

**定理 1.9** 次の式が成り立つ。

$$(1) \sim(\sim A) = A$$

$$(2) \sim U = \phi$$

$$(3) \sim \phi = U$$

$$(4) A \cup \sim A = U$$

$$(5) A \cap \sim A = \phi$$

【証明】

$$(1): \sim(\sim A) = \{x \mid x \notin \sim A\} = \{x \mid x \in A\} = A$$

$$(2): \sim U = \{x \mid x \notin U\} = \{x \mid x \in \phi\} = \phi$$

$$(3): \sim \phi = \{x \mid x \notin \phi\} = \{x \mid x \in U\} = U$$

$$(4): A \cup \sim A = \{x \mid x \in A \text{ または } x \notin A\} = \{x \mid x \in U\} = U$$

$$(5): A \cap \sim A = \{x \mid x \in A \text{ か } x \notin A\} = \{x \mid x \in \phi\} = \phi$$