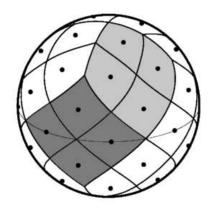
HEALPix Fortran90 Subroutines Overview



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Abstract: This document is an overview of the **HEALPix** For-

tran90 subroutines.

https://healpix.sourceforge.io http://healpix.sf.net

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Conventions

Here we list some conventions which are used in this document.

*	Fortran90 allows generic names which refer to several specific subroutines. Which one of the specific routines is called depends on the type and rank of the arguments supplied in the call. We tag generic names with a \ast in this document.
$\mathbf{N}_{\mathrm{side}}$	$\mathbf{HEALPix}$ resolution parameter — see the $\mathbf{HEALPix}$ Primer.
map	We use the word "map" referring to a function, defined on the set of all HEALPix pixels.
θ	The polar angle or colatitude on the sphere, ranging from 0 at the North Pole to π at the South Pole.
ϕ	The azimuthal angle on the sphere, $\phi \in [0, 2\pi[$.

Changes between releases 3.70 and 3.80

- Improvement of query disc routine in inclusive mode,
- the routines alm2map_spin and map2alm_spin now accept any (integer) spin values $|s| \ge 0$, but the scalar routines alm2map and map2alm are still recommended for vanishing spin (s = 0),
- correction of bugs preventing the compilation with versions 10.* of gfortran,

Older Changes

Changes between releases 3.00 and 3.70

Version 3.70

• Addition of the subroutines read_fits_partial and write_fits_partial to read and write FITS files containing polarized or unpolarized maps defined on a fraction of the sky.

Version 3.60

- Faster Spherical Harmonics Transforms in alm2map, alm2map_der, alm2map_spin, map2alm, map2alm_spin thanks to the new libsharp library.
- The routines and function getArgument, getEnvironment and nArguments now calls F2003 extensions instead of external C routines.

Version 3.50

- correction of a bug in map2alm_iterative, when a mask is used in combination with iter_order > 0,
- addition of zbounds in alm2map, alm2map_der, alm2map_spin in order to simulate (faster) a signal on only a fraction
 of the sphere,
- introduction of apply_mask to apply an arbitrary mask and/or a latitude cut to a map,
- improved support for version 18 and more of Intel C and F90 compilers in configure script,
- edition to fitstools.F90 allowing a proper compilation with g95.

Version 3.40

- The facilities anafast and smoothing now support pixel-based quadrature weights. Introduction of the supporting nside2npweights, unfold_weightsfile, get_healpix_weight_file, get_healpix_pixel_weight_file.
- The subroutine input_map in its default mode test the value of the POLCCONV FITS keyword when reading a polarized map, and interpret the polarization accordingly, as described in the note on POLCCONV in The HEALPix Primer.
- median subroutine: faster by moving an internal array from heap to stack; does not crash anymore when dealing with empty data sets.

Version 3.31

- Bug correction in input_map routine for reading of polarized multi-HDU cut sky FITS files;
- Introduction of winfiledir_* and windowfile_* qualifiers in alteralm facility.

Version 3.30

- new routines nest2uniq and uniq2nest for conversion of standard pixel index to/from Unique ID number. See "The Unique Identifier scheme" section in "HEALPix Introduction Document" for more details.
- alm2cl can now produces nine spectra (TT, EE, BB, TE, TB, EB, ET, BT and BE), instead of six previously, when called with two sets of polarized $a_{\ell m}$ and can also symmetrize the output $C(\ell)$ if requested
- the $a_{\ell m}$ generated by create_alm can now take into account non-zero (exotic) TB and EB cross-spectra (option polar=2) if the input FITS file contains the relevant information
- $\bullet \ \ {\tt addition\ of\ asym_cl\ optional\ keyword\ in\ write_minimal_header\ routine}$
- addition of extno optional keyword in write_asctab routine to write in arbitrary HDU
- improved repeat behavior in write_bintabh routine
- edited map2alm_iterative routine to avoid a bug specific to Intel's Ifort 15.0.2
- CFITSIO version 3.20 (August 2009) or more now required

Version 3.20

- HEALPix-F90 routines and facilities can now also be compiled with the free Fortran95 compiler g95 (www.g95.org)
- a separate build directory is used to store the objects, modules, ... produced during the compilation of the source codes
- bug correction in query_disc for some very small discs in standard mode
- improved handling of long FITS keywords, now producing FITS files fully compatible with the PyFITS and Astropy (https://www.astropy.org) Python libraries
- improved FITS file parsing in generate_beam, affecting the external $B(\ell)$ reading in the F90 facilities alteralm, synfast, sky_ng_sim, smoothing.

Version 3.11

- libsharp C routines used for Spherical Harmonics Transforms and introduced in **HEALPix** 3.10 can now be compiled with any gcc version.
- $\bullet~$ bug correction in <code>query_disc</code> routine in <code>inclusive</code> mode
- bug correction in alm2map_spin routine, which had its spin value set to 2

Version 3.10

- Support for cfitsio "Extended File Name Syntax", and usage of libsharp Spherical Harmonics Transform library. See "Fortran Facilities" for details.
- Faster Spherical Harmonics Transform routines thanks to <a>libsharp C routines¹.

Changes up to release 3.00

Version 3.00

- all input FITS files can now be compressed (with a .gz, .Z, .z, or .zip extension) and/or remotely located (with a ftp:// or http:// prefix). Besides, the fits2cl routine, used to read external beam window functions from FITS files, supports (part of) the CFTISIO Extended File Name Syntax in order to read an arbitrary extension identified by its number or its name.
 - Version 3.14 (March 2009) or newer of CFITSIO is required for HEALPix 3.00.
- new code process_mask and new module mask_tools containing the routines dist2holes_nest, fill_holes_nest, maskborder_nest, size_holes_nest useful for mask apodization,
- improved accuracy of the co-latitude calculation in the vicinity of the poles at high resolution in nest2ring, ring2nest, pix2ang_*, pix2vec_*, ...,
- the pixel query routine query_disc has been improved and will return fewer false positive pixels in the inclusive mode.

Version 2.20

- Spherical Harmonics Transform routines now transparently call libpsht C routines, leading to a significant (2 to 4) speed-up factor. This concerns temperature and polarized transforms (alm2map, map2alm) without precomputation of the P_{ℓm} as well as spin weighted (alm2map_spin, map2alm_spin) transforms for 0 < |s| ≤ 100, but not the generation of spatial derivatives (alm2map_der) which still uses the original F90 code. The compilation and linking to libpsht, now shipped with HEALPix, is done automatically, without any extra download or installation for the user².</p>
- All routines for Spherical Harmonics Transforms and most routines for pixel manipulations (ang2xxx, pix2xxx, vec2xxx,..., nside2npix, npix2nside, nside2ntemplates,...) pixel queries (query_*,...) and FITS I/O (input_map, output_map, read_bintab, write_bintab,...) of sky maps now support resolution parameters N_{side} > 8192. This means that the number of pixels and the pixel indexes can now be stored in either integer(I4B) or integer(I8B) variables (on systems supporting 64 bit variables).
 - The reading and writing of $a_{\ell m}$ containing files remains limited to $\ell < 46340$, though. This restriction does not apply to $C(\ell)$ containing files.
- As a positive side effect of their upgrade, the F90 pixel/coordinate conversion routines are now up to 20% faster.
- Introduction of long_count and long_size functions.

Version 2.14

• In alm2map_der routine, a numerical bug affecting the accuracy of the Stokes parameter derivatives $\partial X/\partial \theta$, $\partial^2 X/(\partial \theta \partial \phi \sin \theta)$, $\partial^2 X/\partial \theta^2$, for X = Q, U has been corrected. See "Fortran Facilities" Appendix for details.

Versions 2.10 and 2.13

- New functions in version 2.13:
 - get_healpix_data_dir, get_healpix_main_dir, get_healpix_test_dir return full path to HEALPix directories.
- New routines in version 2.10:

¹ To revert to the original F90 implementation of these routines, the preprocessing variable DONT_USE_SHARP must be set during compilation.

² To revert to the original F90 implementation of all these routines, the preprocessing variable DONT_USE_PSHT must be set during compilation.

- alm2map_spin: synthesis of maps of arbitrary spin
- map2alm iterative: iterative analysis of map
- map2alm_spin: analysis of maps of arbitrary spin
- healpix modules: meta-module
- write_minimal_header: routine to write minimal FITS header
- parse_check_unused: prints out parameters present in parameter file but not used by the code.
- Improved routines:
 - query_strip: the inclusive option now returns all (and only) the pixels overlapping, even partially, with the strip
 - query_disc: when the disc center is on one of the poles, only the pixels overlapping with the disc are now returned.
 - remove_dipole: can now deal with non-uniform pixel weights.
 - parse_init: silent mode
 - parse_string: can expand environment variables (\${XXX}) and leading ~/

Version 2.0

Some new features have been added

- Most routines dealing with maps and $a_{\ell m}$ (eg, create_alm, map2alm, alm2map, convert_inplace, convert_nest2ring, udgrade_nest, udgrade_ring) or inputting or outputting data (read_*, write_*) now accept both single and double precision arguments.
- The routines map2alm and remove_dipole can now deal with non-symmetric azimuthal cut sky. For backward compatibility, the former calling sequence is still accepted.
- most routines are now parallelized with OpenMP (for shared memory architecture), and some of them are also parallelized with MPI (for distributed memory architecture)

Some new routines have been introduced since version 1.2, as listed below.

- New routines in version 2.0
 - add_dipole, alm2cl, alm2map_der, fits2cl (replaces read_asctab), nside2ntemplates, plm_gen, rand_gauss, rand_init, rand_uni, same_shape_pixels_nest, same_shape_pixels_ring, template_pixel_nest, template_pixel_ring, write_plm (replaces write_dbintab).
- New modules or modules with new name
 - misc_utils: assert_alloc, assert_directory_present, assert_not_present, assert_present, fatal_error, file_present, string, strupcase, strlowcase, upcase, lowcase, wall_clock_time, brag_openmp
 - rngmod: rand_gauss, rand_init, rand_uni
- The following routines are superseded.
 - read_asctab (replaced by fits2cl)
 - write_dbintab (replaced by write_plm)

Version 1.2

Some new routines have been introduced since version 1.1, as listed below.

- New routines in version 1.2
 - angdist, complex_fft, concatnl, del_card, get_card, getargument, getenvironment, input_tod*, nArguments, parse_double, parse_init, parse_int, parse_lgt, parse_long, parse_real, parse_string (see parse_xxx), query_disc (replaces getdisc_ring), query_polygon, query_strip, query_triangle, read_fits_cut4, real_fft, scan_directories, surface_triangle, vect_prod, write_bintabh, write_fits_cut4,

- $\bullet~$ New modules or modules with new name
 - the modules extension (C extensions), healpix_fft (FFT operations), paramfile_io (parameter parsing) have been introduced,
 - the module wrap_fits has been renamed head_fits to reflect its extended capabilities in manipulating FITS headers
- The following routines are superseded. They have been moved to the obsolete module.
 - ask_inputmap, ask_outputmap, ask_lrange (initially in fitstools module)
 - setpar, getpar, anafast_parser, anafast_setpar, anafast_getpar, hotspots_parser, hotspots_setpar, hotspots_getpar, udgrade_parser, udgrade_setpar, udgrade_getpar, smoothing_parser, smoothing_setpar, smoothing_getpar (initially in utilities module).

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add card

Location in HEALPix directory tree: src/f90/mod/head_fits.F90

This routine writes a keyword of any kind into a FITS header. It is a wrapper to other routines that write keywords of different kinds.

Arguments appearing in *italic* are optional.

name & dimensionality	kind in/out	description
header(LEN=80) DIMENSION(:)	CHR INOUT	The header to write the keyword to.
kwd(LEN=*)	CHR IN	the FITS keyword to write.
		Should be shorter or equal to 8 characters.
value	any IN	the value (double, real, integer, logical or character string) to give to the keyword. Note that long string values (more than 68 characters in length) are supported.
comment(LEN=*)	CHR IN	comment to the keyword.

name & dimensionality	kind	in/out	description
update	LGT	IN	if set to .true., the first occurence of the keyword kwd in header will be updated (and all other occurences removed); otherwise, the keyword will be appended at the end (and any previous occurence removed). If the keyword is either 'HISTORY' or 'COMMENT', update is ignored and the keyword is peacefully appended at the end of the header.

EXAMPLE:

```
character(len=80), dimension(1:120) :: header
header = " ! very important
call add_card(header,'NSIDE',256,'the nside of the map')
```

Gives the keyword 'NSIDE' the value 256 in the given headerstring. It is important to make sure that the header string array is empty before attempting to write anything in it.

MODULES & ROUTINES

This section lists the modules and routines used by add_card.

write_hl	more general routine for adding a keyword to a header.
cfitsio	library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to add_card.

write_minimal_header	routine to write HEALPix compliant baselin
	FITS header

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get _card	general purpose routine to read any keywords from a header in a FITS file.
del	routine to discard a keyword from a FITS header
read_par, number_of_alms	routines to read specific keywords from a header in a FITS file.
getsize_fits	function returning the size of the data set in a fits file and reading some other useful FITS keywords
$merge_headers$	routine to merge two FITS headers

add_dipole*

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This routine provides a means to add a monopole and dipole to a **HEALPix** map.

FORMAT call add_dipole*(nside, map, ordering, degree, multipoles[, fmissval])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
nside	I4B	IN	value of N_{side} resolution parameter for in-
4			put map
map(0:12*nside*nside-1)	$\frac{\mathrm{SP}}{\mathrm{SP}}$	INOUT	HEALPix map to which the monopole
	DP		and dipole will be added. Those are
			added to all unflagged pixels.
ordering	I4B	IN	HEALPix scheme 1:RING, 2:
			NESTED
degree	I4B	IN	multipoles to add. It is either 0 (nothing
			done), 1 (monopole only) or 2 (monopole
			and dipole)
multipoles(0:degree*degree-	DP	IN	values of monopole and dipole to add.
1)			The monopole is described as a scalar
			in the same units as the input map, the
			dipole as a 3D cartesian vector, in the
			same units.
fmissval	SP/	IN	value used to flag bad pixel on input
	$\overrightarrow{\mathrm{DP}}$		(default: -1.6375e30). Pixels with that
			value are left unchanged.

add_dipole*

EXAMPLE:

call add_dipole*(128, map, 1, 2, (/ 10.0_dp, 0.0_dp, 1.2_dp, 0.0_dp /))

map is a **HEALPix** map of resolution $N_{\text{side}} = 128$, with the RING ordering scheme. A monopole of amplitude 10 and a dipole of amplitude 1.2 and directed along the y axis will be added to it.

MODULES & ROUTINES

This section lists the modules and routines used by **add_dipole***.

pix_tools module, containing:

RELATED ROUTINES

This section lists the routines related to add_dipole*.

remove_dipole

routine to remove the best fit monopole and monopole from a map.

alm2cl*

Location in HEALPix directory tree: src/f90/mod/alm tools.F90

This routine computes the auto (or cross) power spectra of a one (or two) sets of spherical harmonics coefficients $a_{\ell m}$,

$$C_{12}^{XY}(\ell) = \frac{1}{2\ell+1} \sum_{m=-\ell}^{\ell} a_{1,\ell m}^X a_{2,\ell m}^{Y*}, \tag{1}$$

with X and Y belonging to T, E, B.

If requested, for $X \neq Y$, symmetrized power spectra

$$C_{\{12\}}^{\{XY\}}(\ell) \equiv \frac{C_{12}^{XY}(\ell) + C_{12}^{YX}(\ell)}{2} = \frac{C_{12}^{XY}(\ell) + C_{21}^{XY}(\ell)}{2}$$
(2)

are output.

FORMAT call alm2cl*(nlmax, nmmax, alm1, [alm2,] cl, [symmetric])

Arguments appearing in *italic* are optional.

 $alm2cl^*$

name & dimensionality	kind	in/out	description
		<u> </u>	
nlmax	I4B	IN	the maximum ℓ value used for the
nmmax	I4B	IN	$a_{\ell m}$. the maximum m value used for the
alm1(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	IN	$a_{\ell m}$. First set of $a_{\ell m}$ values. p is 3 or 1 depending on wether polarisation is included or not. In the former case, the first index runs from 1 to 3 corresponding to (T,E,B) .
alm2(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	IN	Second set of $a_{\ell m}$ values.
cl(0:nlmax,1:d)	SP/ DP	OUT	resulting auto or cross power spectra. If both alm1 and alm2 are present, c1 will be their cross power spectrum. If only alm1 is present, c1 will be its power spectrum. If $d=1$, only the temperature spectrum C_ℓ^{TT} will be output. If $d=4$ and $p=3$, the output will be C_ℓ^{TT} , C_ℓ^{EE} , C_ℓ^{BB} and C_ℓ^{TE} . If $d\geq 6$ and $p=3$, C_ℓ^{TB} and C_ℓ^{EB} will also be output, and if $d\geq 9$, $p=3$, and symmetric is not set, C_ℓ^{ET} , C_ℓ^{BT} and C_ℓ^{BE} will be included.
symmetric	LGT	IN	If set to .true. when $d \geq 4$, $p = 3$ and alm2 is present then a symmetrized version of the cross spectra will be output in cl, namely C_{ℓ}^{TT} , C_{ℓ}^{EE} , C_{ℓ}^{BB} , $(C_{\ell}^{TE} + C_{\ell}^{ET})/2$, $(C_{\ell}^{TB} + C_{\ell}^{BT})/2$ and $(C_{\ell}^{EB} + C_{\ell}^{BE})/2$. (default: .false. (unsymmetrized output))

EXAMPLE:

```
lmax = 128 ; mmax = lmax
call alm2cl(lmax, mmax, alm1, cl_auto)
call alm2cl(lmax, mmax, alm1, alm2, cl_cross)
call alm2cl(lmax, mmax, alm1, alm2, cl_sym, symmetric=.true.)
```

cl_auto will contain the (auto) power spectrum of the $a_{\ell m}$ coefficients alm1 up to $\ell=128$, cl_cross will be the cross power spectra of the two sets of $a_{\ell m}$ coefficients alm1 and alm2, while cl_sym will be a symmetrized version of cl_cross.

MODULES & ROUTINES

This section lists the modules and routines used by alm2cl*.

none

RELATED ROUTINES

This section lists the routines related to alm2cl*.

map2alm routine extracting the $a_{\ell m}$ coefficients from a

HEALPix map

create_alm routine to generate randomly distributed $a_{\ell m}$ co-

efficients according to a given power spectrum

 $alm2map^*$

alm2map*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine is a wrapper to 10 other alm2map sc X, alm2map_sc_pre_X, alm2map_pol_X, alm2map_pol_pre1_X, alm2map_pol_pre2_X, where X stands for either s or d. These routines synthesize a ${\bf HEALPix}$ RING ordered temperature map (and if specified, polarisation maps) from input $a_{\ell m}^T$ (and if specified $a_{\ell m}^E$ and $a_{\ell m}^B$) values. The different routines are called dependent on what parameters are passed. Some routines synthesize maps with or without precomputed harmonics (note that since **HEALPix** v2.20 precomputed harmonics most likely won't speed up computation) and some with or without polarisation. The routines accept both single and double precision arrays for alm_TGC and map_TQU. The precision of these arrays should match.

FORMAT	call	alm2map*(nsmax,	nlmax,	nmmax,
	$\mathrm{alm}_{_}$	_TGC, map_TQU[,	plm= zbou	nds=])

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	the N_{side} value of the map to synthesize.
nlmax	I4B	IN	the maximum ℓ value used for
nmmax	I4B	IN	the $a_{\ell m}$. the maximum m value used for
alm_TGC(1:p, 0:nlmax, 0:nmmax)	SPC or DPC	IN	the $a_{\ell m}$. The $a_{\ell m}$ values to make the map from. p is 3 or 1 depending on wether polarisation is respec- tively included or not. In the former case, the first index runs from 1 to 3 corresponding to
			(T,E,B).

map_TQU(0:12*nsmax**2-1)	SP	OUT	if only a temperature map is to
$\operatorname{map}_{-1}\operatorname{QO}(0.12\operatorname{nsmax}^{-1}2\text{-}1)$		001	be synthesized, the map-array
	or DP		
TOU(0.10* **0.1.1.2)		OHT	should be passed with this rank.
$map_TQU(0:12*nsmax**2-1, 1:3)$	SP	OUT	if both temperature an polar-
	or		isation maps are to be syn-
	DP		thesized, the map array should
			have this rank, where the sec-
			ond index is $(1,2,3)$ correspond-
			ing to (T,Q,U) .
$plm(0:n_plm-1),$	DP	IN	If this optional matrix is
OPTIONAL			passed with this rank, precom-
			puted $P_{\ell m}(\theta)$ are used instead
			of recursion. $(n_plm =$
			nsmax*(nmmax+1)*(2*nlmax-
			nmmax+2).
$plm(0:n_plm-1,1:3),$	DP	IN	If this optional matrix is passed
OPTIONAL			with this rank, precomputed
			$P_{\ell m}(\theta)$ AND precomputed
			tensor harmonics are used
			instead of recursion. $(n_plm =$
			nsmax*(nmmax+1)*(2*nlmax-
			nmmax+2).
zbounds $(1:2)$,	DP	IN	section of the sphere on which
OPTIONAL			to perform the map synthe-
			sis, expressed in terms of
			$z = \sin(\text{latitude}) = \cos(\theta).$
			If $zbounds(1) < zbounds(2)$, it
			is performed on the strip
			zbounds $(1) < z < z$ bounds (2) ;
			if not, it is performed out-
			side the strip zbounds(2) \leq
			$z \leq z$ bounds(1). If absent, the
			whole map is processed. Cur-
			rently, zbounds and plm can not
			be used together.
			ac acca vogomer.

EXAMPLE:

use healpix_types

use pix_tools, only : nside2npix
use alm_tools, only : alm2map

integer(I4B) :: nside, lmax, mmax, npix

 $alm2map^*$

```
real(SP), dimension(:,:), allocatable :: map
complex(SPC), dimension(:,:,:), allocatable :: alm
real(DP), dimension(1:2) :: zrange
...
nside=256 ; lmax=512 ; mmax=lmax
npix=nside2npix(nside)
allocate(alm(1:3,0:lmax,0:mmax))
allocate(map(0:npix-1,1:3))
...
zrange =(/ 0.0_dp, 0.5_dp /)
call alm2map(nside, lmax, mmax, alm, map, zbounds=zrange)
```

Make temperature and polarisation maps from the scalar and tensor $a_{\ell m}$ passed in alm. The maps have $N_{\rm side}$ of 256, and are constructed from $a_{\ell m}$ values up to 512 in ℓ and m. In order to save time, the maps are only generated on the range 0 < z < 0.5 (leaving the other pixels to 0) even though the input $a_{\ell m}$ are those of a full sky map.

MODULES & ROUTINES

This section lists the modules and routines used by alm2map*.

Note: Starting with version 3.10, libsharp routines will be called when precomputed $P_{\ell m}$ are not provided.

RELATED ROUTINES

This section lists the routines related to alm2map*.

alm2map_der routine generating a map and its derivatives from its $a_{\ell m}$

alm2map_spin routine generating maps of arbitrary spin from their ${}_sa_{\ell m}$ smoothing executable using alm2map* to smooth maps synfast executable using alm2map* to synthesize maps. map2alm routine performing the inverse transform of alm2map*. create_alm routine to generate randomly distributed $a_{\ell m}$ coefficients according to a given power spectrum

pixel_window, generate_beam

 $alter_alm$

return the ℓ -space $\mathbf{HEALPix}$ -pixel and beam window function respectively modifies $a_{\ell m}$ to emulate effect of real space filtering

 $alm2map_der^*$ 23

$alm2map_der*$

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine is a wrapper to four other routines that synthesize a **HEALPix** temperature (and polarisation) map(s), its (their) first derivatives, and optionally its (their) second derivatives. The routines accept both single and double precision arrays for alm, map, der1 and der2. The precision of these arrays should match. All maps produced are RING ordered.

See "Fortran Facilities" Appendix for a note on a bug affecting the calculation of polarisation derivatives on past versions of this routine.

FORMAT

call alm2map_der*(nsmax, nlmax, nmmax, alm, map, der1[, der2=, zbounds=])

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	the N_{side} value of the map to synthesize.
nlmax	I4B	IN	the maximum ℓ value used for the
nmmax	I4B	IN	$a_{\ell m}$. the maximum m value used for the
alm(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	IN	$a_{\ell m}$. The $a_{\ell m}$ values to make the map from. p is either 1 (temperature only) or 3 (temperature+polarisation).
map(0:12*nsmax**2-1) or $(0:12*nsmax**2-1,1:3)$	SP/ DP	OUT	temperature map $T(p)$ or temperature + polarisation maps $T(p)$, $Q(p)$, $U(p)$ to be synthesized.
der1(0:12*nsmax**2-1, 1:2*p)	SP/ DP	OUT	contains on output the first derivatives of T: $(\partial T/\partial \theta, \partial T/\partial \phi/\sin \theta)$ or the interleaved derivatives of T, Q, and U: $(\partial T/\partial \theta, \partial Q/\partial \theta, \partial U/\partial \theta; \partial T/\partial \phi/\sin \theta,)$
der2(0:12*nsmax**2-1,1:3*p), OPTIONAL	SP/ DP	OUT	If this optional matrix is passed with this rank, it will contain on output the second derivatives $(\partial^2 T/\partial \theta^2, \partial^2 T/\partial \theta \partial \phi/\sin \theta, \partial^2 T/\partial \phi^2/\sin^2 \theta)$ or $(\partial^2 T/\partial \theta^2, \partial^2 Q/\partial \theta^2, \partial^2 Q/\partial \theta^2, \ldots)$
zbounds(1:2), OPTIONAL	DP	IN	section of the sphere on which to perform the map synthesis, expressed in terms of $z = \sin(\operatorname{latitude}) = \cos(\theta)$. If $z = \sin(\operatorname{latitude}) = \cos(\theta)$. If $z = \sin(\operatorname{latitude}) = \cos(\theta)$, it is performed on the strip $z = \sin(1) < z < \operatorname{zbounds}(2)$; if not, it is performed outside the strip $z = \operatorname{latitude}(2) \le z \le \operatorname{zbounds}(1)$. If $z = \operatorname{absent}(2) \le z \le \operatorname{latitude}(2)$. If $z = \operatorname{latitude}(2) \le z \le \operatorname{latitude}(2)$.

EXAMPLE:

use healpix_types

use pix_tools, only : nside2npix

 $alm2map der^*$ 25

```
use alm_tools, only : alm2map_der
integer(I4B) :: nside, lmax, mmax, npix
real(SP), dimension(:), allocatable :: map
real(SP), dimension(:,:), allocatable :: der1, der2
complex(SPC), dimension(:,:,:), allocatable :: alm
...
nside=256 ; lmax=512 ; mmax=lmax
npix=nside2npix(nside)
allocate(alm(1:1,0:lmax,0:mmax))
allocate(alm(1:1,0:lmax,0:mmax))
allocate(der1(0:npix-1,1:2), der2(0:npix-1,1:3))
...
call alm2map_der(nside, lmax, mmax, alm, map, der1, der2=der2)
```

Make temperature maps and its derivatives from the $a_{\ell m}$ passed in alm. The maps have $N_{\rm side}$ of 256, and are constructed from $a_{\ell m}$ values up to 512 in ℓ and m.

MODULES & ROUTINES

This section lists the modules and routines used by alm2map der*.

