

UNIVERSITY OF MANNHEIM
SCHOOL OF SOCIAL SCIENCES
DEPARTMENT OF POLITICAL SCIENCE

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On Using the Metropolis-Hastings Algorithm for Data Imputation

Tobias Stenzel
[tobias.stenzel@students.uni-
mannheim.de](mailto:tobias.stenzel@students.uni-mannheim.de)

Prof. Thomas Gschwend, Ph.D.

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1 Introduction

In recent years scholars have found declining support for democracy in long-established democracies. (Denemark et al. 2016; Foa and Mounk 2016, 2017; Norris 2017; Voeten 2016). This finding raises two important questions: First, what are the reasons for this decline, and second, what are its implications, i.e., does a decline in democratic support endanger the survival of these democracies?

A series of recent articles (Claassen 2019, 2020a, 2020b) researches these questions and presents novel results. Regarding the first question, Claassen (2020a) finds – in contrary to the the widely held belief of self-reinforcing democracies – that democratic support naturally fluctuates over time. The reasons is that increases in democracy levels lead to decreases in public support and vice versa. Regarding question two, so far the results about the relationship between democratic support and its survival have been mixed. Claassen (2020a), however, finds supporting evidence for the natural theory that democratic support plays a positive role in the system’s survival.

A main obstacle for researching democratic support is that current panel data contains a large number of missing values. Claassen (2019) finds an approach to simulate dense panel data from the actual fractured data. The two most recent studies both rely on this data. His approach consists of three steps: First, assume a probabilistic structural model of democratic support. Second, estimate its parameters via the Metropolis Hastings algorithm using the fractured data. Third, simulate the data using the model and the large number of parameter estimates.

The objective of this work is to evaluate the robustness of Claassen’s findings towards changes in the method’s hyperparameters. In other words, I incorporate the uncertainty about the right choice of hyperparameters into Claassen’s results to test their reliability. In particular, I propagate a random set of hyperparameters through Claassen’s estimation procedure. This is important because arbitrary hyperparameter choices can potentially lead to false or at least random results. Therefore, the respective parametric uncertainty should always be reported along the point estimate.

I come to the following results:

The final paper is structured as follows: Section 2 reviews the literature of

public support with a focus on Claassen's papers and defines the concept. Section 3 explains Claassen's model of public support, its estimation and my approach for the uncertainty propagation. Section 4 presents the results and Section 5 discusses the findings. Section 6 concludes.

2 Literature Review

2.1 The Concept of Democratic Support

There are two major conceptualizations of public support for democracy (PSD). First, the "implicit" approach that requires the support for broader sociopolitical values like post-materialism and egalitarianism. Here, people support democracy implicitly if they support the values that are framed as particularly democratic. Second, the "explicit" approach that requires both an appraisal of democracy and a rejection of autocratic alternatives. Some studies also refer to PSD measured on the national level as "mood."

2.2 Drivers of Democratic Support

The main theory about why citizen and societies begin to support democracy are called *generational socialization* and *instrumental regime performance*. The first theory assumes that individuals are taught to support the regime under which they are socialized during late adolescence (insert citation). One implication is that after a shift to democracy, the support for it will grow over time (Denemark et al. (2016)). Indeed, several single-country studies have found evidence for this claim, for example for 1970s Germany (Baker et al. (1981)), 1980s Spain (Montero, Gunther, and Torcal (1997)), and 1990s Russia (Mishler and Rose (2007)). One the other hand, other studies do not find such an effect analyzing other Central and Eastern European countries (Mishler and Rose (2002)). Furthermore, more recent studies even find a decline in PSD over the last years (Foa and Mounk 2016, 2017).

Regarding the second theory, instrumental regime performance, PSD rises if the system performs well in terms of instrumental benefits such as economic

growth and it declines if the opposite is the case (Dalton 1994; Magalhães 2014). Consequently, the theory suggests that during PSD declines during economic crises. However, there are case-studies that do (Dalton 1994; Magalhães 2014; Mishler and Rose 1996) and that do not (Graham and Sukhtankar (2004)) find this relationship in the data.

Claassen (2020b) offers an alternative theory in transferring the thermostatic model of public opinion and policy (Wlezien (1995)) to democracy and democratic support. In particular, he suggests that there is a negative feedback loop between PSD and democracy so that PSD decreases if democracy supply increases and vice versa. In short, the reasoning is that the output of democratic rights and institutions overshoots the initial desire for them which causes another over-compensation in favor of lower levels of democracy. Moreover, Claassen (2020b) finds different causal channels for electoral and minoritarian democracies. These two sub-types differ in the degree to which the majority holds juridical power. Therefore, he tests the following hypotheses: First, increases in democracy have a negative effect on PSD (H1), Second, he specifically looks at electoral (H1-elec) and minoritarian democracies (H1-min). In his analysis he finds evidence for H1 and H1-min but not for H1-elec.

