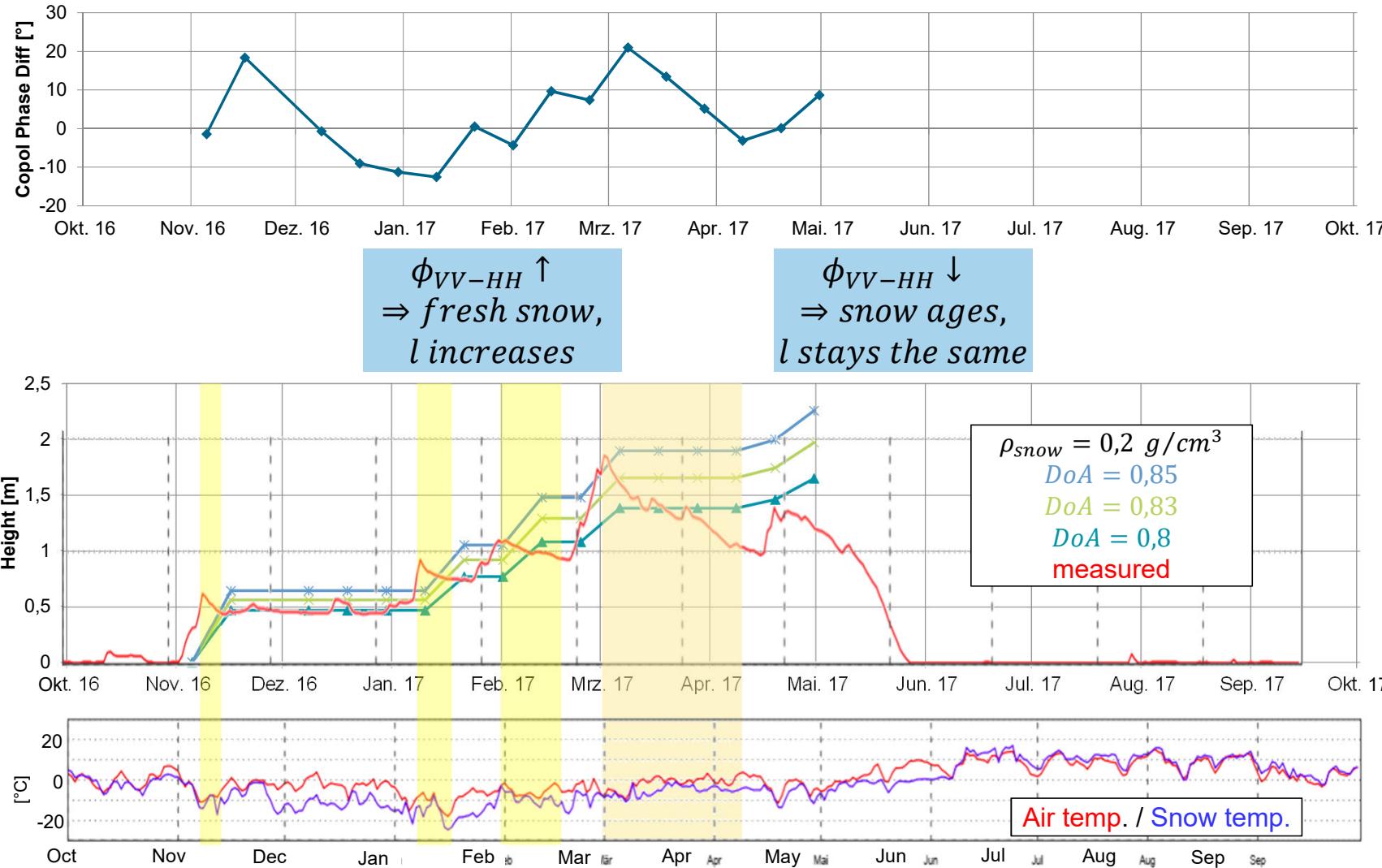
SnowScat shows same result, but with > 50x better temporal resolution

