

Assignment 5

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1 Problem Set 1

1.1 Problem 1

1) $f(t) = e^{2t^2}$

This function is not exponential order. For some K, c, T ,

$$\frac{e^{2t^2}}{Ke^{ct}} = \frac{1}{K}e^{2t^2 - ct}$$

As t approaches infinity, the expression in the exponent approaches infinity regardless of our selection of c .

2) $f(t) = 2t^3$

$$\lim_{t \rightarrow \infty} \frac{2t^3}{Ke^{ct}} = \lim_{t \rightarrow \infty} \frac{6t^2}{cKe^{ct}} = \lim_{t \rightarrow \infty} \frac{12t}{c^2Ke^{ct}} = \lim_{t \rightarrow \infty} \frac{12}{c^3Ke^{ct}}$$

Evaluating this limit, we see that as t approaches infinity, the ratio approaches zero. Therefore $2t^3$ is of exponential order.

1.2 Problem 2

$$\frac{1}{s^2 + 6s + 8}$$

Using partial fraction decomposition,

$$\begin{aligned} \frac{1}{s^2 + 6s + 8} &= \frac{A}{s + 2} + \frac{B}{s + 4} \\ 1 &= As + 4A + Bs + 2B \end{aligned}$$

Comparing coefficients,

$$0 = A + B \quad 1 = 4A + 2B$$

We get $A = 1/2$ and $B = -1/2$. Substituting,

$$\frac{1}{s^2 + 6s + 8} = \frac{1}{2(s + 2)} + \frac{-1}{2(s + 4)}$$

Taking the inverse Laplace transform,

$$f(t) = \frac{1}{2}e^{-2t} - \frac{1}{2}e^{-4t}$$

2 Problem Set 2

2.1 Problem 1

2.2 Problem 2