

(1-1). Train the Perceptron Model to simulate OR operations. There are two input units and one output unit. Input patterns are (0, 0), (0, 1), (1, 0), and (1, 1). The output will be either 1 or 0. Initial weights are given as 0.3 and 0.7. Learning coefficient is 0.6. Threshold value of output unit is 3.2

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	1

Where x_1 and x_2 are the inputs and y represent the output

$x_1 = 0$,
 $x_2 = 0$
 $t = 0$
 $w_i \cdot x_i = 0 \cdot 0.3 + 0 \cdot 0.7 = 0 < 3.2$
 Actual output = 0

$x_1 = 0$,
 $x_2 = 1$ $t = 1$
 $w_i \cdot x_i = 0 \cdot 0.3 + 1 \cdot 0.7 = 0.7$
 $0.7 < 3.2$,
 output = 0

$w_i = w_i + n(t - o)x_i$
 $w_1 = 0.3 + 0.6(1 - 0)0 = 0.3$
 $w_2 = 0.7 + 0.6(1 - 0)1 = 1.3$

i)
 $x_1 = 0, x_2 = 0$ $t = 0$
 $w_i \cdot x_i = 0 \cdot 0.3 + 0 \cdot 1.3 = 0$
 $0 < 3.2$, output = 0

ii)
 $x_1 = 0, x_2 = 1$ and Target = 1
 $w_i \cdot x_i = 0 \cdot 0.3 + 1 \cdot 1.3 = 1.3$
 Threshold = 3.2 < the threshold of 3.2, so the output = 0
 $w_i = w_i + n(t - o)x_i$
 $w_1 = 0.3 + 0.6(1 - 0)0 = 0.3$
 $w_2 = 1.3 + 0.6(1 - 0)1 = 1.9$

i)
 $x_1 = 0, x_2 = 0$ and Target = 0
 $w_i \cdot x_i = 0 \cdot 0.3 + 0 \cdot 1.9 = 0$

< the threshold of 3.2, so the output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i.x_i = 0*0.3 + 1*1.9 = 1.9$$

< than the threshold of 3.2, so the output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 0.3 + 0.6(1 - 0)0 = 0.3$$

$$w_2 = 1.9 + 0.6(1 - 0)1 = 2.5$$

i)

$x_1 = 0, x_2 = 0$ and Target = 0

$$w_i.x_i = 0*0.3 + 0*2.5 = 0$$

< threshold of 3.2, so the output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i.x_i = 0*0.3 + 1*2.5 = 2.5$$

This is not greater than the threshold of 3.2, so the output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 0.3 + 0.6(1 - 0)0 = 0.3$$

$$w_2 = 2.5 + 0.6(1 - 0)1 = 3.1$$

$x_1 = 0, x_2 = 0$ and Target = 0

$$w_i.x_i = 0*0.3 + 0*3.1 = 0$$

0 is not greater than the threshold of 3.2, so
output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i.x_i = 0*0.3 + 1*3.1 = 3.1$$

This is not greater than the threshold of 3.2,
output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 0.3 + 0.6(1 - 0)0 = 0.3$$

$$w_2 = 3.1 + 0.6(1 - 0)1 = 3.7$$

i)

$x_1 = 0, x_2 = 0$ and Target = 0

$$w_i.x_i = 0*0.3 + 0*3.7 = 0$$

0 is not greater than the threshold of 3.2, so the
output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i.x_i = 0*0.3 + 1*3.7 = 3.7$$

This is greater than the threshold of 3.2, so the output = 1

Actual output = 1

Updated weights, $w_1 = 0.3, w_2 = 3.7$

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$$w_i.x_i = 1*0.3 + 0*3.7 = 0.3$$

This is not greater than the threshold of 3.2, so the output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 0.3 + 0.6(1 - 0)1 = 0.9$$

$$w_2 = 3.7 + 0.6(1 - 0)0 = 3.7$$

$$x_1 = 0, x_2 = 0 \text{ and Target} = 0$$

$$w_i.x_i = 0*0.9 + 0*3.7 = 0$$

This is not greater than the threshold of 3.2,
output = 0

ii)

$$x_1 = 0, x_2 = 1 \text{ and Target} = 1$$

$$w_i.x_i = 0*0.9 + 1*3.7 = 3.7$$

>3.2,

output = 1

iii)

$$x_1 = 1, x_2 = 0 \text{ and Target} = 1$$

$$w_i.x_i = 1*0.9 + 0*3.7 = 0.9$$

< threshold of 3.2,

output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 0.9 + 0.6(1 - 0)1 = 1.5$$