Available Ground Measurements

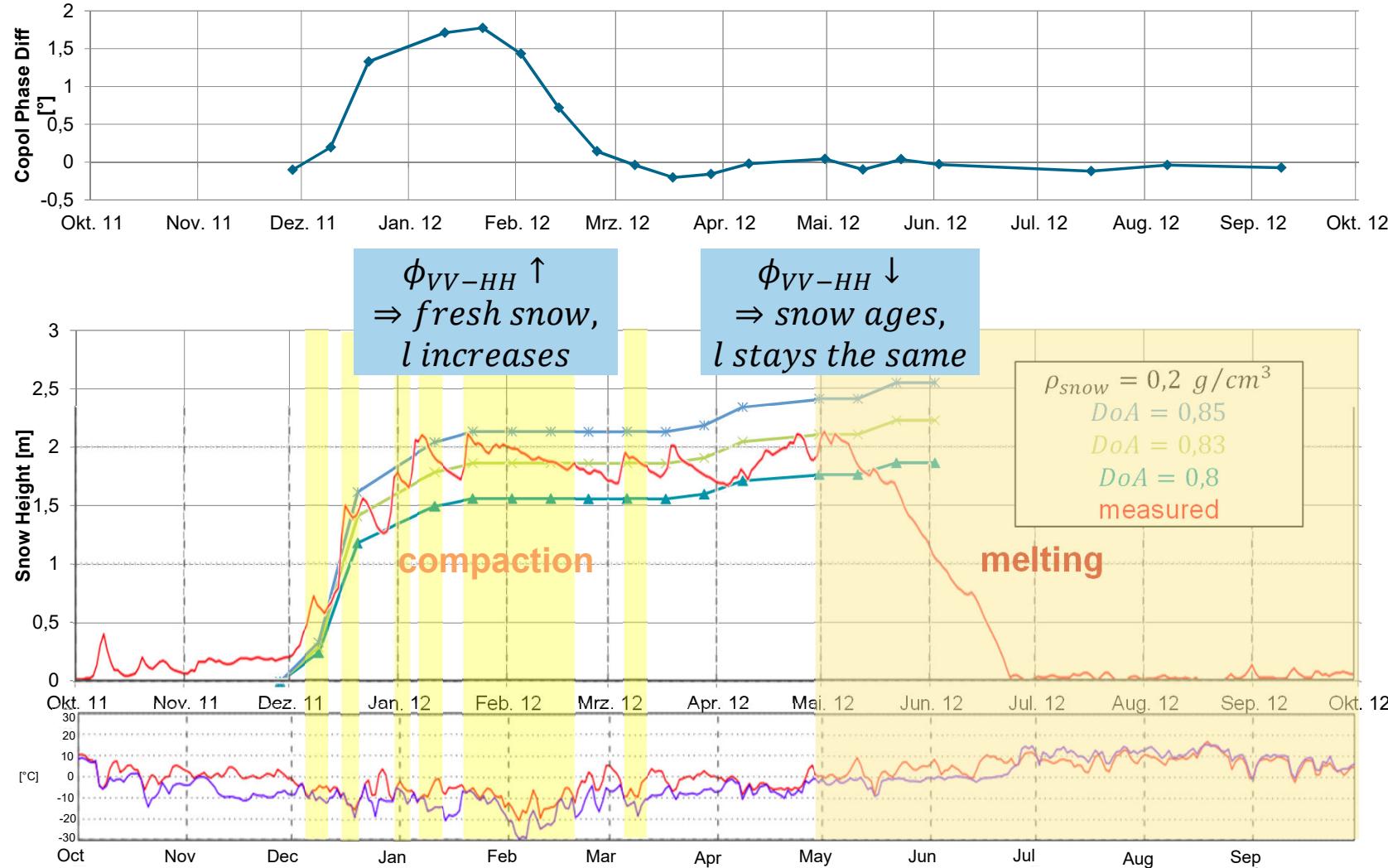
- ✓ With ϕ_{VV-HH} and Propagation Model the aim is to monitor snow accumulation of the Aletsch Glacier
- ✓ Ground measurements provided by the Institute for Snow and Avalanche Research (SLF)
- ✓ Automatic station at 2500 m provides:
 - ✓ Fresh snow height
 - ✓ Total snow height (daily)
 - ✓ Wind speed and direction
 - ✓ Air and snow surface temperature



Inversion of Total Snow Height (2016-17)



Tentative Total Snow Height Estimation (2011-12)



