

Chapter 11

Cryptographic Hash Functions



Hash Function

- Definition 변수가 없이 일정한 다양한 길이의 입력. 정해진 길이 출력
 - A hash function $H(\cdot)$ is an algorithm that maps data sets of variable length to data sets of a fixed length. The values returned by a hash function are called hash values, hash codes, checksums or simply hashes. In cryptography, the data to be encoded are the message and the hash value is sometimes called the message digest or simply digest.

• Example

- A person's name, having a variable length, could be hashed to a single integer of bounded size.

• Main application

- Hash tables

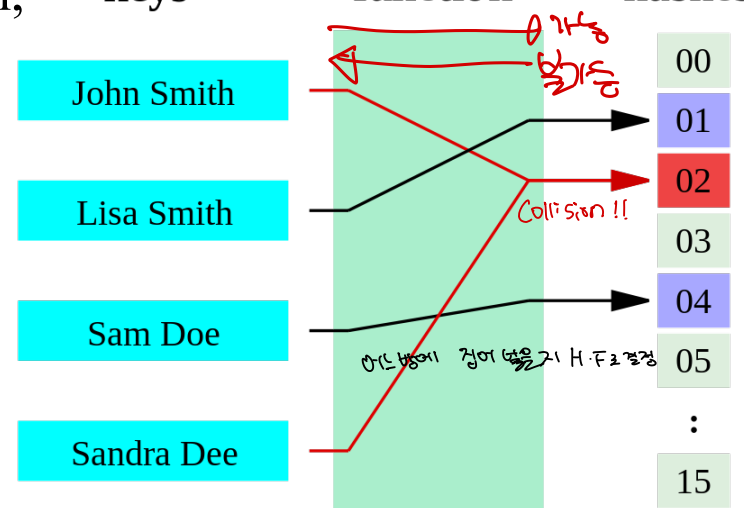
constant time

하나 Hash 입력

data table
keys

hash
function

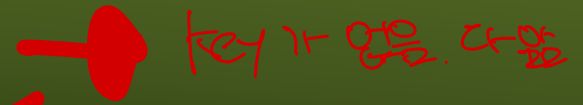
hashes



이항해시

collision 줄일까?

Cryptographic Hash Function



- Pre-image resistance *출력을 알려주고 입력값 찾아보.*
 - Given a hash value h it should be difficult to find any message m such that $h = H(m)$. $y = H(x)$
- Second pre-image resistance *입력과 출력을 알려줌. 출력에 맞는거 하나더 찾아봐*
 - Given an input m_1 it should be difficult to find another input m_2 such that $m_1 \neq m_2$ and $H(m_1) = H(m_2)$. *다르게 하나더 찾아봐*
 - This property is sometimes referred to as weak collision resistance.
- Collision resistance *출력이 같아도 m_1, m_2 찾아봐. y 안알려줌*
 - It should be difficult to find two different messages m_1 and m_2 such that $H(m_1) = H(m_2)$. Such a pair is called a cryptographic hash collision.
 - This property is sometimes referred to as strong collision resistance. It requires a hash value at least twice as long as that required for preimage-resistance; otherwise collisions may be found by a birthday attack. *아주큰 collision 이나 찾아봐*

Birthday Attack

- Birthday problem

- In probability theory, the birthday problem or birthday paradox concerns the probability that, in a set of randomly chosen people, some pair of them will have the same birthday. 계산하기나면 모자라고 부족함
- By the pigeonhole principle, the probability reaches 100% when the number of people reaches 366; where we do not consider February 29.
- The probability reaches 50% with 23 people. 366명이 있으면 100% collision

- Birthday attack

- Given a hash function $H(\cdot)$, the goal of the attack is to find a collision. If the hash function yields N different outputs with equal probability, we need to apply H to $\alpha \approx \sqrt{N}$ inputs to have at least one collision with a probability greater than 0.5. For example, $n = 2^{160}$ gives $\alpha \approx 2^{80}$. 50% 확률로 그냥 생일이 같을려면 23명 필요

n 개의 input, \sqrt{n} 까지 50% collision

Security Level

- For a hash code of length n , the level of effort required by the opponent is as follows.

Preimage resistant	2^n
Second preimage resistant	2^n
Collision resistant	$2^{n/2}$

256 bit 정도 해시값 생성

256 개라면 2^{256} 정도 필요

AES - 128 비트

비트열만 생성: 256 비트

- Note that digital signature schemes require the collision resistance.

