

# 6.4132/16.413 Principles of Autonomy and Decision Making

## Final Project

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## 1 Introduction

Activity planning, motion planning, and trajectory optimization for a robotic arm is challenging. To navigate around an environment, the agent must perform a state space search to plan a sequence of actions and generate a trajectory by either using a sample based planner or modeling the problem as a constraint optimization problem. This project explores 1) defining an activity planning problem with the Planning Domain Definition Language, 2) implementing the Fast-Forward heuristic planner with Enforced Hill Climbing, 3) using RRT with goal-biasing for trajectory generation, and 4) comparing the results with the trajectory generated by constraint optimization. The kitchen simulation environment provides an excellent sandbox for testing and demonstrating the effectiveness of the proposed approach, in addition to learning the benefits and drawbacks of the implemented algorithms.

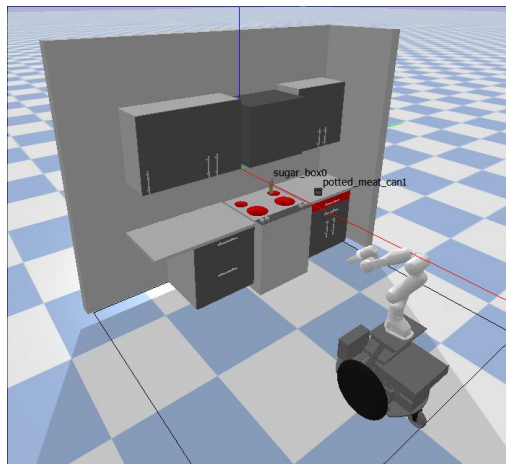


Figure 1: The kitchen simulation environment

## 2 Activity Planning

### 2.1 PDDL Domain and Problem

The PDDL domain and problem files encode the problem as sets of objects, types, predicates, actions, and goals. There are two main types of objects: the **box** type and the **storage** type. The **box** type represents the sugar and spam boxes which are manipulated by the robot arm, and the **storage** type represents the storage spaces in the kitchen. In addition, I separated the **storage** type into two subtypes: **static**, which are storage spaces without actions (stovetop burner and countertop), and **openable**, which are storage spaces that can be opened or closed (drawer, cabinet).

The following assumptions were made when designing the actions and the initial state:

- The robot can only grab one box at a time
- The robot cannot open drawers or cabinets when gripping an object
- Only one box can be placed on each storage space at a time
- Drawers and cabinets must be open when placing or picking up a box inside them
- Drawers and cabinets must be closed at both the beginning and end of the plan

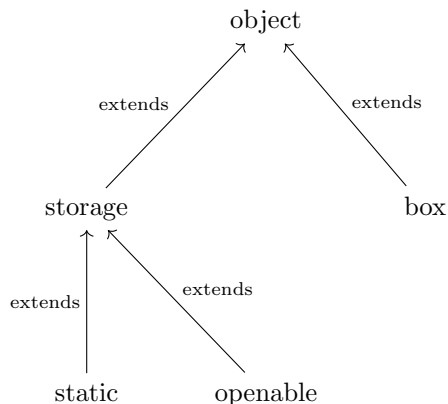


Figure 2: Hierarchical PDDL object types including static/openable storage spaces and boxes

Separating the **storage** type into subtypes allowed separating the action of placing (and picking up) a box on a storage space into **place\_static** and **place\_openable**, which has an extra (**open ?s**) precondition.

I also did not use any negative preconditions to simplify the implementation of the fast-forward heuristic planner. For actions requiring negative preconditions, I defined a second predicate which is always the negation of the predicate needing to express the negative precondition on (e.g. (**open ?s - openable**) and (**closed ?s - openable**)).

## 2.2 Fast-Forward Heuristic Planner

The `ff_planner` file contains all functions to solve the activity planning problem. The `calculate_hff` function computes the fast-forward heuristic  $h_{ff}$  of a given state by counting the number of actions (without delete effects) it takes until the goal condition is a subset of `state`. At each iteration, `new_state` is computed by taking the union of the current state and the add effects of all applicable actions. Because we defined our actions to only have positive preconditions, we can easily determine whether an action is applicable by checking if the precondition is a subset of `new_state`.  $h_{ff}$  is an admissible heuristic that always underestimates the number of actions it takes to reach the goal state, hence an alternative algorithm such as A\* could have been used to find the optimal path.

In this project, I decided to implement Enforced Hill Climbing in the `solve_ff` function. While EHC is not guaranteed to find the optimal solution, its greedy nature typically leads to higher efficiency and lower memory usage. `solve_ff` initially parses the PDDL files and enumerates all possible actions that can be taken by the agent. Next, it performs a greedy search by immediately adding an action that leads to a strictly smaller  $h_{ff}$  to the plan. If no such action is found, there is a “plateau” in the graph, and BFS is used to find a sequence of actions that lead to a smaller  $h_{ff}$ . If BFS fails to find such action, then the algorithm determines that the activity planning problem is unsolvable.

Comparing the performance of BFS and FF Heuristic Planner, on the contrary to my expectation, I found that BFS consistently runs faster ( $650\mu s$  vs.  $950\mu s$ ). This is most likely because the plan graph is rather simple for this problem. For example, the starting state has  $h_{ff} = 2$ , meaning EHC gets stuck on a “plateau” for most of the time, resorting to BFS. In this case, calculating  $h_{ff}$  leads to extra computation time. For more complex problems requiring many actions to be taken, I expect the FF Heuristic Planner to perform significantly faster than BFS.

