Method 1 and Method 2, representing different carbon pricing methods adopted in the paper for comparison, are presented below for your convenience.

$$\begin{split} &\operatorname{Model of TNO \ (Method \ 1):} & \operatorname{Model of PDNO \ (Method \ 1):} \\ & \underset{f_w^c, f_w^c}{\operatorname{min}} C_{\operatorname{tusers}} = \sum_{a \in A_n} (\omega t_a + \phi \varepsilon_a l_a / 10^6) x_a^{\operatorname{g}} \\ & + \sum_{a \in A_n} \omega t_a x_a^c + \sum_{a \in A_c} (\omega t_a + \lambda_a^{\operatorname{M1}} E_{\operatorname{B}}) x_a^c \\ & + \kappa \sum_{j \in \pi(0)} P_{0j} + \phi \left(\sum_{j=2}^{|B|} p_j^{\operatorname{g}} \rho_j^{\operatorname{g}} + P_{0j} \rho_i^{\operatorname{g}} \right) \\ & s.t. \\ & s.t. \\ & \operatorname{Cons} - \operatorname{Flow}: & (1) - (3) \\ & Cons - \operatorname{Time}: & (4) \\ & Cons - \operatorname{Emission}: \ (5) \\ & \operatorname{Cons} - \operatorname{Cost}: \\ & c_{ke}^{rs} = \sum_{a \in A_n} \omega t_a \delta_{a,ke}^{rs} \\ & + \sum_{a \in A_c} (\omega t_a + \lambda_a^{\operatorname{M1}} E_{\operatorname{B}}) \delta_{a,ke}^{rs} \\ & + k_a \in A_c \\ & \forall ke \in K_e^{rs}, \forall rs \in \Gamma \ (6) \\ & (7) \\ & \operatorname{Cons} - \operatorname{UE}: & (8) - (9) \end{split}$$

Model of TNO (Method 2):

$$egin{aligned} \min_{f_{\omega}^{\mathrm{F}},f_{v}^{\mathrm{F}}} C_{\mathrm{users}} &= \sum_{a \in A_{\mathrm{R}}} (\omega t_{a} + \phi arepsilon_{a} l_{a}/10^{6}) x_{a}^{\mathrm{g}} \ &+ \sum_{a \in A_{\mathrm{R}}} \omega t_{a} x_{a}^{\mathrm{e}} + \sum_{a \in A_{\mathrm{C}}} (\omega t_{a} + \lambda_{a}^{\mathrm{M2}} E_{\mathrm{B}}) x_{a}^{\mathrm{e}} \end{aligned}$$

s.t.

Cons – Flow:
$$(1) - (3)$$

$$Cons - Time:$$
 (4)

$$Cons - Emission:$$
 (5)

 $\mathbf{Cons} - \mathbf{Cost} \colon$

(7)

Cons – UE:
$$(8) - (9)$$

Model of PDNO (Method 2):

$$egin{align} \min C_{ ext{PDNO}} &= \sum_{j \in B} [a_j (p_j^{ ext{g}})^2 + b_j \cdot p_j^{ ext{g}}] \ &+ \kappa \sum_{j \in \pi(0)} P_{0j} \end{aligned}$$

s.t.

$$(12) - (16)$$

$$\lambda_a^{\mathrm{M2,energy}} = \lambda_i \Omega_a$$

$$ar{
ho} = rac{1}{|B|} \sum_1^{|B|}
ho_j^{
m g}$$

$$\lambda_a^{\,\mathrm{M2}} = \lambda_a^{\,\mathrm{M2,energy}} + \phi \overline{
ho}$$

(|B| is the number of buses with generator)