2.3 Democratic Support and Survival of Democracy

Claassen (2020a) distinguishes between two types of PSD: diffuse and specific. Specific PSD is instrumental and focuses on regime outputs (similar to the instrumental regime performance theory), whereas diffuse support is normative and focuses on the principles of the regime. Therefore, principled PSD is more durable than specific support and helps cushioning regimes in times of political or economic crises. It is thus principled PSD that helps to ensure the survival of democracy. Although the theory is widely accepted (e.g., Norris (2017), Booth and Seligson (2009), Mattes and Bratton (2007)), the findings so far have also been mixed with supporting contributions (Inglehart (2003), Welzel and Inglehart (2005)) and contributions against the theory (Hadenius and Teorell (2005), Welzel (2007), Fails and Pierce (2010), Qi and Shin (2011)). Astonishingly, these studies essentially analyze the same data from the World Value Survey starting at

wave 3 where respective PSD items are included.

Claassen (2020a) does not only look at the relationship between PSD and democratic survival but also between PSD and democratic emergence. He includes the argument made by Qi and Shin (2011) that PSD may also function as democratic demand, thus increasing the probability of transitioning from autocracy to democracy. Claassen's hypotheses thus are: First, PSD is positively associated with subsequent change in democracy regardless of the initial level of democracy. Second, he specifically looks at PSD in already-existing democracies (H2-dem) and at PSD in autocracies (H2-aut). He finds evidence in support of H2-dem, mixed evidence for H2 and no evidence for H2-aut.

2.4 Measuring Democratic Support and the Data Challenge

2.4.1 Problems in previous studies

We measure PSD with existing survey data on the national level. In particular, we focus on principled support. The questions ask for the respondent's opinion on the appropriateness or desirability of democracy and undemocratic alternatives and comparisons between both.

Such items are available in 14 survey projects,¹ for 150 countries, and from 1988 on. Combined, the dataset includes 3,765 nationally aggregated binary responses from 1,390 nationally representative survey samples.

The data, however, poses the following challenge: It is highly fractured across time and space, with many – oftentimes large – gaps for all countries except Belgium. For instance, China is the country with most participants over all years, namely 20895. However, from 1988 to 2020, the data available covers only 2001-2003, 2006-2009, and 2011/2012. And this is even a good coverage. Many countries are not covered at all or only surveyed once (insert numbers and code).

So far, past research has responded to this issue by discarding most of the available data and using only small cross-sectional data sets consisting of data from only one survey project for one year.

¹World and European Values Surveys, the Afrobarometer, Arab Barometer, Latinobarometer, Asiabarometer, Asian Barometer, South Asia Barometer, New Europe Barometer, Latin American Public Opinion Project, Eurobarometer, European Social Survey, pew Global Attitudes Project, and the Comparative Study of Electoral Systems

2.4.2 Data and items and small sketch of the approach as intro to next section

Both publications use panel data for PSD in many countries and measured by multiple items. However, the respective datasets display many gaps. To solve this problem, Claassen describes a method to estimate the data in the first publication of the three-part series, Claassen (2019).

3 Model and Estimation

Explain Method in 2018b

4 Results and Discussion

5 Conclusion

6 Appendix: Mathematical Background

6.1 Introduction

The Metropolis-Hastings (MH) algorithm is a method for sampling data points from a probability distribution from which direct sampling is difficult. It places among the top 10 algorithms with the greatest influence on science and engineering in the 20th century (Beichl and Sullivan 2000). The MH algorithm belongs to the class of Markov chain Monte Carlo (MCMC) methods. In my explanation I assume prior knowledge on Monte Carlo sampling. However, I will describe the basics of Markov Chains. This section is structured as follows. First, I motivate the usage of the MH algorithm. Second, I explain the basics of Markov Chains. Third, I derive the algorithm and make clear why it works.

6.2 Motivation

One main application for the MH algorithm is Bayesian inference. Specifically, we want to estimate parameters θ of some probabilistic model f . We have only limited prior knowledge of the distribution of θ , $p(\theta)$, and we have a likelihood sample of f given the unknown θ , namely $p(X|\theta)$. The goal is to estimate the posterior distribution of θ , $p(\theta|X)$, given all information that we have. In practice, we do not have a formal definition of the likelihood but only observations. Therefore, we can only approximate the posterior by numerical integration, i.e., we need to sample many points from the posterior to describe it. We can then use the posterior sample to estimate θ with the maximum a posteriori probability estimate.