RELATED ROUTINES

This section lists the routines related to alm2map_der*.

alm2map	routine generating maps of temperature and polarisation from their $a_{\ell m}$
alm2map_spin	routine generating maps of arbitrary spin from their ${}_sa_{\ell m}$

create_alm rou

routine to generate randomly distributed $a_{\ell m}$ coefficients according to a given power spectrum

alm2map_spin* 27

alm2map_spin*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine produces the maps of arbitrary spin s and -s given their alm coefficients. A (complex) map S of spin s is a linear combination of the spin weighted harmonics ${}_{s}Y_{\ell m}$

$${}_{s}S(p) = \sum_{\ell m} {}_{s}a_{\ell m} \quad {}_{s}Y_{\ell m}(p) \tag{3}$$

for $\ell \geq |m|, \ell \geq |s|$, and is such that ${}_sS^* = {}_{-s}S$. The usual phase convention for the spin weighted harmonics is ${}_sY^*_{\ell m} = (-1)^{s+m}{}_{-s}Y_{\ell-m}$ and therefore ${}_sa^*_{\ell m} = (-1)^{s+m}{}_{-s}a_{\ell-m}$. alm2map_spin* expects the alm coefficients to be provided as

$$_{|s|}a_{\ell m}^{+} = -(_{|s|}a_{\ell m} + (-1)^{s}_{-|s|}a_{\ell m})/2,$$
 (4)

$$a_{|s|} = -(|s|a_{\ell m} - (-1)^s - |s|a_{\ell m})/(2i),$$
 (5)

for $m \ge 0$, knowing that, just as for spin 0 maps, the coefficients for m < 0 are given by

$$_{|s|}a_{\ell-m}^+ = (-1)^m{}_{|s|}a_{\ell m}^{+*},$$
 (6)

$$a_{|s|}a_{\ell-m} = (-1)^m a_{|s|}a_{\ell m}^{-*}.$$
 (7)

The two (real) maps produced by $alm2map_spin*$ are defined respectively as

$$_{|s|}S^{+} = (_{|s|}S + _{-|s|}S)/2,$$
 (8)

$$_{|s|}S^{-} = (_{|s|}S - _{-|s|}S)/(2i).$$
 (9)

With these definitions, ${}_2a^+, {}_2a^-, {}_2S^+$ and ${}_2S^-$ match **HEALPix** polarization a^E, a^B, Q and U respectively. **However**, for $s=0, {}_0a^+_{\ell m}=-a^T_{\ell m}, {}_0a^-_{\ell m}=0, {}_0S^+=T, {}_0S^-=0.$

When dealing only with scalar quantities, like temperature or intensity maps, having a spin s = 0, it is highly recommended, and much more memory-efficient, to use directly the routine alm2map, rather then setting spin= 0 in alm2map spin*.

FORMAT

call alm2map_spin*(nsmax, nlmax, nmmax,
spin, alm, map[, zbounds=])

ARGUMENTS

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	the N_{side} value of the map to synthesize.
nlmax	I4B	IN	the maximum ℓ value used for the
nmmax	I4B	IN	$a_{\ell m}$. the maximum m value used for the
spin	I4B	IN	$a_{\ell m}$. spin s of the maps to be generated (only its absolute value is relevant).
alm(1:2, 0:nlmax, 0:nmmax)	SPC/ DPC	IN	The $_{ s }a_{\ell m}^+$ and $_{ s }a_{\ell m}^-$ values to make the map from.
map(0:12*nsmax**2-1, 1:2)	SP/ DP	OUT	$_{ s }S^+$ and $_{ s }S^-$ output maps
zbounds(1:2), OPTIONAL	DP	IN	section of the sphere on which to perform the map synthesis, expressed in terms of $z = \sin(\operatorname{latitude}) = \cos(\theta)$. If $z = \sin(\operatorname{latitude}) = \cos(\theta)$. If $z = \sin(\operatorname{latitude}) = \cos(\theta)$, it is performed on the strip $z = \sin(1) < z < z = \sin(1)$, it is performed outside the strip $z = \cos(2) \le z \le z = \sin(1)$. If absent, the whole map is processed.

EXAMPLE:

```
use healpix_types
use pix_tools, only : nside2npix
use alm_tools, only : alm2map_spin
integer(I4B) :: nside, lmax, mmax, npix, spin
real(SP), dimension(:,:), allocatable :: map
complex(SPC), dimension(:,:,:), allocatable :: alm
...
nside=256; lmax=512; mmax=lmax; spin=4
```

alm2map_spin*

```
npix=nside2npix(nside)
allocate(alm(1:2,0:lmax,0:mmax))
allocate(map(0:npix-1,1:2))
...
call alm2map_spin(nside, lmax, mmax, spin, alm, map)
```

Make spin-4 maps from the $a_{\ell m}$ passed in alm. The maps have N_{side} of 256, and are constructed from $a_{\ell m}$ values up to 512 in ℓ and m.

MODULES & ROUTINES

This section lists the modules and routines used by alm2map_spin*.

ring_synthesis Performs FFT over m for synthesis of the rings. compute_lam_mm, get_pixel_layout, gen_lamfac_der, gen_mfac, gen_mfac_spin, do_lam_lm_spin, gen_recfac, gen_recfac_spin, init_rescale, l_min_ylm Ancillary routines used for $Y_{\ell m}$ recursion module, containing: assert_alloc routine to print error message, when an array can not be allocated properly

Note: Starting with version 3.80, some libsharp routines will be called for any |s| value.

RELATED ROUTINES

This section lists the routines related to alm2map_spin*.

alm2map	routine generating maps of temperature and polarisation from their $a_{\ell m}$
alm2map_der	routine generating maps of temperature and po- larisation, and their spatial derivatives, from their
map2alm_spin	$a_{\ell m}$ routine performing the inverse transform of alm2map.
$create_alm$	routine to generate randomly distributed $a_{\ell m}$ coefficients according to a given power spectrum

alms2fits*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine stores $a_{\ell m}$ values in a binary FITS file. Each FITS file extension created will contain one integer column with $index = \ell^2 + \ell + m + 1$, and 2 or 4 single (or double) precision columns with real/imaginary $a_{\ell m}$ values and real/imaginary standard deviation. One can store temperature $a_{\ell m}$ or temperature and polarisation, $a_{\ell m}^T$, $a_{\ell m}^E$ and $a_{\ell m}^B$. If temperature is specified, a FITS file with one extension is created. If polarisation is specified, a FITS file with 3 extensions one for each set of $a_{\ell m}$, $a_{\ell m}^T$, $a_{\ell m}^E$ and $a_{\ell m}^B$ is created.

FORMAT call alms2fits*(filename, nalms, alms, ncl, header, nlheader, next)

name & dimensionality	kind	in/o	utdescription
filename(LEN=filenamelen)	CHR	IN	filename for the FITS file to store the $a_{\ell m}$ in.
nalms	I4B	IN	number of $a_{\ell m}$ to store.
ncl	I4B	IN	number of columns in the FITS file.
next	I4B	IN	If an standard deviation is given, this number is 5, otherwise it is 3. the number of extensions. 1 for tem-
			perature only, 3 for temperature and polarisation.

alms2fits*

name & dimensions	ality	kind	in/o	utdescription
alms(1:nalms,1:ncl+1,1:next)		SP/ DP	IN	the $a_{\ell m}$ to write to the file. alms(i,1,j) and alms(i,2,j) contain the ℓ and m values for the ith $a_{\ell m}$ (j=1,2,3 for (T,E,B)). alms(i,3,j) and alms(i,4,j) contain the real and imaginary value of the ith $a_{\ell m}$. Finally, the standard deviation for the ith $a_{\ell m}$ is contained in alms(i,5,j) (real) and alms(i,6,j) (imaginary).
nlheader		I4B	IN	number of header lines to write to
header(LEN=80) 1:next)	(1:nlheader,	CHR	IN	the file. the header to the FITS file.

EXAMPLE:

call alms2fits ('alms.fits', 65*66/2, alms, 3, header, 80, 3)

Creates a FITS file with the $a_{\ell m}^T$, $a_{\ell m}^E$ and $a_{\ell m}^B$ values given in alms(1:65*66/2,1:4,1:3). The last index specifies (T,E,B). The second index gives l, m, real($a_{\ell m}$), imaginary($a_{\ell m}$) for each of the $a_{\ell m}$. The number 65*66/2 is the number of $a_{\ell m}$ values up to an ℓ value of 64. 80 lines from header(1:80,1:3) is written to each extension.

MODULES & ROUTINES

This section lists the modules and routines used by alms2fits*.

$write_alms$	routine called by alms2fits* for each extension.
fitstools	module, containing:
printerror	routine for printing FITS error messages.
$\operatorname{cfitsio}$	library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to alms2fits*.

 $fits 2 alms, \ read_conbintab \\ dump_alms$

routines to read $a_{\ell m}$ from a FITS file has the same function as alms2fits* but with parameters passed differently.

alter_alm*

alter alm*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine modifies scalar (and tensor) $a_{\ell m}$ by multiplying them by a beam window function described by a FWHM (in the case of a gaussian beam) or read from an external file (in the more general case of a circular beam) $a_{\ell m} \longrightarrow a_{\ell m} b(\ell)$. It can also be used to multiply the $a_{\ell m}$ by an arbitray function of ℓ .

FORMAT call alter_alm*(nsmax, nlmax, nmmax, fwhm_arcmin, alm_TGC[, beam_file, window])

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	N_{side} resolution parameter of the map associated with the $a_{\ell m}$ considered. Currently has no effect on the routine.
nlmax	I4B	IN	maximum ℓ value for the $a_{\ell m}$.
nmmax	I4B	IN	maximum m value for the $a_{\ell m}$.
fwhm_arcmin	SP/	IN	fwhm size of the gaussian beam in
	DP		arcminutes.
$alm_TGC(1:p,0:nlmax,0:nmmax)$	SPC/	INOUT	complex $a_{\ell m}$ values to be altered.
	DPC		The first index here runs from 1:1
			for temperature only, and 1:3 for po-
			larisation. In the latter case, 1=T,
			2=E, 3=B.

beam_file(LEN=filenamelen) (OPTIONAL)	CHR	IN	name of the file containing the (non necessarily gaussian) window function B_{ℓ} of a circular beam. If present, it will override the argument fwhm_arcmin.
window(0:nlw,1:d) (OPTIONAL)	SP/ DP	IN	arbitrary window by which to multiply the $a_{\ell m}$. If present, it overrides both fwhm_arcmin and beam_file. If nlw < nlmax, the $a_{\ell m}$ with $\ell \in \{\text{nlw+1,nlmax}\}$ are set to 0, and a warning is issued. If $d < p$ the window for temperature is replicated for polarisation.

EXAMPLE:

call alter_alm(64, 128, 128, 1, 5.0, alm_TGC)

Alters scalar and tensor $a_{\ell m}$ of a map with $N_{\rm side}=64$, $\ell_{\rm max}=m_{\rm max}=128$ by multiplying them by the beam window function of a gaussian beam with FWHM = 5 arcmin.

MODULES & ROUTINES

This section lists the modules and routines used by alter_alm*.

$\operatorname{alm_tools}$	module, containing:
generate_beam	routine to generate beam window function
pixel_window	routine to generate pixel window function

RELATED ROUTINES

This section lists the routines related to alter_alm*.

$create_alm$	Routine to create $a_{\ell m}$ coefficients.
rotate_alm	Routine to rotate $a_{\ell m}$ coefficients between 2 dif-
	ferent arbitrary coordinate systems.
$\mathrm{map2alm}$	Routines to analyze a HEALPix sky map into
	its $a_{\ell m}$ coefficients.

alter_alm*

 ${\bf alm2map} \qquad \qquad {\bf Routines\ to\ synthetize\ a\ \bf HEALPix\ sky\ map\ from}$

its $a_{\ell m}$ coefficients.

alms2fits, dump_alms Routines to save a set of $a_{\ell m}$ in a FITS file.

ang2vec

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to convert the position angles (θ, ϕ) of a point on the sphere into its 3D position vector (x, y, z) with $x = \sin \theta \cos \phi$, $y = \sin \theta \sin \phi$, $z = \cos \theta$.

FORMAT

call ang2vec(theta, phi, vector)

ARGUMENTS

name & dimensionality	kind	in/out	description
theta	DP	IN	colatitude in radians measured southward from north pole (in $[0, \pi]$).
phi	DP	IN	longitude in radians measured eastward (in $[0, 2\pi]$).
vector(3)	DP	OUT	three dimensional cartesian position vector (x, y, z) normalised to unity. The north pole is $(0, 0, 1)$

RELATED ROUTINES

This section lists the routines related to ang2vec.

$\operatorname{angdist}$	computes the angular distance between 2 vectors
vec2ang	converts the 3D position vector of point into its position angles on the sphere.
vect_prod	computes the vector product between two 3D vectors

angdist 37

angdist

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Returns the angular distance in radians between two vectors. The input vectors do not have to be normalised. For almost colinear or anti-colinear vectors, renders numerically more accurate results than the \cos^{-1} of the scalar product.

FORMAT

call angdist(v1, v2, dist)

ARGUMENTS

name & dimensionality	kind	in/out	description
v1(3)	DP	IN	cartesian vector. cartesian vector. angular distance in radians between the 2 vectors.
v2(3)	DP	IN	
dist	DP	OUT	

EXAMPLE:

```
use healpix_types
use pix_tools, only : angdist
real(DP) :: dist, one = 1.0_dp
call angdist((/1,2,3/)*one, (/1,2,4/)*one, dist)
print*, dist
```

Returns the angular distance between 2 vectors.

RELATED ROUTINES

This section lists the routines related to **angdist**.

ang2vec

converts the position angles of a point on the sphere into its 3D position vector.

vec2ang	converts the 3D position vector of point into its
	position angles on the sphere.
vect_prod	computes the vector product between two 3D vec-
	tors

apply_mask 39

apply_mask

Location in HEALPix directory tree: $src/f90/mod/pix_tools.F90$

This routine multiplies a ${\bf HEALPix}$ map by an arbitrary pixel mask and/or sets to 0 pixels lying in or out a constant latitude strip

ARGUMENTS

name & dimensionality	kind	in/out	description
map(0:npix-1,1:p)	SP/ DP	INOUT	HEALPix map(s) on which the mask(s) and/or cut will be applied. The map will obviously be modified on output if either mask or zbounds are provided.
ordering	I4B	IN	HEALPix scheme of the map(s) (and mask(s)) 1:RING, 2: NESTED (relevant for zbounds).
mask(0:npix-1,1:q) OPTIONAL	SP/ DP	IN	pixel mask(s). Should have the same ordering and number of pixels (npix) as map. If several maps are provided $(p > 1)$, each map is multiplied by its respective mask, and if there are fewer masks than maps $(q < p)$ the last mask is duplicated as many times as necessary to match the number of maps.
zbounds(1:2) OPTIONAL	DP	IN	section of the map to be set to 0, expressed in terms of $z = \sin(\text{latitude}) = \cos(\theta)$. If $z\text{bounds}(1) < z\text{bounds}(2)$, pixels $outsise$ the strip $z\text{bounds}(1) < z < z\text{bounds}(2)$ are set to 0; if not, pixels on the strip $z\text{bounds}(2) \le z \le z\text{bounds}(1)$ are set to 0. If absent, the map is unchanged.

EXAMPLE:

```
s = sin(15.0_dp * DEG2RAD)
call apply_mask(map, 1, zbounds=(/ s, -s /) )
```

Will set to 0 pixels of the input (RING ordered) map lying in the strip $|b| \leq 15^o$.

MODULES & ROUTINES

This section lists the modules and routines used by apply_mask.

assert_assert_alloc, assert_directory_present,...

Location in HEALPix directory tree: src/f90/mod/misc_utils.F90

The Fortran90 module misc_utils contains a few routines to test an assertion and return an error message if it is false.

SUBROUTINES:

call assert(test [, msg, errcode])

if test is true, proceeds with normal code execution. If test is false, issues a standard error message (unless msg is provided) and stops the code execution with the status errcode (or 1 by default).

call assert_alloc(status, code, array)

if status is 0, proceeds with normal code execution. If not, issues an error message indicating a problem during memory allocation of array in program code, and stops the code execution.

call assert directory present(directory)

issues an error message and stops the code execution if the directory named directory can not be found

call assert_not_present(filename)

issues an error message and stops the code execution if a file with name filename already exists.

call assert present(filename)

issues an error message and stops the code execution if the file named filename can not be found.

call fatal_error([msg])

call fatal_error

issue an (optional user defined) error message and stop the code execution.

ARGUMENTS

name & dimensionality		kind	in/out	description
test msg errorcode	OPTIONAL OPTIONAL	LGT CHR I4B	IN IN IN	result of a logical test character string describing nature of error error status given to code interruption
status		I4B	IN	value of the stat flag returned by the F90
code		CHR	IN	allocate command name of program or code in which alloca- tion is made
array		CHR	IN	name of array allocated
directory		CHR	IN	directory name (contains a '/')
filename		CHR	IN	file name

EXAMPLE:

```
program my_code
use misc_utils
real, allocatable, dimension(:) :: vector
integer :: status
real :: a = -1.

allocate(vector(12345),stat=status)
call assert_alloc(status, 'my_code', 'vector')

call assert_directory_present('/home')

call assert(a > 0., 'a is NEGATIVE !!!')

end program my_code
```

Will issue a error message and stops the code if vector can not be allocated, will stop the code if '/home' is not found, and will stop the code and complain loudly about it because a is actually negative.

brag_openmp 43

brag_openmp

Location in HEALPix directory tree: src/f90/mod/misc_utils.F90

If compiled with shared memory libraries (OpenMP), this routine prints out the number of CPUs used (controlled by the environment variable OMP_NUM_THREADS) and the number of CPUs available.

FORMAT

call brag_openmp()

EXAMPLE:

use misc_utils
call brag_openmp()

Will print out:

Number of OpenMP threads in use: 2 Number of CPUs available: 2

on a bi-pro (or dual core) computer

complex_fft

Location in HEALPix directory tree: src/f90/mod/healpix_fft.F90

This routine performs a forward or backward Fast Fourier Transformation on its argument data.

FORMAT

 $call complex_{fft}(data, backward)$

ARGUMENTS

name&dimensionality	kind in/out	description
data(:)	XXX INOUT	data. It can be of type real(sp), real(dp), complex(spc) or complex(dpc). If it is of
backward	LGT IN	type real, it is interpreted as an array of size(data)/2 complex variables. Optional argument. If present and true, perform backward transformation, else forward

EXAMPLE:

use healpix_fft
call complex_fft (data, backward=.true.)

Performs a backward FFT on data.

RELATED ROUTINES

This section lists the routines related to **complex_fft**.

real fft routine for FFT of real data

compute_statistics*

Location in HEALPix directory tree: src/f90/mod/statistics.f90

This routine computes the min, max, absolute deviation and first four order moment of a data set

FORMAT

call compute_statistics*(data,stats[, badval])

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/outdescription		
data(:)	SP/ DP	IN	data set $\{x_i\}$	
stats	tstats	OUT	structure containing the statistics of the data. The respective fields (stats%field) are:	
ntot	I8B	_	total number of data points	
nvalid	I8B	_	number n of valid data points	
mind, maxd	DP	_	minimum and maximum valid data	
average	DP	_	average of valid points $m = \sum_i x_i/n$	
absdev	DP	_	absolute deviation $a = \sum_{i} x_i - m /n$	
var	DP	_	variance $\sigma^2 = \sum (x_i - m)^2 / (n - 1)$	
rms	DP	_	standard deviation σ	
skew	DP	_	skewness factor $s = \sum (x_i - m)^3 / (n\sigma^3)$	
kurt	DP	_	kurtosis factor $k = \sum (x_i - m)^4 / (n\sigma^4) - 3$	
badval (OPTIONAL)	SP/ DP	IN	sentinel value given to bad data points. Data points with this value will be ignored during calculation of the statistics. If not set, all points will be considered. Do not set to 0! .	

EXAMPLE:

use statistics, only: compute_statistics, print_statistics, tstats

type(tstats) :: stats

. . .

compute_statistics(map, stats)
print*,stats%average, stats%rms
print_statistics(stats)

Computes the statistics of map, prints its average and *rms* and prints the whole list of statistical measures.

RELATED ROUTINES

This section lists the routines related to **compute_statistics***.

median

routine to compute median of a data set

concatnl 47

concatnl

Location in HEALPix directory tree: src/f90/mod/paramfile_io.F90

Function to concatenate up to 10 subtrings interspaced with LineFeed character. Upon printing each subtring will be on a different line.

FORMAT

var=concatnl(string1[, string2, string3, ...])

ARGUMENTS

name & dimensionality	kind	in/out	description
string1 string2	CHR CHR	IN	the first substring to be concatenated. the second substring (if any) to be con-
string3	CHR	optional IN optional	catenated up to 10 substrings can be concatenated.
var	CHR	OUT	concatenation of the substrings interspaced with LineFeed character.

EXAMPLE:

RELATED ROUTINES

This section lists the routines related to **concatnl**.

parse_xxx parse an ASCII file for parameters definition

convert inplace*

convert_inplace*

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to convert a **HEALPix** map from NESTED to RING scheme or vice versa. The conversion is done in place, meaning that it doesn't require memory for a temporary map, like the *convert_nest2ring* or *convert_ring2nest* routines. But for that reason, this routine is slower and not parallelized. The routine is a wrapper for 6 different routines and can threfore process integer, single precision and double precision maps as well as mono or bi dimensional arrays.

FORMAT call convert_inplace*(subcall, map)

ARGUMENTS

name & dimensionality	kind	in/out	description
subcall	_	IN	routine to be called by convert_inplace_real. Set this to ring2nest or nest2ring dependent on wether the conversion is RING to NESTED or vice versa.
map(0:npix-1)	I4B/ SP/	INOUT	mono-dimensional full sky map to be converted, the routine
map(0:npix-1,1:nd)	DP I4B/ SP/ DP	INOUT	finds the size itself. bi-dimensional (nd>0) full sky map to be converted, the routine finds both dimensions itself. Processing a bidimensional map with nd> 1 should be faster than each of the nd 1D-maps consecutively.

EXAMPLE:

call convert_inplace(ring2nest,map)

Converts an map from RING to NESTED scheme.

MODULES & ROUTINES

This section lists the modules and routines used by **convert_inplace***.

nest2ring routine to convert a NESTED pixel index to

RING pixel number.

ring2nest routine to convert a RING pixel index to

NESTED pixel number.

RELATED ROUTINES

This section lists the routines related to **convert_inplace***.

convert_nest2ring convert from NESTED to RING scheme using a

temporary array. Requires more space then con-

vert inplace, but is faster.

convert_ring2nest convert from RING to NESTED scheme using a

temporary array. Requires more space then con-

vert_inplace, but is faster.

convert_nest2ring*

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to convert a $\mathbf{HEALPix}$ map from NESTED to RING scheme.

The routine is a wrapper for 6 different routines and can threfore process integer, single precision and double precision maps as well as mono or bi dimensional arrays.

This routine is fast, and is parallelized for shared memory architecture, but requires extra memory to store a temporary map in.

FORMAT

call convert_nest2ring*(nside, map)

ARGUMENTS

name & dimensionality	kind in/ou	${ m it} { m description}$
nside	I4B IN	the N_{side} parameter of the map to be converted.
map(0:12*nside**2-1)	I4B/ INOU SP/ DP	To be converted to RING scheme.
map(0:12*nside**2-1,1:nd)	I4B/ INOU SP/ DP	bi-dimensional full sky map to be converted to RING scheme. The routine finds the second dimension (nd) by itself. Processing a bidimensional map with nd> 1 should be faster than each of the nd 1D-maps consecutively.

EXAMPLE:

call convert nest2ring(256,map)

Converts an $N_{\rm side}=256$ map given in array map from NESTED to RING scheme.

MODULES & ROUTINES

This section lists the modules and routines used by **convert_nest2ring***.

nest2ring

routine to convert a NESTED pixel index to RING pixel number.

RELATED ROUTINES

This section lists the routines related to **convert_nest2ring***.

convert_ring2nest convert_inplace convert between RING and NESTED schemes. convert between NESTED and RING schemes inplace. This routine is slower than convert_nest2ring*, but doesn't require as much memory.

convert_ring2nest*

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to convert a $\mathbf{HEALPix}$ map from RING to NESTED scheme.

The routine is a wrapper for 6 different routines and can threfore process integer, single precision and double precision maps as well as mono or bi dimensional arrays.

This routine is fast, and is parallelized for shared memory architecture, but requires extra memory to store a temporary map in.

FORMAT

call convert_ring2nest*(nside, map)

ARGUMENTS

name & dimensionality	kind in/ou	${ m it} { m description}$
nside	I4B IN	the N_{side} parameter of the map to be converted.
map(0:12*nside**2-1)	I4B/ INOU SP/ DP	To be converted to RING scheme.
map(0:12*nside**2-1,1:nd)	I4B/ INOU SP/ DP	bi-dimensional full sky map to be converted to RING scheme. The routine finds the second dimension (nd) by itself. Processing a bidimensional map with nd> 1 should be faster than each of the nd 1D-maps consecutively.

EXAMPLE:

call convert ring2nest(256,map)

Converts an $N_{\rm side}=256$ map given in array map from RING to NESTED scheme.

MODULES & ROUTINES

This section lists the modules and routines used by **convert_ring2nest***.

ring2nest

routine to convert a RING pixel index to NESTED pixel number.

RELATED ROUTINES

This section lists the routines related to **convert_ring2nest***.

convert_inplace

convert between NESTED and RING schemes. convert between RING and NESTED schemes inplace. This routine is slower than convert_ring2nest*, but doesn't require as much memory.

coordsys2euler_zyz

Location in HEALPix directory tree: src/f90/mod/coord_v_convert.f90

This routine returns the three Euler angles ψ, θ, φ , corresponding to a rotation between standard astronomical coordinate systems. This angles can then be used in rotate_alm

FORMAT call coordsys2euler_zyz(iepoch, oepoch, isys, osys, psi, theta, phi)

ARGUMENTS

name & dimension-	kind	in/out	description
ality			
iepoch	DP	IN	epoch of the input astronomical coordinate
			system.
oepoch	DP	IN	epoch of the output astronomical coordinate
			system.
isys(len=*)	CHR	IN	input coordinate system, should be
			one of 'E'=Ecliptic, 'G'=Galactic,
			'C'/'Q'=Celestial/eQuatorial.
osys(len=*)	CHR	IN	output coordinate system, same choice as
			above.
psi	DP	OUT	first Euler angle: rotation ψ about the z-axis.
theta	DP	OUT	second Euler angle: rotation θ about the orig-
			inal (unrotated) y-axis;
phi	DP	OUT	third Euler angle: rotation φ about the orig-
			inal (unrotated) z-axis;

EXAMPLE:

```
use coord_v_convert, only: coordsys2euler_zyz
use alm_tools, only: rotate_alm
...
call coordsys2euler_zyz(2000.0_dp, 2000.0_dp, 'E', 'G', psi, theta, phi)
```

call rotate_alm(64, alm_TGC, psi, theta, phi)

Rotate the $a_{\ell m}$ from Ecliptic to Galactic coordinates.

RELATED ROUTINES

This section lists the routines related to **coordsys2euler_zyz**.

rotate_alm apply arbitrary sky rotation to a set of $a_{\ell m}$ coeffi-

cients.

xcc_v_convert rotates a 3D coordinate vector from one astronom-

ical coordinate system to another.

create alm*

create_alm*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine generates scalar (and tensor) $a_{\ell m}$ for a temperature (and polarisation) power spectrum read from an input FITS file. The $a_{\ell m}$ are gaussian distributed with a zero mean, and their amplitude is multiplied with the ℓ -space window function of a gaussian beam characterized by its FWHM or an arbitrary circular beam and a pixel window read from an external file.

FORMAT

call create_alm*(nsmax, nlmax, nmmax, polar, filename, rng_handle, fwhm_arcmin, alm_TGC, header[, windowfile, units, beam_file])

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	N_{side} of the map to be synthetized from the $a_{\ell m}$ created by this routine.
nlmax	I4B	IN	maximum ℓ value to be considered (MAX= $4N_{\rm side}$ if windowfile is provided).
nmmax polar	I4B I4B	IN IN	maximum m value for the $a_{\ell m}$. if set to 0, only Temperature (scalar) $a_{\ell m}$ are generated using TT spectrum. If set to 1, 'conventional' polarization is added, based on EE, BB and TE spectra. If set to 2, and if the relevant information is in filename, polarization is generated assuming non-zero correlation of Curl (B) modes with Temperature (T) and Gradient (E) modes (TB and EB cross-spectra). Note that the synfast facility calls create_alm* with polar=0 or polar=1
filename(LEN = filenamelen)	CHR	IN	name of FITS file containing power spectra in the order TT, [EE, BB, TE, [TB, EB]] (terms in brackets are optional, see polar)
rng_handle	plancl	k_rng INOUT	structure containing information necessary to continue a random sequence initiated previously with the subroutine rand_init. Consecutive calls to create_alm* can be made after a single invocation to rand_init.
fwhm_arcmin alm_TGC(1:p,0:nlmax,0:nmmax)	SP/ DP SPC/ DPC	IN OUT	FWHM size of the gaussian beam in arcminutes. complex $a_{\ell m}$ values generated from the power spectrum in the FITS
			file. The first index here runs form 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.

create alm*

0 10		• , .	
name & dimensionality	kind	in/out	description
header(LEN=80),dimension(60)	CHR	OUT	part of header which will be in-
			cluded in the FITS-file containing
			the map synthesised from the $a_{\ell m}$
			which create_alm generates.
windowfile(LEN=filenamelen)	CHR	IN	full filename specification of the
,			FITS file with the pixel window
			function (defined for $\ell \leq 4N_{\rm side}$)
units(LEN=80), dimension(1:)	CHR	OUT	physical units of the created $a_{\ell m}$
			(square-root of the input power
			spectrum units).
$beam_file(LEN=filenamelen)$	CHR	IN	name of the file containing the
,			(non necessarily gaussian) window
			function B_{ℓ} of a circular beam. If
			present, it will override the argu-
			ment fwhm_arcmin.
			-

EXAMPLE:

use alm_tools, only: create_alm

use rngmod, only: rand_init, planck_rng

type(planck rng) :: rng handle

call rand_init(rng_handle, -1)
call create_alm(64, 128, 128, 1, 'cl.fits', rng_handle, 5.0, alm_TGC, &
 header, 'data/pixel_window_n0064.fits')

Creates scalar and tensor $a_{\ell m}$ from the power spectrum given in the file 'cl.fits'. The map to be created from these $a_{\ell m}$ is assumed to have $N_{\rm side}=64$. C_{ℓ} s from the power spectrum are used up to an ℓ value of 128. Corresponding $a_{\ell m}$ values up to l=128 and m=128 are created as gaussian distributed complex numbers. Their are drawn from a sequence of pseudo-random numbers initiated with a seed of -1. The produced $a_{\ell m}$ are convolved with a gaussian beam of FWHM 5 arcminutes and a pixel window read from 'data/pixel_window_n0064.fits'. It is assumed that after the return from this routine, a map is generated from the created $a_{\ell m}$. For this purpose, header is updated with FITS format information describing the origin and history of these $a_{\ell m}$.