디지털 서명?

Example: Variations with the same meaning

As { the } Dean of Blakewell College, I have { had the pleasure of knowing } Cherise
 — } known

Rosetti for the { last } four years. She { has been } { a tremendous } { asset to }
 { past } { was } { an outstanding } { role model in }

{ our } school. I { would like to take this opportunity to } recommend Cherise for your
 { the } { wholeheartedly }

{ school's } graduate program. I { am } { confident } { that } { she }
 { — } { feel } { certain } { — } { Cherise } will

{ continue to } succeed in her studies. { She } is a dedicated student and
 { — } { Cherise }

{ thus far her grades } { have been } { exemplary } In class,
 { her grades thus far } { are } { excellent }

{ she } { has proven to be } a take-charge { person } { who is } able to
 { Cherise } { has been } { individual } { — }

successfully develop plans and implement them.

{ She } has also assisted { us } in our admissions office. { She } has
 { Cherise } { — }

{ successfully } demonstrated leadership ability by counseling new and prospective student:
 { — }

{ Her } advice has been { a great } help to these students, many of whom
 { Cherise's } { of considerable }

have { taken time to share } their comments with me regarding her pleasant and
 { shared }

{ encouraging } attitude. { For these reasons } I
 { reassuring } { It is for these reasons that }

{ highly recommend } Cherise { without reservation } Her { ambition } and
 { offer high recommendations for } { unreservedly } { drive }

{ abilities } will { truly } be an { asset to } your { establishment }
 { potential } { surely } { plus for } { school }

General Structure of Hash Function

- The hash algorithm involves repeated use of a compression function, f , that takes two inputs (an n -bit input from the previous step, called the chaining variable, and a b -bit block) and produces an n -bit output.

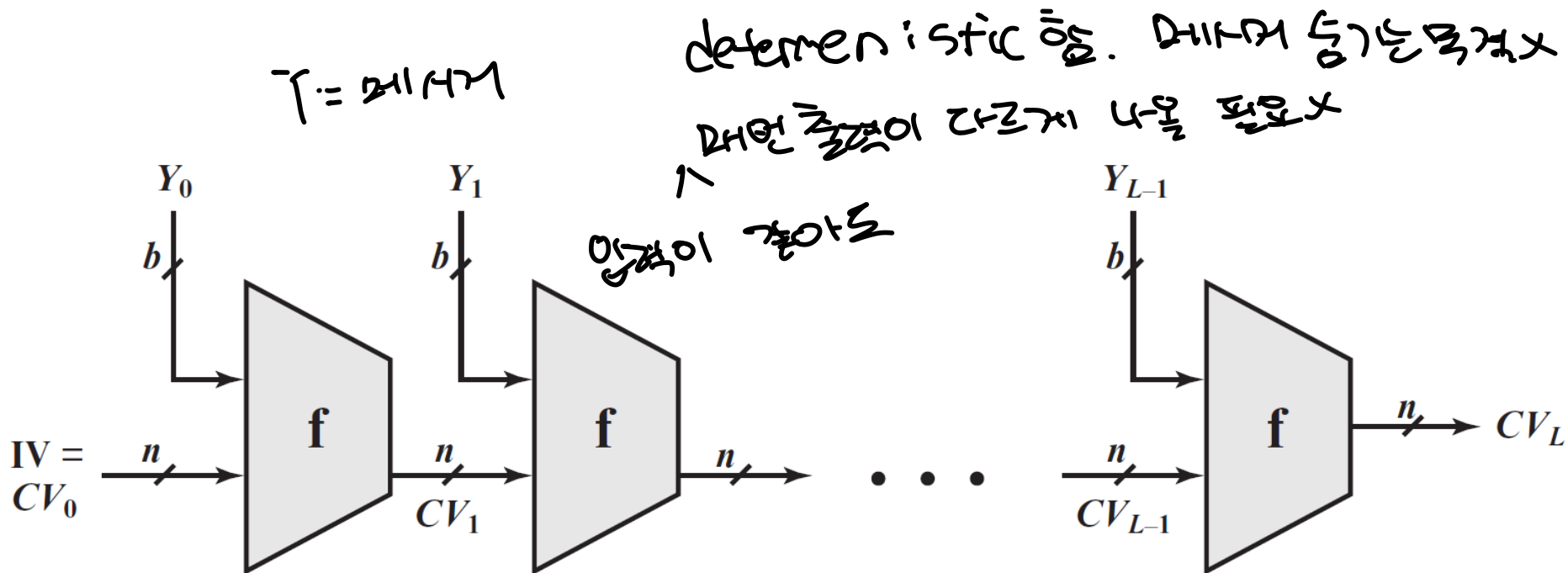
$$CV_0 = IV = \text{initial } n\text{-bit value}$$