Limitations of Snow Height Estimation Approach



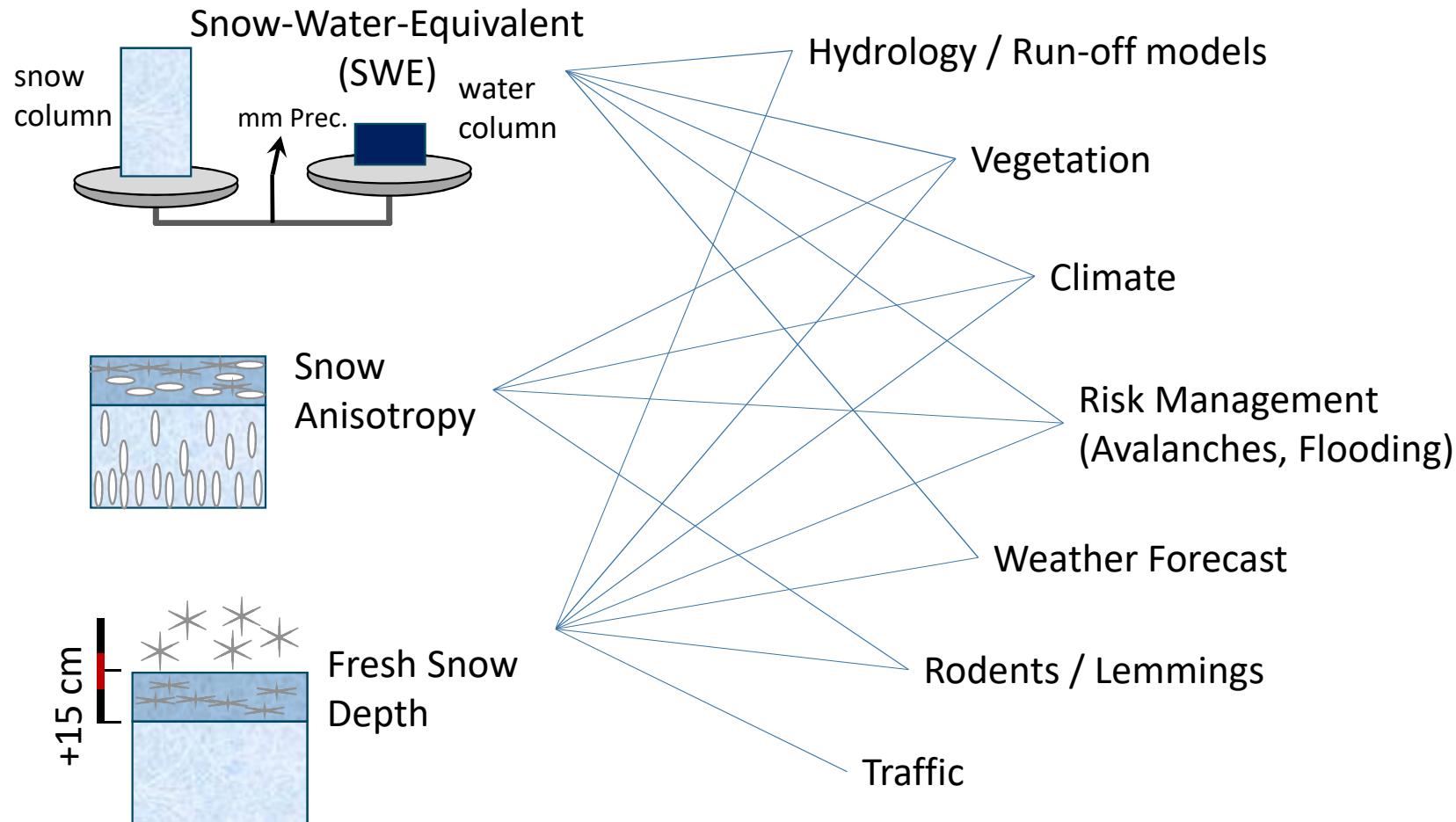
Snow Melting if $T > 0^\circ\text{C}$

- ✓ Snow melting dependent on several parameters
 - ✓ Temperature
 - ✓ Snowpack density
 - ✓ Rain
 - ✓ Mass of the snowpack

