# RH 1.6

#### MATH 5, Jones

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## Refrigerator Homework

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$$\begin{cases} p_s = 0.8p_g + 0.3p_s \\ p_g = 0.2p_g - 0.7p_s \end{cases} \rightarrow \begin{bmatrix} 0.8 & 0.3 - 1 & 0 \\ 0.2 - 1 & 0.7 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 0.8 & -0.7 \\ -0.8 & 0.7 \end{bmatrix} \begin{bmatrix} p_g \\ p_s \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$0.8p_g = 0.7p_s \Rightarrow p_g = \frac{7}{8}p_s$$

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a: 
$$\begin{bmatrix} A & E & M & T \\ A & 0.65 & 0.3 & 0.3 & 0.2 \\ E & 0.1 & 0.1 & 0.15 & 0.1 \\ M & 0.25 & 0.35 & 0.15 & 0.3 \\ T & 0 & 0.25 & 0.4 & 0.4 \end{bmatrix}$$

b: Equations:  $\begin{aligned} p_A &= 0.65p_A + 0.30p_E + 0.30p_M + 0.20p_T & p_E &= 0.10p_A + 0.10p_E + 0.15p_M + 0.10p_T \\ p_M &= 0.25p_A + 0.35p_E + 0.15p_M + 0.30p_T & p_T &= 0.25p_E + 0.40p_M + 0.40p_T \\ 0.35p_A &- 0.30p_E - 0.30p_M - 0.20p_T &= 0 & -0.10p_A + 0.90p_E - 0.15p_M - 0.10p_T &= 0 \\ -0.25p_A &- 0.35p_E + 0.85p_M - 0.30p_T &= 0 & -0.25p_E - 0.40p_M + 0.60p_T &= 0 \end{aligned}$ 

As a matrix: 
$$\begin{bmatrix} 0.35 & -0.30 & -0.30 & -0.20 & 0 \\ -0.10 & 0.90 & -0.15 & -0.10 & 0 \\ -0.25 & -0.35 & 0.85 & -0.30 & 0 \\ 0 & -0.25 & -0.40 & 0.60 & 0 \end{bmatrix}$$

RREF using the Wolfram Compute Engine:  $\begin{bmatrix} 1 & 0 & 0 & -2.02786 & 0 \\ 0 & 1 & 0 & -0.531105 & 0 \\ 0 & 0 & 1 & -1.16806 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$ 

$$p_A = 2.03p_T$$
,  $p_E = 0.53p_T$ ,  $p_M = 1.17p_T$   
 $p_A = 203$ ,  $p_E = 53$ ,  $p_M = 117$ 

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$$\operatorname{NaHCO_3}: \begin{bmatrix} 1\\1\\1\\3 \end{bmatrix}, \quad \operatorname{H_3C_6H_5O_7}: \begin{bmatrix} 0\\8\\6\\7 \end{bmatrix}, \quad \operatorname{Na_3C_6H_5O_7}: \begin{bmatrix} 3\\5\\6\\7 \end{bmatrix}, \quad \operatorname{H_2O}: \begin{bmatrix} 0\\2\\0\\1 \end{bmatrix}, \quad \operatorname{CO_2}: \begin{bmatrix} 0\\0\\1\\2 \end{bmatrix} \quad \begin{array}{l} \operatorname{sodium} \\ \operatorname{hydrogen} \\ \operatorname{carbon} \\ \operatorname{oxygen} \end{array}$$

$$\begin{bmatrix} 1 & 0 & -3 & 0 & 0 & 0 \\ 1 & 8 & -5 & -2 & 0 & 0 \\ 1 & 6 & -6 & 0 & -1 & 0 \\ 3 & 7 & -7 & -1 & -2 & 0 \end{bmatrix} \text{ Becomes } \begin{bmatrix} 1 & 0 & 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 & -1/3 & 0 \\ 0 & 0 & 1 & 0 & -1/3 & 0 \\ 0 & 0 & 0 & 1 & -1 & 0 \end{bmatrix} \text{ when row reduced making the equation}$$

$$3NaHCO_3 + H_3C_6H_5O_7 \rightarrow Na_3C_6H_5O_7 + 3H_2O + 3CO_2$$

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$$\begin{bmatrix} 1 & 0 & -1 & -1 & 0 & 40 \\ 1 & 1 & 0 & 0 & 0 & 200 \\ 0 & 1 & 1 & 0 & -1 & 100 \\ 0 & 0 & 0 & 1 & 1 & 60 \end{bmatrix} \text{ becomes } \begin{bmatrix} 1 & 0 & -1 & 0 & 1 & 100 \\ 0 & 1 & 1 & 0 & -1 & 100 \\ 0 & 0 & 0 & 1 & 1 & 60 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \text{ when row reduced}$$

# Computer Homework

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On next page. Im sick and dont feel like typing out the latex

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