$$CV_i = f(CV_{i-1}, Y_{i-1}) \quad \text{where } 1 \leq i \leq L$$

$$H(M) = CV_L$$

where the input to the hash function is a message M consisting of the blocks Y_0, Y_1, \dots, Y_{L-1} .

General Structure of Hash Function



IV = Initial value

CV_i = Chaining variable

Y_i = i th input block

f = Compression algorithm


L = Number of input blocks

n = Length of hash code

b = Length of input block

복합 X 암호 알고리즘, 기밀성, 무결성, 부인성, 사용 편의성
 사용 편의성, 기밀성, 무결성, 부인성

Cryptographic Hash Functions in Practice

- MD5
 - 128-bit output. 
 - MD5 was introduced in 1991... collision attacks found in 2004... several extensions and improvements since then.
 - However, MD5 is still widely deployed(!)
- SHA (Secure Hash Algorithm)
 - The Secure Hash Algorithm is a family of cryptographic hash functions published by the National Institute of Standards and Technology (NIST) as a U.S. Federal Information Processing Standard (FIPS).

SHA (Secure Hash Algorithm)

- SHA-0
 - A retronym applied to the original version of the 160-bit hash function published in 1993 under the name “SHA.” It was withdrawn shortly after publication due to an undisclosed significant flaw and replaced by the slightly revised version SHA-1.
- SHA-1
 - A 160-bit hash function which resembles the earlier MD5 algorithm. This was designed by the NSA to be part of the Digital Signature Algorithm. Cryptographic weaknesses were discovered in SHA-1, and the standard was no longer approved for most cryptographic uses after 2010.
- SHA-2
 - A family of two similar hash functions, with different block sizes, known as SHA-256 and SHA-512. There are also truncated versions of each standardized, known as SHA-224 and SHA-384.
- SHA-3
 - A hash function formerly called Keccak, chosen in 2012 after a public competition. It supports variable output length (224, 256, 384, 512), and its internal structure differs significantly from the rest of the SHA family.

SHA-1/SHA-2 Parameters

Algorithm	Message Size	Block Size	Word Size	Message Digest Size
SHA-1	$< 2^{64}$	512	32	160
SHA-224	$< 2^{64}$	512	32	224
SHA-256	$< 2^{64}$	512	32	256
SHA-384	$< 2^{128}$	1024	64	384
SHA-512	$< 2^{128}$	1024	64	512
SHA-512/224	$< 2^{128}$	1024	64	224
SHA-512/256	$< 2^{128}$	1024	64	256

(All sizes are measured in bits.)

SHA-3 Parameters

Message Digest Size	224	256	384	512
Message Size	no maximum	no maximum	no maximum	no maximum
Block Size (bitrate r)	1152	1088	832	576
Word Size	64	64	64	64
Number of Rounds	24	24	24	24
Capacity c	448	512	768	1024
<u>Collision Resistance</u>	2^{112}	2^{128}	2^{192}	2^{256}
Second Preimage Resistance	2^{224}	2^{256}	2^{384}	2^{512}

메시지 사이즈 제한이 X Birthday 공격에 안전함.

Cryptographic Hash Functions: Applications

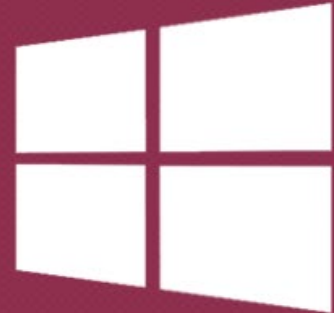
- Motivation
 - Cryptographic hash values are sometimes called (digital) fingerprints.
- Applications
 - Verifying the integrity of files or messages
 - Password files

File Hash Checking



MAMP PRO for Windows
Now on sale

Buy now!



Downloads

Here you find the current installation package of MAMP & MAMP PRO.