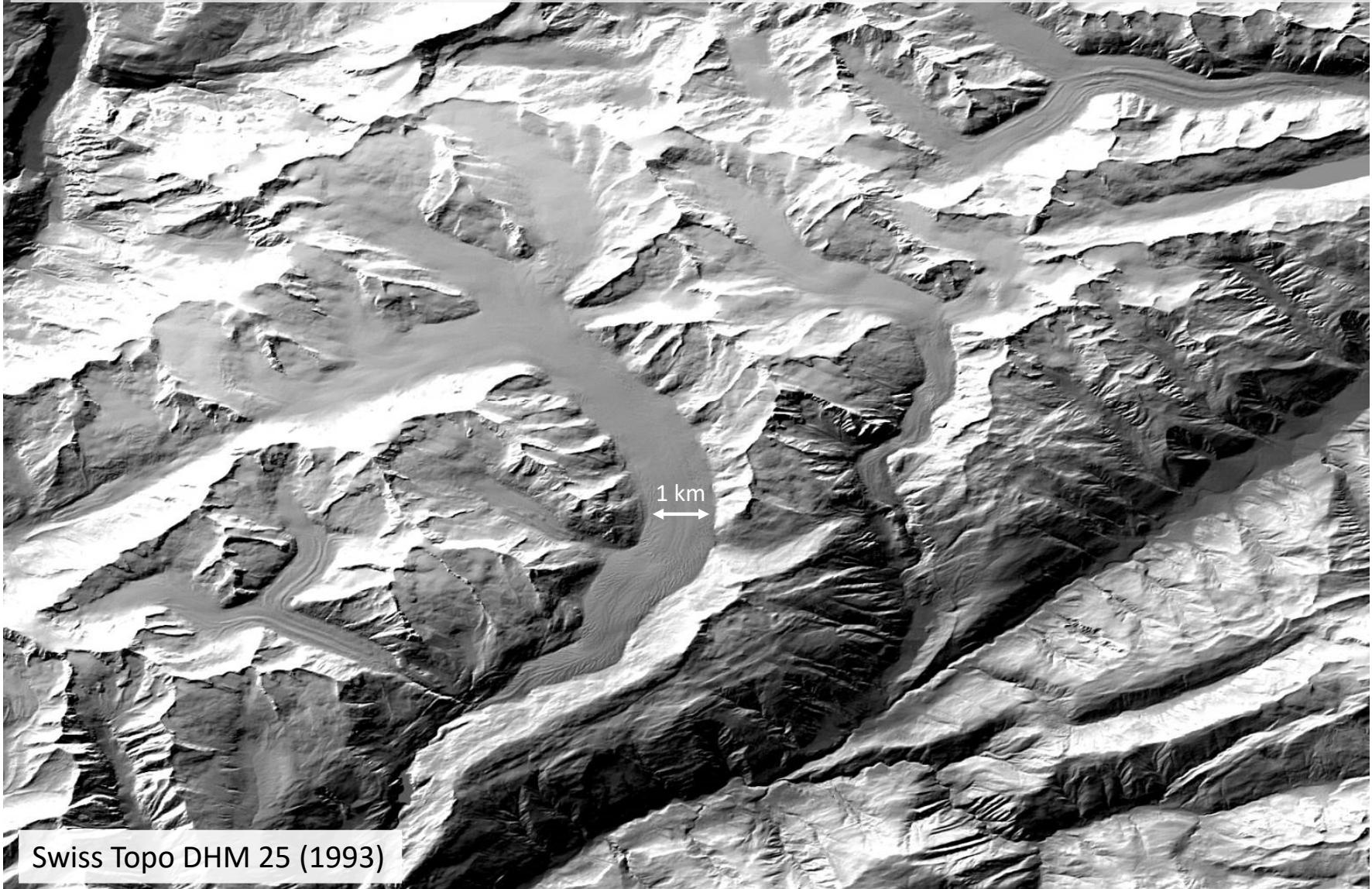
Snow Compaction over Time

- ✓ Snow drift (wind changes density)
- ✓ Snow metamorphism (grains change shape and orientation)
- ✓ Deformation strain (snow compression by its own weight)

Why are snow parameters important?