$$w_2 = 3.7 + 0.6(1 - 0)0 = 3.7$$

i)

$$x_1 = 0, x_2 = 0 \text{ and Target} = 0$$

$$w_i.x_i = 0*1.5 + 0*3.7 = 0$$

< than the threshold of 3.2,

output = 0

ii)

$$x_1 = 0, x_2 = 1 \text{ and Target} = 1$$

$$w_i.x_i = 0*1.5 + 1*3.7 = 3.7$$

>than the threshold of 3.2,

output = 1

iii)

$$x_1 = 1, x_2 = 0 \text{ and Target} = 1$$

$$w_i.x_i = 1*1.5 + 0*3.7 = 1.5$$

< threshold of 3.2,

output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 1.5 + 0.6(1 - 0)1 = 2.1$$

$$w_2 = 3.7 + 0.6(1 - 0)0 = 3.7$$

$$x_1 = 0, x_2 = 0 \text{ and Target} = 0$$

$$w_i.x_i = 0*2.1 + 0*3.7 = 0$$

< than the threshold of 3.2,

output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i \cdot x_i = 0 \cdot 2.1 + 1 \cdot 3.7 = 3.7$$

> of 3.2,

output = 1

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$$w_i \cdot x_i = 1 \cdot 2.1 + 0 \cdot 3.7 = 2.1$$

< than the threshold of 3.2,

output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 2.1 + 0.6(1 - 0)1 = 2.7$$

$$w_2 = 3.7 + 0.6(1 - 0)0 = 3.7$$

i)

$x_1 = 0, x_2 = 0$ and Target = 0

$$x_1 x_i = 0 \cdot 2.7 + 0 \cdot 3.7 = 0$$

< the threshold of 3.2,

output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i \cdot x_i = 0 \cdot 2.7 + 1 \cdot 3.7 = 3.7$$

> threshold of 3.2, so the output = 1

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$$w_i \cdot x_i = 1 \cdot 2.7 + 0 \cdot 3.7 = 2.7$$

< the threshold of 3.2,

output = 0

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 2.7 + 0.6(1 - 0)1 = 3.3$$

$$w_2 = 3.7 + 0.6(1 - 0)0 = 3.7$$

i)

$x_1 = 0, x_2 = 0$ and Target = 0

$$w_i \cdot x_i = 0 \cdot 3.3 + 0 \cdot 3.7 = 0$$

< than the threshold of 3.2,

output = 0

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i \cdot x_i = 0 \cdot 3.3 + 1 \cdot 3.7 = 3.7$$

> than the threshold of 3.2,

output = 1

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$$w_i \cdot x_i = 1 \cdot 3.3 + 0 \cdot 3.7 = 3.3$$

> than the threshold of 3.2, so

outout= 1

Actual Output = 1

Updated Weights, $w_1 = 3.3$, $w_2 = 3.7$

iv)

$x_1 = 1$, $x_2 = 1$ and Target = 1

$w_i \cdot x_i = 1 \cdot 3.3 + 1 \cdot 3.7 = 7$

> than the threshold of 3.2,

output = 1

Actual Output = 1

Final Weights, $w_1 = 3.3$, $w_2 = 3.7$

(1-2). Train the Perceptron Model to simulate NOR (Not OR) operations. There are two input units and one output unit. Input patterns are (0, 0), (0, 1), (1, 0), and (1, 1). The output will be either 1 or 0. Initial weights are given as 0.2 and -0.4. Learning coefficient is 0.5. Threshold value of output unit is -1.1.

NOR(0, 0) = 1

NOR(0, 1) = 0

NOR(1, 0) = 0

NOR (1, 1) = 0 $w_i \cdot x_i = 1 \cdot -1.3 + 1 \cdot -1.4 = -2.7$

< the threshold of -1.1,

output = 0

Actual Output = 0

Final Weights,

$w_1 = -1.3$, $w_2 = -1.4$

(1-3). Train the Perceptron Model to simulate NAND (Not AND) operations. There are two input units and one output unit. Input patterns are (0, 0), (0, 1), (1, 0), and (1, 1). The output will be either 1 or 0. Initial weights are given as 0.4 and 0.9. Learning coefficient is 0.8. Threshold value of output unit is 1.8.

If you do not get the solution with threshold of 1.8, then change the threshold as -1.8 and solve it.

Through your training process, you need to write the followings from the initial status to the final

weights for each epoch.