Mac OS X

Windows

MAMP & MAMP PRO 3.3.0 (Windows)

Download

SHA-256: [adbfc53a3aa5a02f3a00f7c96b61f4b1704e2811e757db223eea658d705b039c](#)

This download package for Windows contains the free MAMP and a free 14-day trial of MAMP PRO. MAMP can be used stand-alone without MAMP PRO.

The trial Version of MAMP PRO can be upgraded to the full version by buying a serial number.

Components

Apache: 2.2.31

Nginx 1.11.0

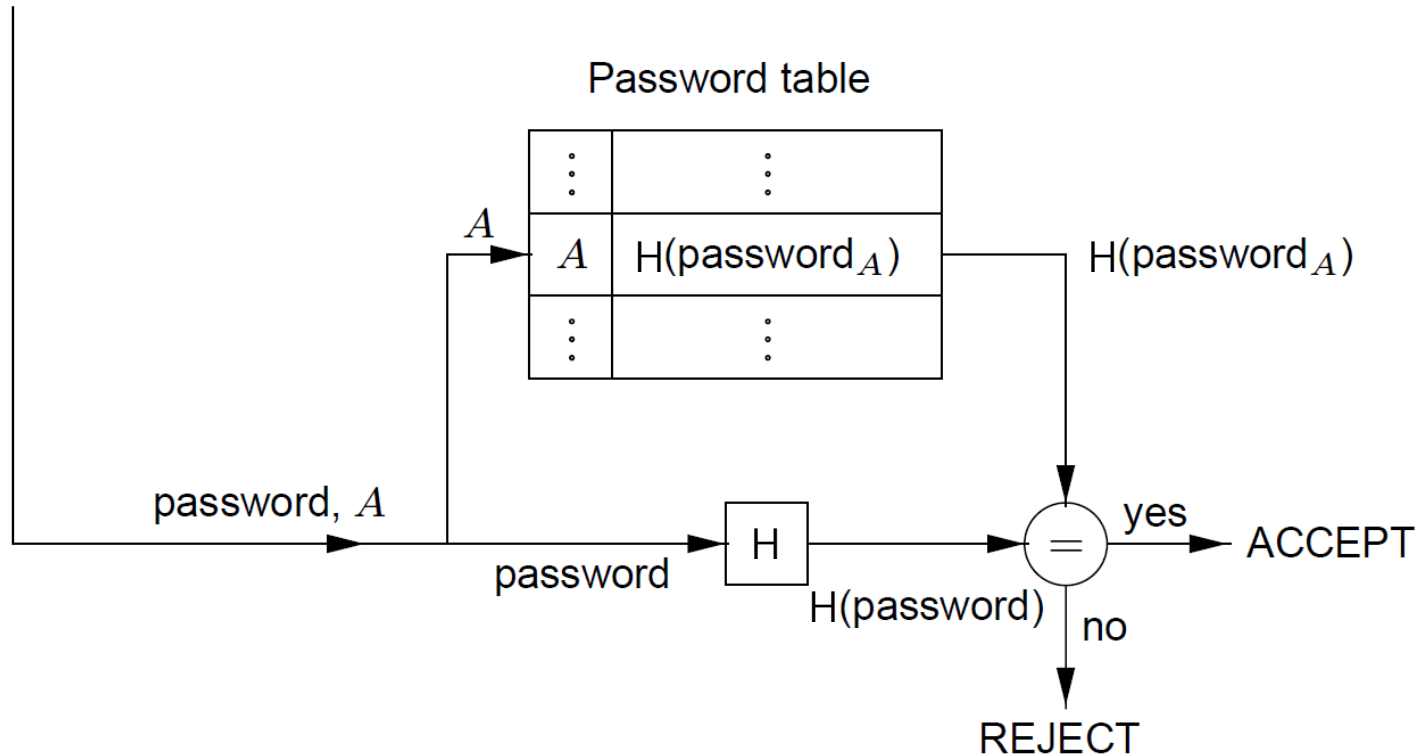
MySQL: 5.6.34

PHP: 5.3.23 & 5.4.1 & 5.4.45 & 5.5.0 & 5.5.24 &
5.5.38 & 5.6.0 & 5.6.28 & 7.0.0 & 7.0.6 & 7.0.13 (for
PHP 7: Windows 7 minimum with SP1 and Windows

Password Hashing

Claimant A

Verifier (system) B



Salting passwords

- To make dictionary attacks less effective, each password may be augmented with a t -bit random string called a salt before applying H .