Great Aletsch Glacier: Mass loss estimated with a DEM



Great Aletsch Glacier: Mass loss estimated with a DEM



Modeled glacier evolution until 2100



initial state (1999)

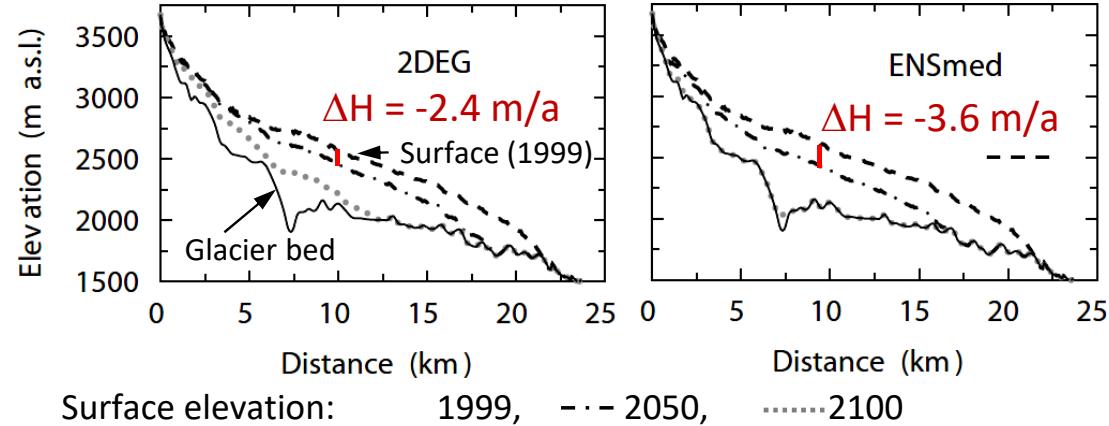
Jouvet et al. J. Glac. (2011)

- 3D glacier dynamic model.
- Calibrated with climate data and field observations from 1880 - 1999.
- Forced by different climate scenarios.

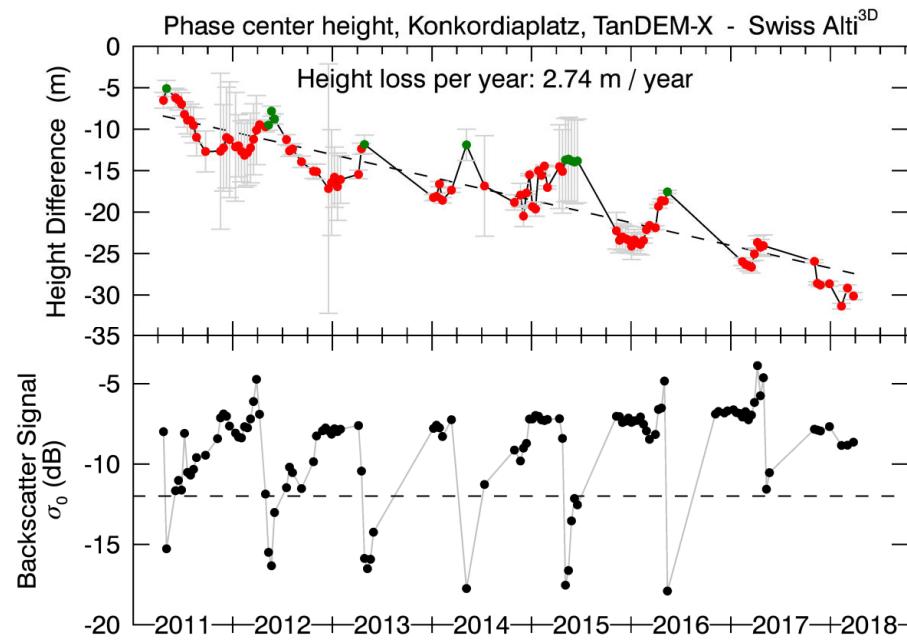
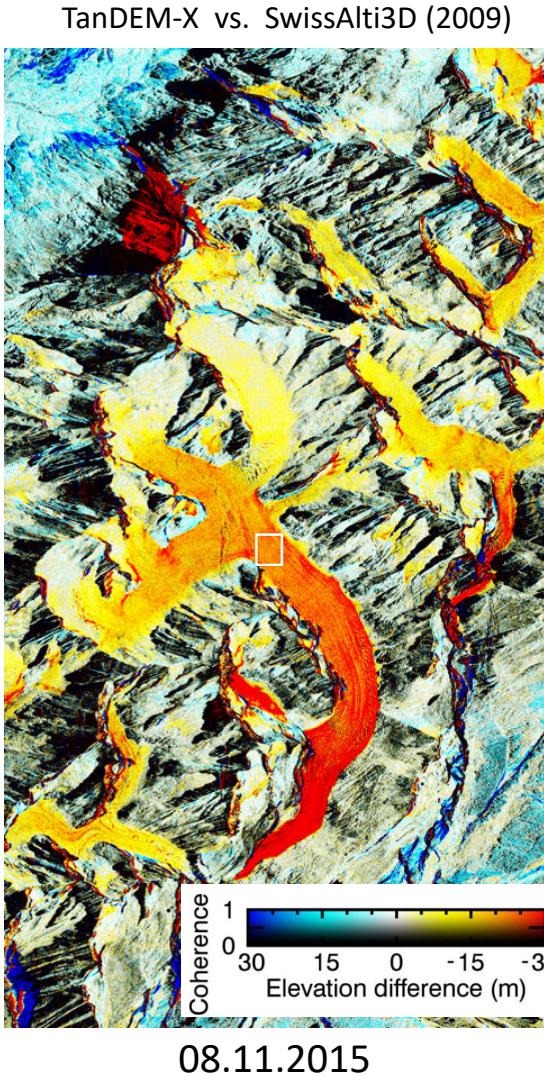


