定理 1.6 集合について,以下の分配律が成り立つ。

(1)
$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$
 (2) $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$

【証明】

(1):
$$A \cap (B \cup C) = \{x \mid x \in A \text{ か} \supset x \in (B \cup C)\}$$

$$= \{x \mid x \in A \text{ か} \supset (x \in B \text{ または} x \in C)\}$$

$$= \{x \mid (x \in A \text{ か} \supset x \in B) \text{ または} (x \in A \text{ か} \supset x \in C)\}$$

$$= \{x \mid x \in (A \cap B) \text{ または} x \in (A \in C)\}$$

$$= (A \cap B) \cup (A \cap C)$$

(2):
$$A \cup (B \cap C) = \{x \mid x \in A \sharp t \exists x \in (B \cap C)\}$$

$$= \{x \mid x \in A \sharp t \exists x \in B \land \exists x \in C)\}$$

$$= \{x \mid (x \in A \sharp t \exists x \in B) \land \exists (x \in A \sharp t \exists x \in C)\}$$

$$= \{x \mid x \in (A \cup B) \land \exists x \in (A \cup C)\}$$

$$= (A \cup B) \cap (A \cup C)$$