MODULES & ROUTINES

This section lists the modules and routines used by **create_alm***.

alm_tools <u>module</u>, containing:

pow2alm_units routine to convert from power spectrum units to

 $a_{\ell m}$ units

generate_beam routine to generate beam window function
pixel_window routine to read in pixel window function

utilities <u>module</u>, containing:

die_alloc routine that prints an error message if there is not

enough space for allocation of variables.

fitstools <u>module</u>, containing:

fits2cl routine to read a FITS file containing a power

spectrum.

read dbintab routine to read a FITS-binary file containing the

pixel window functions.

head fits module, containing:

add_card routine to add a keyword to a FITS header.

get_card routine to read a keyword value from FITS header.

merge_headers routine to merge two FITS headers.

rngmod <u>module</u>, containing:

rand gauss function which returns a gaussian distributed ran-

dom number.

RELATED ROUTINES

This section lists the routines related to **create** alm*.

rand init subroutine to initiate a random number sequence.

synfast executable using create alm* to synthesize CMB

maps from a given power spectrum.

alm2map Routine to transform a set of $a_{\ell m}$ created by cre-

ate_alm* to a **HEALPix** map.

alms2fits, dump_alms Routines to save a set of $a_{\ell m}$ in a FITS file.

del_card 61

del card

Location in HEALPix directory tree: src/f90/mod/head_fits.F90

This routine removes one or several keywords from a FITS header.

FORMAT

call del_card(header, kwds)

ARGUMENTS

name & dimensionality	kind in/out	description
header(LEN=80)(1:nlheader)	CHR INOUT	The header to remove the keyword(s) from. The routines
kwds(LEN=20)(1:nkws)	CHR IN	finds out the header size. list of FITS keywords to re- move. The routine accepts ei-
kwds(LEN=20)	CHR IN	ther a vector a keywords or a single one in a scalar variable the one FITS keyword to remove.

EXAMPLES: #1

```
call del_card(header,(/ 'NSIDE ','COORD ','ORDERING' /) )
```

Removes the keywords 'NSIDE', 'COORD' and 'ORDERING' from Header

EXAMPLES: #2

```
call del_card(header, 'ORDERING')
```

Removes the keyword 'ORDERING' from Header

MODULES & ROUTINES

This section lists the modules and routines used by **del_card**.

write_hl more general routine for adding a keyword to a

header.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **del card**.

add_card general purpose routine to write any keywords

into a FITS file header

get_card general purpose routine to read any keywords

from a header in a FITS file.

read_par, number_of_alms routines to read specific keywords from a header

in a FITS file.

getsize_fits function returning the size of the data set in a fits

file and reading some other useful FITS keywords

merge_headers routine to merge two FITS headers

dist2holes nest 63

dist2holes nest

Location in HEALPix directory tree: src/f90/mod/mask_tools.F90

For a input binary mask in NESTED ordering, dist2holes_nest returns the angular distance (in radians) from each *valid* (1-valued) pixel to the closest *invalid* (0-valued) pixel. Distances are measured between pixel centers.

FORMAT

call dist2holes_nest(nside, mask, distance)

ARGUMENTS

name & dimensionality	kind	in/out	description
nside mask(0:Npix-1) distance(0:Npix-1)	I4B I4B DP	IN IN OUT	the N_{side} value of the input mask. Input NESTED-ordered mask. Npix = 12*nside*nside Output NESTED-ordered angular-
			distance map

EXAMPLE:

use healpix_types
use healpix_modules

. . .

call dist2holes_nest(nside, mask, distance)

???

MODULES & ROUTINES

This section lists the modules and routines used by **dist2holes_nest**.

mask_tools mask processing module (see related routines below)

RELATED ROUTINES

This section lists the routines related to **dist2holes_nest**.

dist2holes_nest	angular distance to closest invalid pixel of the given mask
fill_holes_nest	turn to $valid$ all pixels located in 'holes' containing fewer pixels than the given threshold
maskborder_nest	identify inner boundary pixels of 'holes' for given mask
size_holes_nest	returns size (in pixels) of holes found in input mask

dump_alms*

dump_alms*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine stores $a_{\ell m}$ values in a binary FITS file. The FITS file created will contain one integer column with $index = \ell^2 + \ell + m + 1$ and 2 single precision columns with real/imaginary $a_{\ell m}$ values. One can store temperature $a_{\ell m}$ or polarisation, $a_{\ell m}^E$ or $a_{\ell m}^B$. If temperature is specified, a FITS file is created. If polarisation is specified, an old FITS file is opened and extra extensions is created.

FORMAT call dump_alms*(filename, alms, nlmax, header, nlheader, extno)

ARGUMENTS

name & dimensionality	kind in/out	description
filename(LEN = filenamelen)	CHR IN	filename for the FITS-file to store the $a_{\ell m}$ in.
nlmax	I4B IN	maximum ℓ value to store.
alms(0:nlmax,0:nlmax)	SPC/ IN DPC	array with $a_{\ell m}$, in the format used by eg. map2alm, so alms(1,m) corresponds to $a_{\ell m}$
extno	I4B IN	extension number. If 0 is specified, a FITS file is created and $a_{\ell m}$ is stored in the first FITS extension as temperature $a_{\ell m}$. If 1 or 2 is specified, an already existing file is opened and a 2nd or 3rd extension is created, treating $a_{\ell m}$ as $a_{\ell m}^E$ or $a_{\ell m}^B$.
nlheader	I4B IN	number of header lines to write to the file.
header(LEN=80) (1:nlheader)	CHR IN	the header to the FITS-file.

EXAMPLE:

call dump_alms ('alms.fits', alms, 64, header, 100, 1)

Opens an already existing FITS file which contains temperature $a_{\ell m}$. An extra extension is added to the file where the $a_{\ell m}$ array are written in a three-column format as described above. 100 header lines are written to the file from the array header(1:80).

MODULES & ROUTINES

This section lists the modules and routines used by **dump_alms***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to dump_alms*.

fits2alms, read_conbintab routines to read $a_{\ell m}$ from a FITS-file

alms2fits has the same function as dump_alms* but is more

general.

fill_holes_nest 67

fill holes nest

Location in HEALPix directory tree: src/f90/mod/mask_tools.F90

For a input binary mask in NESTED ordering, fill_holes_nest flip to 1 all pixels located in invalid regions with fewer pixels than the threshold provided.

Two pixels are adjacent (and belong to the same region or hole) if they have at least one point in common.

ARGUMENTS

name & dimensionality	kind	in/out	description
nside	I4B	IN	The N_{side} value of the input mask.
new_min_size	I4B	IN	Minimal size of hole (in pixels) on output
$mask_in(0:Npix-1)$	I4B	IN	Input NESTED-ordered mask. Npix = 12*nside*nside
mask_out(0:Npix-1)	I4B	OUT	Output NESTED-ordered mask. Can be the same array as mask_in.

EXAMPLE:

use healpix_types
use healpix_modules

. . .

call fill_holes_nest(nside, new_min_size, mask_in, mask_in)

???

MODULES & ROUTINES

This section lists the modules and routines used by $fill_holes_nest$.

mask_tools mask processing module (see related routines below)

RELATED ROUTINES

This section lists the routines related to $fill_holes_nest$.

dist2holes_nest	angular distance to closest invalid pixel of the given mask
fill_holes_nest	turn to $valid$ all pixels located in 'holes' containing fewer pixels than the given threshold
maskborder_nest	identify inner boundary pixels of 'holes' for given mask
size_holes_nest	returns size (in pixels) of holes found in input mask

fits2alms*

fits2alms*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads $a_{\ell m}$ values from a binary FITS file. Each FITS file extension is supposed to contain one integer column with $index = \ell^2 + \ell + m + 1$ and 2 or 4 single (or double) precision columns with real/imaginary $a_{\ell m}$ values and real/imaginary standard deviation. One can read temperature $a_{\ell m}$ or temperature and polarisation, $a_{\ell m}^T$, $a_{\ell m}^E$ and $a_{\ell m}^B$.

FORMAT call fits2alms*(filename, nalms, alms, ncl, header, nlheader, next)

ARGUMENTS

name & dimensionality	kind	in/ou	t description
filename(LEN=filenamelen)	CHR	IN	filename of the FITS-file to read the $a_{\ell m}$ from.
nalms ncl	I4B I4B	IN IN	number of $a_{\ell m}$ to read. number of columns to read in the FITS file. If an standard deviation
next	I4B	IN	is to be read, this number is 5, otherwise it is 3. the number of extensions to read. 1 for temperature only, 3 for temperature and polarisation.

alms(1:nalms,1:(ncl+1))),1:next $)$	SP/	OUT	the $a_{\ell m}$ to read from the file.
		DP		alms(i,1,j) and $alms(i,2,j)$ contain
				the ℓ and m values for the ith
				$a_{\ell m}$ (j=1,2,3 for (T,E,B)). alms(i,3,j)
				and alms(i,4,j) contain the real and
				imaginary value of the ith $a_{\ell m}$. Fi-
				nally, the standard deviation for the
				ith $a_{\ell m}$ is contained in alms(i,5,j)
				(real) and alms(i,6,j) (imaginary).
nlheader		I4B	IN	number of header lines to read from
				the file.
header(LEN=80)	(1:nlheader,	CHR	OUT	the header(s) read from the FITS-
1:next)				file.

EXAMPLE:

call fits2alms ('alms.fits', 65*66/2, alms, 3, header, 80, 3)

Reads a FITS file with the $a_{\ell m}^T$, $a_{\ell m}^E$ and $a_{\ell m}^B$ values read into alms(1:65*66/2,1:4,1:3). The last index specifies (T,E,B). The second index gives l, m, real($a_{\ell m}$), imaginary($a_{\ell m}$) for each of the $a_{\ell m}$. The number 65*66/2 is the number of $a_{\ell m}$ values up to an ℓ value of 64. 80 lines is read from the header in each extension and returned in header(1:80,1:3).

MODULES & ROUTINES

This section lists the modules and routines used by **fits2alms***.

$read_alms$	routine called by fits2alms* for each extension.
fitstools	module, containing:
printerror	routine for printing FITS error messages.
$\operatorname{cfitsio}$	library for FITS file handling.

fits2alms*

RELATED ROUTINES

This section lists the routines related to **fits2alms***.

alms2fits, dump_alms read_conbintab

number_of_alms, getsize_fits

routines to store $a_{\ell m}$ in a FITS-file

has the same function as fits2alms* but with pa-

rameters passed differently.

can be used to find out the number of $a_{\ell m}$ available in the file.

fits2cl*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a power spectrum or beam window function from a FITS ASCII or binary table. The routine can read temperature coefficients C_ℓ^{TT} or both temperature and polarisation coefficients C_ℓ^{TT} , C_ℓ^{EE} , C_ℓ^{BB} , C_ℓ^{TE} (and C_ℓ^{TB} , C_ℓ^{EB} , C_ℓ^{ET} , C_ℓ^{BT} , C_ℓ^{BE} when applicable). If the keyword PDM-TYPE is found in the header, fits2cl assumes the table to be in the special format used by Planck and will ignore the first data column. If the input FITS file contains several extensions or HDUs, the one to be read can be specified thanks to the CFITSIO Extended File Name Syntax, using its number (eg, file.fits[2] or file.fits+2) or its EXTNAME value (eg. file.fits[beam_100x100]). By default, only the first valid extension will be read.

FORMAT

call fits2cl*(filename, clin, lmax, ncl, header, [units])

ARGUMENTS

name & dimensionality	kind	in/out	description
filename(LEN=filenamelen)	CHR	IN	the FITS file containing the
			power spectrum.
lmax	I4B	IN	Maximum ℓ value to be read.
ncl	I4B	IN	1 for temperature coeffecients
			only, 4 for polarisation.
clin(0:lmax,1:ncl)	SP/	OUT	the power spectrum read from
	DP		the file.
header(LEN=80) (1:)	CHR	OUT	the header read from the FITS-
			file.
units(LEN= 80) (1:)	CHR	OUT	the column units read from the
			FITS-file.

 $fits2cl^*$

EXAMPLE:

```
use healpix_modules
real(SP), allocatable, dimension(:,:) :: cl
character(len=80), dimension(1:300) :: header
character(len=80), dimension(1:100) :: units
integer(I4B) :: lmax, ncl, np
character(len=filenamelen) :: fitsfile='cl.fits'
np = getsize_fits(fitsfile, nmaps=ncl, mlpol=lmax)
allocate(cl(0:lmax, 1:ncl))
call fits2cl(fitsfile, cl, lmax, ncl, header, units)
```

Reads a power spectrum from the FITS file 'cl.fits' and stores the result in cl(0:lmax,1:ncl) which are the ncl C_{ℓ} coefficients up to ℓ =lmax. The FITS header is returned in header, the column units in units.

MODULES & ROUTINES

This section lists the modules and routines used by fits2cl*.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to fits2cl*.

create_alm Routine to create $a_{\ell m}$ values from an input power

spectrum.

write asctab Routine to create an ascii FITS file containing a

power spectrum.

getsize_fits Routine to parse FITS file header, and determine

the data storage features.

getnumext_fits Routine to determine number of extensions of a

FITS file.

gaussbeam

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine generates the beam window function in multipole space of a gaussian beam parametrized by its FWHM. The polarization beam is also provided assuming a perfectly co-polarized beam (eg, Challinor et al 2000, astro-ph/0008228)

FORMAT call gaussbeam(fwhm_arcmin, lmax, beam)

ARGUMENTS

name & dimensionality	kind	in/oı	ıtdescription
fwhm_arcmin	DP	IN	FWHM of the gaussian beam in arcmin-
lmax	I4B	IN	utes. maximum ℓ value of the window func-
beam(0:lmax,1:p)	DP	OUT	tion. beam window function generated. The second index runs form 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.

EXAMPLE:

call gaussbeam(5.0_dp, 1024, beam)

Generates the window function of a gaussian beam of FWHM = 5 arcmin, for $\ell \leq 1024$.

RELATED ROUTINES

This section lists the routines related to **gaussbeam**.

generate_beam Routine returning a beam window function.

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gaussbeam 75

pixel_window

Routine returning a pixel window function.

generate_beam

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine generates the beam window function in multipole space. It is either a gaussian parametrized by its FWHM in arcmin in real space, or it is read from an external file.

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
fwhm_arcmin	DP	IN	fwhm size of the gaussian beam in arcminutes.
lmax	I4B	IN	maximum ℓ value of the window function.
beam(0:lmax,1:p)	DP	OUT	beam window function generated. The second index runs form 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.
beam_file(LEN=filenamelen) (OPTIONAL)	CHR	IN	name of the file containing the (non necessarily gaussian) window function B_{ℓ} of a circular beam. If present, it will override the argument fwhm_arcmin. If fewer columns than requested are found in the file, missing colums will duplicate the existing ones (based on the assumption that B_{ℓ} is the same in T, E and B). Supports the fitsio 'Extended Filename Syntax' (see examples below).

generate_beam 77

EXAMPLE:

```
use healpix_modules
real(dp), dimension(0:1024, 1:3) :: gb0, b1, b2, b3
call generate_beam(5.0_dp, 1024, gb0)
call generate_beam(0_dp, 1024, b1, beam_file='file.fits')
call generate_beam(0_dp, 1024, b2, beam_file='file.fits[col 1]')
call generate_beam(0_dp, 1024, b3, beam_file='file.fits[col 1; 2=0; 3=0]')
```

gb0 will contain the window function of a gaussian beam of FWHM = 5 arcmin, for $\ell \leq 1024$.

b1 will contain the first 3 columns (if available) of file.fits. If the file contains only two columns, then b1(:,3) = b1(:,2), and if it contains a single column, then b1(:,3) = b1(:,2) = b1(:,1).

b2 will be based on a virtual FITS file containg only the first column of file.fits, and we will have b2(:,3) = b2(:,2) = b2(:,1).

Finally b3 will read a virtual FITS file in which the first column is the same as in file.fits, while the columns 2 and 3 are set to 0. Therefore b3(:,3) = b3(:,2) = 0.

MODULES & ROUTINES

This section lists the modules and routines used by **generate_beam**.

alm_tools module, containing:

gaussbeam routine to generate a gaussian beam

RELATED ROUTINES

This section lists the routines related to **generate_beam**.

create_alm Routine to create $a_{\ell m}$ coefficients using gener-

ate beam.

alter_alm Routine to alter $a_{\ell m}$ coefficients using gener-

ate beam.

pixel window Routine returning a pixel window function.

get_card

Location in HEALPix directory tree: src/f90/mod/head_fits.F90

This routine reads a keyword of any kind from a FITS header. It is a wrapper to other routines that read keywords of different kinds.

FORMAT call get_card(header, kwd, value, comment)

ARGUMENTS

name & dimensionality	kind	in/out	description
header(LEN=80) DIMENSION(:)	CHR	IN	The header to read the keyword from.
kwd(LEN=8)	CHR	IN	the FITS keyword to read (NOT case sensitive).
value	any	OUT	the value read for the keyword. The type of the fortran variable 'value' (double, real, integer, logical or character) should match the type under which the value is written in the FITS file, except if 'value' is a character string, in which case it can read any keyword value, or if 'value' if real or double, in which case it can read any numerical value. Note that long string values (more than 68 characters in length) are supported.
comment(LEN=*)	CHR	OUT	comment read for the keyword.

EXAMPLE:

get_card 79

call get_card(header,'NsIdE',nside,comment)

if nside is defined as an integer, it will contain on output the value of NSIDE (say 256) found in header

EXAMPLE:

call get_card(header, 'ORDERING', ordering, comment)

if ordering is defined as an character string, it will contain on output the value of ORDERING (say 'RING') found in header

MODULES & ROUTINES

This section lists the modules and routines used by **get_card**.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **get_card**.

add_card	general purpose routine to write any keywords into a FITS file header
del	routine to discard a keyword from a FITS header
read_par, number_of_alms	routines to read specific keywords from a header in a FITS file.
getsize_fits	function returning the size of the data set in a fits file and reading some other useful FITS keywords
$ m merge_headers$	routine to merge two FITS headers

$get_healpix_main_dir, \dots$

Location in HEALPix directory tree: src/f90/mod/paramfile_io.F90

A few functions are available to return the full path to **HEALPix** main directory and its **data** and **test** subdirectories. This allow those paths to be controlled by preprocessing macros or environment variables in case of non-standard installation of the **HEALPix** directory structure.

FUNCTIONS:

hmd = get healpix main dir()

returns the full path to the main **HEALPix** directory. It will be determined, in this order, from the value of the preprocessing macros <code>HEALPIX</code> and <code>HEALPIXDIR</code> if they are defined or the environment variable <code>\$HEALPIX</code> otherwise.

hdd = get_healpix_data_dir()

returns the full path to **HEALPix** data subdirectory. It will be determined from the preprocessing macro <code>HEALPIXDATA</code> or the environment variable <code>\$HEALPIXDATA</code>. If both fail, it will return the list of directories <code>{.../data./data...\$HEALPIX}</code> <code>\$HEALPIX/data \$HEALPIX/.../data \$HEALPIX/data}</code> separated by <code>LineFeed</code>.

htd = get healpix test dir()

returns the full path to **HEALPix** test subdirectory. It will be determined, in this order, from the preprocessing macro HEALPIXTEST, the environment variable \$HEALPIXTEST or \$HEALPIX/test.

get_healpix_weight_file, ...

Location in HEALPix directory tree: src/f90/mod/paramfile_io.F90

Functions are available to return the standardized name of pregenerated FITS files required by some **HEALPix** facilities and subroutines. Those files are available in the data subdirectory, whose full path is returned by companion functions such as get healpix data dir.

FUNCTIONS:

winfile = get_healpix_pixel_window_file(nside)

returns, for the nside provided, the name of the FITS file containing the window function associated with the **HEALPix** pixel (of the form pixel_window_n*.fits).

w8file = get_healpix_weight_file(nside, won)

returns the name of the FITS file containing the ring-based or pixel-based weights for the given **HEALPix** resolution parameter nside. If won = 1, the output of get_healpix_ring_weight_file(nside) is returned, while if won = 2, it is the output of get_healpix_pixel_weight_file(nside). won= 0 will return an empty string, while other choices of won will result in errors.

w8rfile = get_healpix_ring_weight_file(nside)

returns, for the nside provided, the name of the FITS file containing the ring-based weights (of the form weight ring n*.fits).

w8pfile = get_healpix_pixel_weight_file(nside)

returns, for the nside provided, the name of the FITS file containing the pixel-based weights (of the form weight_pixel_n*.fits). Some of them (for power of 2 nside in [16,2048]) are located in the data directory, the other ones can be generated with the compute_weights C++ facility.

getArgument

Location in HEALPix directory tree: src/f90/mod/extension.F90

This subroutine emulates the C routine getarg, which returns the value of a given command line argument.

Starting with release 3.60, it calls the F2003 extension subroutine get command argument.

FORMAT call getArgument(index, value)

ARGUMENTS

name & dimensionality	kind	in/out	description
index	I4B	IN	index of the command line argument (where the first argument has index 1)
value	CHR	OUT	value of the argument

RELATED ROUTINES

This section lists the routines related to **getArgument**.

getEnvironment returns value of environment variable

nArguments returns number of command line arguments

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getEnvironment

Location in HEALPix directory tree: src/f90/mod/extension.F90

This subroutine emulates the C routine getenv, which returns the value of an environment variable.

Starting with release 3.60, it calls the F2003 extension subroutine get environment variable.

FORMAT

call getEnvironment(name, value)

ARGUMENTS

name & dimensionality	kind in/out	description
name value	CHR IN CHR OUT	name of the environment variable value of the environment variable

EXAMPLE:

use extension

character(len=128) :: healpixdir

call getEnvironment('HEALPIX', healpixdir)

print*,healpixdir

Will return the value of the \$HEALPIX system variable (if it is defined)

RELATED ROUTINES

This section lists the routines related to **getEnvironment**.

getArgument returns list of command line arguments

nArguments returns number of command line arguments

getdisc_ring

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90
This routine is obsolete, use query_disc instead

getnumext_fits 85

getnumext__fits

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine returns the number of extensions present in a given FITS file.

FORMAT var=getnumext_fits(filename)

name & dimensionality k	kind	in/ou	tdescription
var I.	4B	OUT	number of extensions in the FITS file (excluding the primary unit). According to the current format, HEALPix files have at least one
filename(LEN=filenamelen)	CHR	IN	extension. filename of the FITS file.

EXAMPLE:

next = getnumext_fits('map.fits')

Returns in **next** the number of extensions present in the FITS file 'map.fits'.

MODULES & ROUTINES

This section lists the modules and routines used by **getnumext_fits**.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **getnumext_fits**.

getsize_fits routine returning the number of data points in a

FITS file, as well as much more information on

the file.

input_map routine to read a **HEALPix** FITS file

getsize_fits 87

getsize_fits

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads the number of maps and/or the pixel ordering of a FITS file containing a **HEALPix** map.

FORMAT	var=getsize_fits(filename[, nmaps, ordering,
	obs_npix, nside, mlpol, type, polarisation,
	fwhm_arcmin, beam_leg, coordsys, polcconv,
	extno])

Arguments appearing in *italic* are optional.

name & dim.	kind	in/out	description
var	I8B	OUT	number of pixels or time samples in the cho-
filename(LEN=*)	CHR	IN	sen extension of the FITS file filename of the FITS-file containing HEALPix map(s).

name & dim.	kind	in/out	description
(0.7.7.1.7.)		0.77	
nmaps (OPTIONAL)	I4B	OUT	number of maps in the extension.
ordering (OPTIONAL)	I4B	OUT	pixel ordering, 0=unknown, 1=RING, 2=NESTED
obs_npix (OPTIONAL)	I4B	OUT	number of non blanck pixels. It is set to -1 if it can not be determined from header information alone
nside (OPTIONAL)	I4B	OUT	Healpix resolution parameter Nside. Returns a negative value if not found.
mlpol (OPTIONAL)	I4B	OUT	maximum multipole used to generate the map (for simulated map). Returns a negative value if not found.
type (OPTIONAL)	I4B	OUT	Healpix/FITS file type <0: file not found, or not valid 0: image only fits file, deprecated Healpix format (var = 12 * nside * nside) 1: ascii table, generally used for C(l) storage 2: binary table: with implicit pixel indexing (full sky) (var = 12 * nside * nside) 3: binary table: with explicit pixel indexing (generally cut sky) (var ≤ 12 * nside * nside)
polarisation (OPTIONAL)	I4B	OUT	999: unable to determine the type presence of polarisation data in the file <0: can not find out 0: no polarisation 1: contains polarisation (Q,U or G,C)
fwhm_arcmin (OPTIONAL)	DP	OUT	returns the beam FWHM read from FITS header, translated from Deg (hopefully) to arcmin. Returns a negative value if not found.
beam_leg(LEN=*) (OPTIONAL)	CHR	OUT	filename of beam or filtering window function applied to data (FITS keyword BEAM_LEG). Returns a empty string if not found.
coordsys(LEN=20) (OPTIONAL)	CHR	OUT	string describing the pixelation astrophysical coordinates. 'G' = Galactic, 'E' = ecliptic, 'C' = celestial = equatorial. Returns a empty string if not found.
polcconv (OPTIONAL)	I4B	OUT	polarisation coordinate convention (see Healpix primer for details) 0=unknown, 1=COSMO, 2=IAU, 3=neither COSMO nor IAU
extno (OPTIONAL)	I4B	IN	extension number (0 based) for which information is provided. Default = 0 (first extension). HEALPIX 3.80

getsize_fits 89

EXAMPLE:

npix= getsize_fits('map.fits', nmaps=nmaps, ordering=ordering,
obs_npix=obs_npix, nside=nside, mlpol=mlpol, type=type,
polarisation=polarisation)

Returns 1 or 3 in nmaps, dependent on wether 'map.fits' contain only temperature or both temperature and polarisation maps. The pixel ordering number is found by reading the keyword ORDERING in the FITS file. If this keyword does not exist, 0 is returned.

MODULES & ROUTINES

This section lists the modules and routines used by **getsize_fits**.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **getsize_fits**.

getnumext_fits routine returning the number of extension in a

FITS file

input_map routine to read a **HEALPix** FITS file

healpix_modules

Location in HEALPix directory tree: src/f90/mod/healpix_modules.f90

This module is a meta module containing most of the **HEALPix** modules. It currently includes

- alm_tools,
- bit_manipulation,
- coord_v_convert,
- extension,
- fitstools,
- head_fits,
- healpix fft,
- healpix types,
- long_intrinsic,
- mask_tools,
- misc utils,
- num_rec,
- obsolete,
- paramfile_io,
- pix tools,
- ran_tools,
- rngmod,
- statistics,
- udgrade nr,
- utilities.

Note that mpi_alm_tools is not included since it requires the MPI library for compilation.

EXAMPLE:

```
use healpix_modules
print*,' pi = ',PI
print*,' number of pixels in a Nside=64 map:',nside2npix(64)
```

Invoking $healpix_modules$ gives access to all HEALPix routines and parameters.

healpix_types

Location in HEALPix directory tree: src/f90/mod/healpix_types.F90

This module defines a set of parameters used by most other **HEALPix** modules.