$\Delta T = +4.4^\circ$,
 $\Delta p = +1\%$

Polistacab 2DEG (2100)



Height loss of Aletschgletscher 2011 - 2018



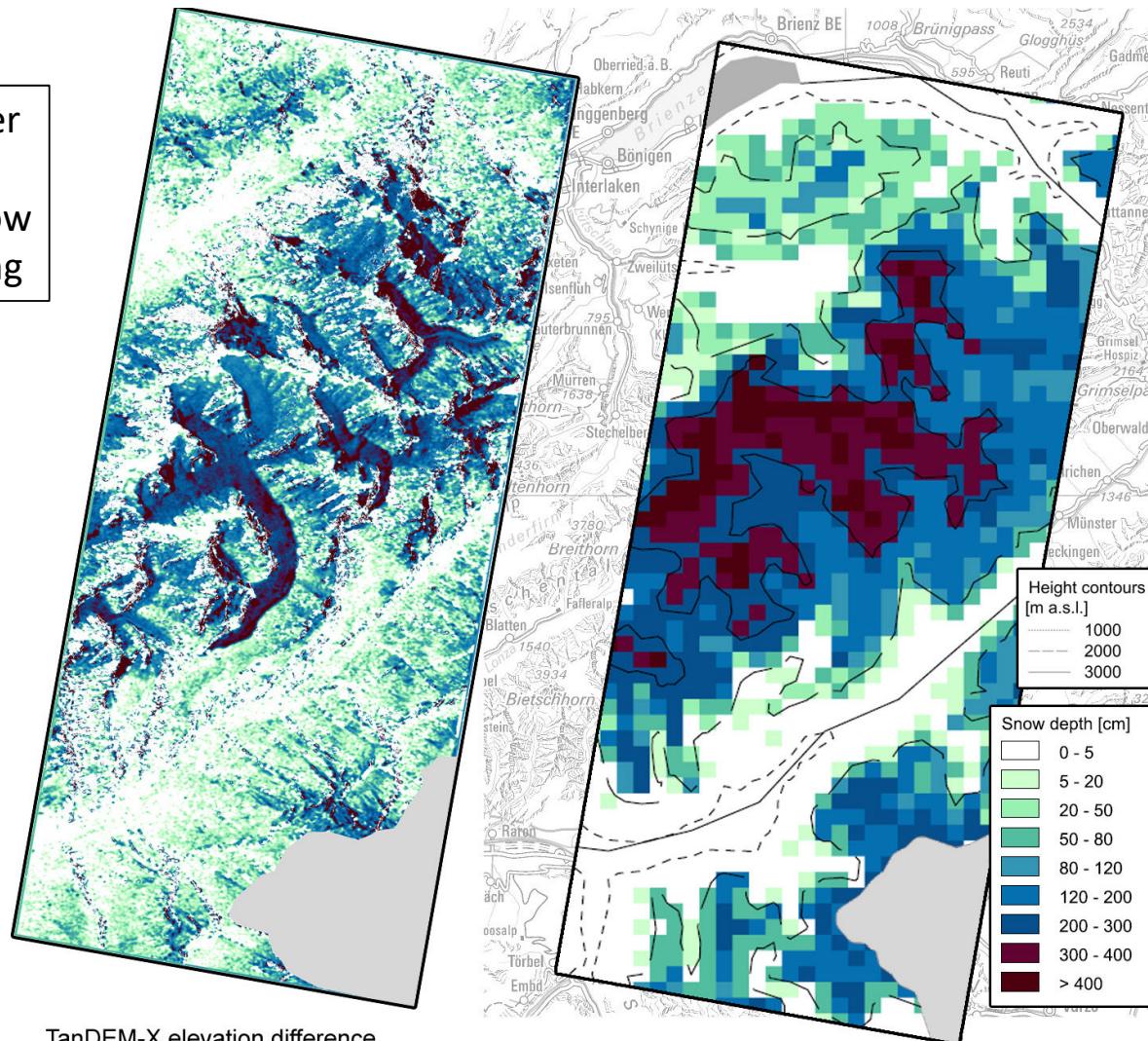
- Agreement with results of climate scenarios:
DEG2: -2.1 m / year (political aim)
ENSmed: -3.6 m / year (business as usual)
- Periodic seasonal changes
- Height increase at the onset of snow melt
(wet snow detected by low backscatter)