Claassen (2019) uses the MH algorithm to impute gaps in a panel data set. His approach consists of four steps: First, assume a data generating process f parameterized by θ . Second, provide the algorithm with the incomplete data X as likelihood and select priors for θ to obtain the posterior distribution $p(\theta|X) = \frac{p(X|\theta)p(\theta)}{P(X)} \propto p(X|\theta)p(\theta)$. Third, use the values for θ with the highest posterior probability as estimates for θ . Finally, insert these estimates into the assumed probabilistic, data generating model f and use it to sample the missing data.

In general and abstracting from Bayesian inference, the MH algorithm generates a sample of random states according to the desired probability distribution $P(X)$. For this purpose, the algorithm employs a Markov process that converges to a unique stationary distribution $\pi(x)$ with $\pi(x) = P(X)$. This distribution can then be used for further steps as previously described. The next section explains the conceptual basics.

6.3 Markov Chains

A Markov chain $(X_t)_{t \in \mathbb{N}}$ is a stochastic process (over time) with the property that the probability of the realization in the next period depends solely on the realization in the current state and not the complete history. This is called the Markov

property. Because Markov chains with a countable, or discrete, state space are much more accessible than their continuous variant, in this chapter we will look at the discrete case. Formally, the Markov property writes

$$P(X_{t+1}|X_t, X_{t-1}, \dots, X_0) = P(X_{t+1}|X_t). \quad (1)$$

Under some conditions, the stochastic process described by a Markov chain converges to a time-invariant probability distribution, i.e. $P(X_{t+k}|X_{t+k-1}) = P(X_t|X_{t-1}), \forall k > 0$. The crucial step for understanding the MH is to see how it samples a Markov Chain that is certain to converge to a stable posterior distribution. Before exploring how the MH algorithm achieves this result, however, it is necessary to understand its conditions conceptually. To this end, we will use the example depicted by the following graph in Figure 1 that shows the intertemporal transition probabilities between three states representing random events.

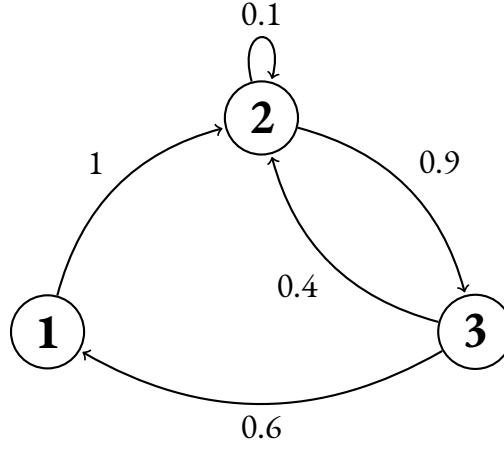


Figure 1: Transition Graph for Markov Chain with 3 states.

This transition graph can be summarized by the $n \times n$ transition matrix T where each element (i, j) represents the probability of moving from state i in period t to state j in period $t + 1$, and where n represents the number of states, i.e. $T_{i,j} = P(X_{t+1} = j|X_t = i)$. For our example, we have

$$T = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0.1 & 0.9 \\ 0.6 & 0.4 & 0 \end{pmatrix}. \quad (2)$$

6.3.1 Limit Distribution

As touched upon in the previous subsection, interesting questions can be what the probabilities of each state $j \in \{1, \dots, s\}$ are after a finite number or infinitely many steps. For this purpose let $\pi_t(j) = P(X_t = j)$ denote the probability of being in state j in period t . Of course, the probabilities in $t > 0$ depend on the probabilities for the initial state π_0 . We can use the law of total probability to calculate the probability of each state for the next period $t = 1$ by

$$P(X_1 = j) = \sum_{i=1}^3 P(X_1 = j | X_0 = i) \pi_0(i). \quad (3)$$

I.e., to compute the probability of being in state j in $t = 1$, for each initial state i , we multiply its probability $\pi_0(i)$ by the probability of moving from i to state j . This is equivalent to $\pi_1 = \pi_0 T$ in vector notation. Further, we can compute the distributions in an arbitrary future period by repeating the matrix multiplication, e.g, $\pi_2 = \pi_0 T T$, or in general, $\pi_t = \pi_0 T^t$.

