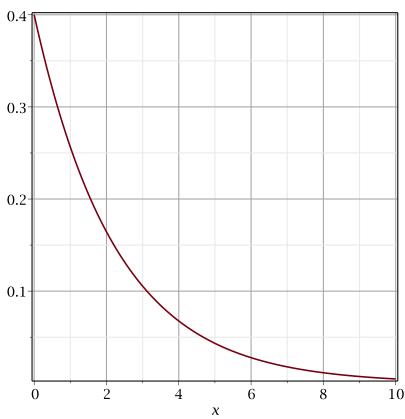
- restart; assume(alpha > 0, beta > 0);with(cl): # Hawkes process with P=1
- > nu := (alpha, beta, t) \rightarrow alpha $\cdot \exp\left(-\frac{\text{alpha}}{\text{beta}} \cdot t\right)$; # kernel function

$$v := (\alpha, \beta, t) \mapsto \alpha e^{-\frac{\alpha t}{\beta}}$$
 (1)

> lambda := int(nu(alpha, beta, t), t = s..t)

$$\lambda := \beta e^{-\frac{\alpha s}{\beta}} - \beta e^{-\frac{\alpha t}{\beta}}$$
 (2)

-|> |> |> pgl(nu(0.4, 0.9, t), 0..10)



$$\rightarrow$$
 assume($a > 0$); assume($b > 0$);

>
$$int(nu(a, b, t), t = 0..inf)$$

> lambda := unapply(int(nu(alpha, beta, t), t = s..u), alpha, beta, s, u);# intensity function

$$\lambda := (\alpha, \beta, s, u) \mapsto \beta e^{-\frac{\alpha s}{\beta}} - \beta e^{-\frac{\alpha u}{\beta}}$$
(4)

(7)

> Lambda := unapply(factor(int(lambda(alpha, beta, s, t), t = s..u)), alpha, beta, s, u); # compensator

$$\Lambda := (\alpha, \beta, s, u) \mapsto \frac{\beta \left(u \alpha + \beta e^{\frac{\alpha(s-u)}{\beta}} - \alpha s - \beta \right) e^{-\frac{\alpha s}{\beta}}}{\alpha}$$
(5)

> InvComp := unapply(factor(solve(Lambda(alpha, beta, s, u) = eps, u)), alpha, beta, s, eps);

solve for the stopping-time u, given the params \Theta={alpha,beta}, a starting-time, and a value of the ideally-unit-exponentially distributed \eps

$$InvComp := (\alpha, \beta, s, \epsilon) \mapsto \frac{W \left(-\frac{e^{-\frac{\alpha s}{\beta}}\beta^2 + \epsilon \alpha}{e^{-\frac{\alpha s}{\beta}}\beta^2}\right) e^{-\frac{\alpha s}{\beta}\beta^2 + e^{-\frac{\alpha s}{\beta}}\alpha\beta s + e^{-\frac{\alpha s}{\beta}}\beta^2 + \epsilon \alpha}}{\beta e^{-\frac{\alpha s}{\beta}}\alpha}$$

$$(6)$$

-> $int(InvComp(1, 1, 0, eps) \cdot exp(-eps), eps = 0..inf);$

1 rather singular case which has a closed-form symbolic answer