The parameters defined in healpix_types include

• 'kind' parameters, used when defining the type of a variable,

name	type	$value^{a\over c}$	definition	
I1B	integer	1	number of bytes in the hardware-supported signed inte-	
			gers covering the range -99 to 99 with the least margin	
I2B	integer	2	same as above for the range -9999 to 9999 (ie, 4 digits)	
I4B	integer	4	same as above for 9 digits	
I8B	integer	8	same as above for 16 digits ^b	
SP	integer	4	number of bytes in the hardware-supported floating-point	
			numbers covering the range 10^{-30} to 10^{30} with the least	
			margin (hereafter single precision)	
DP	integer	8	same as above for the range 10^{-200} to 10^{200} (double pre-	
			cision)	
SPC	integer	4	number of bytes in real (or imaginary) part of single pre-	
			cision complex numbers	
DPC	integer	8	same as above for double precision complex numbers	
LGT	integer	4	number of bytes in logical variables	

 $^{^{}a}$ actual value may depend on hardware or compiler

• largest accessible numbers,

name	type or kind	value a	definition
MAX_I1B	integer	127	largest number accessible to inte-
			gers of kind I1B
MAX_I2B	integer	32767	same as above for I2B integers
MAX_I4B	integer	$2^{31} - 1 \simeq 2.1 \ 10^9$	same as above for I4B integers
MAX_{I8B}	I8B	$2^{63} - 1 \simeq 9.2 \ 10^{18}$	same as above for I8B integers
MAX_SP	SP	$\simeq 3.40 \ 10^{38}$	same as above for SP floating-
			point
MAX_DP	DP	$\simeq 1.80 \ 10^{308}$	same as above for DP floating-
			point

 $[^]a$ actual value may depend on hardware or compiler

 $[^]b$ may not be supported by some hardware or compiler; on those systems, the user should set the preprocessing variable N064BITS to 1 during compilation to demote automatically I8B to I4B

• mathematical definitions,

name	kind	value	definition
QUARTPI	DP	$\pi/4$	
HALFPI	DP	$\pi/2$	
PΙ	DP	$\pi \simeq 3.14159\dots$	
TWOPI	DP	2π	
FOURPI	DP	4π	
SQRT2	DP	$\sqrt{2}$	
EULER	DP	$\gamma \simeq 0.577\dots$	Euler constant
$SQ4PI_INV$	DP	$1/\sqrt{4\pi}$	
TWOTHIRD	DP	2/3	
DEG2RAD	DP	$\pi/180$	Degrees to Radians conversion factor
RAD2DEG	DP	$180/\pi$	Radians to Degrees conversion factor

• and **HEALPix** specific definitions,

name	type or kind	value	definition
HPX_SBADVAL	SP	$-1.6375 \ 10^{30}$	default sentinel value given
			to missing pixels in single
			precision data sets
HPX_DBADVAL	DP	$-1.6375 \ 10^{30}$	same as above for double
			precision data sets
FILENAMELEN	integer	1024	default length in character
			of file names.
HEALPIX_VERSION	character	"3.80"	current HEALPix pack-
			age version.

EXAMPLE:

use healpix_types
real(kind=DP) :: dx
print*,' pi = ',PI

The value of PI, as well as all other healpix_types parameters are made known to the code

in_ring 93

in_ring

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to find the pixel index of all pixels on a slice of a given ring. The output indices can be either in the RING or NESTED scheme, depending on the **nest** keyword.

ARGUMENTS

name & dimensionality	kind	in/out	description
nside	I4B	IN	the N_{side} parameter of the map.
iz	I4B	IN	ring number, counted south-
			wards from the north pole.
phi0	DP	IN	central ϕ position in the slice.
dphi	DP	IN	defines the size of the slice. The
			slice has length $2 \times dphi$ along
			the ring with center at $phi0$.
listir(0:4*nside-1)	I4B/	OUT	The pixel indexes in the slice.
	I8B		
nir	I4B	OUT	the number of pixels in the slice.
			$\mathtt{nir} {\leq 4N_{\mathrm{side}}}$
nest (OPTIONAL)	I4B	IN	The pixel indexes are in the
,			NESTED numbering scheme if
			nest=1, and in RING scheme
			otherwise.

EXAMPLE:

call in_ring(256, 10, 0, 0.1, listir, nir, nest=1)

Returns the NESTED pixel index of all pixels within 0.1 radians on each side of $\phi = 0$ on the 10th ring.

MODULES & ROUTINES

This section lists the modules and routines used by in_ring.

ring2nest conversion from RING scheme pixel index to

NESTED scheme pixel index

next_in_line_nest returns NESTED index of pixel lying to the East

of the current pixel and on the same ring

RELATED ROUTINES

This section lists the routines related to **in_ring**.

pix2ang, ang2pix convert between angle and pixel number.

pix2vec, vec2pix convert between a cartesian vector and pixel num-

ber.

getdisc_ring find all pixels within a certain radius.

input_map* 95

input_map*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a **HEALPix** map from a FITS file. This can deal with full sky as well as cut sky maps, but always outputs a full sky map (with possibly many empty pixels).

FORMAT

call input_map*(filename, map, npixtot, nmaps[, fmissval, header, units, extno, ignore_polcconv])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	i/o	description
filename(len=filenamelen)	CHR	IN	FITS file to be read from, containing a full sky or cut sky map
map(0:npixtot-1,1:nmaps)	SP/ DP	OUT	full sky map(s) constructed from the data present in the file, missing pixels are filled with fmissval
npixtot	I4B/ I8B	IN	number of pixels in the full sky map
nmaps	I4B	IN	number of maps in the file
fmissval	SP/ DP	IN	value to be given to missing pixels, (default: 0)
header(LEN=80)(1:)	CHR	OUT	FITS extension header
units(LEN=20)(1:nmaps)	CHR	OUT	maps units
extno	I4B	IN	extension number to read the data from (0
			based).(default: 0) (the first extension is read)
ignore_polccconv	LGT	IN	by default (ignore_polcconv=.false.) the output of this routine depends on the value of the FITS keyword POLCCONV found in filename, as described in the note on POLCCONV in The HEALPix Primer. Setting ignore_polcconv=.true. will force input_map to ignore that keyword.

EXAMPLE:

```
use pix_tools, only: nside2npix
use fitstools, only: getsize_fits, input_map
...
npixtot = getsize_fits('map.fits',nmaps=nmaps, nside=nside)
npix = nside2npix(nside)
allocate(map(0:npix-1,1:nmaps))
call input_map('map.fits', map, npix, nmaps, fmissval=0.)
```

Reads into map the content of the FITS file 'map.fits'. If there are missing pixels in the input file (ie, having value NaN (Not of Number), \pm Infinity or matching the FITS keyword BAD_DATA) they will take on output the value provided in optional fmissval (here 0, which also is its default value).

input_map*

MODULES & ROUTINES

This section lists the modules and routines used by **input_map***.

fitstools	module, containing:
printerror	routine for printing FITS error messages.
$read_bintab$	routine to read a binary table from a FITS file
$read_fits_cut4$	routine to read cut sky map from a FITS file
${\rm read_fits_partial}$	routine to read a partial sky map from a FITS file
cfitsio	library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to $input_map*$.

anafast	executable that reads a HEALPix map and analyses it.
synfast	executable that generate full sky $\mathbf{HEALPix}$ maps
$getsize_fits$	subroutine to know the size of a FITS file.
$output_map$	subroutine to write a FITS file from a $\mathbf{HEALPix}$
	map
write_bintabh	subroutine to write a large array into a FITS file piece by piece
$input_tod*$	subroutine to read an arbitrary subsection of a large binary table

input_tod*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a large binary table (for instance a Time Ordered Data set) from a FITS file. The user can choose to read only a section of the table, starting from an arbitrary position. The data can be read into a single or double precision array.

FORMAT call input_tod*(filename, tod, npix, ntods[, header, firstpix, fmissval])

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/ou	tdescription
filename(LEN=filenameler)	n)CHR	IN	FITS file to be read from
tod(0:npix-1,1:ntods)	SP/	OUT	array constructed from the data present
	$\overline{\mathrm{DP}}$		in the file (from the sample firstpix to
			firstpix + npix - 1. Missing pixels or time
			samples are filled with fmissval.
npix	I8B	IN	number of pixels or samples to be read. See
			Note below.
ntods	I4B	IN	number of columns to read
header(LEN=80)(1:)	CHR	OUT	FITS extension header
firstpix	I8B	IN	first pixel (or time sample) to read from (0
			based). (default: 0). See Note below.
fmissval	SP/	IN	value to be given to missing pixels, its default
	DP		value is 0. Should be of the same type as tod.

Note: Indices and number of data elements larger than 2^{31} are only accessible in FITS files on computers with 64 bit enabled compilers and with some specific compilation options of cfitsio (see cfitsio documentation).

MODULES & ROUTINES

input_tod*

This section lists the modules and routines used by **input_tod***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **input** tod*.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize_fits subroutine to know the size of a FITS file.

write_bintabh subroutine to write large arrays into FITS files

output_map subroutine to write a FITS file from a **HEALPix**

map

input_map subroutine to read a **HEALPix** map (either full

sky of cut sky) from a FITS file

long_count, long_size

Location in HEALPix directory tree: src/f90/mod/long_intrinsic.F90

The Fortran90 module long_intrinsic contains a subset of intrinsic functions (currently count and size) compiled so that they return I8B variables instead of the default integer (generally I4B), therefore allowing the handling of arrays with more than $2^{31} - 1$ elements.

FUNCTIONS:

```
cnt = long_count(mask1)
```

returns the I8B integer value that is the number of elements of the logical array mask1 that have the value true.

```
sz = long_size(array1 [,dim])
sz = long_size(array2 [,dim])
```

returns the I8B integer value that is the size of the 1D array array1 or 2D array array2 or their extent along the dimension dim if the scalar integer dim is provided.

name & dimensionality	kind	in/out	description
cnt	I8B	OUT	number of elements with value true
SZ	I8B	OUT	size or extent of array
mask1(:)	LGT	IN	1D logical array
array1(:)	I4B/	IN	1D integer or real array
	I8B/		
	SP/		
	$\overrightarrow{\mathrm{DP}}$		
array2(:,:)	I4B/	IN	2D integer or real array
<i>(, ,</i>	I8B/		·
	SP/		
	$\overrightarrow{\mathrm{DP}}$		
dim (OPTIONAL)	I4B	IN	dimension (starting at 1) along which the array extent is measured.

EXAMPLE:

```
use healpix_modules
real(SP), dimension(:,:), allocatable :: bigarray
allocate(bigarray(2_i8b**31+5, 3))
print*, size(bigarray), size(bigarray,1), size(bigarray,dim=2)
print*, long_size(bigarray), long_size(bigarray,1),
long_size(bigarray,dim=2)
deallocate(bigarray)

Will return (with default compilation options)

-2147483633 -2147483643 3
6442450959 2147483653 3

meaning that long_size handles correctly this large array while
```

by default size does not.

map2alm*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine is a wrapper to 5 internal routines:map2alm_sc, map2alm_sc_pre, map2alm_pol, map2alm_pol_pre1, map2alm_pol_pre2. These routines analyse a **HEALPix** RING ordered map and return $a_{\ell m}^T$ (and if specified $a_{\ell m}^E$ and $a_{\ell m}^B$) values up to the desired order in ℓ (maximum $3*N_{\rm side}$). The different routines are called depending on what parameters are passed. Some routines analyse with or without precomputed harmonics and some with or without polarisation.

name & dimensionality	kind	n/outdescription	
nsmax	I4B		e of the map to anal-
nlmax	I4B	yse. N the maximum sis.	ℓ value for the analy-
nmmax	I4B	N the maximum ysis.	m value for the anal-
map_TQU(0:12*nsmax**2-1)	SP/ DP	N if only the te	mperature map is to e map-array should be nis rank.
map_TQU(0:12*nsmax**2-1, 1:3)	SP/ DP	maps are to be ray should hav	rature an polarisation e analysed, the map ar- re this rank, where the is $(1,2,3)$ correspond-).

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alm_TGC(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	OUT	The $a_{\ell m}$ values output from the analysis. p is 1 or 3 dependent on wether polarisation is included
			or not. In the former case, the first index is $(1,2,3)$ corresponding to (T,E,B) .
zbounds(1:2), OPTIONAL	DP	IN	section of the map on which to perform the $a_{\ell m}$ analysis, expressed in
01 1101.112			terms of $z = \sin(\text{latitude}) = \cos(\theta)$. If $z = \sin(1) < z = \sin(2)$, it
			is performed on the strip
			zbounds(1) $< z <$ zbounds(2); if not, it is performed <i>outside</i> the strip
			zbounds(2) $\leq z \leq$ zbounds(1). If absent, the whole map is processed.
w8ring_TQU(1:2*nsmax, 1:p), OPTIONAL	DP	IN	ring weights for quadrature corrections. If ring weights are not used,
OI HOIME			this array should be 1 everywhere. p
			is 1 for a temperature analysis and 3 for (T,Q,U) .
plm(0:(nlmax+1)*(nlmax+2)*nsmax-1),	DP	IN OP-	If this optional matrix is passed with this rank, precomputed $P_{\ell m}(\theta)$ are
TIONAL			used instead of recursion. Note that since version 2.20 this feature has
			become obsolete because of algo-
plm(0:(nlmax+1)*(nlmax+2)*nsmax-	DP	IN	rithm optimizations. If this optional matrix is passed with
1, 1:3), OPTIONAL			this rank, precomputed $P_{\ell m}(\theta)$ AND precomputed tensor harmonics are
			used instead of recursion.

EXAMPLE:

```
use healpix_modules
integer(i4b) :: nside, lmax
real(dp), allocatable, dimension(:,:) :: dw8
real(dp), dimension(2) :: z
real(sp), allocatable, dimension(:,:) :: map
complex(spc), allocatable, dimension(:,:) :: alm
nside = 256
lmax = 512
allocate(dw8(1:2*nside, 1:3))
```

```
allocate(map(0:nside2npix(nside)-1,1:3))
allocate(alm(1:3, 0:lmax, 0:lmax)
dw8 = 1.0_dp
z = sin(10.0_dp * DEG2RAD)
call map2alm(nside, lmax, lmax, map, alm, (/ z, -z /) , dw8)
```

Analyses temperature and polarisation maps passed in map. The map has an $N_{\rm side}$ of 256, and the analysis is performed up to 512 in ℓ and m. The resulting $a_{\ell m}$ coefficients for temperature and polarisation are returned in alm. A 10°cut on each side of the equator is applied. Uniform weights are used.

MODULES & ROUTINES

This section lists the modules and routines used by map2alm*.

ring_analysis	Performs FFT for the ring analysis.
${f misc_util}$	module, containing:
$assert_alloc$	routine to print error message when an array is
	not properly allocated

Note: Starting with version 3.10, libsharp routines will be called when precomputed $P_{\ell m}$ are not provided.

RELATED ROUTINES

This section lists the routines related to map2alm*.

ana fast	executable using map2alm* to analyse maps.
alm2map	routine performing the inverse transform of map2alm*.
$\operatorname{dump_alms}$	write $a_{\ell m}$ coefficients computed by map2alm* into a FITS file
map2alm_iterative	similar to map2alm* with iterative scheme.

map2alm_iterative

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine covers and extends the functionalities of map2alm: it analyzes a (polarised) **HEALPix** RING ordered map and returns its $a_{\ell m}$ coefficients for temperature (and polarisation) up to a specified multipole, and use precomputed harmonics if those are provided, but it also can also perform an iterative (Jacobi) determination of the $a_{\ell m}$, and apply a pixel mask if one is provided.

Denoting **A** and **S** the analysis (map2alm) and synthesis (alm2map) operators and **a**, **m** and **w**, the $a_{\ell m}$, map and pixel mask vectors, the Jacobi iterative process reads

$$\mathbf{a}^{(n)} = \mathbf{a}^{(n-1)} + \mathbf{A}. \left(\mathbf{w}.\mathbf{m} - \mathbf{S}.\mathbf{a}^{(n-1)} \right), \tag{10}$$

with

$$\mathbf{a}^{(0)} = \mathbf{A}.\mathbf{w}.\mathbf{m}.\tag{11}$$

During the processing, the standard deviation of the input map $(\mathbf{w}.\mathbf{m})$ and the current residual map $(\mathbf{w}.\mathbf{m} - \mathbf{S}.\mathbf{a}^{(n-1)})$ is printed out, with the latter expected to get smaller and smaller as n increases.

The standard deviation of map x has the usual definition $\sigma \equiv \sqrt{\sum_{p=1}^N \frac{(x(p)-\bar{x})^2}{N-1}}$, where the mean is $\bar{x} \equiv \sum_{p=1}^N \frac{x(p)}{N}$, and the index p runs over all pixels.

In version 3.50 a bug affecting previous versions of map2alm_iterative has been fixed. (It occured when iter_order> 0 was used in conjonction with a mask and/or a restrictive zbounds, with a magnitude that depended on each of those factors and was larger for non-boolean masks (ie, $\mathbf{w}^2 \neq \mathbf{w}$). To assess the impact of this bug on previous results, the old implementation remains available in map2alm_iterative_old). The result was correct when the mask (if any) was applied to the map prior to the map2alm_iterative calling, or when no iteration was requested.

\mathbf{FORMAT}

call map2alm_iterative(nsmax, nlmax, nmmax, iter_order, map_TQU, alm_TGC[, zbounds, w8ring_TQU, plm, mask])

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	the $N_{\rm side}$ value of the map to anal-
nlmax	I4B	IN	yse. the maximum ℓ value (ℓ_{max}) for the analysis.
nmmax	I4B	IN	the maximum m value for the analysis.
iter_order	I4B	IN	the order of Jacobi iteration. Increasing that order improves the accuracy of the final $a_{\ell m}$ but increases the computation time $T_{\text{CPU}} \propto 1 + 2 \times \text{iter_order.}$ iter_order = 0 is a straight analysis, while iter_order = 3 is usually a good compromise.
map_TQU(0:12*nsmax**2-1, 1:p)	SP/ DP	INOUT	input map. p is 1 or 3 depending if temperature (T) only or temperature and polarisation (T, Q, U) are to be analysed. It will be altered on output if a mask is provided and/or if iter_order> 0 and zbounds is provided.
alm_TGC(1:p, 0:nlmax, 0:nm-max)	SPC/ DPC	OUT	The $a_{\ell m}$ values output from the analysis. p is 1 or 3 depending on whether polarisation is included or not. In the former case, the first index is $(1,2,3)$ corresponding to (T,E,B) .
zbounds(1:2), OPTIONAL	DP	IN	section of the map on which to perform the $a_{\ell m}$ analysis, expressed in terms of $z=\sin(\operatorname{latitude})=\cos(\theta)$. If $z\operatorname{bounds}(1)< z\operatorname{bounds}(2)$, it is performed on the strip $z\operatorname{bounds}(1)< z < z\operatorname{bounds}(2)$; if not, it is performed outside the strip $z\operatorname{bounds}(2) \le z \le z\operatorname{bounds}(1)$. If $z\operatorname{absent}$, the whole map is processed.

w8ring_TQU(1:2*nsmax,1:p), OPTIONAL	DP	IN	ring weights for quadrature corrections. p is 1 for a temperature anal-
			ysis and 3 for (T,Q,U) . If absent, the
			ring weights are all set to 1.
plm(0:,1:p),	DP	IN	If this optional matrix is passed, pre-
OPTIONAL			computed scalar (and tensor) $P_{\ell m}(\theta)$ are used instead of recursion.
mask(0:12*nsmax**2-1,1:q),	SP/	IN	pixel mask, assumed to have the
OPTIONAL	DP	111	same resolution (and RING order-
	Dī		ing) as the map. The map map TQU
			is multiplied by that mask before be-
			ing analyzed, and will therefore be
			altered on output. q should be in
			$\{1, 2, 3\}$. If $p = q = 3$, then each
			of the 3 masks is applied to the re-
			spective map. If $p = 3$ and $q = 2$,
			the first mask is applied to the first
			map, and the second mask to the
			second (Q) and third (U) map. If
			p = 3 and $q = 1$, the same mask
			is applied to the 3 maps. Note: the
			output $a_{\ell m}$ are computed directly on
			the masked map, and are <i>not</i> cor-
			rected for the loss of power, correla-
			tion or leakage created by the mask.

EXAMPLE:

```
use healpix_types
use alm_tools
use pix_tools
integer(i4b) :: nside, lmax, npix, iter
real(sp), allocatable, dimension(:,:) :: map
real(sp), allocatable, dimension(:) :: mask
complex(spc), allocatable, dimension(:,:,:) :: alm

nside = 256
lmax = 512
iter = 2
npix = nside2npix(nside)
allocate(map(0:npix-1,1:3))
allocate(mask(0:npix-1))
```

```
mask(0:) = 0. ! set unvalid pixels to 0
mask(0:10000-1) = 1. ! valid pixels
allocate(alm(1:3, 0:lmax, 0:lmax)
call map2alm iterative(nside, lmax, lmax, iter, map, alm, mask=mask)
```

Analyses temperature and polarisation signals in the first 10000 pixels of map (as determined by mask). The map has an $N_{\rm side}$ of 256, and the analysis is supposed to be performed up to 512 in ℓ and m. The resulting $a_{\ell m}$ coefficients for temperature and polarisation are returned in alm. Uniform weights are assumed. In order to improve the $a_{\ell m}$ accuracy, 2 Jacobi iterations are performed.

MODULES & ROUTINES

This section lists the modules and routines used by map2alm_iterative.

m map2alm	Performs the alm analysis
alm2map	Performs the map synthesis
${f misc_util}$	module, containing:
$assert_alloc$	routine to print error message when an array is
	not properly allocated

RELATED ROUTINES

This section lists the routines related to map2alm_iterative.

anafast	executable using map2alm_iterative to analyse
	maps.
alm2map	routine performing the inverse transform of map2alm_iterative.
alm2map_spin	synthesize spin weighted maps.
dump_alms	write $a_{\ell m}$ coefficients computed by map2alm_iterative into a FITS file
map2alm_spin	analyze spin weighted maps.

map2alm_spin*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine extracts the alm coefficients out of maps of spin s and -s. A (complex) map S of spin s is a linear combination of the spin weighted harmonics ${}_sY_{\ell m}$

$${}_{s}S(p) = \sum_{\ell m} {}_{s}a_{\ell m} \quad {}_{s}Y_{\ell m}(p) \tag{12}$$

for $\ell \geq |m|, \ell \geq |s|$, and is such that ${}_{s}S^{*} = {}_{-s}S$.

The usual phase convention for the spin weighted harmonics is ${}_sY_{\ell m}^*=(-1)^{s+m}{}_{-s}Y_{\ell -m}$ and therefore ${}_sa_{\ell m}^*=(-1)^{s+m}{}_{-s}a_{\ell -m}$. The two (real) input maps for map2alm_spin* are defined respectively as

$$_{|s|}S^{+} = (_{|s|}S + _{-|s|}S)/2,$$
 (13)

$$_{|s|}S^{-} = (_{|s|}S - _{-|s|}S)/(2i).$$
 (14)

map2alm_spin* outputs the alm coefficients defined as

$$|s|a_{\ell m}^{+} = -(|s|a_{\ell m} + (-1)^{s} - |s|a_{\ell m})/2$$
 (15)

$$_{|s|}a_{\ell m}^{-} = -(_{|s|}a_{\ell m} - (-1)^{s}_{-|s|}a_{\ell m})/(2i),$$
 (16)

for $m \ge 0$, knowing that, just as for spin 0 maps, the coefficients for m < 0 are given by

$$_{|s|}a_{\ell-m}^+ = (-1)^m{}_{|s|}a_{\ell m}^{+*},$$
 (17)

$$a_{\ell-m}^- = (-1)^m{}_{|s|} a_{\ell m}^{-*}.$$
 (18)

With these definitions, ${}_2a^+, {}_2a^-, {}_2S^+$ and ${}_2S^-$ match **HEALPix** polarization a^E, a^B, Q and U respectively. **However**, for $s=0, {}_0a^+_{\ell m}=-a^T_{\ell m}, {}_0a^-_{\ell m}=0, {}_0S^+=T, {}_0S^-=0.$

When dealing only with scalar quantities, like temperature or intensity maps, having a spin s = 0, it is highly recommended, and much more memory-efficient, to use directly the routine map2alm, rather then setting spin= 0 in map2alm_spin*.

FORMAT

call map2alm_spin*(nsmax, nlmax, nmmax, spin, map, alm[, zbounds=, w8ring_TQU=])

map2alm_spin*

ARGUMENTS

name & dimensionality	kind	in/oı	utdescription
nsmax	I4B	IN	the $N_{\rm side}$ value of the map to analyse.
nlmax	I4B	IN	the maximum ℓ value for the analysis.
nmmax	I4B	IN	the maximum m value for the analysis.
spin	I4B	IN	the spin s of the maps to be analysed (only its absolute value is relevant).
map(0:12*nsmax**2-1, 1:2)	SP/ DP	IN	$_{ s }S^+$ and $_{ s }S^-$ input maps
alm(1:2, 0:nlmax, 0:nmmax)	SPC/ DPC	OUT	The $_{ s }a_{\ell m}^+$ and $_{ s }a_{\ell m}^-$ output values.
zbounds(1:2), OPTIONAL	DP	IN	section of the map on which to perform the $a_{\ell m}$ analysis, expressed in terms of $z = \sin(\text{latitude}) = \cos(\theta)$. If $z = \sin(z) = \sin(z)$, it is performed on the strip $z = z = \sin(z)$, if not, it is performed outside the strip $z = z = z = z$. If $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z = z = z$, if $z = z$
w8ring_TQU(1:2*nsmax,1:2), OPTIONAL	DP	IN	ring weights for quadrature corrections. If ring weights are not used, this array should be 1 everywhere.

$\overline{\text{EXAMPLE}}$:

```
use healpix_types
use alm_tools
use pix_tools
integer(i4b) :: nside, lmax, spin
real(sp), allocatable, dimension(:,:) :: map
complex(spc), allocatable, dimension(:,:,:) :: alm
nside = 256
lmax = 512
```

```
spin = 5
allocate(map(0:nside2npix(nside)-1,1:2))
allocate(alm(1:2, 0:lmax, 0:lmax)
...
call map2alm_spin(nside, lmax, lmax, spin, map, alm)
```

Analyses spin 5 and -5 maps. The maps have an N_{side} of 256, and the analysis is performed up to 512 in ℓ and m. The resulting $a_{\ell m}$ coefficients for are returned in alm.

MODULES & ROUTINES

This section lists the modules and routines used by **map2alm** spin*.

Note: Starting with version 3.80, some libsharp routines will be called for any |s| value.

RELATED ROUTINES

This section lists the routines related to map2alm_spin*.

alm2map_spin	routine performing the inverse transform of
	map2alm_spin*.
map2alm	routine analyzing temperature and polarization
	maps

maskborder nest 113

maskborder nest

Location in HEALPix directory tree: src/f90/mod/mask_tools.F90

For a input binary mask in NESTED ordering, maskborder_nest identifies the pixels located on the inner boundary of *invalid* regions

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/out	description
nside mask_in(0:Npix-1)	I4B I4B	IN IN	The N_{side} value of the input mask. Input binary NESTED-ordered
· · · · · · · · · · · · · · · · · · ·			mask. Npix = $12*$ nside*nside
mask_out(0:Npix-1)	I4B	OUT	Output NESTED-ordered mask, in which inner border pixels (defined as 0-valued and adjacent to 1-valued pixels) take the value 2 (or border_value). Can be the same array as mask_in.
nbordpix border_value	I4B I4B	OUT IN	Number of border pixels found value to be given to border pixels in output mask. (default: 2).

EXAMPLE:

```
use healpix_types
use healpix_modules
...
call maskborder nest(nside, mask in, mask in, nbordpix)
```

For a binary input mask mask_in, it will look for border pixels and output their number in nborpix. In this example the mask_in will be modified so that border pixels take value 2 on output.

MODULES & ROUTINES

This section lists the modules and routines used by **maskborder_nest**.

mask_tools mask processing module (see related routines be-

low)

RELATED ROUTINES

This section lists the routines related to maskborder_nest.

dist2holes_nest	angular distance to closest invalid pixel of the given mask
fill_holes_nest	turn to $valid$ all pixels located in 'holes' containing fewer pixels than the given threshold
maskborder_nest	identify inner boundary pixels of 'holes' for given mask
size_holes_nest	returns size (in pixels) of holes found in input mask

medfiltmap*

medfiltmap*

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This routine performs the median filtering of a ${\bf HEALPix}$ full sky map for a given neighborhood radius

ARGUMENTS

name & dimensionality	kind	in/outdescription			
$in_map(0:npix-1)$	SP/	IN	Full sky HEALPix map to filter. npix		
	DP		should be valid HEALPix pixel number.		
radius	DP	IN	Radius in RADIANS of the disk on which the		
			median is computed.		
$med_map(0:npix-1)$	SP/	OUT	Median filtered map: each pixel is the median		
	DP		of the input map valid neighboring pixels con-		
			tained within a distance radius		
nest OPTIONAL	I4B	IN	set to 1 if the map ordering is NESTED, set		
			to 0 if it is RING.		
fmissval OPTIONAL	SP/	IN	sentinel value given to missing or non-		
	$\overline{\mathrm{DP}}$		valid pixels. Default: HPX_SBADVAL or		
			${\tt HPX_DBADVAL} = -1.6375 \ 10^{30}$		
fill_holes OP-	LGT	IN	if set to .true. will replace non-valid pixels		
TIONAL			by median of neighbors; if set to .false. will		
			leave non-valid pixels unchanged. Default:		
			.false.		