- actual output
- updated weight

$x_1 = 0$, $x_2 = 0$ and Target = 1

$w_i \cdot x_i = 0 \cdot 0.4 + 0 \cdot 0.9 = 0$

This is not greater than the threshold of 1.8,

output = 0

$w_i = w_i + n(t - o)x_i$

$$w_1 = 0.4 + 0.8(1 - 0)0 = 0.4$$

$$w_2 = 0.9 + 0.8(1 - 0)0 = 0.9$$

We change the threshold to -1.8

$$w_1 = 0.4$$

$$w_2 = 0.9$$

Learning coefficient $n = 0.8$

Threshold = -1.8

$x_1 = 0, x_2 = 0$ and Target = 1

$$w_i \cdot x_i = 0 \cdot 0.4 + 0 \cdot 0.9 = 0$$

0 < -1.8,

output = 1

Actual Output = 1

Initial Weights: $w_1 = 0.4, w_2 = 0.9$

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i \cdot x_i = 0 \cdot 0.4 + 1 \cdot 0.9 = 0.9$$

0.9 > -1.8,

output = 1

Actual Output = 1

Initial Weights: $w_1 = 0.4, w_2 = 0.9$

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$$w_i \cdot x_i = 1 \cdot 0.4 + 0 \cdot 0.9 = 0.4$$

0.4 < -1.8,

output = 1

Actual Output = 1

Initial Weights: $w_1 = 0.4, w_2 = 0.9$

iv)

$x_1 = 1, x_2 = 1$ and Target = 0

$$w_i \cdot x_i = 1 \cdot 0.4 + 1 \cdot 0.9 = 1.3$$

1.3 > -1.8,

output = 1

$$w_i = w_i + n(t - o)x_i$$

$$w_1 = 0.4 + 0.8(0 - 1)1 = -0.4$$

$$w_2 = 0.9 + 0.8(0 - 1)1 = 0.1$$

i)

$x_1 = 0, x_2 = 0$ and Target = 1

$$w_i \cdot x_i = 0 \cdot -0.4 + 0 \cdot 0.1 = 0$$

0 > -1.8,

output = 1

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$$w_i \cdot x_i = 0 \cdot -0.4 + 1 \cdot 0.1 = 0.1$$

0.1 > -1.8,

output = 1

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$w_i.x_i = 1*-0.4 + 0*0.1 = -0.4$

> the threshold of -1.8,

output = 1

iv)

$x_1 = 1, x_2 = 1$ and Target = 0

$w_i.x_i = 1*-0.4 + 1*0.1 = -0.3$

> threshold of -1.8,

output = 1

$w_i = w_i + n(t - o)x_i$

$w_1 = -0.4 + 0.8(0 - 1) = -1.2$

$w_2 = 0.1 + 0.8(0 - 1) = -0.7$

i)

$x_1 = 0, x_2 = 0$ and Target = 1

$w_i.x_i = 0*-1.2 + 0*-0.7 = 0$

> threshold of -1.8,

output = 1

ii)

$x_1 = 0, x_2 = 1$ and Target = 1

$w_i.x_i = 0*-1.2 + 1*-0.7 = -0.7$

> threshold of -1.8,

output = 1

iii)

$x_1 = 1, x_2 = 0$ and Target = 1

$w_i.x_i = 1*-1.2 + 0*-0.7 = -1.2$

> threshold of -1.8,

output = 1

iv)

$x_1 = 1, x_2 = 1$ and Target = 0

$w_i.x_i = 1*-1.2 + 1*-0.7 = -1.9$

< the threshold of -1.8,

output = 0

Actual output = 0 Final weights, $w_1 = -1.2, w_2 = -0.7$

(2-1). Program the Perceptron Model to simulate OR operations. There are two input units and

one output unit. Input patterns are (0, 0), (0, 1), (1, 0), and (1, 1). The output will be either 1 or 0.