Now we are ready to define the limit distribution that describes the probability distribution after infinitely many periods by

$$\pi_\infty = \lim_{t \rightarrow \infty} \pi_t = \lim_{t \rightarrow \infty} \pi_0 T^t. \quad (4)$$

We can further ask two additional important questions. First, does a limit distribution exist? And second, is it unique, or in other word, do we have the same limit distribution independent from the realization of the initial state X_0 ? In our example, there does not only exist a limit distribution with $\pi_\infty = (0.2, 0.4, 0.4)$, it is even unique regardless of start distribution π_0 . This means that independent of the start state, the probability of each state converges to the same number. For the context of the MH algorithm, this is an important property because we always want to compute the same estimates for our parameters θ , regardless of the

starting values of our simulation. In the next section, we introduce and simplify conditions that guarantee a unique limit distribution.

6.3.2 Irreducibility, Periodicity and Stationarity

Definition 6.1. A Markov chain is called *irreducible* if each state is reachable from any other state in a finite number of steps.

Figure 2 shows a Markov chain represented by a bipartite graph. This graph is composed by two times the graph in Figure 1. Obviously, this chain is not irreducible because the initial state impacts all future distributions. More precisely, starting in one subgraph sets the probability of reaching states in the other subgraph to zero. We see that a Markov Chain is only irreducible if there is at least an indirect link between every pair of states. We also observe that if the Markov Chain is not irreducible there can be no limit distribution.

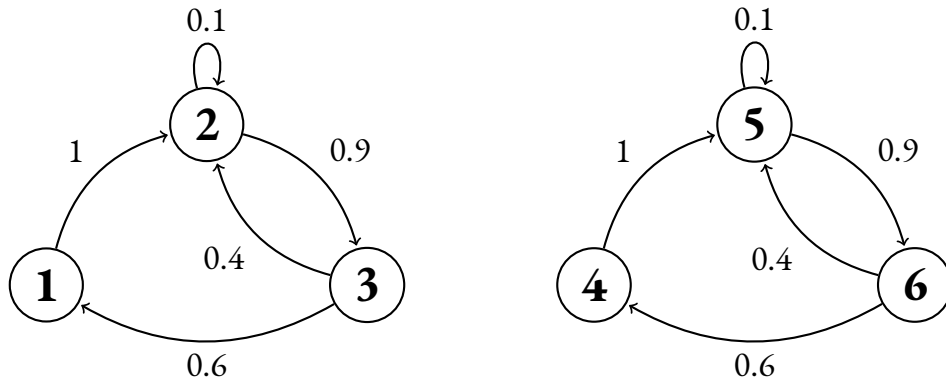


Figure 2: Transition Graph for Irreducible Markov Chain.

Definition 6.2. A state i has a period k if the greatest common denominator of possible revisits is k . A Markov chain is *aperiodic* if the period of all its states is 1.

Consider the five-state Markov chain in Figure 3 as an illustration for the above definition and suppose we start in state 1. Observe that, independent of the random draw for next period, we will arrive again in state 1 after two or four steps. Therefore, state 1 has a period of 2. If a state is revisited in random rather than a fixed time period then the state has period 1. This is automatically the case if a state has a positive edge with itself.

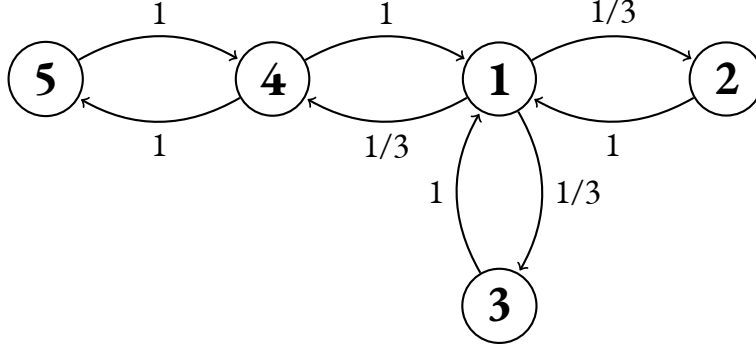


Figure 3: Markov Chain with 2-periodic State 1

Definition 6.3. π^* is the *stationary distribution* of a Markov Chain with Transition matrix T if $\pi^* = \pi^* T$ and π^* is a probability vector.

Verbally, this means that the probability distribution π^* does not change anymore over time. If π^* is also unique, then π^* is our aim, the limit distribution introduces in section 1.3.1, i.e., $\pi^* = \pi_\infty$.

These three definitions are enough to understand the next fundamental theorem.

6.3.3 The Fundamental Theorem of Markov Chains

The next theorem defines formally the condition when a Markov Chain converges to a unique distribution, i.e. the limit distribution.