EXAMPLE:

```
use healpix_types
use pix_tools
...
call medfiltmap(map, 0.5*DEG2RAD, med)
```

Output in \mathtt{med} the median filter of $\mathtt{map},$ using a filter radius of $0.5~\mathrm{Deg}$

MODULES & ROUTINES

This section lists the modules and routines used by **medfiltmap***.

statistics module, containing:

median routine to compute the median of a data set

pix_tools module, containing:

module, containing:

routines to find the location of a pixel on the sky

query_disc routine to find pixels lying within a radius of a

given point

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m HEALPix}$ 3.80

median* 117

median*

Location in HEALPix directory tree: src/f90/mod/statistics.f90

This function computes the median of a data set

FORMAT var=median*(data[, badval, even])

ARGUMENTS

name & dimensionality	kind	in/outdescription		
var	SP/ DP	OUT	median of the data set, defined as the middle number (or the average of the 2 middle num- bers) once the valid data points are sorted in monotonous order	
data(:)	SP/ DP	IN	data set	
badval (OPTIONAL)	SP/ DP	IN	sentinel value given to bad data points. Data points with this value will be ignored during calculation of the median. If not set, all points will be considered. Do not set to 0! .	
even (OPTIONAL)	LGT	IN	if set to .true. and the number of valid data points is even, will output the average of the 2 middle points (which doubles the calculation time). If the number of points is odd, the single middle point is output and this keyword is ignored.	

EXAMPLE:

```
use statistics, only: median
...
med = median(map, even=.true.)
```

Outputs in med the median of map

MODULES & ROUTINES

This section lists the modules and routines used by **median***.

m_indmed module of the Orderpack 2.0 package, written

by: Michel Olagnon, http://www.fortran-2000.com/rank/, also available in

src/f90/mod/indmed.f90

indmed routine of m_indmed to output rank of median

RELATED ROUTINES

This section lists the routines related to **median***.

compute_statistics routine min, max, absolute deviation, and first

four order moments of a data set

merge_headers 119

merge_headers

Location in HEALPix directory tree: src/f90/mod/head_fits.F90
This routine merges two FITS headers.

FORMAT

call merge_headers(header1, header2)

ARGUMENTS

name&dimensionality	kind in/out	description
header1(LEN=80) DIMENSION(:) header2(LEN=80) DIMENSION(:)	CHR IN CHR INOUT	First header. Second header. On output, will contain the concatenation of (in that order) header2 and header1. If header2 is too short to allow the merging the output will be truncated

EXAMPLE:

call merge_headers(header1, header2)

On output header2 will contain the original header2, followed by the content of header1

MODULES & ROUTINES

This section lists the modules and routines used by merge_headers.

$write_hl$	more general routine for adding a keyword to a
	header.
${f cfitsio}$	library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to merge_headers.

${ m add_card}$	general purpose routine to write any keywords into a FITS file header
get _card	general purpose routine to read any keywords from a header in a FITS file.
del _card	routine to discard a keyword from a FITS header
read_par, number_of_alms	routines to read specific keywords from a header in a FITS file.
getsize_fits	function returning the size of the data set in a fits file and reading some other useful FITS keywords

mpi alm tools*

mpi_alm_tools*

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This module implements MPI parallelization of the alm2map and map2alm routines. It is not compiled by default during installation, but rather intended for users who need massive parallelization in their own programming. Typical applications are Monte Carlo simulations and Markov chain type analyses.

The routines can be called in two modes, either simple or advanced. The former mimics the interface of the standard routines, but with an additional MPI handle as a first argument, and is intended for applications which requires only one or a few transforms. The latter interface provides both more flexibility (in particular the option of pre-computation of the Legendre polynomials) and a simpler interface when multiple transforms are required. This interface is particularly well suited for Monte Carlo simulations and Markov chain type analyses.

EXAMPLE:

- Simple one-line interfaces:
 - mpi map2alm simple
 - mpi alm2map simple
- Three-step advanced interfaces:
 - 1. Initialization:
 mpi_initialize_alm_tools
 - 2. Execution of spherical harmonics transforms
 - mpi map2alm (root processor)
 - mpi alm2map (root processor)
 - mpi map2alm slave (slave processor)
 - mpi alm2map slave (slave processor)
 - 3. Finalizing:
 mpi_cleanup_alm_tools

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mpi_alm2map*

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine implements MPI parallelization of the serial alm2map routine. It supports both temperature and polarization inputs in both single and double precision. It must only be run by the root node of the MPI communicator.

FORMAT

call mpi_alm2map*(alms, map)

ARGUMENTS

name & dimensionality	kind	in/ou	tdescription
alms(1:nmaps,0:lmax,0:nmax)	SPC or DPC	IN	Input alms. If nmaps=1, only temperature information is included; if nmaps=3, polarization information
map(0:npix,1:nmaps)	SP or DP	OUT	is included Output map. nmaps must match that of the input alms array.

EXAMPLE:

This example 1) initializes the mpi_alm_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel alm2map operation, and 3) frees the previously allocated memory.

MODULES & ROUTINES

This section lists the modules and routines used by mpi_alm2map*.

alm_tools module

RELATED ROUTINES

This section lists the routines related to mpi_alm2map*.

mpi_cleanup_alm_tools	Frees memory that is allocated by the current routine.
$mpi_initialize_alm_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
mpi_map2alm	Routine for executing a parallel spherical harmonics transform (root processor interface)
mpi_map2alm_slave	Routine for executing a parallel spherical harmonics transform (slave processor interface)
mpi_alm2map_simple	One-line interface to the parallel inverse spherical harmonics transform
mpi_map2alm_simple	One-line interface to the parallel spherical harmonics transform

mpi_alm2map_simple*

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine provides a simplified (one-line) interface to the MPI version of alm2map. It supports both temperature and polarization inputs in both single and double precision. It must only be run by all nodes in the MPI communicator.

ARGUMENTS

name & dimensionality	kind	in/ou	utdescription
$\begin{array}{l} comm \\ alms(1:nmaps,0:lmax,0:nmax) \end{array}$	I4B SPC or	IN IN	MPI communicator. Input alms. If nmaps=1, only temperature information is included; if
	DPC		nmaps=3, polarization information is included
map(0:npix,1:nmaps)	SP or DP	OUT	Output map. nmaps must match that of the input alms array.

EXAMPLE:

call mpi_alm2map_simple(comm, map, alms)

This example executes a parallel map2alm operation through the one-line interface. Although all processors must supply allocated arrays to the routine, only the root processor's information will be used as input, and only the root processor's alms will be complete after execution.

MODULES & ROUTINES

This section lists the modules and routines used by mpi_alm2map_simple*.

alm_tools module

RELATED ROUTINES

This section lists the routines related to mpi_alm2map_simple*.

$mpi_cleanup_alm_tools$	Frees memory that is allocated by the current rou-
	tine.
$mpi_initialize_alm_tools$	Allocates memory and defines variables for the
	mpi_alm_tools module.
${ m mpi_alm2map}$	Routine for executing a parallel inverse spherical
	harmonics transform (root processor interface)
$mpi_alm2map_slave$	Routine for executing a parallel inverse spherical
	harmonics transform (slave processor interface)
${ m mpi_map2alm}$	Routine for executing a parallel spherical harmon-
	ics transform (root processor interface)
$mpi_map2alm_slave$	Routine for executing a parallel spherical harmon-
	ics transform (slave processor interface)
$mpi_map2alm_simple$	One-line interface to the parallel spherical har-
	monics transform

mpi_alm2map_slave

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine complements the master routine mpi_alm2map, and should be run by all slaves in the current MPI communicator. It is run without arguments, but after an appropriate call to initialize_mpi_alm_tools.

FORMAT

call mpi_alm2map_slave()

ARGUMENTS

None.

EXAMPLE:

This example 1) initializes the mpi_alm_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel alm2map operation, and 3) frees the previously allocated memory.

MODULES & ROUTINES

This section lists the modules and routines used by mpi alm2map slave.

alm_tools module

RELATED ROUTINES

This section lists the routines related to mpi_alm2map_slave.

mpi_cleanup_alm_tools	Frees memory that is allocated by the current routine.
$mpi_initialize_alm_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
mpi_alm2map	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
$mpi_map2alm$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi_map2alm_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi_alm2map_simple$	One-line interface to the parallel inverse spherical harmonics transform
mpi_map2alm_simple	One-line interface to the parallel spherical harmonics transform

mpi_cleanup_alm_tools

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine deallocates any private arrays previously allocated in the mpi_alm_tools module. It should be run (without arguments) by all processors in the current communicator after the last call to any of the working routines.

FORMAT

call mpi_cleanup_alm_tools()

ARGUMENTS

None.

EXAMPLE:

This example 1) initializes the mpi_alm_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

RELATED ROUTINES

This section lists the routines related to mpi cleanup alm tools.

$mpi_initialize_alm_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
${ m mpi_alm2map}$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
mpi_map2alm	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi_map2alm_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
mpi_alm2map_simple	One-line interface to the parallel inverse spherical harmonics transform
mpi_map2alm_simple	One-line interface to the parallel spherical harmonics transform

mpi_initialize_alm_tools

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine initializes the mpi_alm_tools module, and must be run prior to any of the advanced interface working routines by all processors in the MPI communicator. The root processor must supply all arguments, while it is optional for the slaves. However, the information is disregarded if they do.

A major advantage of MPI parallelization is large quantities of memory, allowing for pre-computation of the Legendre polynomials even with high $N_{\rm side}$ and $\ell_{\rm max}$, since each processor only needs a fraction $(1/N_{\rm procs})$ of the complete table. This feature is controlled by the "precompute_plms" parameter. In general, the CPU time can be expected to decrease by roughly 50% using pre-computed Legendre polynomials for temperature calculations, and by about 30% for polarization calculations.

\mathbf{FORMAT}

call mpi_initialize_alm_tools(comm, [nsmax], [nlmax], [nmmax], [zbounds], [polarization], [precompute_plms], [w8ring])

ARGUMENTS

name & dimensionality	kind	in/oı	utdescription
	T.AD	TNI	MDI
comm	I4B	IN	MPI communicator.
nsmax	I4B	IN	the N_{side} value of the HEALPix map. (OPTIONAL)
nlmax	I4B	IN	the maximum ℓ value used for the $a_{\ell m}$. (OPTIONAL)
nmmax	I4B	IN	the maximum m value used for the $a_{\ell m}$. (OPTIONAL)

zbounds $(1:2)$	DP	IN	section of the map on which to per-
			form the $a_{\ell m}$ analysis, expressed in
			terms of $z = \sin(\text{latitude}) = \cos(\theta)$.
			If $zbounds(1) < zbounds(2)$, it
			is performed on the strip
			zbounds(1)< z < z bounds(2); if
			not, it is performed <i>outside</i> the strip
			zbounds(2) $\leq z \leq$ zbounds(1). If
			absent, the whole map is processed.
			(OPTIONAL)
polarization	LGT	IN	if polarization is required, this
polarization	LG1	111	
			should be set to true, else it should
, 1	TAD	TAT	be set to false. (OPTIONAL)
precompute_plms	I4B	IN	$0 = \text{do not pre-compute any } P_{\ell m}$'s;
			$1 = \text{pre-compute } P_{\ell m}^{\text{T}}; 2 = \text{pre-}$
			compute $P_{\ell m}^{\rm T}$ and $P_{\ell m}^{\rm P}$. (OP-
			TIONAL)
$w8ring_TQU(1:2*nsmax, 1:p)$	DP	IN	ring weights for quadrature correc-
			tions. If ring weights are not used,
			this array should be 1 everywhere. p
			is 1 for a temperature analysis and
			3 for (T,Q,U). (OPTIONAL)
			\

EXAMPLE:

This example 1) initializes the mpi_alm_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

RELATED ROUTINES

This section lists the routines related to ${\bf mpi_initialize_alm_tools}.$

mpi_cleanup_alm_tools	Frees memory that is allocated by the current routine.
mpi_alm2map	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
mpi_map2alm	Routine for executing a parallel spherical harmonics transform (root processor interface)
mpi_map2alm_slave	Routine for executing a parallel spherical harmonics transform (slave processor interface)
mpi_alm2map_simple	One-line interface to the parallel inverse spherical harmonics transform
mpi_map2alm_simple	One-line interface to the parallel spherical harmonics transform

${ m mpi_map2alm*}$

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine implements MPI parallelization of the serial map2alm routine. It supports both temperature and polarization inputs in both single and double precision. It must only be run by the root node of the MPI communicator.

FORMAT

call mpi_map2alm*(map, alms)

ARGUMENTS

name & dimensionality	kind	in/outdescription
map(0:npix,1:nmaps)	SP or	IN map to analyse. If nmaps=1, only temperature information is in-
	DP	cluded; if nmaps=3, polarization information is included
alms(1:nmaps,0:lmax,0:nmax)	SPC or DPC	OUT output alms. nmaps must equal that of the input map

EXAMPLE:

mpi_map2alm* 135

This example 1) initializes the mpi_alm_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

MODULES & ROUTINES

This section lists the modules and routines used by mpi_map2alm*.

alm_tools module

RELATED ROUTINES

This section lists the routines related to mpi_map2alm*.

mpi_cleanup_alm_tools	Frees memory that is allocated by the current routine.
mpi_initialize_alm_tools	Allocates memory and defines variables for the mpi_alm_tools module.
mpi_alm2map	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
mpi_map2alm_slave	Routine for executing a parallel spherical harmonics transform (slave processor interface)
mpi_alm2map_simple	One-line interface to the parallel inverse spherical harmonics transform
mpi_map2alm_simple	One-line interface to the parallel spherical harmonics transform

mpi_map2alm_simple*

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine provides a simplified (one-line) interface to the MPI version of map2alm. It supports both temperature and polarization inputs in both single and double precision. It must only be run by all processors in the MPI communicator.

ARGUMENTS

name & dimensionality	kind	in/outdescription
comm map(0:npix-1,1:nmaps)	I4B SP or DP	IN MPI communicator. IN input map. If nmaps=1, only temperature information is included; if nmaps=3, polarization information
alms(1:nmaps,0:lmax,0:nmax)	SPC or DPC	is included IN output alms. nmaps must equal that of the input map
zbounds(1:2)	DP	IN section of the map on which to perform the a_{lm} analysis, expressed in terms of $z = \sin(\operatorname{latitude}) = \cos(\theta)$. If $z \operatorname{bounds}(1) < z \operatorname{bounds}(2)$, it is performed on the strip $z \operatorname{bounds}(1) < z < z \operatorname{bounds}(2)$; if not, it is performed outside the strip $z \operatorname{bounds}(2) \le z \le z \operatorname{bounds}(1)$. If $z \operatorname{absent}$, the whole map is processed. (OPTIONAL)

$w8ring_TQU(1:2*nsmax, 1:p)$	DP	IN	ring weights for quadrature correc-
			tions. If ring weights are not used,
			this array should be 1 everywhere. p
			is 1 for a temperature analysis and
			3 for (T,Q,U). (OPTIONAL)

EXAMPLE:

call mpi_map2alm_simple(comm, map, alms)

This example executes a parallel map2alm operation through the one-line interface. Although all processors must supply allocated arrays to the routine, only the root processor's information will be used as input, and only the root processor's alms will be complete after execution.

MODULES & ROUTINES

This section lists the modules and routines used by mpi_map2alm_simple*.

alm_tools module

RELATED ROUTINES

This section lists the routines related to mpi_map2alm_simple*.

$mpi_cleanup_alm_tools$	Frees memory that is allocated by the current routine.
mpi_initialize_alm_tools	Allocates memory and defines variables for the mpi_alm_tools module.
mpi_alm2map	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
mpi_map2alm	Routine for executing a parallel spherical harmonics transform (root processor interface)
mpi_map2alm_slave	Routine for executing a parallel spherical harmonics transform (slave processor interface)

mpi_alm2map_simple

One-line interface to the parallel inverse spherical harmonics transform $\,$

mpi_map2alm_slave

Location in HEALPix directory tree: src/f90/mod/mpi_alm_tools.f90

This subroutine complements the master routine mpi_map2alm, and should be run by all slaves in the current MPI communicator. It is run without arguments, but after an appropriate call to initialize_mpi_alm_tools.

FORMAT

call mpi_map2alm_slave()

ARGUMENTS

None.

EXAMPLE:

This example 1) initializes the mpi_alm_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

MODULES & ROUTINES

This section lists the modules and routines used by mpi map2alm slave.

alm_tools module

RELATED ROUTINES

This section lists the routines related to mpi_map2alm_slave.

$mpi_cleanup_alm_tools$	Frees memory that is allocated by the current rou-
	tine.
$mpi_initialize_alm_tools$	Allocates memory and defines variables for the
	mpi_alm_tools module.
${ m mpi_alm2map}$	Routine for executing a parallel inverse spherical
	harmonics transform (root processor interface)
$mpi_alm2map_slave$	Routine for executing a parallel inverse spherical
	harmonics transform (slave processor interface)
${ m mpi_map2alm}$	Routine for executing a parallel spherical harmon-
	ics transform (root processor interface)
$mpi_alm2map_simple$	One-line interface to the parallel inverse spherical
	harmonics transform
$mpi_map2alm_simple$	One-line interface to the parallel spherical har-
	monics transform

nArguments 141

nArguments

Location in HEALPix directory tree: src/f90/mod/extension.F90

This function emulates the C routine iargc, which returns the number of command line arguments provided.

Starting with release 3.60, it calls the F2003 extension function command argument count.

FORMAT var=nArguments()

ARGUMENTS

name&dimensionality	kind	in/out	description
var	I4B	OUT	number of command line arguments

RELATED ROUTINES

This section lists the routines related to nArguments.

getEnvironment returns value of environment variable getArgument returns list of command line arguments

neighbours_nest

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This subroutine returns the number and locations (in terms of pixel numbers) of the topological neighbours of a central pixel. The pixels are ordered in a clockwise sense about the central pixel with the southernmost pixel in first element. For the 4 pixels in the southern corners of the equatorial faces which have two equally southern neighbours the routine returns the southwestern pixel first and proceeds clockwise.

FORMAT

call neighbours_nest(nside, ipix, list, nneigh)

ARGUMENTS

name & dimensionality	kind	in/out	description
nside	I4B	IN	The $N_{\rm side}$ parameter of the map.
ipix	I4B/	IN	The NESTED pixel index of the
	I8B		central pixel.
list(8)	I4B/	OUT	On exit, the vector of neigh-
	I8B		bouring pixels. This contains
			nneigh relevant elements.
nneigh	I4B	OUT	The number of neighbours
			(mostly 8, except at 8 sites,
			where there are only 7 neigh-
			bours).
			•

EXAMPLE:

```
use pix_tools
integer :: nneigh, list(1:8)
call neighbours_nest(4, 1, list, nneigh)
```

print*,nneigh

print*,list(1:nneigh)

neighbours nest 143

This returns nneigh= 8 and a vector list, which contains the pixel numbers (90, 0, 2, 3, 6, 4, 94, 91).

MODULES & ROUTINES

This section lists the modules and routines used by **neighbours_nest**.

mk_xy2pix, mk_pix2xy precomputing arrays for the conversion of

NESTED pixel numbers to Cartesian coords in

each face.

pix2xy_nest, xy2pix_nest Conversion between NESTED pixel numbers to

Cartesian coords in each face.

bit_manipulation module, containing:

invMSB, invLSB,swapLSBMSB,invswapLSBMSB functions which manipu-

late the bit vector which represents the NESTED pixel numbers. They correspond to NorthWest<->SouthEast, SouthWest<->NorthEast, East<->West and North-South flips of the diamond

faces, respectively.

RELATED ROUTINES

This section lists the routines related to **neighbours_nest**.

pix2ang, ang2pix convert between angle and pixel number.

pix2vec, vec2pix convert between a cartesian vector and pixel num-

ber.

nest2uniq

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This F90 facility turns the parameter N_{side} (a power of 2) and the pixel index p into the Unique ID number $u = p + 4N_{\text{side}}^2$. See "The Unique Identifier scheme" section in "HEALPix Introduction Document" for more details.

FORMAT

call nest2uniq(nside, pnest, puniq)

ARGUMENTS

name	kind	in/out	description
nside	I4B	IN	The HEALPix N_{side} parameter.
pnest		IN	(NESTED scheme) pixel identification number over
puniq	I4B/I8B	OUT	the range $\{0.12N_{\text{side}}^2 - 1\}$. The HEALPix Unique pixel identifier.

EXAMPLE:

```
use healpix_modules
integer(I4B) :: puniq
call nest2uniq(1, 0, puniq)
print*,puniq
```

returns

since the first pixel (p = 0) at $N_{\text{side}} = 1$ is the pixel with Unique ID number 4.

RELATED ROUTINES

This section lists the routines related to **nest2uniq**.

uniq2nest] Transforms Unique **HEALPix** pixel ID number into Nside and Nested pixel number

nest2uniq 145

pix2xxx, ...

to turn NESTED pixel index into sky coordinates and back

npix2nside

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Function to provide the resolution parameter N_{side} corresponding to N_{pix} pixels over the full sky.

FORMAT var=npix2nside(npix)

ARGUMENTS

kind	in/out	description
I4B/ I8B I4B	IN OUT	the number $N_{\rm pix}$ of pixels over the whole sky. the parameter $N_{\rm side}$. If $N_{\rm pix}$ is valid (12 times a power of 2 in $\{1,\ldots,2^{28}\}$), $N_{\rm side} = \sqrt{N_{\rm pix}/12}$ is returned; if not, an error message is issued and -1 is returned
		error message is issued and -1 is returned.
	I4B/ I8B	I8B

EXAMPLE:

use healpix_modules
integer(I4B) :: nside
nside= npix2nside(786432)

Returns the resolution parameter $N_{\rm side}$ (256) corresponding to 786432 pixels on the sky.

RELATED ROUTINES

This section lists the routines related to npix2nside.

nside2npix returns the number of pixels $N_{\rm pix}$ corresponding to resolution parameter $N_{\rm side}$

npix2nside 147

nside2npix

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Function to provide the number of pixels $N_{\rm pix}$ over the full sky corresponding to resolution parameter $N_{\rm side}$.

FORMAT var=nside2npix(nside)

ARGUMENTS

name & dimensionality	kind	in/out	description
nside var	I4B I8B	IN OUT	the $N_{\rm side}$ parameter of the map. the number of pixels $N_{\rm pix}$ of the map. If $N_{\rm side}$ is valid (a power of 2 in $\{1,\ldots,2^{28}=268435456\}$), $N_{\rm pix}=12N_{\rm side}^2$ is returned; if not, an error message is issued and -1 is returned.

EXAMPLE:

use healpix_modules
integer(I8B) :: npix
npix= nside2npix(256)

Returns the number of **HEALPix** pixels (786432) for the resolution parameter 256.

RELATED ROUTINES

This section lists the routines related to **nside2npix**.

npix2nside

returns resolution parameter corresponding to the number of pixels.

nside2npix 149

nside2npweights

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Function to return the number of pixel-based weights (in compact form) for a given Nside:

$$N_w = \frac{(N_{\text{side}} + 1)(3N_{\text{side}} + 1)}{4} \simeq \frac{N_{\text{pix}}}{16}$$

FORMAT

var = nside 2 npweights (nside)

ARGUMENTS

name & dimensionality	kind	in/out	description
nside	I4B	IN	the N_{side} parameter.
var	I8B	OUT	the number of template pixels N_w .

EXAMPLE:

use healpix_modules
integer(I8B) :: nw8
nw8 = nside2npweights(256)

Returns in nw8 the number of non-redundant **HEALPix** pixel-based weights (49408) for the resolution parameter 256.

RELATED ROUTINES

This section lists the routines related to nside2npweights.

unfold_weightsfile

reads of FITS file containing a list ring-based or pixel-based weights into a full sky map nside2ntemplates 151

nside2ntemplates

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Function to provide the number of template pixels

$$N_{\text{template}} = \frac{1 + N_{\text{side}}(N_{\text{side}} + 6)}{4}$$

corresponding to resolution parameter N_{side} . Each template pixel has a different shape that $can \ not$ be matched (by rotation or reflexion) to that of any of the other templates.

FORMAT

var=nside2ntemplates(nside)

ARGUMENTS

name & dimensionality	kind	in/out	description
nside	I4B	IN	the N_{side} parameter.
var	I8B	OUT	the number of template pixels N_{template} .

EXAMPLE:

use healpix_modules
integer(I8B) :: ntpl
ntpl= nside2ntemplates(256)

Returns in **ntpl** the number of **HEALPix** template pixels (16768) for the resolution parameter 256.

RELATED ROUTINES

This section lists the routines related to **nside2ntemplates**.

template_pixel_ring

template_pixel_nest	return the template pixel associated with any $\mathbf{HEALPix}$ pixel
$same_shape_pixels_ring$	
same_shape_pixels_nest	return the ordered list of pixels having the same shape as a given pixel template

number_of_alms 153

number of alms

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This function returns the number of $a_{\ell m}$ values stored in each FITS extension in a FITS file containing $a_{\ell m}$

FORMAT var=number_of_alms(filename[, extnum])

ARGUMENTS

name & dimensionality	kind i	$_{ m in/out}$	description
filename(LEN = filenamelen)	CHR I	IN	filename of the FITS-file con-
extnum	I4B (OUT	taining $a_{\ell m}$. number of extensions in the file

EXAMPLE:

print*,number_of_alms('alms.fits')

Prints the number of $a_{\ell m}$ stored in each extension of the file 'alms.fits'

MODULES & ROUTINES

This section lists the modules and routines used by number_of_alms.

${ m fitstools}$	module, containing:
printerror	routine for printing FITS error messages.
${f cfitsio}$	library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **number_of_alms**.

fits2alms, read_conbintab

routines that read $a_{\ell m}$ values from FITS files.

output_map* 155

output_map*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine writes a full sky **HEALPix** map into a FITS file. The map can be either single or double precision real. It *has* to be 2-dimensional.

ARGUMENTS

name & dimensionality	kind	in/out	description
map(0:,1:)	SP/ DP	IN	full sky map(s) to be output
header(LEN=80)(1:)	CHR	IN	string array containing the FITS header to be
filename(LEN=*)	CHR	IN	included in the file filename of the FITS-file to contain HEALPix map(s).
extno	I4B	IN	extension number in which to write the data (0 based). (default: 0)

EXAMPLE:

MODULES & ROUTINES

This section lists the modules and routines used by **output_map***.

fitstools module, containing:

printerror routine for printing FITS error messages.

write_bintab routine to write a binary table into a FITS file.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **output_map***.

anafast executable that reads a **HEALPix** map from a

FITS file and analyses it.

synfast executable that generate full sky **HEALPix** maps

input_map subroutine to read a HEALPix map from a a

FITS file

write_bintabh subroutine to write a large array into a FITS file

piece by piece

input_tod* subroutine to read an arbitrary subsection of a

large binary table

write minimal header routine to write minimal FITS header

parse__init, parse__int, ..., parse__finish

Location in HEALPix directory tree: src/f90/mod/paramfile_io.F90
The Fortran90 module paramfile_io contains functions to obtain parameters from parameter files or interactively

ARGUMENTS

name&dimensionality	kind	in/out	description
			40001-P101-
fname	CHR	IN	file containing the simulation parameters. If empty, parameters are obtained interactively.
handle	PMF	INOUT	Object of type (paramfile_handle) used to store parameter information
keyname	CHR	IN	name of the required parameter
default	XXX	IN	optional argument containing the default value for a given simulation parameter; must be of appropriate type.
vmin	XXX	IN	optional argument containing the minimum value for a given simulation parameter; must be of appropriate type.
vmax	XXX	IN	optional argument containing the maximum value for a given simulation parameter; must be of appropriate type.
descr	CHR	IN	optional argument containing a description of the required simulation parameter
filestatus	CHR	IN	optional argument. If present, the parameter must be a valid filename. If filestatus=='new', the file must not exist; if filestatus=='old', the file must exist.
code	CHR	IN	optional argument. Contains the name of the executable.
silent	LGT	IN	optional argument. If set to .true. the parsing routines will run silently in non-interactive mode (except for warning or error messages, which will always appear). This is mainly intended for MPI usage where many processors parse the same parameter file: silent can be set to .true. on all CPUs except one.

handle = parse init (fname [,silent])

ROUTINES:

```
initializes the parser to work on the file fname, or interactively, if fname is empty intval = parse_int (handle, keyname [, default, vmin, vmax, descr]) longval = parse_long (handle, keyname [, default, vmin, vmax, descr]) realval = parse_real (handle, keyname [, default, vmin, vmax, descr]) doubleval = parse_double (handle, keyname [, default, vmin, vmax, descr]) stringval = parse_string (handle, keyname [, default, descr, filestatus]) logicval = parse_lgt (handle, keyname [, default, descr])
```

These routines obtain integer(i4b), integer(i8b), real(sp), real(dp), character(len=*) and logical values, respectively.