L. Leinss

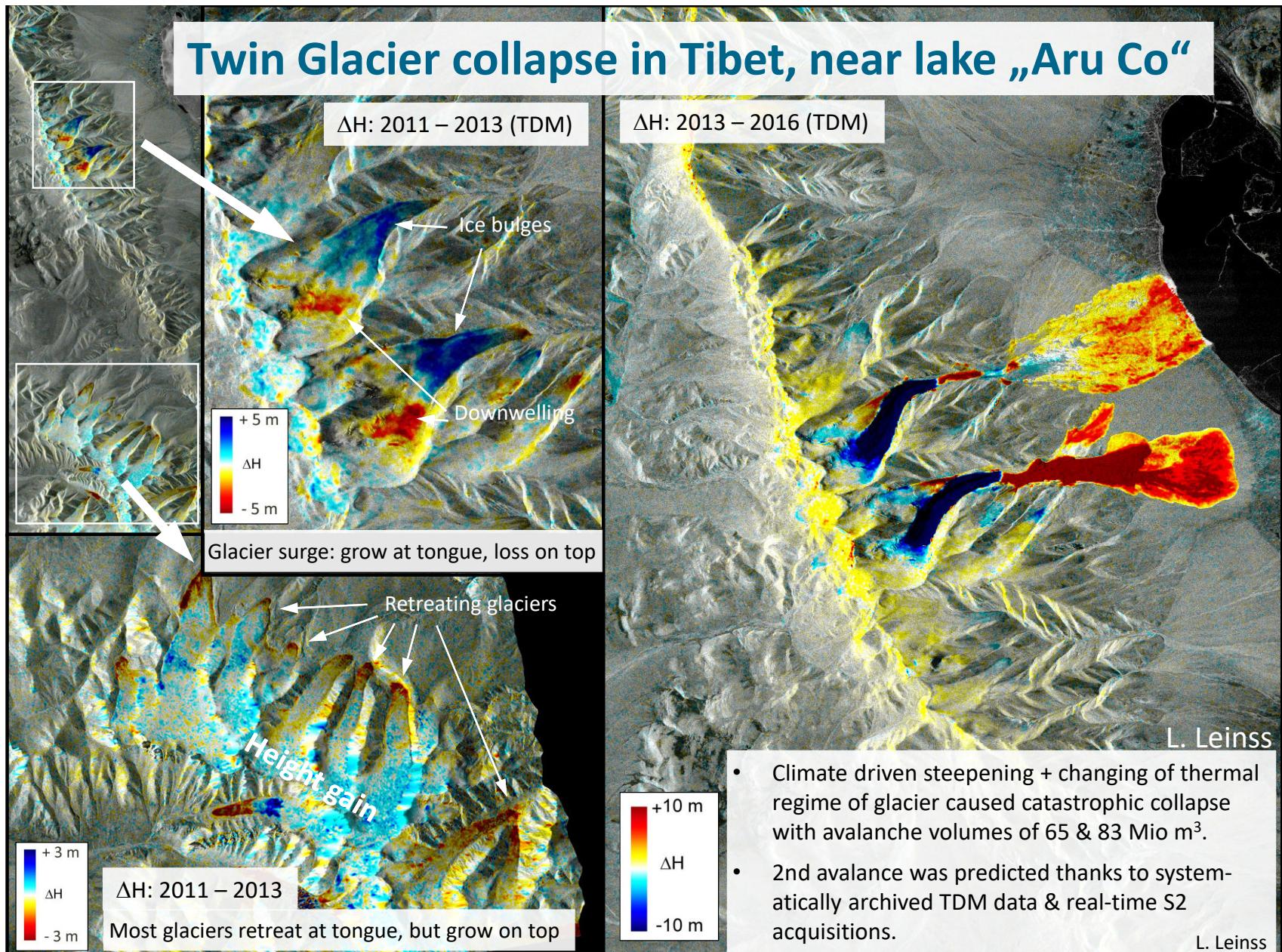
Snow Depth determined by DEM Differencing



