

## Comments on homework (Week 5)

- ▶ No difference in means (average) between the two populations ( $H_0$ )
- ▶ The direction of difference can be inferred from the means.
- ▶ Confidence intervals show the range of the magnitude of difference at a specified level of confidence.
- ▶ Confidence intervals allow to test the hypothesis (95% CI for 5% significance level)

## Some useful formulas (t-test last week)

- ▶ T-test statistic:  $t = \frac{\hat{\Delta}}{\hat{\sigma}_{\hat{\Delta}}} = \frac{\bar{Y}_1 - \bar{Y}_2}{\hat{\sigma}_{\hat{\Delta}}}$
- ▶ Estimated standard error:  $\hat{\sigma}_{\hat{\Delta}} = \frac{\hat{\sigma}}{\sqrt{n}} = \hat{\sigma} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$
- ▶ Estimated common population standard deviation:  
$$\hat{\sigma} = \sqrt{\frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1 + n_2 - 2}}$$
- ▶ Confidence intervals:  $\hat{\Delta} \pm z_{\alpha/2} \hat{\sigma}_{\hat{\Delta}}$
- ▶ Confidence intervals (95%, standard normal/ t-distribution with  $df > 120$ ):  $\hat{\Delta} \pm 1.96 \hat{\sigma}_{\hat{\Delta}}$

# Z-test (inference in proportions)

Recall the conceptual framework we use for statistical inference:

1. **Type** of data (**level** of measurement)
2. **Assumptions** about the data (often assumed implicitly)
3. Statistical **hypotheses**:
  - ▶ Null hypothesis ( $H_0$ )
  - ▶ Alternative hypothesis ( $H_1$ )
4. **Test statistic**
5. **P-value** (using sampling distribution of the test statistic)
6. Substantive **conclusion** (inference in the population)

## Some useful formulas (Z-test this week)

- ▶ Z-test statistic:  $z = \frac{\hat{\Delta}}{\hat{\sigma}_{\hat{\Delta}}} = \frac{\hat{\pi} - \pi_0}{\hat{\sigma}_{\hat{\Delta}}}$
- ▶ Estimated standard error:  $\hat{\sigma}_{\hat{\Delta}} = \sqrt{\frac{\hat{\pi}(1-\hat{\pi})}{n}}$
- ▶ Z-test statistic (two-sample):  $z = \frac{\hat{\Delta}}{\hat{\sigma}_{\hat{\Delta}}} = \frac{\hat{\pi}_1 - \hat{\pi}_2}{\hat{\sigma}_{\hat{\Delta}}}$
- ▶ Estimated standard error (two-sample):  
$$\hat{\sigma}_{\hat{\Delta}} = \sqrt{\hat{\pi}(1-\hat{\pi})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}$$
- ▶ Estimated standard error (two-sample) for confidence intervals:  
$$\hat{\sigma}_{\hat{\Delta}} = \sqrt{\frac{\hat{\pi}_1(1-\hat{\pi}_1)}{n_1} + \frac{\hat{\pi}_2(1-\hat{\pi}_2)}{n_2}}$$
- ▶ Confidence intervals:  $\hat{\pi} \pm z_{\alpha/2} \hat{\sigma}_{\hat{\pi}}$
- ▶ Confidence intervals (95%, standard normal):  $\hat{\pi} \pm 1.96 \hat{\sigma}_{\hat{\pi}}$