Note: parse_string will expand all environment variables of the form \${XXX} (eg: \${HOME}). It will also replace a *leading* ~/ by the user's home directory.

```
call parse summarize (handle [, code])
```

if the parameters were set interactively, this routine will print out a parameter file performing the same settings.

```
call parse_check_unused (handle [, code])
```

if a parameter file was read, this routine will print out all the parameters found in the file but not used by the code. Intended at detecting typos in parameter names.

```
call parse_finish (handle)
```

frees the memory

EXAMPLE:

```
program who_r_u
use healpix_types
use paramfile_io
use extension

implicit none
type(paramfile_handle) :: handle
character(len=256) :: parafile, name
real(DP) :: age

parafile = "
if (nArguments() == 1) call getArgument(1, parafile)
handle = parse_init(parafile)
name = parse_string(handle, 'name',descr='Enter your last name: ')
age = parse_double(handle, 'age', descr='Enter your age in years: ', &
```

```
& default=18.d0,vmin=0.d0)
call parse_summarize(handle, 'who_r_u')
end program who r u
```

If a file is provided as command line argument when running the executable who_r_u, that file will be parsed in search of the lines starting with 'name =' and 'age =', otherwise the same questions will be asked interactively.

RELATED ROUTINES

This section lists the routines related to parse_init, parse_int, ..., parse_finish.

concatnl generates from a set of strings the multi-line description

nArguments returns the number of command line arguments getArgument returns the list of command line arguments

pixel_window 161

pixel_window

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine returns the averaged ℓ -space window function $w_{\rm pix}(\ell)$ (for temperature and polarisation) associated to **HEALPix** pixels of resolution parameter $N_{\rm side}$. Because of the integration of the signal over the pixel area, the $a_{\ell m}^{\rm (pix)}$ coefficients of a pixelated map are related to the unpixelated underlying $a_{\ell m}$ by $a_{\ell m}^{\rm (pix)} = a_{\ell m} w_{\rm pix}(\ell)$.

Unless specified otherwise, the $w_{\rm pix}(\ell)$ are read from the files $HEALPIX/data/pixel_window_n????.fits.$

FORMAT

call pixel_window(pixlw, nside[, windowfile])

ARGUMENTS

name & dimensionality	kind	in/oı	ıtdescription
pixlw(0:lmax,1:p)	DP	OUT	pixel window function(s) $w_{\rm pix}(\ell)$ generated. The first index must be $\ell_{\rm max} \leq 4N_{\rm side}$. The second index runs from 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.
nside	I4B	IN	HEALPix N_{side} resolution parameter. Unless windowfile is set, the file associated with N_{side} and shipped with the package is read by default. If $nside = 0$, the pixel is assumed infinitely small and $pixlw$ is returned with value 1.
windowfile (OPTIONAL)	CHR	IN	FITS file containing the pixel window to be read instead of the default.

EXAMPLE:

call pixel_window(pixlw, 64)

returns in pixlw the pixel window function for $N_{\text{side}} = 64$.

MODULES & ROUTINES

This section lists the modules and routines used by **pixel_window**.

misc_utils module, containing:

assert, fatal_error interrupt code in case of error

extension module, containing:

getEnvironment read environment variable

fitstools module, containing:

read_dbintab reads double precision binary table

RELATED ROUTINES

This section lists the routines related to **pixel_window**.

gaussbeam routine to generate a gaussian beam window func-

tion

generate_beam returns a beam window function

alter_alm, rotate_alm modifies $a_{\ell m}$ to emulate effect of real space filter-

ing and coordinate rotation respectively

alm2map synthetize a **HEALPix** map from its $a_{\ell m}$ (or

 $a_{\ell m}^{(\mathrm{pix})}$).

alm2map_der synthetize a map and its derivatives from its $a_{\ell m}$

(or $a_{\ell m}^{(\text{pix})}$).

$\begin{array}{c} pix2xxx, ang2xxx, vec2xxx, \\ nest2ring, ring2nest \end{array}$

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

The Fortran90 module pix_tools contains some subroutines to convert between pixel number in the **HEALPix** map and (θ, ϕ) or (x, y, z) coordinates on the sphere. Some of these routines are listed here.

ARGUMENTS

kind	in/out	description
I4B	IN	$N_{\rm side}$ parameter for the HEALPix map.
I4B/		pixel identification number in NESTED
I8B		scheme over the range $\{0, N_{pix} - 1\}$.
I4B/		pixel identification number in RING
I8B		scheme over the range $\{0, N_{pix} - 1\}$.
DP		colatitude in radians measured southward
		from north pole in $\{0,\pi\}$.
DP		longitude in radians, measured eastward in
		$[0, 2\pi]$.
DP		three dimensional cartesian position vector
		(x, y, z). The north pole is $(0, 0, 1)$. An
		output vector is normalised to unity.
DP	OUT	three dimensional cartesian position vec-
		tors (x, y, z) (normalised to unity) point-
		ing to the 4 vertices of a given pixel. The
		four vertices are listed in the order North,
		West, South, East.
	I4B I4B/ I8B I4B/ I8B DP DP	I4B IN I4B/ — I8B I4B/ — I8B DP — DP —

ROUTINES:

call pix2ang_ring(nside, ipring, theta, phi)

renders theta and phi coordinates of the nominal pixel center given the pixel number ipring and a map resolution parameter nside.

call pix2vec_ring(nside, ipring, vector [,vertex])

renders cartesian vector coordinates of the nominal pixel center given the pixel number **ipring** and a map resolution parameter **nside**. Optionally renders cartesian vector coordinates of the considered pixel four vertices.

call ang2pix_ring(nside, theta, phi, ipring)

renders the pixel number ipring for a pixel which, given the map resolution parameter nside, contains the point on the sphere at angular coordinates theta and phi.

call vec2pix ring(nside, vector, ipring)

renders the pixel number ipring for a pixel which, given the map resolution parameter nside, contains the point on the sphere at cartesian coordinates vector.

call pix2ang nest(nside, ipnest, theta, phi)

renders theta and phi coordinates of the nominal pixel center given the pixel number ipnest and a map resolution parameter nside.

call pix2vec nest(nside, ipnest, vector [,vertex])

renders cartesian vector coordinates of the nominal pixel center given the pixel number **ipnest** and a map resolution parameter **nside**. Optionally renders cartesian vector coordinates of the considered pixel four vertices.

call ang2pix_nest(nside, theta, phi, ipnest)

renders the pixel number ipnest for a pixel which, given the map resolution parameter nside, contains the point on the sphere at angular coordinates theta and phi.

call vec2pix_nest(nside, vector, ipnest)

renders the pixel number <code>ipnest</code> for a pixel which, given the map resolution parameter <code>nside</code>, contains the point on the sphere at cartesian coordinates <code>vector</code>.

call nest2ring(nside, ipnest, ipring)

performs conversion from NESTED to RING pixel number.

call ring2nest(nside, ipring, ipnest)

performs conversion from RING to NESTED pixel number.

MODULES & ROUTINES

This section lists the modules and routines used by pix2xxx,ang2xxx,vec2xxx, nest2ring,ring2nest.

mk_pix2xy, mk_xy2pix

routines used in the conversion between pixel values and "cartesian" coordinates on the Healpix face.

RELATED ROUTINES

This section lists the routines related to pix2xxx,ang2xxx,vec2xxx, nest2ring,ring2nest.

neighbours_nest	find neighbouring pixels.
m ang2vec	convert (θ, ϕ) spherical coordinates into (x, y, z) cartesian coordinates.
vec2ang	convert (x, y, z) cartesian coordinates into (θ, ϕ) spherical coordinates.
convert_inplace	in-place conversion between RING and NESTED for integer/real/double maps.
convert_nest2ring	convert from NESTED to RING scheme using a temporary array.
nest2uniq, uniq2nest	conversion of standard pixel index to/from Unique ID number

planck_rng

Location in HEALPix directory tree: src/f90/mod/rngmod.f90

The derived type planck_rng is used by the Random Number Generation routines rand_init, rand_uni, rand_gauss to describe fully the current RNG sequence.

Most users do not need to know about the planck_rng definition. It may be useful for those wanting to take a snapshot of the RNG sequence they are using (by eg, dumping the latest values of planck_rng structure on disk) so that the same sequence can be resumed later on from that same point.

The type planck_rng is a structure defined as

name	type	definition
x, y, z, w	I4B	internal variables of uniform RNG
gset	DP	internal variable for Gaussian RNG
empty	LGT	flag used by Gaussian RNG

RELATED ROUTINES

This section lists the routines related to planck_rng.

$rand_gauss$	function which returns a random normal deviate.
rand_uni	function which returns a random uniform deviate.
$rand_init$	subroutine to initiate a random number sequence.

plm_gen 167

plm_gen

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine computes the latitude dependent part $\lambda_{\ell m}$ of the spherical harmonics $(Y_{\ell m}(\theta,\phi) = \lambda_{\ell m}(\theta)e^{im\phi})$ of spin 0 and 2 (see **HEALPix** primer) used to synthetize or analyze **HEALPix** maps of temperature and polarisation. Since version 2.20, which introduced optimized algorithms for spherical harmonic transforms, it has become obsolete and should no longer be used.

FORMAT

call plm_gen(nsmax, nlmax, nmmax, plm)

ARGUMENTS

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	The N_{side} value for which to compute the $\lambda_{\ell m}$.
nlmax	I4B	IN	The maximum multipole order ℓ of the generated $\lambda_{\ell m}$.
nmmax	I4B	IN	The maximum degree m of the generated $\lambda_{\ell m}$.
plm(0:n_plm-1, 1:p)	DP	OUT	The $\lambda_{\ell m}$ values, either for temperature only $(p=1)$ or temperature and polarisation $(p=3)$. The number of $\lambda_{\ell m}$ is n_plm = nsmax*(nmmax+1)*(2*nlmax-nmmax+2). They are stored in the order of increasing order ℓ , increasing degree m , for all the HEALPix ring colatitudes θ from North Pole to Equator, ie $\lambda_{00}(\theta_1)$, $\lambda_{10}(\theta_1)$, $\lambda_{20}(\theta_1)$,, $\lambda_{11}(\theta_1)$, $\lambda_{21}(\theta_1)$;, $\lambda_{00}(\theta_2)$

EXAMPLE:

```
use healpix_types
use alm_tools, only : plm_gen
integer(I4B) :: nside, lmax, mmax, n_plm
real(DP), dimension(:,:), allocatable :: plm
...
nside=256 ; lmax=512 ; mmax=lmax
npix=nside2npix(nside)
n_plm=nside*(mmax+1)*(2*lmax-mmax+2)
allocate(plm(0:n_plm-1,1:3))
...
call plm_gen(nside, lmax, mmax, plm)
```

Computes the spherical harmonics for temperature and polarisation for $N_{\rm side}=256,$ up to 512 in ℓ and m.

MODULES & ROUTINES

This section lists the modules and routines used by plm_gen.

RELATED ROUTINES

This section lists the routines related to plm_gen.

alm2map	routine generating maps of temperature and polarisation from their $a_{\ell m}$ that can use precom-
	puted $\lambda_{\ell m}$ generated by plm_gen
map2alm	routine analysing maps of temperature and polarisation that can use precomputed $\lambda_{\ell m}$ generated
	by plm_gen

plm_gen 169

plmgen

executable using plm_gen to compute the $\lambda_{\ell m}$ and writting them on disc

query_disc

Location in HEALPix directory tree: $src/f90/mod/pix_tools.F90$

Routine to find the index of all pixels within an angular distance radius from a defined center. The output indices can be either in the RING or NESTED scheme

FORMAT	call query_	_disc(nside,	vector0,	radius,	listpix,
	nlist[, nest,	inclusive])			

ARGUMENTS

name & dimensional-	kind	in/out	description
ity			
nside	I4B	IN	the N_{side} parameter of the map.
vector0(3)	DP	IN	cartesian vector pointing at the disc center.
radius	DP	IN	disc radius in radians.
listpix(0:*)	I4B/	OUT	the index for all pixels within radius.
	I8B		Make sure that the size of the array is big enough to contain all pixels.
nlist	I4B/	OUT	The number of pixels listed in listpix.
	I8B		
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED num-
			bering scheme if nest=1, and in RING scheme otherwise.
inclusive (OPTIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even partially) with the disc are listed, otherwise only those whose center lies within the disc are listed.

EXAMPLE:

```
use healpix_modules
call query_disc(256,(/0,0,1/),pi/2,listpix,nlist,nest=1)
```

query_disc 171

Returns the NESTED pixel index of all pixels north of the equatorial line in a $N_{\text{side}} = 256$ map.

MODULES & ROUTINES

This section lists the modules and routines used by query_disc.

in_ring routine to find the pixels in a certain slice of a

given ring.

ring_num function to return the ring number corresponding

to the coordinate z

RELATED ROUTINES

This section lists the routines related to query_disc.

pix2ang, ang2pix convert between angle and pixel number.

pix2vec, vec2pix convert between a cartesian vector and pixel number.

ber.

query_disc, query_polygon,
query_strip, query_triangle render the list of pixels enclosed respectively in

a given disc, polygon, latitude strip and triangle surface_triangle computes the surface in steradians of a spherical

triangle defined by 3 vertices

query_polygon

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to find the index of all pixels enclosed in a polygon. The polygon should be convex, or have only one concave vertex. The edges should not intersect each other. The output indices can be either in the RING or NESTED scheme

FORMAT call query_polygon(nside, vlist, nv, listpix, nlist[, nest, inclusive])

ARGUMENTS

name & dimension-	kind	in/out	description
ality		•	
nside	I4B	IN	the N_{side} parameter of the map.
vlist(1:3,0:*)	DP	IN	cartesian vector pointing at polygon respec- tive vertices.
nv	I4B	IN	number of vertices, should be equal to 3 or larger.
listpix(0:*)	I4B/ I8B	OUT	the index for all pixels enclosed in the triangle. Make sure that the size of the array is big enough to contain all pixels.
nlist	I4B/ I8B	OUT	The number of pixels listed in listpix.
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED numbering scheme if nest=1, and in RING scheme otherwise.
inclusive (OP-TIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even partially) with the polygon are listed, otherwise only those whose center lies within the polygon are listed.

EXAMPLE:

query_polygon 173

```
use healpix_modules
real(dp), dimension(1:3,0:9) :: vertices
vertices(:,0) = (/0.,0.,1./) ! +z
vertices(:,1) = (/1.,0.,0./) ! +x
vertices(:,2) = (/1.,1.,-1./) ! x+y-z
vertices(:,3) = (/0.,1.,0./) ! +y
call query_polygon(256,vertices,4,listpix,nlist,nest=0)
```

Returns the RING pixel index of all pixels in the polygon with vertices of cartesian coordinates (0,0,1), (1,0,0), (1,1,-1) and (0,1,0) in a $N_{\rm side}=256$ map.

MODULES & ROUTINES

This section lists the modules and routines used by query_polygon.

isort	routine to sort integer number
query_triangle	render the list of pixels enclosed in a given triangle
surface_triangle	computes the surface of a spherical triangle defined by 3 vertices
vect_prod	routine to compute the vectorial product of two 3D vectors

RELATED ROUTINES

This section lists the routines related to query_polygon.

pix2ang, ang2pix	convert between angle and pixel number.
pix2vec, vec2pix	convert between a cartesian vector and pixel num-
	ber.
query_disc, query_polygon,	
query_strip, query_triangle	render the list of pixels enclosed respectively in a given disc, polygon, latitude strip and triangle
$surface_triangle$	computes the surface in steradians of a spherical triangle defined by 3 vertices

query_strip

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to find the index of all pixels enclosed in a latitude strip. The output indices can be either in the RING or NESTED scheme

FORMAT call query_strip(nside, theta1, theta2, listpix, nlist[, nest, inclusive])

ARGUMENTS

name&dimensionality	kind in/out		description	
nside	I4B	IN	the N_{side} parameter of the map.	
theta1	DP	IN	colatitude lower bound in radians measured from North Pole (between 0 and π).	
theta2	DP	IN	colatitude upper bound in radians measured from North Pole (between 0 and π). If theta1< theta2, the pixels lying in [theta1,theta2] are output, otherwise, the pixel lying in [0, theta2] and those lying in [theta1, π] are output.	
listpix(0:*)	I4B/ I8B	OUT	the index for all pixels enclosed in the strip(s). Make sure that the size of the array is big enough to contain all pixels.	
nlist	I4B/ I8B	OUT	The number of pixels listed in listpix.	
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED numbering scheme if nest=1, and in RING scheme otherwise.	
inclusive (OPTIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even partially) with the strip are listed; otherwise only those whose center lies within the strip are listed.	

query_strip 175

EXAMPLE:

call query_strip(256,0.75*PI,0.2*PI,listpix,nlist,nest=1)

Returns the NESTED pixel index of all pixels with colatitude in $[0,\pi/5]$ and those with colatitude in $[3\pi/4,\pi]$

MODULES & ROUTINES

This section lists the modules and routines used by query_strip.

in_ring	routine to find the pixels in a certain slice of a
	given ring.
intrs_intrv	routine to compute the intersection of 2 intervals on a circle
ring_num	function to return the ring number corresponding to the coordinate \boldsymbol{z}
vect_prod	routine to compute the vectorial product of two 3D vectors

RELATED ROUTINES

This section lists the routines related to query_strip.

convert between angle and pixel number.
convert between a cartesian vector and pixel num-
ber.
render the list of pixels enclosed respectively in
a given disc, polygon, latitude strip and triangle
computes the surface in steradians of a spherical triangle defined by 3 vertices

query_triangle

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to find the index of all pixels enclosed in a spherical triangle described by its three vertices. The output indices can be either in the RING or NESTED scheme

ARGUMENTS

name&dimensionality	kind	in/out	$\operatorname{description}$	
: 1.	I4D	IN	41 - N	
nside	I4B	IN	the N_{side} parameter of the map.	
v1(3)	DP	IN	cartesian vector pointing at the triangle first vertex.	
v2(3)	DP	IN	cartesian vector pointing at the triangle second vertex.	
v3(3)	DP	IN	cartesian vector pointing at the triangle third vertex.	
listpix(0:*)	I4B/	OUT	the index for all pixels enclosed in the tri-	
1 ()	$18B^{'}$		angle. Make sure that the size of the array	
			is big enough to contain all pixels.	
nlist	I4B/	OUT	The number of pixels listed in listpix.	
	I8B			
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED num-	
,			bering scheme if nest=1, and in RING	
			scheme otherwise.	
inclusive (OPTIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even	
,			partially) with the triangle are listed, oth-	
			erwise only those whose center lies within	
			the triangle are listed.	
			one originate are notice.	

EXAMPLE:

query_triangle 177

call query_triangle(256,(/1,0,0/),(/0,1,0/),(/0,0,1/),listpix,nlist)

Returns the RING pixel index of the (98560) pixels in the octant (x, y, z > 0) in a $N_{\text{side}} = 256$ map.

MODULES & ROUTINES

This section lists the modules and routines used by query_triangle.

in_ring	routine to find the pixels in a certain slice of a given ring.
$intrs_intrv$	routine to compute the intersection of 2 intervals on a circle
ring_num	function to return the ring number corresponding to the coordinate \boldsymbol{z}
vect_prod	routine to compute the vectorial product of two 3D vectors

RELATED ROUTINES

This section lists the routines related to query_triangle.

pix2ang, ang2pix	convert between angle and pixel number.
pix2vec, vec2pix	convert between a cartesian vector and pixel number.
query_disc, query_polygon,	
query_strip, query_triangle	render the list of pixels enclosed respectively in a given disc, polygon, latitude strip and triangle
$surface_triangle$	computes the surface in steradians of a spherical triangle defined by 3 vertices

rand_gauss

Location in HEALPix directory tree: src/f90/mod/rngmod.f90

This routine returns a number out of a pseudo-random normal deviate (ie, its probability distribution is a Gaussian of mean 0 and variance 1).

FORMAT

var=rand_gauss(rng_handle)

ARGUMENTS

name & dimensionality	kind	in/out	description
rng_handle	planck_rng INOUT		structure of type planck_rng containing on all information
var	DP	OUT	necessary to continue same random sequence. number belonging to a pseudorandom normal deviate.

EXAMPLE:

use healpix_types

use rngmod

type(planck_rng) :: rng_handle

real(dp) :: gauss

call rand_init(rng_handle, 12345, 6789012)
gauss = rand_gauss(rng_handle)

initiates a random sequence with the pair of seeds (12345, 6789012), and generates one number out of the normal deviate.

RELATED ROUTINES

rand_gauss 179

This section lists the routines related to rand_gauss.

planck_rng	derived type describing RNG state
rand_uni	function which returns a random uniform deviate.
rand init	subroutine to initiate a random number sequence.

rand init

Location in HEALPix directory tree: src/f90/mod/rngmod.f90

This routine initializes, with up to 4 seeds, a randomn number sequence. The generator being primed is an F90 port of an xorshift generator described in Marsaglia, Journal of Statistical Software 2003, vol 8. It has a theoretical period of $2^{128} - 1 \approx 3.410^{38}$. Please refer to the "Comment on Random Number Generator" in the Fortran90 facilities guidelines.

ARGUMENTS

name & dimensionality	kind	in/out	description
rng_handle	planck_rng	OUT	structure of type planck_rng containing on output all infor-
seed1 (OPTIONAL)	I4B	IN	mation necessary to continue same random sequence. first seed of the random se- quence. Can be of arbitray sign. If set to zero or not provided will be replaced internally by a
seed2 (OPTIONAL)	I4B	IN	non-zero hard coded value. second seed. Same properties as above
seed3 (OPTIONAL) seed4 (OPTIONAL)	I4B I4B	IN IN	third seed. Same as above. fourth seed. Same as above.

EXAMPLE:

use rngmod

type(planck_rng) :: rng_handle

call rand init(rng handle, 12345, 6789012)

rand_init 181

initiates a random sequence with the pair of seeds (12345, 6789012).

RELATED ROUTINES

This section lists the routines related to **rand_init**.

planck_rng	derived type describing RNG state
$rand_gauss$	function which returns a random normal deviate.
rand uni	function which returns a random uniform deviate.

rand uni

Location in HEALPix directory tree: src/f90/mod/rngmod.f90

This routine returns a number out of a pseudo-random uniform deviate (ie, its probability distribution is uniform in the range]0,1[).

FORMAT

var=rand_uni(rng_handle)

ARGUMENTS

name & dimensionality	kind	in/out	description
rng_handle	planck_rng	INOUT	structure of type planck_rng containing on all information
var	DP	OUT	necessary to continue same ran- dom sequence. number belonging to a pseudo- random uniform deviate.

EXAMPLE:

use healpix_types

use rngmod

type(planck_rng) :: rng_handle

real(dp) :: uni

call rand_init(rng_handle, 12345, 6789012)

uni = rand_uni(rng_handle)

initiates a random sequence with the pair of seeds (12345, 6789012), and generates one number out of the uniform deviate.

RELATED ROUTINES

This section lists the routines related to rand_uni.

rand_uni 183

planck_rng rand_gauss rand_init derived type describing RNG state function which returns a random normal deviate. subroutine to initiate a random number sequence.

read asctab*

 read bintab*

read bintab*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a **HEALPix** map from a binary FITS-file. The routine can read a temperature map or both temperature and polarisation maps (T,Q,U)

FORMAT call read_bintab*(filename, map, npixtot, nmaps, nullval, anynull/, header, units, extno/)

Arguments appearing in italic are optional.

name &d imensionality	kind	in/oı	ıtdescription
$\mathrm{filename}(\mathrm{LEN} {=} \mathtt{filenamelen})$	CHR	IN	filename of FITS-file containing the map(s).
npixtot	I4B	IN	Number of pixels to be read from map.
nmaps	I4B	IN	number of maps to be read, 1 for temperature only, and 3 for (T,Q,U).
map(0:npixtot-1,1:nmaps)	SP/ DP	OUT	the map read from the FITS-file.
nullval	SP/ DP	OUT	value of missing pixels in the map.
anynull	LGT	OUT	.TRUE., if there are missing pixels, and .FALSE. otherwise.
header(LEN=80)(1:) (OPTIONAL)	CHR	OUT	character string array containing the FITS header read from the file. Its dimension has to be defined prior to calling the routine
units(LEN=*)(1:nmaps)	CHR	OUT	character string array containing the physical units of each map read
extno	I4B	IN	extension number to read the data from (0 based).(default: 0) (the first extension is read)

read bintab*

EXAMPLE:

call read bintab ('map.fits', map, 12*32**2, 1, nullval, anynull)

Reads a **HEALPix** temperature map from the file 'map.fits' to the array map(0:12*32**2-1,1:1). The pixel number 12*32**2 is the number of pixels in a $N_{\rm side}=32$ **HEALPix** map. If there are missing pixels in the input file (with value NaN (Not a Number), $\pm {\tt Infinity}$, or matching the FITS keyword BAD_DATA) then anynull is .TRUE. and these pixels get the value returned in nullval.

MODULES & ROUTINES

This section lists the modules and routines used by **read_bintab***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **read** bintab*.

input_map Routine which reads a map using read_bintab*

and fills missing pixels with a given value.

map2alm Routine which analyse a map and returns the a_{lm}

coefficients.

read fits cut4 Routine to read cut sky **HEALPix** FITS maps

write_plm, write_bintab Routines to write HEALPix FITS maps

read conbintab*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a FITS file containing $a_{\ell m}$ values for constained realisation. The FITS file is supposed to contain one integer column with $index = \ell^2 + \ell + m + 1$ and 2 or 4 single (or double) precision columns with real/imaginary $a_{\ell m}$ values and real/imaginary standard deviation on these $a_{\ell m}$. It is supposed to contain either 1 or 3 extension(s) containing respectively the $a_{\ell m}$ for T and if applicable E and B.

FORMAT

call read_conbintab*(filename, alms, nalms[, units, extno])

name&dimensionality	name&dimensionality kind		t description
filename(LEN=filenamelen) nalms	CHR I4B	IN IN	filename of FITS file containing $a_{\ell m}$. Number of $a_{\ell m}$ values to read from the file.
alms(0:nalms-1,1:6)	SP/ DP	OUT	the $a_{\ell m}$ read from the file. alms(i,1) and alms(i,2) contain the ℓ and m values for the ith $a_{\ell m}$. alms(i,3) and alms(i,4) contain the real and imaginary value of the ith $a_{\ell m}$. Finally, the standard deviation for the ith $a_{\ell m}$ is contained in alms(i,5) (real) and alms(i,6) (imaginary).
units(len=20)(1:) (OPTIONAL)	CHR	OUT	character string containing the units of the $a_{\ell m}$
extno (OPTIONAL)	I4B	IN	extension (0 based) of the FITS file to be read

read conbintab*

EXAMPLE:

call read combintab ('alms.fits',alms,65*66/2)

Read 65*66/2 (the number of $a_{\ell m}$ needed to fill the whole range from l=0 to l=64) $a_{\ell m}$ values from the file 'alms.fits' into the array alms(0:65*66/2-1,1:6).

MODULES & ROUTINES

This section lists the modules and routines used by **read_conbintab***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **read_conbintab***.

alms2fits, dump_alms routines to write $a_{\ell m}$ to a FITS-file

fits2alms has the same function as read_conbintab but is

more general.

number_of_alms, getsize_fits can be used to find out the number of $a_{\ell m}$ avail-

able in the file.

read_dbintab

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a double precision binary array from a FITS-file. It is used by **HEALPix** to read precomputed $P_{\ell m}(\theta)$ values and pixel window functions.

FORMAT call read_dbintab(filename, map, npixtot, nmaps, nullval, anynull, units)

name & dimensionality	kind	in/out	description
$\mathrm{filename}(\mathrm{LEN} \texttt{=} \mathtt{filenamelen})$	CHR	IN	filename of FITS-file containing the double precision array.
npixtot	I4B	IN	Number of values to be read from the file.
nmaps	I4B	IN	number of 1-dim. arrays, 1 for scalar $P_{\ell m}$ s and pixel windows, 3 for scalar and tensor $P_{\ell m}$ s.
map(0:npixtot-1,1:nmaps)	DP	OUT	the array read from the FITS-file.
nullval	DP	OUT	value of missing pixels in the array.
anynull	LGT	OUT	TRUE, if there are missing pixels, and FALSE otherwise.
units(len=20)(1:nmaps)	CHR	OUT	respective physical units of the maps in the FITS file.

read dbintab

EXAMPLE:

call read_dbintab ('plm_32.fits',plm,65*66*32,1,nullval,anynull)

Reads precomputed scalar $P_{\ell m}(\theta)$ from the file 'plm_32.fits'. The values are returned in the array plm(0:65*66*32,1:1). The number of values 65*66*32 is the number of precomputed $P_{\ell m}(\theta)$ for a $N_{\rm side}=32$, $\ell_{\rm max}=64$ map. If there are missing values in the file, anynull is TRUE and nullval contains the values of these pixels.