summer
vs.
wet snow
in spring



L. Leinss

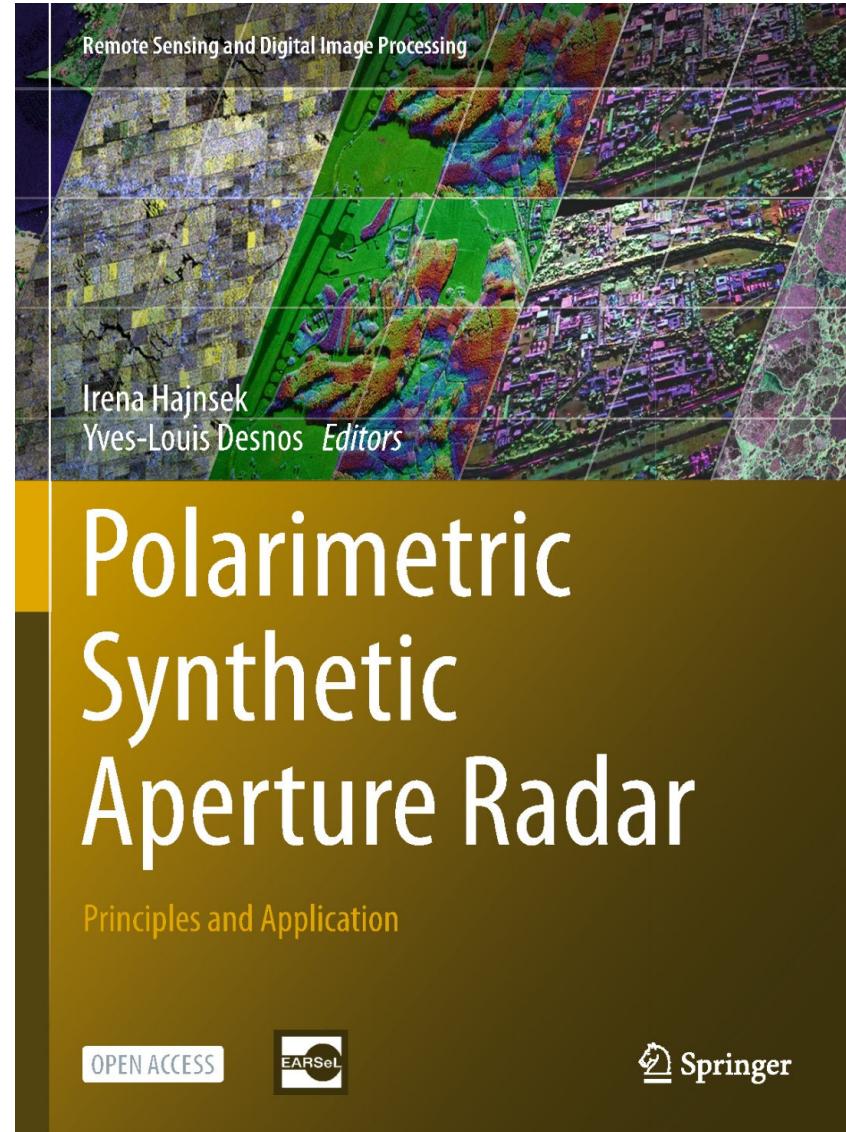


Polarimetric Applications

<https://link.springer.com/book/10.1007%2F978-3-030-56504-6>

Open Access Book

- Basic Principles of SAR Polarimetry
- Forest Applications
- Agriculture Wetland Applications
- Cryosphere Applications
- Urban Applications
- Ocean Applications



I am happy to answer your
question?