Initial weights are given as 0.5 and 0.8. Learning coefficient is 0.4. Threshold value of output unit

is 2.9.

the python code that represent the perceptron algorithm

important to importing numpy library

```

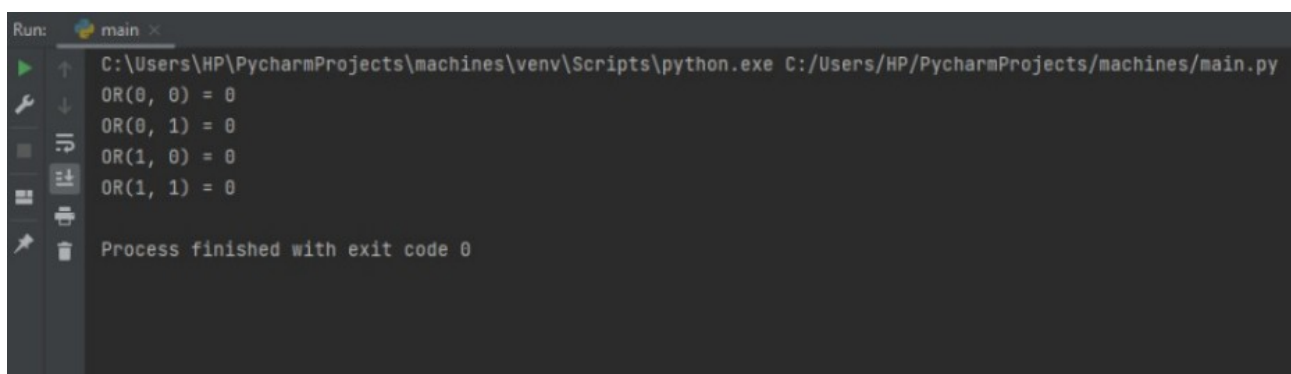
import numpy as np

def StepFunction(threshold):
    if threshold >= 3.1:
        return 1
    else:
        return 0
# designing the Perceptron
def designed_Percept(x, weight, bias):
    threshold = np.dot(weight, x) + bias
    # print("Thereshold: ", threshold)
    y = StepFunction(threshold)
    return y

# w1 = 0.9, w2 = 0.8, bias = 0.7
def OR_logic(x):
    weight = np.array([0.9, 0.8])
    bias = 0.7
    return designed_Perceptron(x, weight, bias)
# Perceptron Model
input_01 = np.array([0, 1])
input_11 = np.array([1, 1])
input_00 = np.array([0, 0])
input_10 = np.array([1, 0])
print("OR({}, {}) = {}".format(0, 0, OR_logic(input_00)))
print("OR({}, {}) = {}".format(0, 1, OR_logic(input_01)))
print("OR({}, {}) = {}".format(1, 0, OR_logic(input_10)))print("OR({}, {}) = {}".format(1, 1,
OR_logic(input_11)))

```

output



```

Run: main x
C:\Users\HP\PycharmProjects\machines\venv\Scripts\python.exe C:/Users/HP/PycharmProjects/machines/main.py
OR(0, 0) = 0
OR(0, 1) = 0
OR(1, 0) = 0
OR(1, 1) = 0
Process finished with exit code 0

```


(2-2). Program to simulate the following input data and target output relations. The initial weight for W1 is 0.6, the initial weight for W2 is 0.8, and the initial weight for W3 is 0.9. The learning coefficient is 0.4. The Threshold value is -1.0

```
# importing numpy to do the circulation
import numpy as np

def StepFunction(threshold):
    if threshold >= -1.5:
        return 1
    else:
        return 0

def perceptronMod(x, weight, b):
    threshold = np.dot(weight, x) + b
    # print("Threshold: ", threshold)
    y = StepFunction(threshold)
    return y
# NOT Logic Function
# weight_NOT = -1, bias_NOT = 0.5
def NOT_Function(x):
    weight_NOT = -1
    bias_NOT = 0.5
    return perceptronMod(x, weight_NOT, bias_NOT)

# given w1 = 0.9, w2 = 0.8, bias_OR = 0.7
def OR_Function(x):
    weight = np.array([0.9, 0.8])
    bias_OR = 0.7
    return perceptronMod(x, weight, bias_OR)
# NOR Logic Function with OR and NOT

def NOR_Function(x):
    OR_out = OR_Function(x)
    NOT_output = NOT_Function(OR_out)
    return NOT_output
# test
input_01 = np.array([0, 1])
input_11 = np.array([1, 1])
input_00 = np.array([0, 0])
input_10 = np.array([1, 0])
print("NOR({}, {}) = {}".format(0, 0, NOR_Function(input_00)))
print("NOR({}, {}) = {}".format(0, 1, NOR_Function(input_01)))
print("NOR({}, {}) = {}".format(1, 0, NOR_Function(input_10)))
print("NOR({}, {}) = {}".format(1, 1, NOR_Function(input_11)))
```

output

```
OR(0, 0) = 0  
OR(0, 1) = 0  
OR(1, 0) = 0  
OR(1, 1) = 0  
  
Process finished with exit code 0
```