MODULES & ROUTINES

This section lists the modules and routines used by **read_dbintab**.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **read dbintab**.

plmgen Executable to create files with precomputed

 $P_{\ell m}(\theta)$.

write_plm Routine to create a file to be read by

read dbintab.

read fits cut4

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads a cut sky ${\bf HEALPix}$ map from a FITS file. The format used for the FITS file follows the one used for Boomerang98 and is adapted from COBE/DMR

Arguments appearing in *italic* are optional.

name&dimensionality	kind	in/ou	tdescription
	\		
filename(LEN=filenamele)	n)CHR	IN	FITS file to be read from, containing a cut
			sky map
np	I4B	IN	number of pixels to be read from the file
pixel(0:np-1)	I4B	OUT	index of observed (or valid) pixels
signal(0:np-1)	SP	OUT	value of signal in each observed pixel
(OPTIONAL)			
$n_obs(0:np-1)$	I4B	OUT	number of observation per pixel
serror(0:np-1)	SP	OUT	rms of signal in pixel. (For white noise, this
			would be $\propto 1/\sqrt{\text{n}_{\text{obs}}}$)
header(LEN=80)(1:)	CHR	OUT	FITS extension header
units(LEN=20)	CHR	OUT	maps units (applies only to Signal and Serror,
			which are assumed to have the same units)
extno	I4B	IN	extension number (0 based) for which map is
			read. Default $= 0$ (first extension).

read_fits_cut4

MODULES & ROUTINES

This section lists the modules and routines used by read_fits_cut4.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **read_fits_cut4**.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize_fits routine to know the size of a FITS file and its type

(eg, full sky vs cut sky)

input_map all purpose routine to input a map of any kind

from a FITS file

output_map subroutine to write a FITS file from a **HEALPix**

map

write_fits_cut4 subroutine to write a cut sky map into a FITS file

read_fits_partial

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads unpolarised or polarised partial sky **HEALPix** map from a FITS file.

For more information on the FITS file format supported in **HEALPix**, including the one implemented in read_fits_partial, see https://healpix.sourceforge.io/data/examples/healpix_fits_specs.pdf.

FORMAT

call read_fits_partial(filename, pixel, cutmap, [header, extno])

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/out	description
filename(LEN=filenameler	ı)CHR	IN	FITS file to be read from, containing a partial sky map
pixel(0:np-1)	I4B/ I8B	OUT	index of observed (or valid) pixels
$\operatorname{cutmap}(0:\operatorname{np-1,1:nc})$	SP/ DP	OUT	value of unpolarised or polarised map for each observed pixel
header(LEN=80)(1:) extno	CHR I4B	OUT IN	FITS extension header extension number (0 based) for which map is read. Default = 0 (first extension).

EXAMPLE:

```
use healpix_modules
```

```
character(len=FILENAMELEN) :: file
integer(i4b) :: nmaps, polarisation, npix, nside
integer(i4b), allocatable, dimension(:) :: pixel
real(SP), allocatable, dimension(:,:) :: data
character(len=80), dimension(1:100) :: header=""
```

read_fits_partial 195

```
file="https://healpix.sourceforge.io/data/examples/partial_TQU.fits"
npix = getsize_fits(file, nmaps=nmaps, polarisation=polarisation)
print*, npix, nmaps, polarisation
allocate(pixel(0:npix-1))
allocate(data(0:npix-1,1:3))
call read_fits_partial(file, pixel, data, header=header)
print*,pixel(0), data(0,1:3)
```

reads a remote partial sky FITS file and prints the index and IQU values of the first pixel its contains.

MODULES & ROUTINES

This section lists the modules and routines used by read_fits_partial.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to read_fits_partial.

anafast	executable that reads a HEALPix map and anal-
	yses it.
synfast	executable that generate full sky $\mathbf{HEALPix}$ maps
getsize_fits	routine to know the size of a FITS file and its type (eg, full sky vs cut sky)
${ m input_map}$	all purpose routine to input a map of any kind from a FITS file
$\operatorname{output_map}$	subroutine to write a FITS file from a full sky $\mathbf{HEALPix}$ map
write_fits_partial	subroutine to write a partial map into a FITS file which can be read by read_fits_partial and/or input_map.

read_par

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine reads the 'NSIDE', 'TFIELDS', 'MAX-LPOL', and optionally 'MAX-MPOL' keywords from a FITS-file. These keywords desribe $N_{\rm side}$, number of datasets (maps) and maximum multipole ℓ (order) and m (degree) value for the file. If a keyword is not found in the FITS file, a value of -1 is returned instead. The file could eg. be a **HEALPix** map, or a set of $a_{\ell m}$ or precomputed $P_{\ell m}(\theta)$

FORMAT

call read_par(filename, nside, lmax, tfields[, mmax])

ARGUMENTS

name & dimensionality	kind	in/outdescription		
filename(LEN=filenamelen)	CHR	IN	filename of the FITS file.	
nside	I4B	OUT	'NSIDE' keyword value from the FITS	
			header.	
lmax	I4B	OUT	'MAX-LPOL' keyword value from the	
			FITS header.	
tfields	I4B	OUT	'TFIELDS' keyword value from the FITS	
			header.	
mmax (OPTIONAL)	I4B	OUT	'MAX-MPOL' keyword value from the	
,			FITS header.	

EXAMPLE:

call read_par('plm_128p.fits', nside, lmax, nhar)

Checks the N_{side} and maximum ℓ value used for the precomputed $P_{\ell m}(\theta)$ that are stored in the file 'plm_128p.fits'. If the file also contains tensor harmonics, nhar is returned with the value 3, otherwise it is 1.

read_par 197

MODULES & ROUTINES

This section lists the modules and routines used by **read_par**.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **read_par**.

synfast, plmgen executables that produce FITS-files with key-

words relevant to this routine.

real fft

Location in HEALPix directory tree: src/f90/mod/healpix_fft.F90

This routine performs a forward or backward Fast Fourier Transformation on its argument data.

FORMAT call real_fft(data, backward)

ARGUMENTS

name & dimensionality	kind in/out	description
data(:)	XXX INOUT	
backward	LGT IN	data. Can be of type real(sp) or real(dp) Optional argument. If present and true, perform backward transformation, else forward

EXAMPLE:

use healpix_fft
call real fft (data, backward=.true.)

Performs a backward FFT on data.

RELATED ROUTINES

This section lists the routines related to **real_fft**.

complex_fft routine for FFT of complex data

remove dipole*

remove_dipole*

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This routine provides a means to fit and remove the dipole and monopole from a **HEALPix** map. The fit is obtained by solving the linear system

$$\sum_{j=0}^{d^2-1} A_{ij} f_j = b_i \tag{19}$$

with, d = 1 or 2, and

$$b_i \equiv \sum_{p \in \mathcal{P}} s_i(p) w(p) m(p), \tag{20}$$

$$A_{ij} \equiv \sum_{p \in \mathcal{P}} s_i(p) w(p) s_j(p), \tag{21}$$

where \mathcal{P} is the set of valid, unmasked pixels, m is the input map, w is pixel weighting, while $s_0(p) = 1$ and $s_1(p) = x$, $s_2(p) = y$, $s_3(p) = z$ are respectively the monopole and dipole templates. The output map is then

$$m'(p) = m(p) - \sum_{i=0}^{d^2 - 1} f_i s_i(p).$$
 (22)

FORMAT

call remove_dipole*(nside, map, ordering, degree, multipoles, zbounds[, fmissval, mask, weights])

name & dimensionality	kind	in/out	description
nside	I4B	IN	value of N_{side} resolution parameter for input map
map(0:12*nside*nside-1)	SP/ DP	INOUT	HEALPix map from which the monopole and dipole will be removed. Those are removed from all unflagged pixels, even those excluded by the cut zounds or the mask.
ordering	I4B	IN	HEALPix scheme 1:RING, 2: NESTED
degree	I4B	IN	multipoles to fit and remove. It is either 0 (nothing done), 1 (monopole only) or 2 (monopole and dipole).
	DP	OUT	values of best fit monopole and dipole. The monopole is described as a scalar in the same units as the input map, the dipole as a 3D cartesian vector, in the same units.
zbounds(1:2)	DP	IN	section of the map on which to perform the fit, expressed in terms of $z=\sin(\operatorname{latitude})=\cos(\theta)$. If $\operatorname{zbounds}(1)<\operatorname{zbounds}(2)$, it is performed on the strip $\operatorname{zbounds}(1)< z<\operatorname{zbounds}(2)$; if not, it is performed outside the strip $\operatorname{zbounds}(2) \leq z \leq \operatorname{zbounds}(1)$. If absent , the whole map is processed.
fmissval (OPTIONAL)	SP/ DP	IN	value used to flag bad pixel on input (default: -1.6375e30). Pixels with that value are ignored during the fit, and left unchanged on output.
mask(0:12*nside*nside-1) (OPTIONAL)	SP/ DP	IN	mask of valid pixels. Pixels with $ \text{mask} < 10^{-10}$ are not used for fit. Note: the map is <i>not</i> multiplied by the mask.
weights(0:12*nside*nside-1) (OPTIONAL)	SP/ DP	IN	weight to be given to each map pixel before doing the fit. By default pixels are given a uniform weight of 1. Note: the output map is <i>not</i> multiplied by the weights.

remove_dipole* 201

EXAMPLE:

```
s = sin(15.0_dp * DEG2RAD)
call remove_dipole*(128, map, 1, 2, multipoles, (/ s, -s /) )
```

Will compute and remove the best fit monopole and dipole from a map with $N_{\rm side} = 128$ in RING ordering scheme. The fit is performed on pixels with $|b| > 15^{\circ}$.

MODULES & ROUTINES

This section lists the modules and routines used by **remove_dipole***.

pix_tools module, containing:

RELATED ROUTINES

This section lists the routines related to **remove_dipole***.

add_dipole routine to add a dipole and monopole to a map.

ring_analysis

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This subroutine computes the Fast Fourier Transform of a single ring of pixels and extends the computed coefficients up to the maximum m of the transform.

FORMAT call ring_analysis(nsmax, nlmax, nmmax, datain, nph, dataout, kphi0)

ARGUMENTS

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	$N_{\rm side}$ of the map.
nlmax	I4B	IN	Maximum ℓ of the analysis.
nmmax	I4B	IN	Maximum m of the analysis.
nph	I4B	IN	The number of points on the
			ring.
datain(0:nph-1)	DP	IN	Function values on the ring.
dataout(0:nmmax)	DPC	OUT	Fourier components, replicated
			to Nmmax.
kphi0	I4B	IN	0 if the first pixel on the ring is
			at $\phi = 0$; 1 otherwise.

EXAMPLE:

call ring_analysis(64,128,128,datain,8,dataout,0)

Returns the periodically extended complex Fourier Transform of datain in dataout. They are returned in the following order: 0 1 2 3 4 5 6 7 6 5 4 3 2 1 0 The value kphi0 = 0 specifies that no phase factor needed to be applied, because the ring starts at $\phi = 0$.

 $ring_analysis$ 203

MODULES & ROUTINES

This section lists the modules and routines used by ring_analysis.

healpix_fft module.

RELATED ROUTINES

This section lists the routines related to ring_analysis.

ring_synthesis Inverse transform (complex-to-real), alm2map, alm2map_der and synfast

ring_num

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This function returns the ring number for a z coordinate.

FORMAT var=ring_num(nside, z)

ARGUMENTS

name&dimensionality	kind in	n/out	description
nside z	I4B IN DP IN	N	the $N_{\rm side}$ parameter of the map. the z coordinate to find the ring number for.

EXAMPLE:

print*,ring_num(256, 0.5)

Prints the ring number of the ring at position z = 0.5.

MODULES & ROUTINES

This section lists the modules and routines used by ring_num.

None

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RELATED ROUTINES

This section lists the routines related to ring_num.

in_ring Returns the pixels in a slice on a given ring.

ring_synthesis

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

FORMAT	call ring_synthesis(nsmax,	nlmax,	nmmax,
	datain, nph, dataout, kphi0)		

ARGUMENTS

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	$N_{\rm side}$ of the map.
nlmax	I4B	IN	Maximum ℓ of the analysis.
nmmax	I4B	IN	Maximum m of the analysis.
nph	I4B	IN	The number of points on the
			ring.
datain(0:nmmax)	DPC	IN	Fourier components as com-
,			puted from the a_{lm} .
dataout(0:nph-1)	DP	OUT	Synthesized function values on
· ·			the ring.
kphi0	I4B	IN	0 if the first pixel on the ring is
-			at $\phi = 0$; 1 otherwise.
dataout(0:nph-1)	DP	OUT	puted from the a_{lm} . Synthesized function values on the ring. 0 if the first pixel on the ring is

EXAMPLE:

call ring_synthesis(64,128,128,datain,8,dataout,1)

This computes the inverse (complex-to-real) Fast Fourier Transform for the second ring from the pole, containing 8 pixels, for a map resolution of $N_{\rm side}=64$. 128 complex Fourier components contribute to these 8 pixels. The value kphi0=1 specifies that a phase factor needed to be applied to correctly rotate the ring into position on the **HEALPix** grid.

ring_synthesis 207

MODULES & ROUTINES

This section lists the modules and routines used by ring_synthesis.

healpix_fft module.

RELATED ROUTINES

This section lists the routines related to ring_synthesis.

ring_analysis Forward transform, used in map2alm and anafast

rotate alm*

Location in HEALPix directory tree: src/f90/mod/alm_tools.F90

This routine transform the scalar (and tensor) $a_{\ell m}$ coefficients to emulate the effect of an arbitrary rotation of the underlying map. The rotation is done directly on the $a_{\ell m}$ using the Wigner rotation matrices, computed by recursion. To rotate the $a_{\ell m}$ for $\ell \leq \ell_{\rm max}$ the number of operations scales like $\ell_{\rm max}^3$.

FORMAT call rotate_alm*(nlmax, alm_TGC, psi, theta, phi)

name & dimensionality	kind	in/out	description
nlmax alm_TGC(1:p,0:nlmax,0:nlmax)	I4B SPC/ DPC	IN INOUT	maximum ℓ value for the $a_{\ell m}$. complex $a_{\ell m}$ values before and after rotation of the coordinate system. The first index here runs from 1:1 for temperature only, and 1:3 for po- larisation. In the latter case, 1=T, 2=E, 3=B.
psi	DP	IN	first rotation: angle ψ about the z-axis. All angles are in radians and should lie in $[-2\pi,2\pi]$, the rotations are active and the referential system is assumed to be right handed, the routine coordsys2euler_zyz can be used to generate the Euler angles ψ, θ, φ for rotation between standard astronomical coordinate systems;
theta	DP	IN	second rotation: angle θ about the original (unrotated) y-axis;
phi	DP	IN	third rotation: angle φ about the original (unrotated) z-axis;

rotate_alm* 209

EXAMPLE:

```
use alm_tools, only: rotate_alm
...
call rotate_alm(64, alm_TGC, PI/3., 0.5_dp, 0.0_dp)
```

Transforms scalar and tensor $a_{\ell m}$ for $\ell_{\text{max}} = m_{\text{max}} = 64$ to emulate a rotation of the underlying map by $(\psi = \pi/3, \theta = 0.5, \varphi = 0)$.

EXAMPLE:

```
use coord_v_convert, only: coordsys2euler_zyz
use alm_tools, only: rotate_alm
...
call coordsys2euler_zyz(2000.0_dp, 2000.0_dp, 'E', 'G', psi, theta, phi)
call rotate_alm(64, alm_TGC, psi, theta, phi)
```

Rotate the $a_{\ell m}$ from Ecliptic to Galactic coordinates.

RELATED ROUTINES

This section lists the routines related to **rotate_alm***.

can be used to generate the Euler angles ψ, θ, φ for rotation between standard astronomical coordinate systems
Routine to create $a_{\ell m}$ coefficients.
Routine to modify $a_{\ell m}$ coefficients to apply or remove the effect of an instrumental beam.
Routines to analyze a HEALPix sky map into its $a_{\ell m}$ coefficients.
Routines to synthetize a HEALPix sky map from its $a_{\ell m}$ coefficients.
Routines to save a set of $a_{\ell m}$ in a FITS file.
rotates a 3D coordinate vector from one astronom-

ical coordinate system to another.

same_shape_pixels_nest, same_shape_pixels_ring

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

These routines provide the ordered list of all **HEALPix** pixels having the same shape as a given template, for a resolution parameter N_{side} . Depending on the template considered the number of such pixels is either 8, 16, $4N_{\text{side}}$ or $8N_{\text{side}}$.

The template pixels are all located in the Northern Hemisphere, or on the Equator. They are chosen to have their center located at

$$z = \cos(\theta) \ge 2/3,$$
 $0 < \phi \le \pi/2,$ $2/3 > z \ge 0,$ $\phi = 0,$ or $\phi = \frac{\pi}{4N_{\text{side}}}.$ (23)

They are numbered continuously from 0, starting at the North Pole, with the index increasing in ϕ , and then increasing for decreasing z.

FORMAT call same_shape_pixels_nest(nside, template [, list, reflexion, nrep])

FORMAT call same_shape_pixels_ring(nside, template [, list, reflexion, nrep])

name & dimensionality	kind	in/out	description
nside template	I4B I4B/ I8B	IN IN	the HEALPix N_{side} parameter. identification number of the template pixel (the numbering scheme of the pixel tem-
list(0:nrep-1) OPTIONAL	I4B/ I8B	OUT	plates is the same for both routines). pointer containing the ordered list of NESTED/RING scheme identification
			numbers (in $\{0,12N_{\text{side}}^2-1\}$) of all pixels having the same shape as the template provided. The routines will allocate the list array if it is not allocated upon calling.
reflexion(0:nrep-1) OPTIONAL	I4B	OUT	pointer containing the transformation(s) (in $\{0, 3\}$) to apply to each of the returned pixels to match exactly in shape and position its respective template. 0: rotation around the polar axis only, 1:
			rotation + East-West swap (ie, reflexion around meridian), 2: rotation + North-South swap (ie, reflexion around Equator), 3: rotation + East-West and North-South swaps. The routines will allocate the list
nrep OPTIONAL	I4B/ I8B	OUT	array if it is not allocated upon calling. number of pixels having the same template (either 8, 16, $4N_{\text{side}}$ or $8N_{\text{side}}$).

EXAMPLE:

```
use healpix_modules
integer, parameter :: IXB = I4B ! for nside <= 8192
!integer, parameter :: IXB = I8B ! for any valid nside
integer(I4B):: nside
integer(IXB):: template, nrep
integer(I4B), dimension(:), pointer :: listref
integer(IXB), dimension(:), pointer :: listpix

allocate(listref(0:0)) ! only the lower bound matters
allocate(listpix(0:0)) ! only the lower bound matters
nside = 256
template = 1234</pre>
```

```
call same_shape_pixels_ring(nside, template, list=listpix,
reflexion=listref, nrep=nrep)
print*,nrep
print*,listpix(0:nrep-1)
print*,listref(0:nrep-1)
```

Returns in listpix the RING-scheme index of the all the pixels having the same shape as the template #1234 for $N_{\rm side}=256$. Upon return listref will contain the rotation/reflexions to apply to each pixel returned to match the template, and nrep will contain the number of pixels having that same shape (16 in that case). Note that some variables (corresponding to arguments template, list and nrep) must be of type I8B instead of I4B if $N_{\rm side}>8192$ is to be used.

RELATED ROUTINES

This section lists the routines related to **same_shape_pixels_ring**.

nside2templates returns the number of template pixel shapes avail-

able for a given N_{side} .

 $template_pixel_ring$

template_pixel_nest return the template shape matching the pixel pro-

vided

scan_directories

Location in HEALPix directory tree: src/f90/mod/paramfile_io.F90 Function to scan a set of directories for a given file

FORMAT var=scan_directories(directories, filename, fullpath)

ARGUMENTS

name&dimensionality	kind	in/out	description
directories	CHR	IN	contains the set of directories (up to 20), separated by an ASCII character of value < 32 (see concatn1). During the search, it is assumed that the given directories and filename can be separated by noth-
filename fullpath	CHR CHR	IN OUT	ing, a / (slash) or a \ (backslash) the file to be found. returns the full path to the first occurrence of the file among the directories provided. Empty if the file is not found.
var	LGT	OUT	The search is not recursive. set to true if the file is found, to false otherwise.

EXAMPLE:

scan_directories 215

RELATED ROUTINES

This section lists the routines related to **scan_directories**.

parse_xxx concatnl

parse an ASCII file for parameters definition concatenates a set of substrings into one string, interspaced with LineFeed character

size holes nest

Location in HEALPix directory tree: src/f90/mod/mask_tools.F90

For a input binary mask in NESTED ordering, size_holes_nest identifies the pixels located on the inner boundary of invalid regions

FORMAT call size_holes_nest(nside, mask, nholes, nph, [tags, sizeholes, listpix])

Arguments appearing in *italic* are optional.

name & dim.	kind	in/out	description
nside	I4B	IN	The <i>nside</i> value of the input mask.
mask(0:Npix-1)	I4B	IN	Input binary NESTED-ordered mask. Npix = 12*nside*nside
nholes	I4B	OUT	Number of holes found
nph	I4B	OUT	Number of pixels in holes
tags(0:Npix-1) (OPTIONAL)	I4B	OUT	Pointer allocated by size_holes_nest, containing a sky map in which <i>invalid</i> pixels belonging to the largest hole have value -1, those belonging to the second largest hole have value -2, and so on, while valid pixels keep value +1.
sizeholes(0:nholes-1)	I4B	OUT	Pointer allocated by size_holes_nest, containing on output the respective size of each hole (in decreasing order). Eg, sizeholes(0) is the number of pixels in the largest hole (taking value -1 in tags).
listpix(0:nholes+nph)	I4B	OUT	Pointer allocated by size_holes_nest, containing on output the indexed list of pixels in each hole. Pixels located in the first (and largest) hole are given by listpix(listpix(0):listpix(1)-1)

size_holes_nest 217

EXAMPLE:

```
use healpix_types
use healpix_modules
...
call size_holes_nest(nside, mask, nholes, nph)
```

???

MODULES & ROUTINES

This section lists the modules and routines used by **size_holes_nest**.

mask_tools mask processing module (see related routines be-

low)

RELATED ROUTINES

This section lists the routines related to **size_holes_nest**.

$dist2holes_nest$	angular distance to closest invalid pixel of the
	given mask
$fill_holes_nest$	turn to valid all pixels located in 'holes' containing
	fewer pixels than the given threshold
$maskborder_nest$	identify inner boundary pixels of 'holes' for given
	mask
size_holes_nest	returns size (in pixels) of holes found in input
	mask

string, strlowcase, strupcase

Location in HEALPix directory tree: src/f90/mod/misc_utils.F90

The Fortran90 module misc_utils contains three functions to create or manipulate character strings.

ARGUMENTS

name & dimensionality	kind in/out	description
number	LGT/ IN I4B/ SP/ DP	number or boolean flag to be turned into a character string.
instring outstring format OPTIONAL	CHR IN CHR — CHR IN	arbitrary character string. output character string. character string describing Fortran format of output.

FUNCTIONS:

outstring = string(number [,format])

returns in outstring its argument number converted to a character string. If format is provided it is used to format the output, if not, the fortran default format matching number's type is used.

outstring = strlowcase(instring)

returns in outstring its argument instring converted to lowercase. ASCII characters in the [A-Z] range are mapped to [a-z], while all others remain unchanged.

outstring = strupcase(instring)

returns in outstring its argument instring converted to uppercase. ASCII characters in the [a-z] range are mapped to [A-Z], while all others remain unchanged.

EXAMPLE:

```
use misc_utils
character(len=24) :: s1
s1 = string(123,'(i5.5)')
print*, trim(s1)
print*,trim(strupcase('*aBcD-123'))
print*,trim(strlowcase('*aBcD-123'))
```

Will printout 00123, *ABCD-123 and *abcd-123.

surface_triangle

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Returns the surface in steradians of the spherical triangle described by its three vertices

FORMAT

call surface_triangle(v1, v2, v3, surface)

ARGUMENTS

name&dimensiona	alitykind	in/out	description
v1(3)	DP	IN	cartesian vector pointing at the triangle first vertex.
v2(3)	DP	IN	cartesian vector pointing at the triangle second vertex.
v3(3)	DP	IN	cartesian vector pointing at the triangle third vertex.
surface	DP	OUT	surface of the triangle in steradians.

EXAMPLE:

use healpix_types

use pix_tools, only : surface_triangle

real(DP) :: surface, one = 1.0 dp

call surface_triangle((/1,0,0/)*one, (/0,1,0/)*one, (/0,0,1/)*one,

surface)

print*, surface

Returns the surface in steradians of the triangle defined by the

octant (x, y, z > 0): 1.5707963267948966

RELATED ROUTINES

This section lists the routines related to **surface_triangle**.

surface_triangle 221

pix2ang, ang2pix pix2vec, vec2pix convert between angle and pixel number. convert between a cartesian vector and pixel number.

query_disc, query_polygon, query_strip, query_triangle

render the list of pixels enclosed respectively in a given disc, polygon, latitude strip and triangle

template_pixel_nest, template_pixel_ring

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routines to provide the index of the template pixel associated with a given **HEALPix** pixel, for a resolution parameter N_{side} .

Any pixel can be *matched in shape* to a single of these templates by a combination of a rotation around the polar axis with reflexion(s) around a meridian and/or the equator.

The template pixels are all located in the Northern Hemisphere, or on the Equator. They are chosen to have their center located at

$$z = \cos(\theta) \ge 2/3,$$
 $0 < \phi \le \pi/2,$ $2/3 > z \ge 0,$ $\phi = 0,$ or $\phi = \frac{\pi}{4N_{\text{side}}}.$ (24)

They are numbered continuously from 0, starting at the North Pole, with the index increasing in ϕ , and then increasing for decreasing z.

FORMAT	call template_pixel_nest(nside, template, reflexion)	pixel_nest,
FORMAT	call template_pixel_ring(nside, template, reflexion)	pixel_ring,

name & dimensionality	kind	in/out	description
nside	I4B	IN	the HEALPix $N_{\rm side}$ parameter.
$pixel_nest$	I4B/	IN	NESTED scheme pixel identification
	I8B		number over the range $\{0.12N_{\text{side}}^2 - 1\}$.
pixel_ring	I4B/	IN	RING scheme pixel identification num-
	I8B		ber over the range $\{0.12N_{\text{side}}^2 - 1\}$.
template	I4B/	OUT	identification number of the template
	I8B		matching in shape the pixel provided
			(the numbering scheme of the pixel tem-
			plates is the same for both routines).
reflexion	I4B	OUT	in $\{0, 3\}$ encodes the transformation(s)
			to apply to each pixel provided to match
			exactly in shape and position its respec-
			tive template. 0: rotation around the
			polar axis only, 1: rotation + East-West
			swap (ie, reflexion around meridian), 2:
			rotation + North-South swap (ie, reflex-
			ion around Equator), 3: rotation + East-
			West and North-South swaps

EXAMPLE:

```
use healpix_modules
integer(I4B):: nside, reflexion
integer(I4B):: pixel, template ! for nside <= 8192
!integer(I8B):: pixel, template ! for any valid nside
nside = 256
pixel = 500000
call template_pixel_ring(nside, pixel, template, reflexion)
print*, template, reflexion</pre>
```

Returns in template the index of the template pixel (16663) whose shape matches that of the pixel #500000 for $N_{\rm side} = 256$. Upon return reflexion will contain 2, meaning that the template must be reflected around a meridian and around the equator (and then rotated around the polar axis) in order to match the pixel. Note that the variables pixel and template must be of type I8B instead of I4B if $N_{\rm side} > 8192$ is to be used.

RELATED ROUTINES

This section lists the routines related to **template_pixel_ring**.

nside2templates	returns the n	number of te	mplate:	pixel shape	es avail-
iibiac 2 to iii piatob	I COULTID OIL I	Idilio of of	TITPICCO	pizzoi biiap	JD COVCUIT

able for a given N_{side} .

same_shape_pixels_ring

same_shape_pixels_nest return the ordered list of pixels having the same

shape as a given pixel template

udgrade nest* 225

$udgrade_nest*$

Location in HEALPix directory tree: src/f90/mod/udgrade_nr.F90

Routine to degrade or prograde the pixel size of a **HEALPix** map indexed with the NESTED scheme. The degradation/progradation is done assuming an intensive quantity (like temperature) that does NOT scale with surface area.