Theorem 6.1. (*Fundamental Theorem of Markov Chains*) *If a Markov chain is irreducible and aperiodic (called ergodic) then it has a stationary distribution π^* that is unique ($\lim_{t \rightarrow \infty} P(X_t = i) = \pi_i^*, \forall i$).*

Therefore, if we want to construct a stable distribution $P(X)$ via Markov chains, we need to ensure that it is irreducible and aperiodic with stationary distribution $\pi^* = P(X)$. In the next subsection, we substitute the stationarity condition by a stronger one before we finally derive the MH algorithm.

6.3.4 Reversibility

Definition 6.4. A Markov chain is *reversible* if there is a probability distribution π over its states such that $\pi(i)T_{ij} = \pi(j)T_{ji}, \forall i, j$ (reversibility condition).

Theorem 6.2. *A sufficient condition for distribution π^* to be a stationary distribution of a Markov chain with transition matrix T is that it fulfills the reversibility condition.*

Proof. $\sum_i \pi(i)T_{i,j} = \sum_i \pi(j)T_{j,i} = \pi(j) \sum_i T_{j,i} = \pi(j) \implies \pi T = \pi$ \square

Reversibility is a stronger condition than stationarity because it requires that the probability flux from i to j is equal to the one from j to i for each possible pair of states. Recall, that stationarity only requires that the probability flux to one state is equal on aggregate and not that it is symmetric between each pair of states over time. Therefore, if we want to achieve a stationary distribution it is enough to ensure that it is reversible.

6.4 The Algorithm

Recall that we want to generate a sample of a desired distribution $P(X)$. For this purpose, we use a Markov process that is uniquely defined by its transition probabilities $P(X_{t+1}|X)$ with limit distribution π so that $\pi = P(X)$. As explained in the previous section, a Markov process has a limit distribution if each transition $X_t \rightarrow X_{t+1}$ is reversible and if the stationary distribution π is ergodic. With the MH algorithm, we construct such a Markov process with stationary distribution $\pi = P(X)$. The derivation starts with another way of writing reversibility²:

$$P(x'|x)P(x) = P(x|x')P(x') \iff \frac{P(x'|x)}{P(x|x')} = \frac{P(x')}{P(x)} \quad (5)$$

The main idea is to separate transition $P(x'|x)$ in two steps: the proposal step and the acceptance-or-rejection step. Let $g(x')$ be the proposal distribution, i.e., the conditional probability of proposing state x' given x . And let $A(x'|x)$ be the probability of accepting proposed state X' . Formally, we have $P(x'|x) = g(x'|x)A(x'|x)$. Inserting this in Equation (5) gives

$$\frac{P(x')}{P(x)} = \frac{g(x'|x)A(x',x)}{g(x|x')A(x',x)} \iff \frac{A(x',x)}{A(x,x')} = \frac{P(x')}{P(x)} \frac{g(x|x')}{g(x'|x)}. \quad (6)$$

²We simplify our notation by using x' and x instead of X_{t+1} and X_t .

The following choice, termed the Metropolis choice, is commonly used as an acceptance ratio for sampling x' from $P(x')$ that fulfills the above reversibility condition:

$$A(x', x) = \min \left(1, \frac{P(x')}{P(x)} \frac{g(x|x')}{g(x'|x)} \right) \quad (7)$$

Note that the minimizer in $A(x', x)$ enforces that the probability is below 1. The MH algorithm writes as follows:

Algorithm 1 Metropolis-Hastings algorithm

```

Initialize  $X_0$ 
for  $t \leftarrow 0$  to  $T - 1$  do
    Draw  $u \sim \mathcal{U}_{[0,1]}$ 
    Draw candidate  $X^* \sim P(X^*|X_{t-1})$ 
    if  $u < \min\{1, \frac{p(X^*)g(X_t|X^*)}{p(X_t)g(X^*|X_t)}\}$  then
         $X_{t+1} \leftarrow X^*$ 
    else
         $X_{t+1} \leftarrow X_t$ 
    end if
end for

```

Obviously, the construction of the acceptance ratio ensures reversibility. Ergodicity is ensured by the random nature with which we accept proposed states: First, the chain is irreducible because each state is reachable from any other state with positive probability at every single step. Second, for each state x , $P(x' = x)$ is always positive and therefore the Markov chain is aperiodic.

In a general setting, the choice for transition distribution $g(x'|x)$ and the number of iterations until the limit distribution is reached are unclear. These two choices are the hyperparameters of the MH algorithm. In the Bayesian inference application in the article series starting from Claassen (2019), additional choices are the prior distribution $p(\theta)$ and the model choice f .

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