## 3 Motion Planning

To view the sample-based motion planner in action, see [FF Heuristic Planner and RRT Trajectory Generator](#) or go to the following url: [https://drive.google.com/file/d/1sknWGIKYpLsJexYLzeWbSfdt8TrVTznH/view?usp=drive\\_link](https://drive.google.com/file/d/1sknWGIKYpLsJexYLzeWbSfdt8TrVTznH/view?usp=drive_link).

### 3.1 Environment Assumptions

Hard-coded values can be found in `constants.py` and includes:

- The initial 2D poses of the spam and sugar boxes (were not modified significantly from the original positions, simply moved the sugar box closer for the robot arm to reach)
- The 3D poses of the spam and sugar boxes after moved by the robot
- The 7D goal joint position vectors for the different actions
- `JOINT_STEP_SIZE`, `GOAL_SAMPLE`, and `GOAL_THRESHOLD` (explained in [Trajectory Generation using RRT](#))

In addition, the following assumptions were made when implementing the motion planner:

- The sugar/spam box attaches to the end-effector once the “grab” action finishes
- The drawer opens after the “open drawer” action ends and closes before the “close drawer” action begins

Importantly, the collision detection in my RRT implementation is simplified from traditional methods. Typically, when checking if a newly sampled point can be reached without collisions, RRT calculates whether the line between the new point and its nearest point in the tree intersects with an obstacle. However, in my implementation, I only check whether the new sampled point is inside an obstacle, meaning the robot collides with an object in the kitchen environment. This simplification can be made because the robot bodies are large and the distance between each node in the tree are small, meaning if a new joint configuration does not cause a collision, it is almost guaranteed that all joint configurations between the new point and its closest point are valid.

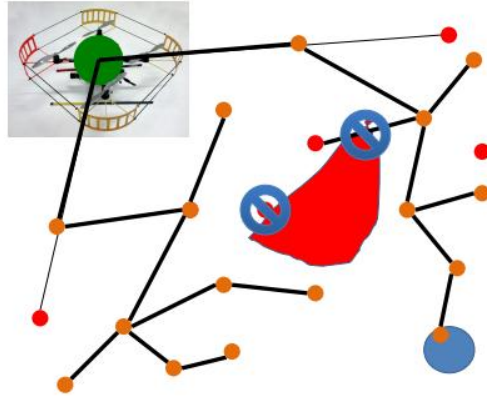


Figure 3: Collision detection in RRT

### 3.2 Trajectory Generation using RRT

The sample-based motion planning algorithm is written in `rrt.py`. `get_sample_fn` returns a sampling function that returns a random valid joint configuration  $x_{\text{rand}}$ . I also defined a class `Tree` which keeps track of its `parent`, `children`, and value (`point`), which is the 7D joint configuration. `Tree` has function `add_child`, which appends a new `Tree` to its `children` and sets the child’s `parent` to itself.

Class `TrajectoryGenerator` contains the main motion planning algorithm in the `rrt` method. It also includes four helper functions:

1. `find_nearest`: returns  $x_{\text{nearest}}$ , the node in the tree closest to  $x_{\text{rand}}$  by recursively traversing the tree.
2. `steer`: creates a straight line from  $x_{\text{nearest}}$  to  $x_{\text{rand}}$  limited to length `JOINT_STEP_SIZE`. Returns this new point  $x_{\text{new}}$ .

3. **obstacle\_free**: returns true if the input joint configuration does not cause the robot to collide with a kitchen object.
4. **find\_path**: returns a list of joint configurations from the initial state to the goal state by following the parent pointers.

RRT is then implemented as follows using the helper functions:

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**Algorithm 1** Rapidly-Exploring Random Tree (RRT)

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```

tree  $\leftarrow$  Tree()
i  $\leftarrow$  1
while True do
  if i mod GOAL_SAMPLE = 0 then
    xrand  $\leftarrow$  xgoal
  else
    xrand  $\leftarrow$  sample_free()
  end if
  xnearest  $\leftarrow$  find_nearest(tree, xrand)
  xnew  $\leftarrow$  steer(xnearest, xrand)
  if obstacle_free(xnew) then
    xlast  $\leftarrow$  Tree(xnew)
    xnearest.add_child(xlast)
    if dist(xnew, xgoal)  $\leq$  GOAL_THRESHOLD then
      return find_path(xlast)
    end if
    i  $\leftarrow$  i + 1
  end if
end while

```

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Instead of getting a random sample every time, the algorithm uses the goal state as the “random” value every **GOAL\_SAMPLE** cycles to bias the tree towards the goal. Additionally, we determine whether *x*<sub>new</sub> is in the goal state by checking if the euclidian distance between *x*<sub>new</sub> and *x*<sub>goal</sub> is less than **GOAL\_THRESHOLD**.

While the algorithm successfully generates a trajectory as shown in the video, it can be slow depending on the initial and goal state. Constants needed to be tuned to increase the performance of the algorithm.

### 3.3 Integration with the Activity Planner

The `robot.py` file includes a `Robot` class with methods for each action in the PDDL domain. It also includes methods to move the robot base closer to the objects and the robot arm back to the initial state. Finally, the dictionary `function_map` maps PDDL actions to its corresponding methods, and the `act` method uses this dictionary to perform a task based on the input PDDL action.

The overall plan execution is written in `plan_executor.py`. The code initially solves the activity planning problem using the FF Heuristic Planner, which returns a list of tasks to execute. `plan_executor` simply iterates through this list and calls the `Robot().act` method for each action to fully execute the plan.

## **4 Trajectory Optimization**

## **5 Conclusion**

[1]

## **References**

1. Cui T. Research: The First Science Partner Journal. Research 2018;2018:1.