In case of degradation, a big pixel that contains one or several bad pixels will take the average of the valid small pixels, unless a 'pessimistic' behavior is assumed in which case the big pixel will take the bad pixel sentinel value. In case of progradation, a bad pixel only spawns bad pixels.

The routine accepts both mono and bi-dimensional maps.

FORMAT call udgrade_nest*(map_in, nside_in, map_out, nside_out[, fmissval, pessimistic])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
$map_in(0:12*nside_in**2-$	SP/	IN	mono-dimensional full sky map to be
1)	DP		prograded or degraded.
map_in	SP/	IN	bi-dimensional full sky map to be pro-
$(0:12*nside_in**2-1,1:nd)$	DP		graded or degraded. The routine finds the second dimension (nd) by itself.
nside_in	I4B	IN	the N_{side} resolution parameter of the input map. Must be a power of 2.
map_out(0:12*nside_out**	2-SP/	OUT	mono-dimensional full sky map after
1)	$\overline{\mathrm{DP}}$		degradation or progradation.
map_out	SP/	OUT	bi-dimensional full sky map after degra-
$(0:12*nside_out**2-$	DP		dation or progradation. The second di-
1,1:nd)			mension (nd) should match that of the input map.
nside_out	I4B	IN	the $N_{\rm side}$ resolution parameter of the output map. Must be a power of 2. If nside_out > nside_in, the map is prograded (ie, more and smaller pixels) with each pixel having the same value as its parent; otherwise, the map in degraded (ie, fewer larger pixels), with each pixel being the average of its (nside_in/nside_out) ² components.
fmissval	SP/ DP	IN	sentinel value given to bad pixels in input and output maps.(default: HPX_SBADVAL or HPX_DBADVAL)
pessimistic	LGT	IN	if set to .true., during a degradation, a big pixel containing at least a small bad pixel will be returned as bad as well, instead of taking the average of the remaing valid pixels. (default: .false.)

EXAMPLE:

use udgrade_nr
call udgrade_nest(map_hi, 256, map_low, 64)

Degrades a NESTED ordered map with $N_{\rm side}=256$ into a NESTED map with $N_{\rm side}=64$

udgrade_nest* 227

RELATED ROUTINES

This section lists the routines related to **udgrade_nest***.

udgrade_ring

prograde or degrade a RING ordered map.

udgrade_ring*

Location in HEALPix directory tree: src/f90/mod/udgrade_nr.F90

Routine to degrade or prograde the pixel size of a **HEALPix** map indexed with the RING scheme. The degradation/progradation is done assuming an intensive quantity (like temperature) that does NOT scale with surface area.

In case of degradation, a big pixel that contains one or several bad pixels will take the average of the valid small pixels, unless a 'pessimistic' behavior is assumed in which case the big pixel will take the bad pixel sentinel value. In case of progradation, a bad pixel only spawns bad pixels.

The routine accepts both mono and bi-dimensional maps.

FORMAT call udgrade_ring*(map_in, nside_in, map_out, nside_out[, fmissval, pessimistic])

Arguments appearing in *italic* are optional.

udgrade_ring* 229

name & dimensionality	kind	in/out	description
map_in(0:12*nside_in**2-1)	SP/ DP	INOUT	mono-dimensional full sky map to be prograded or degraded. The routine finds the second dimension (nd) by itself. Note that the map is modified on output (reordered into NESTED scheme).
map_in (0:12*nside_in**2-1,1:nd)	SP/ DP	INOUT	bi-dimensional full sky map to be prograded or degraded. Note that the map is modified on output (reordered into NESTED scheme).
nside_in	I4B	IN	the $N_{\rm side}$ resolution parameter of the in-
map_out(0:12*nside_out**, 1)	2-SP/ DP	OUT	put map. Must be a power of 2. mono-dimensional full sky map after degradation or progradation.
map_out (0:12*nside_out**2- 1,1:nd)	SP/ DP	OUT	bi-dimensional full sky map after degradation or progradation. The second dimension (nd) should match that of the input map.
nside_out	I4B	IN	the N_{side} resolution parameter of the output map. Must be a power of 2. If nside_out > nside_in, the map is prograded (ie, more and smaller pixels) with each pixel having the same value as its parent; otherwise, the map in degraded (ie, fewer larger pixels), with each pixel being the average of its (nside_in/nside_out) ² components.
fmissval	SP/ DP	IN	sentinel value given to bad pixels in input and output maps.(default: HPX_SBADVAL or HPX_DBADVAL)
pessimistic	LGT	IN	if set to .true., during a degradation, a big pixel containing at least a small bad pixel will be returned as bad as well, instead of taking the average of the remaing valid pixels. (default: .false.)

EXAMPLE:

use udgrade_nr

call udgrade_ring(map_hi, 256, map_low, 64)

Degrades a RING ordered map with $N_{\rm side}=256$ into a RING map with $N_{\rm side}=64$

RELATED ROUTINES

This section lists the routines related to **udgrade_ring***.

udgrade_nest

prograde or degrade a NESTED ordered map.

unfold_weightsfile 231

unfold_weightsfile

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine read a ring-based or pixel-based quadrature weight file and turn it into a full sky (ring-ordered) **HEALPix** map.

FORMAT

call unfold_weightsfile(w8file, w8map)

ARGUMENTS

name & dimensionality	kind in/out	description
w8 file(LEN= filenamelen)	CHR IN	filename of FITS-file containing a list of ring-ordered or pixel-ordered
w8map(0:12*Nside**2-1)	SP/ OUT DP	quadrature weights for some Nside. an array containing a full sky map of weights for the same Nside.

EXAMPLE:

```
use healpix_modules
real(DP), allocatable(:) :: w8map
character(len=FILENAMELEN) :: dirname, filename
integer(I4B) :: nside, won
won = 2
nside = 128
npix = nside2npix(nside)
allocate(w8map(0:npix-1))
dirname = get_healpix_data_dir()
filename = get_healpix_weights_file(nside, won)
filename = trim(dirname)//'//trim(filename)
call unfold_weightsfile(filename, w8map)
```

This code snippet looks for a pixel-based (won=2) weights file in standard location, with a standard name, for nside=128, reads it and unfolds it into a full sky ring-ordered map named w8map.

MODULES & ROUTINES

This section lists the modules and routines used by **unfold_weightsfile**.

pixtools module, containing: nside2npweights function returning the number of pixel-based weights expected for a given Nside when stored in compact form function returning the number of pixels on the full nside2npix sky, for a given Nside fitstools module, containing: routine for printing FITS error messages. printerror function returning the size of a FITS file, and parsgetsize fits ing its header. routine to read FITS file.

library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to **unfold weightsfile**.

input_map

cfitsio

get healpix data dir routine returning actual path to data directory get healpix weights file routine returning the standard name of precomputed weights file these two facilities use unfold weightsfile to apanafast, smoothing ply quadrature weighting to the maps they respectively analyze and smooth

uniq2nest 233

uniq2nest

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

This F90 facility turns the Unique Identifier $u = p + 4N_{\text{side}}^2$, into the parameter N_{side} (a power of 2) and the pixel index p. See "The Unique Identifier scheme" section in "HEALPix Introduction Document" for more details.

FORMAT

call uniq2nest(puniq, nside, pnest)

ARGUMENTS

name	kind	in/out	description
puniq nside pnest	I4B/I8B I4B I4B/I8B	OUT	The HEALPix Unique pixel identifier. Must be ≥ 4 . The HEALPix $N_{\rm side}$ parameter. (NESTED scheme) pixel identification number over the range $\{0.12N_{\rm side}^2-1\}$.

EXAMPLE:

```
use healpix_modules
```

integer(I4B) :: nside, pnest
call uniq2nest(4, nside, pnest)
print*,nside,pnest

 $\begin{array}{cc} \mathrm{returns} \\ 1 & 0 \end{array}$

since the pixel with Unique ID number 4 is the first pixel (p=0) at $N_{\rm side}=1$.

RELATED ROUTINES

This section lists the routines related to **uniq2nest**.

nest2uniq

Transforms Nside and Nested pixel number into Unique **HEALPix** pixel ID number

pix2xxx, ...

to turn NESTED pixel index into sky coordinates and back

vec2ang 235

vec2ang

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Routine to convert the 3D position vector (x, y, z) of point into its position angles (θ, ϕ) on the sphere with $x = \sin \theta \cos \phi$, $y = \sin \theta \sin \phi$, $z = \cos \theta$.

FORMAT

call vec2ang(vector, theta, phi)

ARGUMENTS

name&dimensionality	kind	in/out	description
vector(3)	DP	IN	three dimensional cartesian position vector (x, y, z) . The north pole is $(0, 0, 1)$
theta	DP	OUT	colatitude in radians measured southward from north pole (in $[0,\pi]$).
phi	DP	OUT	longitude in radians measured eastward (in $[0, 2\pi]$).

RELATED ROUTINES

This section lists the routines related to **vec2ang**.

ang2vec	converts the position angles of a point on the
	sphere into its 3D position vector.
$\operatorname{angdist}$	computes the angular distance between 2 vectors
$\operatorname{vect}\operatorname{\underline{\hspace{1em}prod}}$	computes the vector product between two 3D vec-
	tors

vect_prod

Location in HEALPix directory tree: src/f90/mod/pix_tools.F90

Returns the vectorial product of two vectors.

FORMAT call vect $_prod(v1, v2, v3)$

ARGUMENTS

name & dimensionality	kind	in/out	description
v1(3)	DP	IN	cartesian vector \mathbf{v}_1 . cartesian vector \mathbf{v}_2 . cartesian vector $\mathbf{v}_3 = \mathbf{v}_1 \times \mathbf{v}_2$
v2(3)	DP	IN	
v3(3)	DP	OUT	

EXAMPLE:

use healpix_types

use pix_tools, only : vect_prod
real(DP), dimension(3) :: vec

real(DP) :: one = 1.0_dp

call vect_prod((/2,0,0/)*one, (/0,1,0/)*one, vec)

print*, vec

will return: 0.00E+000 0.00E+000 2.00

RELATED ROUTINES

This section lists the routines related to **vect_prod**.

ang2vec converts the position angles of a point on the

sphere into its 3D position vector.

anglist computes the angular distance between 2 vectors

vect_prod 237

vec2ang

converts the 3D position vector of point into its position angles on the sphere.

write asctab*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine stores a power spectrum in an ascii FITS-file. The routine can store temperature coeffecients C_ℓ^T or both temperature and polarisation coeffecients C_ℓ^T , C_ℓ^E , C_ℓ^B , $C_\ell^{T \times E}$.

FORMAT

call write_asctab*(clout, lmax, ncl, header, nl-header, filename[, extno])

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/out	description
filename(LEN=filenamelen)	CHR	IN	the FITS file to which the power
,			spectrum is written.
lmax	I4B	IN	Maximum ℓ value to be written.
ncl	I4B	IN	1 for temperature coeffecients
			only, 4 for polarisation.
clout(0:lmax,1:ncl)	SP/	IN	the powerspectrum to be saved
	DP		in the file.
nlheader	I4B	IN	number of header lines to write
			to the file.
header(LEN=80) (1:nlheader)	CHR	IN	the header to the FITS-file.
extno	I4B	IN	extension number in which
			to write the data (0 based).
			$(\mathbf{default:}\ 0)$

EXAMPLE:

```
use healpix_modules
real(SP), allocatable, dimension(:,:) :: cl
character(len=80), dimension(1:100) :: header
allocate(cl(0:64,1:1))
call write_minimal_header(header,'cl',nlmax=64)
```

write $asctab^*$

call write_asctab (cl,64,1,header,100,'cl.fits')

Writes a power spectrum in the array cl(0:64,1:1) to a FITS-file called 'cl.fits'. The cl array contains the temperature power spectrum C_{ℓ}^{T} up to an ℓ value of 64. 100 header lines are written to the file from the array header(1:100) which was previously filled the minimal required information for a power spectrum file.

MODULES & ROUTINES

This section lists the modules and routines used by write_asctab*.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write asctab*.

alm2cl Routine computing the power spectrum from

spherical harmonics coefficients $a_{\ell m}$

fits2cl Routine to read a FITS file created by

write_asctab.

write_minimal_header routine to write minimal FITS header

write bintab*

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine creates a binary FITS-file from a **HEALPix** map. The routine can save a temperature map or both temperature and polarisation maps (T,Q,U) to the file.

Arguments appearing in *italic* are optional.

ARGUMENTS

name & dimensionality	kind	in/out	description
map(0:npix-1,1:nmap)	SP/	IN	the map to write to the FITS-file.
npix	DP I4B/	IN	Number of pixels in the map.
nmap	I8B I4B	IN	number of maps to be written, 1 for temper-
header(LEN=80) (1:nl-	CHR	IN	ature only, and 3 for (T,Q,U). The header for the FITS-file.
header) nlheader	I4B	IN	number of header lines to write to the file.
filename(LEN=*)	CHR	IN	the map(s) is (are) written to a FITS-file with this filename.
extno	I4B	IN	extension number in which to write the data (0 based). (default: 0)

EXAMPLE:

call write bintab (map,12*32**2,3,header,120,'map.fits')

write bintab* 241

Makes a binary FITS-file called 'map.fits' from the **HEALPix** maps (T,Q,U) in the array map(0:12*32**2-1,1:3). The number of pixels 12*32**2 corresponds to the number of pixels in a $N_{\text{side}} = 32$ **HEALPix** map. The header for the FITS-file is given in the string array header and the number of lines in the header is 120.

MODULES & ROUTINES

This section lists the modules and routines used by **write_bintab***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write bintab*.

input_map, read_bintab routines which read a file created by

write bintab*.

map2alm subroutine which analyse a map and returns the

 $a_{\ell m}$ coefficients.

output_map subroutine which calls write_bintab*

write bintabh subroutine to write a large array into a FITS file

piece by piece

input_tod* subroutine to read an arbitrary subsection of a

large binary table

write_minimal_header routine to write minimal FITS header

write bintabh

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine is designed to write large (or huge) arrays into a binary table extension of a FITS file. The user can choose to write the array piece by piece. This is designed to deal with Time Ordered Data set (tod).

FORMAT

call write_bintabh(tod, npix, ntod, header, nl-header, filename, [extno, firstpix, repeat])

Arguments appearing in *italic* are optional.

write_bintabh* 243

name & dimensionality	kind	in/out	description
tod(0:npix-1,1:ntod)	SP/ DP	IN	The map or tod to write to the FITS file. It will be written in the file at the location corresponding to pixels (or time samples) firstpix to firtpix + npix -1.
npix	I8B	IN	Number of pixels or time samples in the map or TOD. See Note below.
ntod	I4B	IN	Number of maps or tods to be written. Each of them will be in a different col- umn of the FITS binary table.
header(LEN=80) (1:nlheader)	CHR	IN	The header for the FITS file.
nlheader	I4B	IN	number of header lines to write to the file.
filename(LEN = filenamelen)	CHR	IN	The array is written into a FITS file with this filename.
extno	I4B	IN	extension number in which to write the data (0 based). (default: 0)
firstpix	I8B	IN	0 Location in the FITS file of the first pixel (or time sample) to be written (0 based). (default: 0). See Note below.
repeat	I4B	IN	Length of the element vector used in the binary table. (default: 1024 if npix

Note: Indices and number of data elements larger than 2^{31} are only accessible in FITS files on computers with 64 bit enabled compilers and with some specific compilation options of cfitsio (see cfitsio documentation).

EXAMPLE:

```
use healpix_types
use fitstools, only : write_bintabh
character(len=80), dimension(1:128) :: hdr
real(SP), dimension(0:49,1) :: tod
character(len=FILENAMELEN) :: fname='tod.fits'
hdr(:) = ' '
tod(:,1) = 1.
call write_bintabh(tod, 50_i8b, 1, hdr, 128, fname, firstpix=0_i8b,
repeat=10)
tod = tod * 3.
call write_bintabh(tod, 20_i8b, 1, hdr, 128, fname, firstpix=40_i8b)
```

Writes into the FITS file 'tod.fits' a 1 column binary table, where the first 40 data samples have the value 1. and the next 20 have the value 3. (Note that in this example the second call to write_bintabh overwrites some of the pixels written by the first call). The samples will be written in element vectors of length 10. The header for the FITS file is given in the string array hdr and its number of lines is 128.

MODULES & ROUTINES

This section lists the modules and routines used by write_bintabh.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write bintabh.

input_tod* routine that reads a file created by write_bintabh.
input_map, read_bintab routines to read **HEALPix** sky map,
write_minimal_header routine to write minimal FITS header

write_dbintab 245

write_dbintab

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine is obsolete.

To write P_{lm} polynoms into a FITS file, use write_plm instead. To write a Healpix map into a FITS file, use write_bintab or output_map.

write fits cut4

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine writes a cut sky **HEALPix** map into a FITS file. The format used for the FITS file follows the one used for Boomerang98 and is adapted from COBE/DMR. This routine can be used to store polarized maps, where the information relative to the Stokes parameters I, Q and U are placed in extension 0, 1 and 2 respectively by successive invocation of the routine.

FORMAT

call write_fits_cut4(filename, np, pixel, signal, n_obs, serror[, header, coord, nside, order, units, extno, polarisation])

Arguments appearing in *italic* are optional.

write_fits_cut4 247

name&dimensionality	kind	in/oı	ıtdescription
Clarama (LEN 6:1	- VIID	INI	FITC 61s into online the cost along one will be
filename(LEN=filenamelen	прпк	IN	FITS file into which the cut sky map will be written
np	I4B	IN	number of pixels to be written in the file
pixel(0:np-1)	I4B	IN	index of observed (or valid) pixels
signal(0:np-1)	SP	IN	value of signal in each observed pixel
$n_obs(0:np-1)$	I4B	IN	number of observation per pixel
serror(0:np-1)	SP	IN	rms of signal in pixel, for white noise, this is $\propto 1/\sqrt{\text{n_obs}}$.
header(LEN=80)(1:)	CHR	IN	FITS extension header to be included in the
(OPTIONAL)			FITS file
coord(LEN=1)	CHR	IN	astrophysical coordinates ('C' or 'Q' Ce-
,			lestial/eQuatorial, 'G' for Galactic, 'E' for
			Ecliptic)
nside	I4B	IN	HEALPix resolution parameter of data set
order	I4B	IN	HEALPix ordering scheme, 1: RING, 2: NESTED
units(LEN=20)	CHR	IN	maps units (applies only to Signal and Serror)
extno	I4B	IN	(0 based) extension number in which to write data. (default: 0). If set to 0 (or not set) a new file is written from scratch. If set to a value larger than 1, the corresponding extension is added or updated, as long as all previous extensions already exist. All extensions of the same file should use the same Nside, Order and Coord
polarisaton	I4B	IN	if set to a non zero value, specifies that file will contain the I, Q and U polarisation Stokes parameter in extensions 0, 1 and 2 respectively, and sets the FITS header keywords accordingly. If not set, the keywords found in header will prevail. Note: the information relative to Nside, Order and Coord has to be given, either thru these keyword or via the FITS Header.

MODULES & ROUTINES

This section lists the modules and routines used by write_fits_cut4.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write fits cut4.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize_fits routine to know the size of a FITS file and its type

(eg, full sky vs cut sky)

input_map all purpose routine to input a map of any kind

from a FITS file

output_map subroutine to write a FITS file from a **HEALPix**

map

read_fits_cut4 subroutine to read a **HEALPix** cut sky map from

a FITS file

write_minimal_header routine to write minimal FITS header

write_fits_partial 249

write_fits_partial

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine writes unpolarised or polarised partial sky **HEALPix** map into a FITS file.

For more information on the FITS file format supported in **HEALPix**, including the one implemented in write_fits_partial, see https://healpix.sourceforge.io/data/examples/healpix_fits_specs.pdf.

FORMAT call write_fits_partial(filename, pixel, cutmap[, header, coord, nside, order, units, extno])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
filename(LEN=filenamelen	n)CHR	IN	FITS file in which the partial sky map will be written
pixel(0:np-1)	I4B/ I8B	IN	index of observed (or valid) pixels
$\operatorname{cutmap}(0:\operatorname{np-1,1:nc})$	SP/ DP	IN	value of polarised (if nc= 3) or unpolarised (if nc= 1) map value in each observed pixel
header(LEN=80)(1:) (OPTIONAL)	CHR	IN	FITS extension header to be included in the FITS file
coord(LEN=1)	CHR	IN	astrophysical coordinates ('C' or 'Q' Celestial/eQuatorial, 'G' for Galactic, 'E' for Ecliptic)
nside	I4B	IN	HEALPix resolution parameter of data set
order	I4B	IN	HEALPix ordering scheme, 1: RING, 2: NESTED
units(LEN=20)	CHR	IN	maps physical units (applies to all columns except PIXEL)
extno	I4B	IN	(0 based) extension number in which to write data. (default: 0). If set to 0 (or not set) a new file is written from scratch. If set to a value larger than 1, the corresponding extension is added or updated, as long as all previous extensions already exist. All extensions of the same file should use the same Nside, Order and Coord Note: the information relative to Nside, Order and Coord has to be given, either thru these keyword or via the FITS Header.

write_fits_partial 251

MODULES & ROUTINES

This section lists the modules and routines used by write_fits_partial.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write_fits_partial.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize_fits routine to know the size of a FITS file and its type

(eg, full sky vs cut sky)

input_map all purpose routine to input a map of any kind

from a FITS file

output_map subroutine to write a FITS file from a **HEALPix**

map

read_fits_partial subroutine to read a HEALPix partial sky map

from a FITS file

write_minimal_header routine to write minimal FITS header

write minimal header

Location in HEALPix directory tree: src/f90/mod/head_fits.F90

This routine writes the baseline FITS header for the most common **HEALPix** data sets: (cut sky or full sky) map, $C(\ell)$ power spectra and $a_{\ell m}$ coefficients.

FORMAT

call write_minimal_header(header, dtype, [append, nside, order, ordering, coordsys, creator, version, randseed, beam_leg, fwhm_degree, units, nlmax, polar, nmmax, bcross, deriv, asym_cl])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
header(LEN=80) DIMENSION(:)	CHR	INOUT	The FITS header to fill in.
dtype(LEN=*)	CHR	IN	data to be put in the FITS file, must be one of 'ALM', 'CL', 'MAP', 'CUTMAP' (case un-sensitive).

name & dimensionality	kind	in/out	description
append	LGT	IN	if set to TRUE, the keywords will be appended to the content of header instead of written from scrath
nside	I4B	IN	map resolution parameter; required for dtype='MAP' and dtype='CUTMAP'
order	I4B	IN	map ordering, either 1 (=ring) or 2 (=nested); see ordering
ordering(LEN=*)	CHR	IN	map ordering, either 'RING' or 'NESTED' (case un-sensitive); either order or ordering is required for dtype='MAP' and dtype='CUTMAP'
coordsys(LEN=*)	CHR	IN	map coordinate system; Valid choices are 'G' = Galactic, 'E' = Ecliptic, 'C'/'Q' = Celestial = eQuatorial
creator(LEN=*)	CHR	IN	name of software generating the data set
version(LEN=*)	CHR	IN	version of creator software
randseed	I4B	IN	random number generator seed used to gen-
			erate the data
$beam_leg(LEN=*)$	CHR	IN	File containing Legendre transform of symmetric beam
fwhm_degree	DP	IN	FWHM in degrees of gaussian symmetric beam (FITS keyword: FWHM)
units(LEN=*)	CHR	IN	physical units of the data set (FITS keyword: TUNIT*)
nlmax	I4B	IN	maximum multipole order l of the data set (FITS keyword: MAX-LPOL)
polar	LGT	IN	if set to .TRUE., the file to be written contains polarized data
nmmax	I4B	IN	maximum degree m of data set (FITS keyword: MAX-MPOL)
bcross	LGT	IN	if set to .TRUE., the magnetic cross terms power spectra (TB and EB) are included;
deriv	I4B	IN	only applies to dtype='CL' order of derivatives to included in FITS file (0, 1 or 2); only applies to dtype='MAP'
asym_cl	LGT	IN	if set to .TRUE., the asymmetric power spectra (ET, BT and BE on top of TE, TB and EB) are included; only applies to dtype='CL'

EXAMPLE:

```
use healpix_types
use head_fits
character(len=80), dimension(1:60) :: header
call write_minimal_header(header, 'MAP', nside=256, ordering='Nested')
call add_card(header, 'HISTORY', 'Dummy map')
```

Writes in header a **HEALPix** compliant FITS header for a $N_{\text{side}} = 256$ map with NESTED ordering. Further HISTORY information is added with add card

MODULES & ROUTINES

This section lists the modules and routines used by write_minimal_header.

write_hl more general routine for adding a keyword to a

header.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write minimal header.

${ m add_card}$	general purpose routine to write/edit an arbitrary keyword into a FITS file header.
get _card	general purpose routine to read any keywords from a header in a FITS file.
del	routine to discard a keyword from a FITS header
read_par, number_of_alms	routines to read specific keywords from a header in a FITS file.
getsize_fits	function returning the size of the data set in a fits file and reading some other useful FITS keywords
$ m merge_headers$	routine to merge two FITS headers

write_plm 255

write_plm

Location in HEALPix directory tree: src/f90/mod/fitstools.F90

This routine creates a double precision binary FITS-file from a given array. The routine is used by the **HEALPix** facility plungen to store precomputed $P_{\ell m}(\theta)$.

FORMAT call write_plm(plm, nplm, nhar, header, nl-header, filename, nsmax, nlmax)

name&dimensionality	kind	in/o	utdescription
plm(0:nplm-1,1:nhar)	DP	IN	the array with the precomputed
nplm	I4B	IN	$P_{\ell m}(\theta)$ values. Number of $P_{\ell m}$ values to store.
nhar	I4B	IN	1 for scalar $P_{\ell m}$ only and 3 for tensor harmonics.
header(LEN=80) (1:nlheader)	CHR	IN	The header for the FITS-file.
nlheader	I4B	IN	number of header lines to write to the file.
filename(LEN = filenamelen)	CHR	IN	the precomputed $P_{\ell m}(\theta)$ values are written to this file.
nsmax	I4B	IN	$N_{\rm side}$ for the precomputed $P_{\ell m}$ s.
nlmax	I4B	IN	maximum ℓ value for the precomputed $P_{\ell m}$ s.

EXAMPLE:

call write plm (plm, 65*66*32, 1, header, 120, 'plm 32.fits', 32, 64)

Makes a double precision binary FITS-file called 'plm_32.fits' from the precomputed $P_{\ell m}(\theta)$ in the array plm(0:65*66*32-1,1:1). The number 65*66*32 corresponds to the number of precomputed $P_{\ell m}$ s needed for a $N_{\rm side}=32$ HEALPix map synthesis/analysis. The header for the FITS-file is given in the string array header and the number of lines in the header is 120.

MODULES & ROUTINES

This section lists the modules and routines used by write_plm.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

RELATED ROUTINES

This section lists the routines related to write_plm.

read_dbintab, read_bintab routines which reads a file created by write_plm.

map2alm, alm2map routines using precomputed $P_{\ell m}(\theta)$.

xcc_v_convert 257

xcc v convert

Location in HEALPix directory tree: src/f90/mod/coord_v_convert.f90

This routine rotates a 3D coordinate vector from one astronomical coordinate system to another.

ARGUMENTS

name & dimension-	kind	in/out	description
ality			
ivector(1:3)	DP	IN	3D coordinate vector of one astronomical ob-
			ject, in the input coordinate system.
iepoch	DP	IN	epoch of the input astronomical coordinate
			system.
oepoch	DP	IN	epoch of the output astronomical coordinate
			system.
isys(len=*)	CHR	IN	input coordinate system, should be
			one of 'E'=Ecliptic, 'G'=Galactic,
			'C'/'Q'=Celestial/eQuatorial.
osys(len=*)	CHR	IN	output coordinate system, same choice as
			above.
ovector(1:3)	DP	IN	3D coordinate vector of the same object, in
			the output coordinate system.

EXAMPLE:

```
use healpix_types
use coord_v_convert, only: xcc_v_convert
real(dp) :: vecin(1:3), vecout(1:3)
vecin = (/ 0_dp, 0_dp, 1_dp /)
call xcc_v_convert(vecin, 2000.0_dp, 2000.0_dp, 'g', 'c', vecout)
```

Will produce in vecout the location in Celestial coordinates (2000 epoch) of the North Galactic Pole (defined in vecin)

RELATED ROUTINES

This section lists the routines related to xcc_v_convert.

coordsys2euler_zyz produces the Euler angles ψ, θ, φ in (Z,Y,Z) con-

vention for rotation between standard astronomi-

cal coordinate systems.

ang2vec, vec2ang Routine to convert spherical coordinates (co-

latitude and longitude) into 3D vector coordinates

and vice-versa.